

# FRB repetition and non-Poissonian statistics

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## ABSTRACT

We discuss some of the claims that have been made regarding the statistics of fast radio bursts (FRBs). We show how if their repeat rate were non-Poissonian and had some associated flicker noise then the current limits of repetition ( $\leq$  daily) would be weakened. The repeat rate has implications for observing strategy, favouring shallow wide-field surveys in the case where bursts repeat regularly. We also discuss the statistics of the apparent latitudinal dependence of FRBs, which is also affected by repetition. We show that the non-uniformity of bursts on the sky cannot be ruled out with  $N\text{-}\sigma$ , as has been claimed.

**Key words:**

## 1 INTRODUCTION

There is mounting evidence that the new class of transients known as fast radio bursts (FRBs) are of astronomical origin. The most striking features of FRBs are their large dispersion measures (DMs) – too high to be attributed to our own Galaxy’s ISM – and their event rate ( $10^3 - 10^4 \text{ sky}^{-1} \text{ day}^{-1}$ ). They last for  $\sim$ millisecond with peak flux of  $\sim$ Jy, and none has been conclusively shown to repeat. This has led to the interpretation that FRBs are cosmological, since the intergalactic medium (IGM) would naturally provide DMs between  $\sim 300\text{--}1600 \text{ pc cm}^{-3}$  for sources at  $z \sim 0.3\text{--}1$ .

Given their apparent phenomenological richness (polarization, scattering, etc.) and considering how little we know about their location and physical origin, it is likely that FRBs will be of interest to the community for years to come, assuming they are not terrestrial. Though we are in the regime of only  $\sim$ dozen published FRBs, at present the conventional wisdom is that they are likely cosmological in origin (Thornton 2013), they seem to not repeat regularly (Petroff et al. 2015), and there is a dearth of bursts at low galactic latitudes (Petroff et al. 2014; Burke-Spolaor & Banister 2014; Macquart & Johnston 2015). There have been a number of models proposed to describe this cataclysmic, cosmological scenario (Mickaliger et al. 2012; Totani 2013; Falcke & Rezzolla 2014; Mingarelli et al. 2015). However since the field is still in its infancy it is important to leave as many conceptual doors open as possible; assumptions about

the statistics of their event rate, spatial distribution, and repetition are important for the design and observing strategy of upcoming surveys. In section 2 we explore the consequences of repeating FRBs in the case where their burst rate is non-Poissonian and exhibits a  $1/f$  power spectrum, or pink noise. We also investigate the claims of Maoz et al. (2015) that FRB 140514 could have been the same source as FRB 100220, and comment on its implications. In section 3 we discuss the statistical treatment of the apparent latitudinal dependence of event rate and the lack of detections at low galactic latitude. In section 4 discuss the impact of FRB repetition on survey strategy.

## 2 REPEAT RATES

Though no source has been shown with certainty to repeat, the limits on the repeatability of FRBs are still weak. Several models generical predict repetition, whether periodic or stochastic. Galactic flaring stars (Maoz et al. 2015), radio bursting magnetars (Popov & Postnov 2007; Pen & Connor 2015), and pulsar planet systems (Mottez & Zarka 2014) all predict repetition with varying rates and burst distributions. In Connor et al. (2015) we proposed supergiant pulses from very young pulsars in supernova remnants of nearby galaxies could explain the high DMs, Faraday rotation, scintillation, and polarization properties of the observed FRBs. We also conjecture that if the repetition of supergiant pulses were non-Poissonian (with a pink or red distribution) then one might expect several bursts in a short period of time.

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### 2.1 Flicker noise

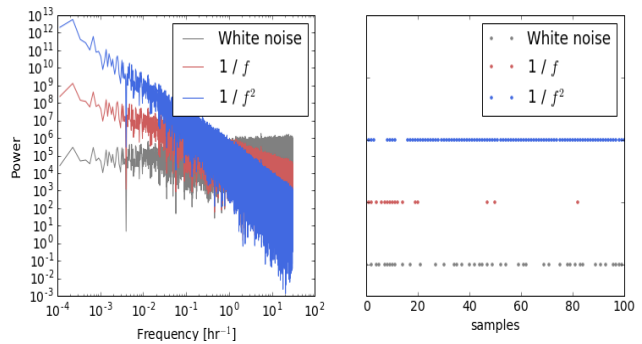
Pink noise is ubiquitous in physical systems, showing up in geology and meteorology, a number of astrophysical sources including quasars and the sun, human biology, nearly all electronic devices, finance, and even music and speech (Press 1978; Voss & Clarke 1975). Though there is no agreed upon mathematical explanation for this phenomenon (Milotti 2002), fluctuations are empirically known to be inversely proportional to frequency for a variety of dynamical systems. In the case of a time-domain astronomical source, this results in uniformity on short timescales, i.e. a burst of clustered events followed by extended periods of quiescence. If FRBs were to exhibit such flicker noise then their repetition would not only be non-periodic, but would also have a time varying burst rate. Therefore the number of events seen in a follow-up observation would depend strongly on the time passed since the initial event.

In Petroff et al. (2015) the fields of eight FRBs discovered between 2009 and 2013 were followed up from April to October of 2014, for an average of  $\sim 11.4$  hours per field. During this followup programme FRB 140514 was found in the same beam as FRB 110220, however the authors argue that it is likely a new source due to its lower DM. After its discovery, the field of 140514 was monitored five more times, starting 41 days later on 2014-05-24, without seeing anything. Under the assumption that 140514 was a new FRB that only showed up in the same field coincidentally and that the repeat rate is uncorrelated, Petroff et al. (2015) rule out repetition with  $P \leq 8.6$  hours and reject  $8.6 < P < 21$  hours with 90% confidence. However it is possible that one or both of those premises is invalid, so it is useful to explore the possibility of non-stationary repeat rate statistics and repeating FRBs with variable DM.

If the statistics of the FRB's repeat rate were non-Poissonian and initial bursts from FRBs were to have aftershocks similar to earthquakes, then the non-immediate followup observations impose far weaker repeat rate limits than has been suggested. We constructed a mock followup observation of the eight FRBs whose fields were observed in Petroff et al. (2015). We then asked how many bursts are seen to repeat if we do an immediate follow up vs. a followup several years after the initial event at times corresponding to those in Petroff et al. (2015). We Monte Carlo this simple simulation with one sample per hour and a probability of 0.5 that a given sample has a burst in it. In the stationary Poisson case, the rate of bursts in the immediate followup is the same as the multi-year followup since all times are uncorrelated. When we use a spectrum of events to be described by a  $1/f$  powerlaw, we see  $\sim 20\%$  more events in the case where we stay on the source after first observing it than when the followup takes place several months or years later.

### 2.2 FRBs 110220 and 140514

Using the event rate of  $\sim 10^4 \text{ sky}^{-1} \text{ day}^{-1}$  from Thornton (2013), it was originally reported that the probability of seeing a new FRB in the field of 110220 during the 85 hours of followup was  $\sim 0.32$  (Petroff et al. 2015). It was then pointed out by Maoz et al. (2015) that this underestimated the coincidence, since FRB 140514 was found in the same pointing as 110220 during the gridded followup, and not one of the



**Figure 1.** *left panel:* Power spectrum for pulse arrival times of a single FRB. Grey shows a flat spectrum, corresponding to the often assumed Poissonian repetition rate. The red and blue spectra show flicker noise, with pink ( $1/f$ ) noise and Brownian ( $1/f^2$ ) noise respectively. *right panel:* Repeat events following an initial burst for the three different spectra. The average probability of a burst in this simulation is 0.5, which is why roughly half of the bins in the white case have events. In the  $1/f^\alpha$  cases the initial event is followed by a number of pulses due to the increased event rate when in an “on” state.

four other staggered pointings near the field. The probability also dropped due to the updated daily event rate, given the Thornton (2013) estimate is now thought to likely be high. Using the rate calculated in Rane et al. (2015), and following the procedure of Maoz et al. (2015), we find the likelihood of  $\sim 0.25$ -2.5%. Given the relatively low probability of finding a new FRB in the same field and since there are models that predict burst repetition with variable DMs (Connor et al. 2015; Maoz et al. 2015) one can then ask the question: If one FRB out of eight is found to repeat during 85 hours of followup, what are the limits on the expected repeat rate?

### 3 LATITUDINAL DEPENDENCE

There is now evidence that the FRB rate is nonuniform on the sky, with fewer detectable events at low galactic latitudes (Burke & Graham-Smith 2014). However the statistical significance of this finding may be overstated and some of the initial claims premature. In Petroff et al. (2014) the authors compute the probability of the disparity between the number of bursts seen in the the high and low latitude components of the High Time Resolution Universe survey (HTRU). They calculate the probability of seeing  $N=0$  in the low-lat survey and  $M=4$  in the high-lat, despite having searched 88% more data in the latter. We would point out that in general  $P(N|M)$  describes a very specific outcome, and  $P(\leq N | \geq M)$  would be more appropriate since it includes all outcomes equally or more unlikely. That number might also be multiplied by two, since if the survey found four low-latitude FRBs and zero high-lat ones, we would ask the same question. HTRU has since reported five more bursts in the high galactic region, but using a dataset that spent  $\sim 2.5$  times more time at high-lat. Below we try and quantify the likelihood of this.

If one wants to test a statistical hypothesis, then that claim should be treated as true and one should ask with

what confidence it can be rejected. In the case of testing the abundance of FRBs at high latitudes, the sky should be bifurcated into high and low regions a priori (e.g. the predefined high-lat HTRU and its complement). The rate in both regions is then taken to be the same, and the likelihood of a given spatial distribution of observed sources can be calculated. This situation is naturally described by a biased binomial distribution with a fixed number of events. Suppose  $K$  FRBs are observed in a given survey. We then ask the question, what is the probability of seeing  $M$  events in the high region and  $(K-M)$  events in the lower region? This probability can be calculated as

$$P(M|K, p) = \binom{K}{M} p^M (1-p)^{K-M} \quad (1)$$

where  $p$  is the probability that an event happens to show up in the northern region. In a survey where more time is spent on one part of the sky than the other,  $p = \alpha / (1 + \alpha)$ , where  $\alpha$  is the ratio of time spent in the high-lat region vs. the low region. In the case of the HTRU survey,  $K=9$  and since none were found in the low-lat region,  $M=9$ . Roughly 2500 hours were spent searching the upper region and  $\sim 1000$  hours were spent at  $|b| < 15^\circ$ , giving  $\alpha = 2.5$ . Using equation 1, this outcome is only 13% unlikely.

#### 4 EVENT RATES AND TOTAL NUMBER OF SOURCES

If FRBs were found to repeat, their statistics and the average frequency of their repetition should affect the search strategy of upcoming surveys. For instance, if it were found that FRBs repeated, on average, five times a day, then the number of unique sources would be five times smaller than the per-sky daily event rate. This means the rate  $3.3^{+5.0}_{-2.5} \times 10^3 \text{ sky}^{-1}$  estimated by Rane et al. (2015) would be produced by only  $\sim 160$ -1600 sources. In this scenario there is no FRB in almost every pixel on the sky, which means one could integrate on most patches forever without seeing an event. Therefore deep surveys are at a disadvantage to those that sweep large regions of the sky (CHIME (Bandura 2014), UTMOST<sup>1</sup>, HIRAX) because the non-repeating scenario is unaffected; shallow observations should not hurt the detection rate, no matter what their repetition. Ideally, a survey needs only to spend a few dispersion delay times on each beam before moving on.

#### 5 CONCLUSIONS

#### 6 ACKNOWLEDGEMENTS

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