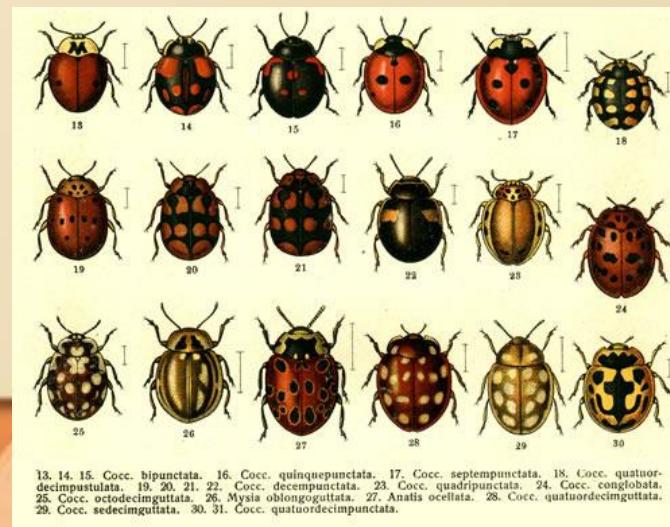
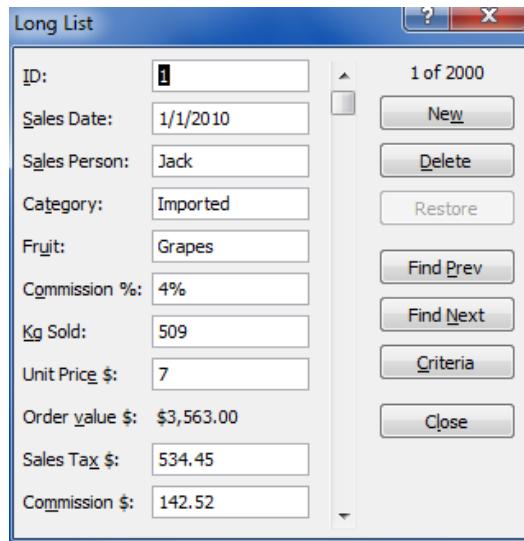


Lecture 1-2

Data Types



Data



User view

An image on the screen

```
salesDate = "1/1/2010";
salesPerson = "Jack";
...
commission = 0.04;
kgSold = 509;
unitPrice = 7;
...
orderSent = true;
...
```

Programmer view

Data is manipulated using variables, statements, ...

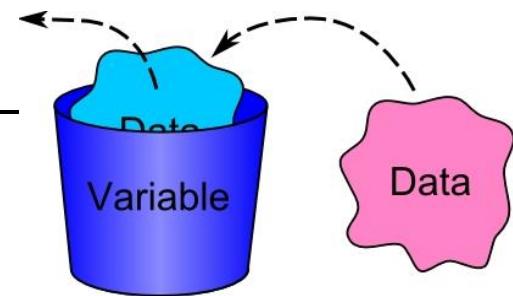
```
...
101000110011100111001100110011001100
1010101001010101010100100101010100
111010100101010010101010101001010100
111100101001010101010100101001010100
1110101001010010100101001010010100010
00000001001001000010100101010010
101000110011100111001100110011001100
11101010010101001010101010101010100
111100101001010101010100101001010100
1110101001010010100101001010010100010
00000001001001000010100101010010
101000110011100111001100110011001100
101010100101010101010010010101010100
111100101001010101010100101001010100
...
```

Computer view

Data is represented as 0's and 1's (bits)

Different representations of the same data

Variables



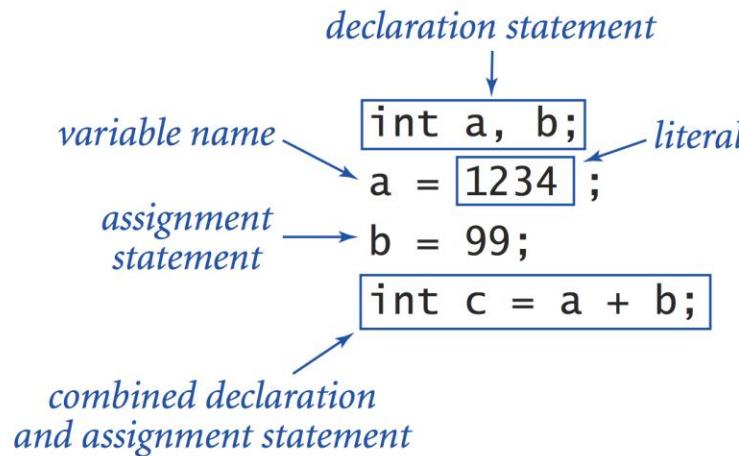
Variable: a container that has a *name*, a *type*, and a *value*

Examples:

```
int x = 17;           // a variable of type int, now holding the value 17  
  
String city = "Herzliya"; // a variable of type String, now holding the value "Herzliya"  
  
double sum = 5012.35;    // a variable of type double, now holding the value 5012.35
```

Code examples:

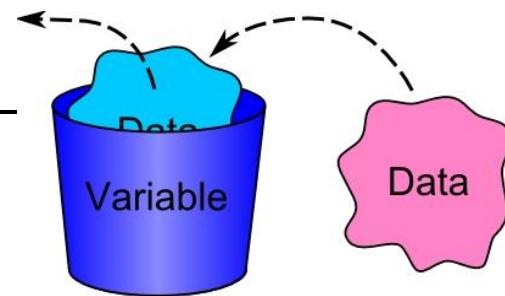
```
...  
int a, b;  
a = 1234;  
b = 99;  
int c = a + b;  
...
```



Variable declaration: a statement that creates (and initializes) a variable

Assignment: a statement that assigns a value to a variable.

Data types



Variable: an abstract container that has a *name*, a *type*, and a *value*

Examples:

```
int x = 17;           // a variable of type int, now holding the value 17  
  
String city = "Herzliya"; // a variable of type String, now holding the value "Herzliya"  
  
double sum = 5012.35;    // a variable of type double, now holding the value 5012.35
```

Code examples:

```
...  
int a, b;  
a = 1234;  
b = 99;  
int c = a + b;  
...
```

Variable declaration: a statement that creates, and optionally initializes, a variable

Assignment: a statement that assigns a value to a variable.

Data types

Data type: Set of possible values, and possible operations

Primitive types

type	set of values	example values	typical operations
int	integer numbers	17 -5034	add, subtract, multiply, divide
double	floating point numbers	3.1415 -171.19	add, subtract, multiply, divide
boolean	truth values	true false	and, or, not
char	characters	'c' 'K' '?' '5' '+'	compare
...			

- Represent “scalar” / single values
- The Java language features eight primitive data types
- Built-into the language

Object types

String	sequences of characters	"xckd" "hello world"	concatenate
Date	dates	03/11/2018	equals, greater than, less than
...			

- Represent “aggregates” of values
- Java libraries feature many object types
- More object types can be created, as needed

Variables

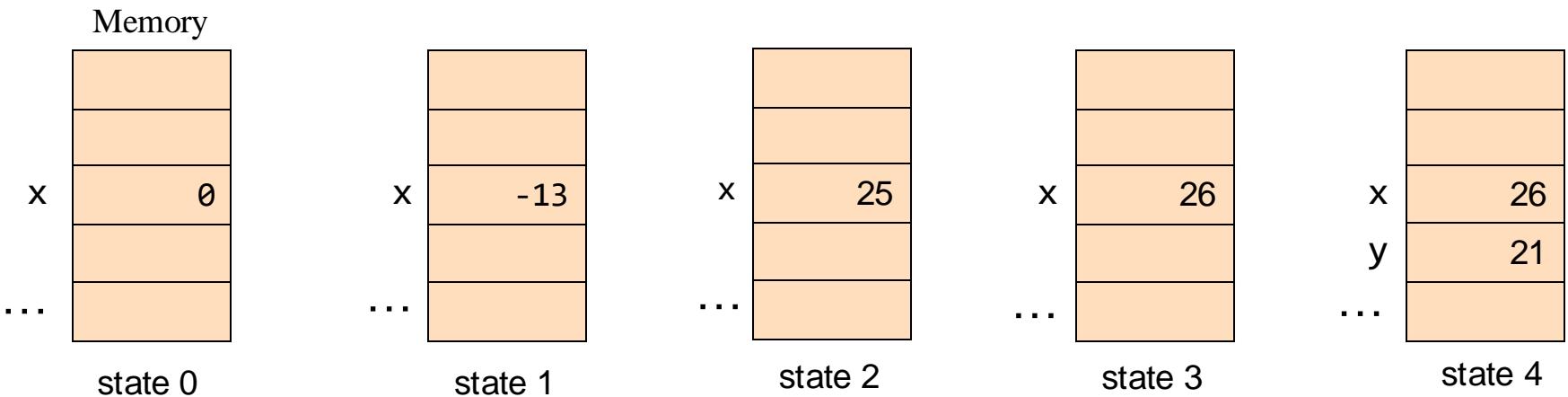
Abstraction

A container that has three properties: *name* (fixed), *type* (fixed), *value* (changing)

```
public class Demo1 {  
    public static void main(String[] args) {  
        int x;          // state 0  
        x = -13;       // state 1  
        x = 25;        // state 2  
        x = x + 1;    // state 3  
        int y = x - 5; // state 4  
    }  
}
```

Implementation

A physical memory location, assigned to represent the variable



Variables

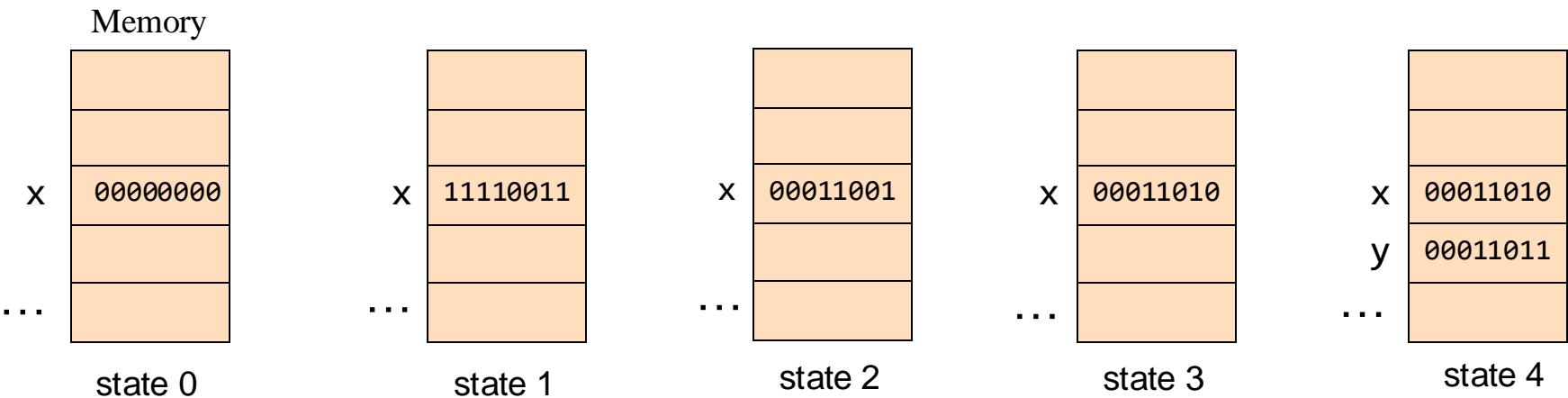
Abstraction

A container that has three properties: *name* (fixed), *type* (fixed), *value* (changing)

```
public class Demo1 {  
    public static void main(String[] args) {  
        int x;          // state 0  
        x = -13;       // state 1  
        x = 25;        // state 2  
        x = x + 1;    // state 3  
        int y = x - 5; // state 4  
    }  
}
```

Implementation (bits...)

A physical memory location, assigned to represent the variable, contains bits



Variable declaration

Examples:

```
int weight;
```

Syntax:

```
type varName;
```

```
int x1, x2, n;
```

```
type varName1, varName2 ... ;
```

```
int z = x + y;
```

```
type varName = expression;
```

- Variables are declared (typed and named) by the programmer, anywhere in the program, as needed
- Can only hold data of the declared type.

The assignment operation

Examples:

```
int x = 5, y = 9;  
...  
x = -3;  
...  
y = x;  
...  
x = y * y - 10 / x + 17;  
...  
int celsius, f;  
f = 120;  
celsius = (f - 32) * 5 / 9;  
...
```

Syntax:

```
variableName = expression;
```

Assignment anatomy:

1. The expression on the right hand side is evaluated
2. The resulting value is assigned to the variable on the left hand side, overwriting its current value

(some languages use `let`, to make the syntax more explicit:

```
let variableName = expression; )
```

f: example of a badly named variable

Notes

- Variable names (and program readability) are critically important
- The assignment operator ‘=’ has nothing to do with algebra’s ‘=’
- What happens if the type of the right hand side does not match the variable’s type?
More about this, later.

Lecture plan

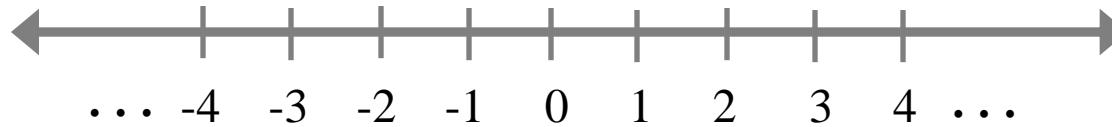


Variables

→ Representing integers: `int`

- Representing text: `string`
- Representing real numbers: `double`
- Representing logical values: `boolean`
- Casting (“data type conversions”)

Integer numbers



Java data types for integers

`byte`: (8 bits), stores integers from -128 to 127

`short`: (16 bits), stores integers from -32,768 to 32,767

`char`: (16 bits), stores integers from 0 to 65535 (used to represent characters, later)

`int`: (32 bits), stores integers from -2,147,483,648 to 2,147,483,647

`long`: (64 bits), stores integers from -9,223,372,036,854,775,808 to
9,223,372,036,854,775,807

As a convention, in this course we'll represent integer numbers using `int`

Typical operations

`a + b` Addition

`a - b` Subtraction

`a * b` Multiplication

`a / b` Integer division

`a % b` Modulo (remainder)

Integer expressions

```
public class Demo2 {  
  
    public static void main(String[] args) {  
  
        System.out.println(5 + 3); // 8  
  
        System.out.println(5 - 3); // 2  
  
        System.out.println(5 * 3); // 15  
  
        System.out.println(5 / 5); // 1  
  
        System.out.println(5 % 3); // 2  
  
        System.out.println(1 / 0); // Run-time error
```

Integer expressions

```
public class Demo2 {  
  
    public static void main(String[] args) {  
  
        System.out.println(5 + 3); // 8  
  
        System.out.println(5 - 3); // 2  
  
        System.out.println(5 * 3); // 15  
  
        System.out.println(5 / 5); // 1  
  
        System.out.println(5 % 3); // 2  
  
        System.out.println(1 / 0); // Run-time error  
  
        System.out.println(3 * 5 - 2); // 13 (* has precedence)  
  
        System.out.println(3 + 5 / 2); // 5 (/ has precedence)  
  
        System.out.println(3 - 5 - 2); // -4 (- associates to the left)  
  
        System.out.println((3 - 5) - 2); // -4 (better style)  
  
        System.out.println(3 - (5 - 2)); // 0 (parentheses have precedence)  
  
    }  
  
}
```

Lecture plan

✓ Variables

✓ Representing integers: `int`

→ Representing text: `string`

- Representing real numbers: `double`
- Representing logical values: `boolean`
- Casting (“data type conversions”)

Textual information

Text:

We hold these truths to be self-evident, that all men are created equal, that they are endowed by their Creator with certain unalienable Rights, that among these are Life, Liberty and the pursuit of Happiness. That to secure these rights, Governments are instituted among Men, ...

DNA:



HTML:

```
<!DOCTYPE html>
<html lang="en-US">
<head>
  <meta charset="UTF-8">
  <link rel="profile" href="http://gmug.org/xfn/11">
  <link rel="pingback" href="https://www.metatags.org/seo-mar
  <meta name="viewport" content="width=device-width, init
  user-scalable=no" />
  <title>Official USA Metatags Website | the secrets of
  <!-- This site is optimized by Metatags.org -->
  <meta name="description" content="Metatags resea
  contain metatags and over />
  <link rel="canonical" href="https://www.metat
  <meta property="og:locale" content="en_US" />
  <meta property="og:type" content="website" />
  <meta property="og:title" content="Offici
  </meta> />
  <!-- description content -->
```

Java:

```
String textSegment =
    "We hold these truths ...";
```

```
String dnaSegment = "ATGTTGCGGCTCGGGGCCAA ...";
```

```
String HTMLSegment =
    "<!DOCTYPE html> <html lang=\"en-US\"> ...";
```

Java represents a sequence of characters using a data type called **String**

Strings

Common operation: concatenation

```
public class Demo3 {  
  
    public static void main(String[] args) {  
  
        String s1 = "Tel";  
        String s2 = "Aviv";  
  
        System.out.println(s1 + s2);          // "TelAviv"  
        System.out.println(s2 + s1);          // "AvivTel"  
        System.out.println(s1 + " " + s2);    // "Tel Aviv"  
        System.out.println(s1 + 3);           // "Tel3"  
        System.out.println(6 + 5);            // 11  
        System.out.println("6" + "5");       // "65"  
        System.out.println("6" + 5);          // "65"  
        System.out.println(2 + " " + 3 + " = " + (2 + 3)); // "2 + 3 = 5"  
    }  
}
```

When a String value is concatenated with a value of *any other type*:

- Java casts the other value as a String
- The type of the resulting expression is a String

Strings

```
// Illustrates "growing" a string
public class Demo4 {
    public static void main(String[] args) {
        String s = "1";           // "1"
        s = s + " 2 " + s;       // "1 2 1"
        s = s + " 3 " + s;       // "1 2 1 3 1 2 1"
        s = s + " 4 " + s;       // etc.
        System.out.println(s);
    }
}
```

```
% java Demo4
```

```
1 2 1 3 1 2 1 4 1 2 1 3 1 2 1
```

Command line arguments

```
public class Demo5 {  
    public static void main(String[] args) {  
        // Performs simple arithmetic operations on two command-line arguments  
        int a = Integer.parseInt(args[0]);  
        int b = Integer.parseInt(args[1]);  
        System.out.println(a + " + " + b + " = " + (a + b));  
        System.out.println(a + " * " + b + " = " + (a * b));  
        System.out.println(a + " / " + b + " = " + (a / b));  
        System.out.println(a + " % " + b + " = " + (a % b));  
    }  
}
```

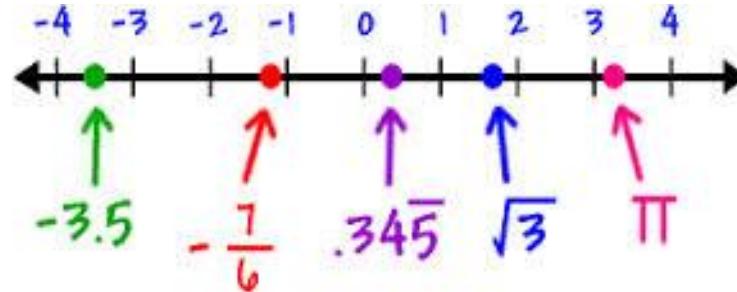
```
% javac Demo5.java  
  
% java Demo5 5 3  
5 + 3 = 8  
5 * 3 = 15  
5 / 3 = 1  
5 % 3 = 2  
  
% java Demo5 12 4  
12 + 4 = 16  
12 * 4 = 48  
12 / 4 = 3  
12 % 4 = 0
```

- Inputs can be entered into a program as *command-line arguments*
- Convention: The command-line arguments are named `args[0]`, `args[1]`, `args[2]`, ...
- The entered values (say, 12, 4) are treated as Strings ("12", "4").
- `Integer.parseInt(String)`: A function that returns a string of digits as an `int`, part of a Java class library named `Integer`.

Lecture plan

- ✓ Variables
- ✓ Representing integers: `int`
- ✓ Representing text: `string`
- Representing real numbers: `double`
 - Representing logical values: `boolean`
 - Casting (“data type conversions”)

Real Numbers



Java data types for approximating real numbers

`float`: Uses 32 bits,
represents values up to 7 digits after the decimal point

`double`: Uses 64 bits,
represents values up to 15 digits after the decimal point

As a convention, in this course we'll represent real numbers using `double`.

The double data type

```
3.141 + 0.03    // 3.171
3.141 - .03     // 3.111
6.02e23 / 2      // 3.01E23
5.0 / 2.0        // 2.5
5 / 2            // 2
5.0 / 2          // 2.5
5 / 2.0          // 2.5
1 / 3            // 0
1.0 / 3.0        // 0.3333333333333333
1.0 / 0.0        // Infinity
1 / 0            // Runtime error
Math.sqrt(2.0)   // 1.4142135623730951
Math.sqrt(-1.0)  // NaN (Not a Number)
```

Scientific notation

Shorthand notation for 3.01×10^{23}

Type of $x \text{ op } y$ (op being $+$, $-$, $*$, $/$):

If either x or y is double, the resulting type is double

Observations

- Computers represent real numbers using finite *numerals* like 3.141592653589793
- Therefore, most real numbers are not represented accurately
- For example, $1/3$ is represented as 0.3333333333333333
- Can lead to exotic bugs (discussed later).

The double data type

```
// Illustrates expressions that use double values.

public class Demo6 {
    public static void main(String[] args) {
        System.out.println(3.141 + .03);          // 3.171
        System.out.println(3.141 - .03);          // 3.111
        System.out.println(6.02e23 / 2);          // 3.01E23
        System.out.println(5.0 / 2.0);            // 2.5
        System.out.println(5 / 2);                // 2
        System.out.println(5.0 / 2);              // 2.5
        System.out.println(5 / 2.0);              // 2.5
        System.out.println(1 / 3);                // 0
        System.out.println(1.0 / 3.0);            // 0.3333333333333333
        System.out.println(1.0 / 0.0);            // Infinity
        System.out.println(1 / 0);                // Runtime error
        System.out.println(Math.sqrt(2.0));        // 1.4142135623730951
        System.out.println(Math.sqrt(-1.0));       // NaN
    }
}
```

(Same examples
in executable form)

Example: Solve the quadratic equation $x^2 + bx + c = 0$

$$\text{roots} = \frac{-b \pm \sqrt{b^2 - 4c}}{2}$$

Inputs: b and c (assumption: the coefficient of x^2 is 1)

$$x^2 - 3x + 2$$

```
% java Quad1 -3.0 2.0
```

2.0

1.0

the two solutions

command-line arguments

$$x^2 - x - 1$$

```
% java Quad1 -1.0 -1.0
```

1.618033988749895

-0.6180339887498949

$$x^2 + x + 1$$

```
% java Quad1 1.0 1.0
```

NaN

NaN

not a number

invalid argument

```
% java Quad1 1.0 hello
```

java.lang.NumberFormatException: hello

missing argument

```
% java Quad1 1.0
```

java.lang.ArrayIndexOutOfBoundsException

Error messages can be cryptic;

But, they actually make sense, and one gets used to them.

Example: Solve the quadratic equation $x^2 + bx + c = 0$

$$\text{roots} = \frac{-b \pm \sqrt{b^2 - 4c}}{2}$$

Inputs: b and c (assumption: the coefficient of x^2 is 1)

```
public class Quad1 {  
    // Computes the roots of the equation x^2 + bx + c = 0  
    public static void main(String[] args) {  
        // Gets and parses b and c from the command-line  
        double b = Double.parseDouble(args[0]);  
        double c = Double.parseDouble(args[1]);  
  
        // Calculates the roots  
        double discriminant = b * b - 4.0 * c;  
        double d = Math.sqrt(discriminant);  
        double root1 = (-b + d) / 2.0;  
        double root2 = (-b - d) / 2.0;  
  
        // Prints the roots  
        System.out.println(root1);  
        System.out.println(root2);  
    }  
}
```

Calling a function from a Java library named Double

Calling a function from a Java library named Math

Calling a function from a Java library named System

In any programming language, a lot of action is done by functions that are called from libraries. The libraries are classes that extend the basic language.

Java's Math library

Offers common math functions:

double abs(double a)	<i>absolute value of a</i>
double max(double a, double b)	<i>maximum of a and b</i>
double min(double a, double b)	<i>minimum of a and b</i>

Note 1: abs(), max(), and min() are defined also for int, long, and float.

double sin(double theta)	<i>sine function</i>
double cos(double theta)	<i>cosine function</i>
double tan(double theta)	<i>tangent function</i>

Note 2: Angles are expressed in radians. Use toDegrees() and toRadians() to convert.

Note 3: Use asin(), acos(), and atan() for inverse functions.

double exp(double a)	<i>exponential (e^a)</i>
double log(double a)	<i>natural log ($\log_e a$, or $\ln a$)</i>
double pow(double a, double b)	<i>raise a to the bth power (a^b)</i>



long round(double a)	<i>round to the nearest integer</i>
double random()	<i>random number in [0, 1)</i>
double sqrt(double a)	<i>square root of a</i>
double E	<i>value of e (constant)</i>
double PI	<i>value of π (constant)</i>

Math.random()

A function that returns a pseudo-random double value,
distributed uniformly in the interval [0,1)

```
public class Demo7 {  
  
    public static void main(String[] args) {  
  
        // prints a random value in [0,1)  
        double x = Math.random();  
        System.out.println(x);  
  
        // prints a random value in [0,2)  
        System.out.println(2.0 * Math.random());  
  
        // prints a random value in [-1,+1)  
        System.out.println(2.0 * Math.random() - 1.0);  
    }  
}
```

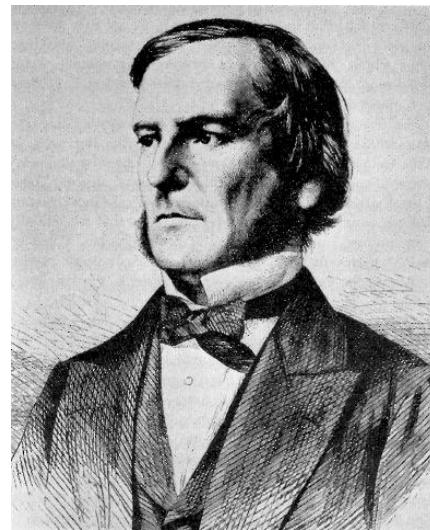
```
% javac Demo7.java  
  
% java Demo7  
  
0.43628266723130604  
1.86291944429295026  
-0.62346234623466346  
  
% java Demo7  
  
0.63453463443333444  
0.88666695959595995  
0.773688444443443434
```

Each program run produces
(with high likelihood...)
different results.

Lecture plan

- ✓ Variables
- ✓ Representing whole, signed numbers: `int`
- ✓ Representing text: `string`
- ✓ Representing real numbers: `double`
- Representing logical values: `boolean`
- Casting (“data type conversions”)

Booleans



George Boole
(1815-1864)

Described a 2-valued
calculus now called
“Boolean logic”

Booleans

Boolean logic is used for:

- Representing and evaluating logical expressions. Example: `(speed > 120)`
- Controlling program flow. Example: `if (speed > 120) {
 giveTicket(licenseNumber)
}`

The boolean data type

Two values only:

`true`

`false`

The boolean data type

Examples

```
...
String city = "";
int age = 0;

// Gets city and age data from the user (code omitted)
// Checks city
if (city == "Tel Aviv") System.out.println("you are paying too much rent");

// Checks age
if (age < 18) System.out.println("you are too young for this");

// Same effect (makes sense if we have to age-check many times):
boolean tooYoung = age < 18;
if (tooYoung) System.out.println("you are too young for this");

...

// Checks the parity of x
if ((x % 2) == 0) System.out.println(x + " is even");
else             System.out.println(x + " is odd");
...
```

if and **if/else** statements: Will be discussed in the next lecture.

Boolean operators

Examples

```
(b * b - 4.0 * a * c) >= 0    // Nonnegative?  
(year % 100) == 0                // Beginning of a century?  
x != 1                          // Not equal 1?
```

Boolean expressions: $x \text{ op } y$ where:

x and y are compatible Java expressions and op is $==$, $!=$, $<$, \leq , $>$, \geq

<i>op</i>	<i>meaning</i>	<i>true</i>	<i>false</i>
$==$	<i>equal</i>	$2 == 2$	$2 == 3$
$!=$	<i>not equal</i>	$3 != 2$	$2 != 2$
$<$	<i>less than</i>	$2 < 13$	$2 < 2$
\leq	<i>less than or equal</i>	$2 \leq 2$	$3 \leq 2$
$>$	<i>greater than</i>	$13 > 2$	$2 > 13$
\geq	<i>greater than or equal</i>	$3 \geq 2$	$2 \geq 3$

Boolean connectors (Not, And, Or)

! (not)

a	!a
false	true
true	false

Truth table: gives the output of a Boolean function
(in this case, Not, And, Or) for every possible input

&& (and)

a	b	a && b
false	false	false
false	true	false
true	false	false
true	true	true

|| (or)

a	b	a b
false	false	false
false	true	true
true	false	true
true	true	true

In other words

$!a$ is true iff a is false

$(a \&\& b)$ is true iff both a and b are true

$(a || b)$ is true iff either a or b or both are true

Example: leap year

Task: determine if a given year is a leap year (שנה מעוברת)

Rule: yes if the year is (i) divisible by 400 or
(ii) divisible by 4 but not by 100

```
public class LeapYear {  
    public static void main(String[] args) {  
        int year = Integer.parseInt(args[0]);  
        boolean isLeapYear;  
  
        // Checks if the year is divisible by 400  
        isLeapYear = ((year % 400) == 0);  
  
        // Then checks if the year is divisible by 4 but not by 100  
        isLeapYear = isLeapYear || (((year % 4) == 0) && ((year % 100) != 0));  
  
        System.out.println(isLeapYear);  
    }  
}
```

```
% java LeapYear 2020  
true
```

```
% java LeapYear 1900  
false
```

```
% java LeapYear 2028  
true
```

Example: leap year

Task: determine if a given year is a leap year (שנה מעוברת)

Rule: yes if the year is (i) divisible by 400 or
(ii) divisible by 4 but not by 100

```
public class LeapYear {  
    public static void main(String[] args) {  
        int year = Integer.parseInt(args[0]);  
        boolean isLeapYear;  
  
        // Checks if the year is divisible by 400  
        isLeapYear = ((year % 400) == 0);  
  
        // Then checks if the year is divisible by 4 but not by 100  
        isLeapYear = isLeapYear || (((year % 4) == 0) && ((year % 100) != 0));  
  
        System.out.println(isLeapYear);  
    }  
}
```

```
// Same as:  
leapYear = ((year % 400) == 0) || ((year % 4) == 0) && ((year % 100) != 0);
```

Lecture plan

- ✓ Variables
- ✓ Representing whole, signed numbers: `int`
- ✓ Representing text: `string`
- ✓ Representing real numbers: `double`
- ✓ Representing logical values: `boolean`
- Casting (also known as “data type conversions”)

Casting

What happens when we create an expression made of different data types?

- In some cases Java handles the resulting type *implicitly* (example: `5.0 / 2`)
- In other cases the programmer must handle the resulting type *explicitly*

Implicit casting (examples)

```
"1234" + 99           // "123499" (String)  
  
11 * 0.3              // 3.3 (double)
```

Explicit casting (examples)

```
Integer.parseInt("123") // 123 (int)  
  
(int) 2.71828          // 2 (int)  
  
(int) 11 * 0.3         // 3.3 (double)  
  
(11 * (int) 0.3)      // 0 (int)  
  
(int) (11 * 0.3)      // 3 (int)
```

Casting

What happens when we create an expression made of different data types?

- In some cases Java handles the resulting type *implicitly* (example: `5.0 / 2`)
- In other cases the programmer must handle the resulting type *explicitly*

```
public class Demo8 {  
    public static void main(String[] args) {  
  
        System.out.println("1234" + 99);           // "123499" (String)  
  
        System.out.println(11 * 0.3);              // 3.3 (double)  
  
        System.out.println(Integer.parseInt("123")); // 123 (int)  
  
        System.out.println((int) 2.71828);         // 2 (int)  
  
        System.out.println((int) 11 * 0.3);          // 3.3 (double)  
  
        System.out.println((11 * (int) 0.3));       // 0 (int)  
  
        System.out.println((int) (11 * 0.3));        // 3 (int)  
    }  
}
```

(Same examples in executable form)

Casting

Example: generate a random integer in the range [0,N), where N is a command-line argument

Basic idea: Use `Math.random()` to create a random `double` value in [0,1),
then manipulate this value to create an `int` in the range [0,N).

```
public class RandomInt {  
    // Generates a random integer from 0,...,N-1  
    public static void main(String[] args) {  
        // Gets N from the user  
        int N = Integer.parseInt(args[0]);  
        double r = Math.random();  
        int n = (int) (r * N);  
        System.out.println("random integer is " + n);  
    }  
}
```

Explicit casting: Converts the value on the right to an `int` (ignoring the value after the decimal point)

Implicit casting:
`double * int` gives `double`

Explicit casting: `args[0]`, which is a `String`, is cast as `int`, using a function call.

Implicit casting: `String + int` gives `String`

```
% java RandomInt 10  
random integer is 6
```

```
% java RandomInt 10  
random integer is 2
```

```
% java RandomInt 35  
random integer is 32
```

```
% java RandomInt 10000  
random integer is 2184
```

Summary

Java data types (discussed in this lecture)

- `int, double` for mathematical calculations
- `String` for text processing
- `boolean` for logical expression and controlling program flow
- ...

Java is a “strongly-typed” language

- Variables must be declared before they are used, and proper use is checked by the compiler
- When needed, type conversion is done either
 - *implicitly* (by the compiler), or
 - *explicitly* (by the programmer)

Watch out:

Programmers must be alert to potential exotic bugs resulting from implicit casting



Arianne 5 rocket crash (1996):
Cause: type cast error.

Overflow and rounding off errors

```
public class Demo9 {  
    public static void main(String[] args) {  
        System.out.println(100000 * 100000 * 100000);  
        System.out.println(1.03 - 0.42);  
        System.out.println(1.00 - 9 * .10);  
        System.out.println((0.7 + 0.1) == (0.9 - 0.1));  
    }  
}
```

Expected results

```
% java Demo9  
1000000000000000  
0.61  
0.1  
true
```

Actual results

```
% java Demo9  
-1530494976  
0.610000000000001  
0.0999999999999998  
false
```

Explanation: Computers represent numbers using a fixed number of bits (0's and 1's). Results:

- Overflow / underflow
- Many real values are not represented accurately.



What to do?

- **Be aware**
- Study the application's requirements
- If necessary, write code that handles rounding-off errors
- Test extreme values
- If exact values are important, there are solutions. But, these solutions may make the program less efficient.