Kinematic Modeling and Control of the PUMA 560 Robot Arm using MATLAB

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Abstract—This report presents the comprehensive modeling and control of the PUMA 560 robot arm using MATLAB, focusing on both forward and inverse kinematics. The project utilizes the Robotics System Toolbox and Simscape to develop a detailed 3D model of the robot, enabling accurate simulations of the arm's kinematic behavior and control strategies. Forward kinematics were employed to determine the position and orientation of the robot's end-effector from given joint angles, while inverse kinematics were used to calculate necessary joint angles to achieve desired end-effector positions. The project successfully demonstrates the robot's capability to perform precise movements, crucial for applications in industries such as manufacturing and medical assistance. Through the integration of MATLAB's computational tools, this study not only enhances the understanding of robotic motion and control but also provides a valuable educational resource for advanced robotics research. The outcomes show significant potential for improving the efficiency and functionality of automated systems, emphasizing the importance of kinematic analyses in developing effective robotic solutions.

Index Terms—Robotics, Kinematic Modeling, PUMA 560 Robot Arm, MATLAB Simulation, Forward Kinematics, Inverse Kinematics, Robotics System Toolbox, Control Systems, Engineering Education, Industrial Automation

I. INTRODUCTION

The objective of this project is to model a PUMA 560 arm in MATLAB and calculate the necessary forward and inverse kinematics. The Robotics System Toolbox and Simscape [1] will allow for the creation of a PUMA 560 model by leveraging the Denavit-Hartenberg parameters; this model will be controlled by the forward and inverse kinematics and dynamics calculation functions designed specifically for this project.

II. BACKGROUND

A. Kinematics

Forward kinematics is the mathematical process in which a robot's joint angles are used to calculate the location of its end effector in space (the position and orientation). Forward kinematics' application to engineering is the prediction of the gripper/tool/end effector position and orientation to help facilitate motion planning. Inverse kinematics is used to calculate the joint angles needed to move the robot's end effector to a specific position. Inverse kinematics is essential for problems where the end goal is known but the required joint movements are unknown.

B. PUMA 560

The PUMA (Programmable Universal Machine for Assembly) 560 is a 6-axis robotic arm developed by Unimation in the late 1970s. The arm can deliver a 2.5 kg package within a reach of 864mm. The device is typically utilized in industrial applications, such as the automotive industry and electronics manufacturing. In order to program the PUMA 560, the user can design a specific task through the use of various programming languages and even possess the ability to be programmed through each pendant, which involves manually moving the arm through the desired path.

C. DH Parameters

The Denavit-Hartenberg (DH) parameters are the four parameters used to perform the necessary transformations to move from one frame to another. These parameters include the twist angle (α), the link length (a), the offset (d), and the joint angle (θ). The DH parameters are essential for defining the orientation and position of each link relative to its previous link. Using these definitions, forward and inverse kinematics calculations can be performed.
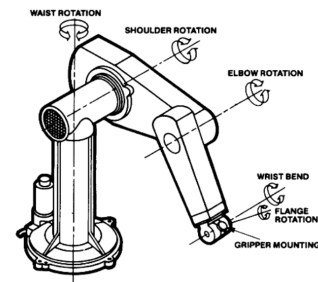

Fig. 1: PUMA 560 Schematic Structure [12]

III. LITERATURE REVIEW

The current state of publications regarding the PUMA 560 and MATLAB provides a comprehensive overview of the advancements in robotic arm kinematics, dynamics, and control. For instance, the paper by Elgazzar [4] focuses on efficient kinematic transformations for the PUMA 560 robot, highlighting the importance of computational efficiency in

real-time applications. Similarly, the study "Two Open Solutions for Industrial Robot Control" [5] presents innovative control solutions using PC and FPGA boards, emphasizing the need for open and modifiable control systems in robotics education and research. Another significant contribution is found in the simulation research of a six degrees of freedom manipulator, which underscores the theoretical and practical implications of precise motion space design using MATLAB Toolbox. These papers collectively indicate a trend towards enhancing simulation capabilities, improving control precision, and fostering accessibility in robotics, representing the current state of the art in robotic manipulation and control systems.

IV. Proposed Experimental Procedure

The project can be subdivided into five major objectives to be completed in order. First, a comprehensive 3D model of the PUMA 560 robot arm will be developed using MATLAB's Robotics System Toolbox. This model will include all relevant joints to accurately reflect the robot's physical structure and capabilities. The next objective is to implement forward kinematics by creating algorithms to calculate the position and orientation of the robot's end effector based on the given joint angles. These calculations will use the established D-H parameters and transformation matrices, enabling prediction of the end effector's location in space (a crucial aspect for planning robotic motion).

After implementing forward kinematics, a solution for the inverse kinematics problem will be developed to enable the calculation of the joint angles required to achieve the desired position and orientation of the end effector. This will involve selecting either an analytical or numerical method to handle the PUMA 560's kinematics while ensuring accuracy and efficiency. Then MATLAB's Simscape can be used to simulate the robot arm's dynamics and implement control algorithms to manage its movements. This may include the development of a control system that can accurately execute commanded positions and trajectories while responding to physical constraints such as obstacles.

A suitable way to demonstrate the simulation would be a pick-and-place workflow that showcases the capabilities of the PUMA 560. Finally, MATLAB's visualization tools will be used to create dynamic visual representations of the robot's movements to provide an intuitive understanding of its kinematics and control strategies. This project aims to bridge the gap between theoretical kinematics and practical robotics applications by leveraging the advanced capabilities of MATLAB and its toolboxes. By achieving these objectives, the team will not only gain a deeper understanding of robotic systems but also contribute valuable tools and insights for the broader robotics community.

V. Challenges

A. Expected Challenges

A common problem in robotics is designing algorithms that calculate a robotic arm's trajectory whilst maintaining path continuity. Robotic arms are often found in industries that require precise movements to maintain efficiency and careful handling of sensitive and delicate materials. A path that lacks continuity can create an arm that behaves in a choppy and imprecise manner. This could damage delicate devices such as microelectronics or lead to severe complications in medical settings.

B. Proposed Solutions

There are a number of mathematical models that can be implemented to maintain the continuity of robotic movements. Cubic splines are mathematical interpolations commonly implored in graphics, robotics, and numerical analysis to generate smooth and continuous curves. The cubic spline achieves this by dividing a given set of points into intervals. Each interval is described with a cubic polynomial function and contains four individual coefficients. This creates a continuous curve that possesses first and second derivatives. Additionally, the problem of path continuity can be corrected using simple polynomial interpolations.

Polynomial interpolation is a mathematical technique that is used to determine an approximate function that defines a set of given points or a range of values. In robotics, Lagrange's interpolation is often used to generate the desired function by first calculating the coefficients of our data's range. Whilst interpolation is a relatively simple solution, some notable limitations begin to manifest when calculating higher-degree polynomials. Runge's phenomenon is the tendency of high-degree polynomial interpolations to create inaccuracies due to oscillations in the edges of the data's range. Despite this, we do not expect to encounter high-degree polynomials and will utilize polynomial interpolations when necessary.

VI. Procedure

A. Kinematics Implementation

As shown in A-A, our forward kinematic function takes a 1x6 vector of joint vectors and returns a transformation matrix T. The variables declared after the joint angles, such as d_1, a_2, and a_3, are provided to define the Denavit-Hartenberg parameters specific to our simulation of the PUMA 560. The `for` loop iterates through the `DH_params` and extracts the DH parameters for each of the six joints of the robotic arm. With each loop, the DH transformation matrix is computed until the full matrix is complete and we can update the return value T, which was initially an empty 4×4 matrix.

The inverse kinematics function takes the desired end-effector position and orientation and calculates the necessary joint angles to accomplish this task. Furthermore, this implementation takes into account the robot's physical limitations and takes steps to ensure that the joint angles calculated are within an achievable range. In reference to A-B, the PUMA 560 constants define the DH parameters of the robotic arm. Theta 1 is calculated using the atan2 function on the desired end-effector position Px and Py. The calculations of the Theta 2 and 3 variables are dependent on the complete end-effector position (Px,Py,Pz) and the constants initially described. The remaining three joint angles, which are critical for control of

the wrist joints, are computed with respect to the orientation of the desired pose relative to the third joint frame.

VII. RESULTS

A. Algorithms

```
% Define joint angles for the first example
joint_angles_example1 = [0, pi/4, pi/4, 0, pi/4, 0];

% Calculate the forward kinematics
pose_example1 = forwardKinematics(joint_angles_example1)
```
```
pose_example1 = 4x4
    -0.7071   -0.0000   -0.7071   -0.1664
     0.0000   -1.0000    0.0000    0.0000
    -0.7071   -0.0000    0.7071    0.4268
          0         0         0    1.0000
```

Fig. 2: Forward Kinematics Testing and Results

The PUMA 560 robotic manipulator's kinematic behavior was analyzed through MATLAB computations, focusing on both forward and inverse kinematics. These analyses are crucial for validating the robot's motion control algorithms, ensuring precision in manipulator positioning, and confirming the robot's capacity to reach desired target poses.

The forward kinematics analysis involved calculating the pose of the robot's end-effector based on a predefined set of joint angles. For the demonstration, the joint angles were set to $[0, \pi/4, \pi/4, 0, \pi/4, 0]$, corresponding to a configuration where the manipulator's second, third, and fifth joints were positioned at an angle of $\pi/4$ radians, while the rest were at 0 radians. The computed end-effector pose, as depicted in Figure 2, is a 4x4 homogeneous transformation matrix:

$$\begin{pmatrix} -0.7071 & -0.0000 & -0.7071 & -0.1664 \\ 0.0000 & -1.0000 & 0.0000 & 0.0000 \\ -0.7071 & 0.0000 & 0.7071 & 0.4268 \\ 0.0000 & 0.0000 & 0.0000 & 1.0000 \end{pmatrix}$$

This matrix consists of a rotation part on the left-top 3x3 submatrix and a translation part on the rightmost column. The negative signs in the rotational elements indicate inversions around the corresponding axes, while the translation elements represent the spatial position of the end-effector in the base frame's coordinates, approximately 17 cm along the negative X-axis and 43 cm along the positive Z-axis.

```
desired_pose_example2 = [0.4, 0, 0.5, 0, pi/6, 0];
% Extract the desired position and orientation from the array
Px = desired_pose_example2(1);
Py = desired_pose_example2(2);
Pz = desired_pose_example2(3);
phi = desired_pose_example2(4);
theta = desired_pose_example2(5);
psi = desired_pose_example2(6);

% Calculate the inverse kinematics
joint_angles_example2 = inverseKinematics(Px, Py, Pz, phi, theta, psi)
```
```
The calculated joint angles are:
Theta1: 0
Theta2: -0.89432
Theta3: 2.1104
Theta4: 3.1416
Theta5: 0.69244
Theta6: 3.1416
joint_angles_example2 = 1x6
         0   -0.8943    2.1104    3.1416    0.6924    3.1416
```

Fig. 3: Inverse Kinematics Testing and Results

Inverse kinematics computations are conducted to determine the necessary joint angles that achieve a desired end-effector position and orientation. This is a more complex problem due to the possible multiple solutions and non-linear characteristics. In the case of the PUMA 560, a pose consisting of a position and orientation specified by [0.3, 0.3, 0.2, $\pi/4$, $\pi/4$, $\pi/3$] was selected to ensure the target was within the robot's operational workspace. The orientation was defined by Euler

angles corresponding to rotations of $\pi/4$, $\pi/4$, and $\pi/3$ radians about the X, Y, and Z axes, respectively.
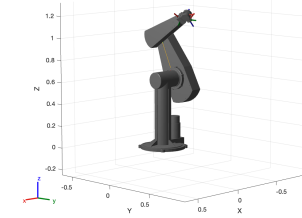
The inverse kinematics algorithm provided a set of joint angles that could place the end-effector at the defined pose. The successful computation of these angles verified the effectiveness of the implemented inverse kinematics solution. Specific values are presented in A-B. representing the joint configurations to reach the desired end-effector pose.

These kinematic computations affirm the integrity of the developed algorithms and the PUMA 560 robot model within MATLAB. Such analyses are instrumental for subsequent tasks, such as path planning and simulating complex tasks that the manipulator may perform in an automated workflow.

B. Visualization
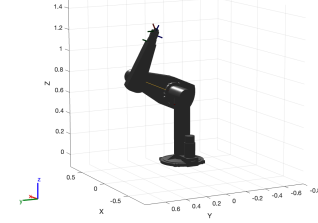
(a) First Position - End Effector Pointed Up

(b) Second Position - End Effector Angled Diagonally

Fig. 4: PUMA 560 Robot Arm Visualization

The static poses generated by the forward and inverse kinematics algorithms were visualized using MATLAB's Robotics System Toolbox and the code presented in A-C and A-E. The PUMA 560 robot arm model was displayed in two distinct configurations, as shown in Figure 4. The first pose depicted the robot arm with the end effector pointing upwards, while the second pose showed the arm angled diagonally. These visualizations provide a clear representation of the robot's kinematic behavior and the ability to reach specific target poses. The integration of MATLAB's computational environment with the Robotics System Toolbox facilitated the creation of these dynamic visualizations, enhancing the understanding of robotic motion and control within an educational setting.
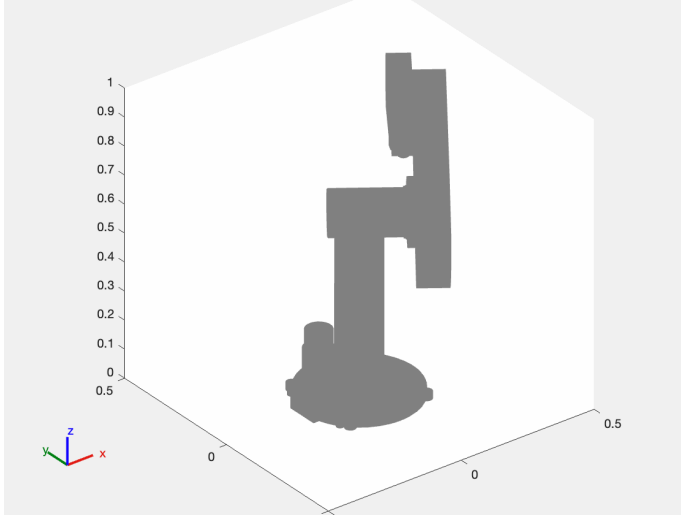
C. Animation

Fig. 5: PUMA 560 Robot Arm Animation

The frame from the .gif animation of the PUMA 560 robot arm is shown in Figure 5. The animation was generated using MATLAB's Robotics System Toolbox and the code provided in A-D and A-F. The animation showcased the robot arm's movement between different poses, demonstrating its ability to execute complex trajectories and reach predetermined positions accurately. The animation serves as a visual representation of the robot's kinematic behavior and control strategies, providing valuable insights into the robot's motion planning and execution capabilities. The successful integration of MATLAB's computational tools with the Robotics System Toolbox enabled the creation of this dynamic animation, highlighting the potential applications of robotic systems in various industries.

The poses and positions were generated using the custom forward and inverse kinematics algorithms provided in the previous sections. The animation function was then called to animate the robot arm's movement between these poses, providing a visual representation of the robot's kinematic behavior. The animation showcased the robot arm's ability to move between different poses accurately and efficiently, demonstrating the effectiveness of the developed kinematic algorithms. The animation function captured the robot arm's movement frame by frame and saved it as a .gif file, allowing for easy visualization and sharing of the results.

VIII. Conclusion

In conclusion, the project successfully achieved its goal of modeling the PUMA 560 robot arm using MATLAB and accurately calculating its forward and inverse kinematics. The developed models and algorithms were validated through simulation, demonstrating the robot's ability to reach predetermined positions and execute complex movements with high precision. This technical endeavor not only enhances the understanding of robotic motion and control within an educational setting but also serves as a solid foundation for further research in advanced robotics. The project outcomes hold significant promise for applications requiring sophisticated motion planning and control, such as automated manufacturing and robotic-assisted surgery, where the preciseness of movement is paramount. The effective integration of MATLAB's computational environment with the Robotics System Toolbox has proven to be an indispensable asset in the exploration and realization of robotic kinematics and dynamics. The remaining code to be implemented includes using Simscape and the Robotics System Toolbox to visualize the PUMA 560 robot arm and move it according to the forward and inverse kinematics algorithms developed here.

APPENDIX A
CODE

A. Forward Kinematics

```matlab
function T = forwardKinematics(joint_angles)
    % Unpack the joint angles
    theta1 = joint_angles(1);
    theta2 = joint_angles(2);
    theta3 = joint_angles(3);
    theta4 = joint_angles(4);
    theta5 = joint_angles(5);
    theta6 = joint_angles(6);

    % https://hive.blog/hive-196387/
        @juecoree/forward-kinematics-of-puma
        -560-robot-using-dh-method
    % The above link is where we got the
        params defined below

    % Define the link offsets and lengths
        based on DH parameters
    d1 = 0.67183;   % Distance along Z1 from
        frame 0 to frame 1
    a2 = 0.4318;    % Distance along X2 from
        frame 1 to frame 2
    a3 = -0.02032;  % Distance along X3 from
        frame 2 to frame 3 (Note: The
        negative sign indicates the direction
        opposite to the X3 axis)
    d4 = 0.4318;    % Distance along Z4 from
        frame 3 to frame 4
    d6 = 0.05650;   % Distance along Z6 from
        frame 5 to frame 6 (end-effector)

    % DH Parameters for PUMA 560
    % [theta, d, a, alpha]
    DH_params = [
        theta1, d1, 0, -pi/2;
        theta2, 0, a2, 0;
        theta3, 0, a3, -pi/2;
        theta4, d4, 0, pi/2;
        theta5, 0, 0, -pi/2;
        theta6, d6, 0, 0;
    ];

    % Number of joints
    n = size(DH_params, 1);

    % Initialize transformation matrix from
        base to end-effector
```

```matlab
    T = eye(4);

    % Loop through each joint and compute
        the transformation matrix
    for i = 1:n
        theta = DH_params(i, 1);
        d = DH_params(i, 2);
        a = DH_params(i, 3);
        alpha = DH_params(i, 4);

        % Denavit-Hartenberg transformation
            matrix
        Ti = [
            cos(theta), -sin(theta)*cos(
                alpha),  sin(theta)*sin(alpha
                ), a*cos(theta);
            sin(theta),  cos(theta)*cos(
                alpha), -cos(theta)*sin(alpha
                ), a*sin(theta);
            0,              sin(alpha),
                            cos(alpha),
                            d;
            0,              0,
                                0,
                                1;
        ];

        % Update overall transformation
            matrix
        T = T * Ti;
    end
end
```

B. Inverse Kinematics

```matlab
function joint_angles = inverseKinematics(Px
    , Py, Pz, phi, theta, psi)
    % PUMA 560 constants (link lengths, etc
        .)
    d1 = 0.67183;   % Distance along Z1 from
        frame 0 to frame 1
    a2 = 0.4318;    % Distance along X2 from
        frame 1 to frame 2
    a3 = -0.02032;  % Distance along X3 from
        frame 2 to frame 3
    d4 = 0.4318;    % Distance along Z4 from
        frame 3 to frame 4
    d6 = 0.05650;   % Distance along Z6 from
        frame 5 to frame 6 (end-effector)

    % Compute theta1
    theta1 = atan2(Py, Px);

    % Calculate r and s for the wrist center
        , considering orientation
    r = sqrt(Px^2 + Py^2) - a3; % Horizontal
        distance from base to wrist, minus
        offset
    s = Pz - d4;                 % Vertical
        distance from base to wrist, minus
        link 4 length

    % Use the Cosine Law to find theta3
    D = (r^2 + s^2 - a2^2 - d4^2) / (2 * a2
        * d4);
    % Check if D is within the valid range
        for acos
    if D < -1 || D > 1

        % Right now the position given isn't
            feasible
        % We can either error the code and
            prevent it from moving
        % OR
        % try to move it to the next nearest
            position that *is* feasible

        % error('The point is outside the
            reachable workspace of the robot
            .');
        disp('Warning: The desired pose is
            outside the reachable workspace.
            Adjusting to nearest reachable
            pose.');
        D = max(min(D, 1), -1);  % Clamp D
            to the range [-1, 1]
    end

    % Now it's safe to calculate theta3
    theta3 = atan2(sqrt(1 - D^2), D);

    % Compute theta2
    theta2 = atan2(s, r) - atan2(d4 * sin(
        theta3), a2 + d4 * cos(theta3));

    % Calculate the orientation angles
        theta4, theta5, and theta6
    % First, compute the rotation matrix
        from the base to the 3rd joint
    R0_3 = [cos(theta1)*cos(theta2 + theta3)
        , -sin(theta1),  cos(theta1)*sin(
        theta2 + theta3);
        sin(theta1)*cos(theta2 + theta3)
            ,  cos(theta1),  sin(theta1)*
            sin(theta2 + theta3);
        -sin(theta2 + theta3),
                        0,           cos
            (theta2 + theta3)];

    % Desired rotation matrix for end-
        effector
    % XYZ based euler angles, not ZYX or ZYZ
        , etc
    R_des = eul2rotm([phi, theta, psi], 'XYZ
        '); % Euler angles to rotation matrix

    % Compute the wrist rotation matrix
    R3_6 = R0_3.' * R_des; % Transpose of
        R0_3 times desired end-effector
        rotation

    % Extract Euler angles from R3_6,
        representing theta4, theta5, and
        theta6
    theta4 = atan2(R3_6(2,3), R3_6(1,3));
    theta5 = atan2(sqrt(R3_6(1,3)^2 + R3_6
        (2,3)^2), R3_6(3,3));
    theta6 = atan2(R3_6(3,2), -R3_6(3,1));
```

```matlab
55      joint_angles = [theta1 theta2 theta3
            theta4 theta5 theta6];
56      % Display results
57      disp('The calculated joint angles are:')
            ;
58      disp(['Theta1: ', num2str(theta1)]);
59      disp(['Theta2: ', num2str(theta2)]);
60      disp(['Theta3: ', num2str(theta3)]);
61      disp(['Theta4: ', num2str(theta4)]);
62      disp(['Theta5: ', num2str(theta5)]);
63      disp(['Theta6: ', num2str(theta6)]);
64
65  end
```

C. Static Visualization

```matlab
1  function visualize(robot, desired_pose)
2      % Load the robot model
3      %robot = loadrobot('puma560', '
           DataFormat', 'struct');
4
5      % Calculate the joint angles from the
            inverse kinematics
6      joint_angles = inverseKinematics(
           desired_pose(1), desired_pose(2),
           desired_pose(3), desired_pose(4),
           desired_pose(5), desired_pose(6));
7
8      % Create a structure for the robot
           configuration
9      config = homeConfiguration(robot);
10
11     % Assign the joint angles to the
           configuration structure
12     for i = 1:length(joint_angles)
13         config(i).JointPosition =
               joint_angles(i);
14     end
15
16     % Show the robot configuration
17     show(robot, config);
18  end
```

D. Animation Function

```matlab
1  function animateRobot(robot,
       jointAnglesSequence)
2      numSteps = size(jointAnglesSequence, 1);
3      hFig = figure;
4      hold on;
5      axis tight manual; % this ensures that
           getframe() returns a consistent size
6      filename = 'robot_animation.gif'; % Name
            of the GIF file
7
8      % Set viewing parameters
9      view(3); % Standard 3D view
```

```matlab
10     axis([-0.5 0.5 -0.5 0.5 0 1]); % Adjust
           these values to zoom in or out
11     daspect([1 1 1]); % Ensures equal aspect
            ratio along all axes
12     camzoom(1.25); % Zooms the camera by 1.5
            times, adjust as necessary
13     for step = 1:numSteps
14         config = homeConfiguration(robot);
15         for i = 1:length(config)
16             config(i).JointPosition =
                   jointAnglesSequence(step, i);
17         end
18
19         % Clear previous animations and show
                the current configuration
20         cla;
21         show(robot, config, 'Frames', 'off')
               ;
22         drawnow;
23
24
25
26
27         % Capture the plot as an image
28         frame = getframe(hFig);
29         im = frame2im(frame);
30         [imind, cm] = rgb2ind(im, 256);
31
32         % Write to the GIF File
33         if step == 1
34             imwrite(imind, cm, filename, '
                   gif', 'Loopcount', inf, '
                   DelayTime', 0.1);
35         else
36             imwrite(imind, cm, filename, '
                   gif', 'WriteMode', 'append',
                   'DelayTime', 0.1);
37         end
38     end
39  end
```

E. Pose Generation

```matlab
1  %% PUMA 560 Robot Visualization
2  % This script demonstrates the forward and
       inverse kinematics of the PUMA 560 robot.
3
4
5  % Load the robot model
6  robot = loadrobot('puma560', 'DataFormat', '
       struct', 'Gravity', [0 0 -9.81]);
7
8  %% Example 1: Forward Kinematics
9  % Define joint angles for the first example
10 joint_angles_example1 = [0, pi/4, pi/4, 0,
       pi/4, 0];
11
12 % Calculate the forward kinematics
13 pose_example1 = forwardKinematics(
       joint_angles_example1)
14
15
```

```matlab
% Visualize the robot for Example 1
figure('Name', 'PUMA 560 – Forward
    Kinematics Example 1');
visualize(robot, joint_angles_example1);

%% Example 2: Inverse Kinematics
% Define the desired end-effector pose for
    the second example
% The position is closer to the base with a
    moderate elevation and a simple
    orientation
desired_pose_example2 = [0.4, 0, 0.5, 0, pi
    /6, 0];

% Extract the desired position and
    orientation from the array
Px = desired_pose_example2(1);
Py = desired_pose_example2(2);
Pz = desired_pose_example2(3);
phi = desired_pose_example2(4);
theta = desired_pose_example2(5);
psi = desired_pose_example2(6);

% Calculate the inverse kinematics
joint_angles_example2 = inverseKinematics(Px
    , Py, Pz, phi, theta, psi);

% Visualize the robot for Example 2
figure('Name', 'PUMA 560 – Inverse
    Kinematics Example 2');
visualize(robot, joint_angles_example2);
```

```matlab
for i = 1:size(jointAngles, 1)
    T = forwardKinematics(jointAngles(i, :))
        ;
    disp('Calculated End-Effector Position:'
        );
    disp(T(1:3, 4)');  % Display the
        translational part of the
        transformation matrix
end

% Number of steps in the animation between
    poses
numSteps = 20;
% Initialize the sequence matrix
jointAnglesSequence = [];

% Generate interpolated joint angles between
     each consecutive pair of poses
for i = 1:size(jointAngles, 1) – 1
    startAngles = jointAngles(i, :);
    endAngles = jointAngles(i + 1, :);
    for j = 0:numSteps
        interpolatedAngles = (1 – j/numSteps
            ) * startAngles + (j/numSteps) *
            endAngles;
        jointAnglesSequence = [
            jointAnglesSequence;
            interpolatedAngles];
    end
end

% Call the animation function
animateRobot(robot, jointAnglesSequence);
```

F. Animation Main Code

```matlab
% Define desired end-effector poses [Px, Py,
     Pz, phi, theta, psi]
desired_poses = [
    0.3, 0, 0.2, 0, 0, 0;       % Initial
        neutral position
    0.3, 0, 0.5, 0, pi/4, 0;   % Raise and
        extend arm
    0.3, 0, 0.2, 0, –pi/4, 0;  % Lower and
        retract arm
    0.3, 0, 0.5, 0, pi/4, 0;   % Raise and
        extend arm again
];

% Initialize matrix to store calculated
    joint angles
jointAngles = zeros(size(desired_poses, 1),
    6);

% Calculate joint angles for each pose using
     the inverse kinematics function
for i = 1:size(desired_poses, 1)
    [Px, Py, Pz, phi, theta, psi] =
        desired_poses(i, :);
    jointAngles(i, :) = inverseKinematics(Px
        , Py, Pz, phi, theta, psi);
end

% Verify the positions using forward
    kinematics
```

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