

# Quiz 6

Student ID Number:

Name \_\_\_\_\_

Math 140B, 5PM

Please justify all your answers

February 28, 2019

Please also write your full name on the back

1. Let  $f$  be bounded on  $[a, b]$  and suppose there exists a partition  $P$  with  $L(f, P) = U(f, P)$ . Describe  $f$ . Is it integrable? If so, what is the value of  $\int_a^b f$ ?

2. Show that if  $f$  is bounded on  $[a, b]$  and  $|f(x) - f(y)| \leq M|x - y|$  for some constant  $M$  and all  $x, y \in [a, b]$  then for any partition  $P$  of  $[a, b]$ , we have

$$U(f, P) - L(f, P) \leq M(b - a) \cdot \text{mesh}(P).$$

Recall that the mesh of the partition  $P = \{a = x_0 < x_1 < \dots < x_n = b\}$  is defined to be  $\max_{1 \leq i \leq n} (x_i - x_{i-1})$ .