

# Quiz 5

Student ID Number:

Name \_\_\_\_\_

Math 140B, 5PM

Please justify all your answers

February 21, 2019

Please also write your full name on the back

1. Suppose that  $f$  is differentiable on an open interval  $I$  containing the point  $b$  and that  $f'(b) < 0$ . Show there are numbers  $a$  and  $c$  with  $a < b < c$  such that  $f(a) > f(b) > f(c)$ .

2. Find the Taylor polynomial of order 3 centered at zero,  $P_3(x)$ , of  $f(x) = \sinh x = \frac{1}{2}(e^x - e^{-x})$ . Find an upper bound for the remainder,  $|f(x) - P_3(x)|$ , at  $x = 1$ .