Math 2A Worksheet: 3.3/3.4 Trigonometric Derivatives & The Chain Rule

Write your names and Student ID numbers at the top of the page

1. Use the derivatives of $\sin x$ and $\cos x$ and the quotient rule to verify the following.

(a)
$$\frac{d}{dx}(\tan x) = \sec^2 x$$

(b)
$$\frac{d}{dx}(\sec x) = \sec x \tan x$$

2. Find the limits:

(a)
$$\lim_{x \to 0} \frac{\sin x}{\sin \pi x}$$

(b)
$$\lim_{x \to 0} \frac{\sin 3x \sin 5x}{x^2}$$

3. Find the derivatives:

(a)
$$f(x) = x \cos x + 2 \tan x$$

(b)
$$g(\theta) = \cos^2 \theta$$

(c)
$$s(t) = \sqrt{\frac{1+\sin t}{1+\cos t}}$$

(d)
$$f(t) = \tan(\sec(\cos t))$$