REAL ANALYSIS MATH 205B/H140B, HW#6

Chapter 14, exercises 6, 7, 8, 18, 19, 20, 24, 25, 27, and the following problem:

Problem 1.

Let us call a partition P of the interval [0,1] "special" if it has a form

$$P = \{x_0, x_1, \dots, x_{2^n}\}, \ x_i = \frac{i}{2^n}.$$

TRUE or FALSE: A bounded function $f:[0,1]\to\mathbb{R}$ is Riemann integrable if and only if

$$\inf_{P} U(f, P) = \sup_{P} L(f, P),$$

where both inf and sup are taken over all special partitions.