Quiz 1

Form A	Name	
Math 130B, 5 PM		
Please justify all your answers		March 30, 2022
Please also write your full name on the back		

1. An urn contains n red balls and m blue balls. They are withdrawn one at a time until a total of r red balls have been withdrawn (here $r \le n$). Find the probability that a total of k balls are withdrawn. Hint: if k balls are withdrawn in total, what color is the last ball? How many of each color are there in the other k-1 withdrawn balls?

2. Let X be a continuous random variable having cumulative distribution function F. Define the random variable Y by Y = F(X). Show that Y is uniformly distributed over (0,1). Hint: what is the cumulative distribution function for Y? You can assume that F is invertible.

Quiz 1

Form B	Name	
Math 130B, 6 PM		
Please justify all your answers		March 30, 2022
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