

Today: Canvas worksheet

Files → Discussion Docs

1-2- - -
* *

1. Write the truth table for the Boolean function Maj_3 , which takes 3 arguments and returns true if at least two of its arguments are true and returns false if at least two of its arguments are false.

P	Q	R	$Maj_3(P, Q, R)$	
T	T	T	T	*
T	T	F	T	*
T	F	T	T	*
T	F	F	F	
F	T	T	T	*
F	T	F	F	
F	F	T	F	
F	F	F	F	

2. Use your truth table to write the same idea to write

$(P \vee Q) \wedge (P \vee R) \wedge (Q \vee R)$

$\vee (P \wedge Q)$

$\vee (P \wedge R)$

$\vee (Q \wedge R)$

$P \wedge Q \wedge R$

le from the previous problem to write Maj_3 using only \wedge , \vee and \neg . Use
rite \implies using only \wedge , \vee and \neg .

$$\begin{aligned} & (P \wedge Q \wedge R) \\ & (P \wedge Q \wedge \neg R) \\ & (P \wedge \neg Q \wedge R) \\ & (\neg P \wedge Q \wedge R) \end{aligned}$$

$$Maj_3 = (P \wedge Q) \wedge (P \wedge R) \wedge (Q \wedge R)$$

4. Let $A = \{1, 2, \{3, 4\}\}$. Which of the following are true and which are false?

- (a) $1 \in A$.
- (b) $\{1\} \in A$.
- (c) $3 \in A$.
- (d) $\{3\} \in A$.
- (e) $\{3\} \subseteq A$.

a) "1 is an element"

True

$1 \neq \{1\}$

b) " $\{1\}$ is an element"
"the set containing"

c) The set A has three elements

1, 2, $\{3, 4\}$

The number 3 is not any of the

Similarly $\{3, 4\} \notin A$ ($B \subseteq A$ means B is a subset of A)

$\{\{3, 4\}\} \subseteq A$ True

Since $\{3, 4\} \in A$

of A''

elt, of A''

is an element of A''

are $\Rightarrow \exists \notin A$

of every elt of
is an elt of A