

D In scalar form, take only $\frac{dL_w}{dw_i}$ for one sample, n

$$\frac{dL_{w,n}}{dw_1} = -2(y - a_5^n) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_1^n,$$

$$\left(\begin{aligned} \text{where } z &= x_1^n w_1 + x_2^n w_2 + x_3^n w_3 + x_4^n w_4 + w_0, \\ \sigma(z) &= \frac{1}{1 + e^{-z}}, \text{ and} \\ a_{5,n} &= \sigma(z) \end{aligned} \right)$$

$$\frac{dL_{w,n}}{dw_2} = -2(y - a_5^n) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_2^n,$$

$$\frac{dL_{w,n}}{dw_3} = -2(y - a_5^n) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_3^n,$$

$$\frac{dL_{w,n}}{dw_4} = -2(y - a_5^n) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_4^n,$$

$$\frac{dL_{w,n}}{dw_0} = -2(y - a_5^n) \cdot \sigma(z) (1 - \sigma(z))$$

Now in Vector form, for all N samples n

$$\frac{dlw}{dw_1} = \begin{bmatrix} -2(y - a_s^1) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_1^1 \\ -2(y - a_s^2) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_1^2 \\ \dots \\ -2(y - a_s^N) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_1^N \end{bmatrix} \begin{matrix} \leftarrow n=1 \\ \leftarrow n=2 \\ \dots \\ \leftarrow n=N \end{matrix}$$

$$\frac{dlw}{dw_2} = \begin{bmatrix} -2(y - a_s^1) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_2^1 \\ -2(y - a_s^2) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_2^2 \\ \dots \\ -2(y - a_s^N) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_2^N \end{bmatrix}$$

$$\frac{dlw}{dw_3} = \begin{bmatrix} -2(y - a_s^1) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_3^1 \\ -2(y - a_s^2) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_3^2 \\ \dots \\ -2(y - a_s^N) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_3^N \end{bmatrix}$$

$$\frac{dlw}{dw_4} = \begin{bmatrix} -2(y - a_s^1) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_4^1 \\ -2(y - a_s^2) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_4^2 \\ \dots \\ -2(y - a_s^N) \cdot \sigma(z) (1 - \sigma(z)) \cdot x_4^N \end{bmatrix}$$

$$\frac{dlw}{dw_0} = \begin{bmatrix} -2(y - a_s^1) \cdot \sigma(z) (1 - \sigma(z)) \\ -2(y - a_s^2) \cdot \sigma(z) (1 - \sigma(z)) \\ \dots \\ -2(y - a_s^N) \cdot \sigma(z) (1 - \sigma(z)) \end{bmatrix} \begin{matrix} \leftarrow n=1 \\ \leftarrow n=2 \\ \dots \\ \leftarrow n=N \end{matrix}$$