# project

Liancheng

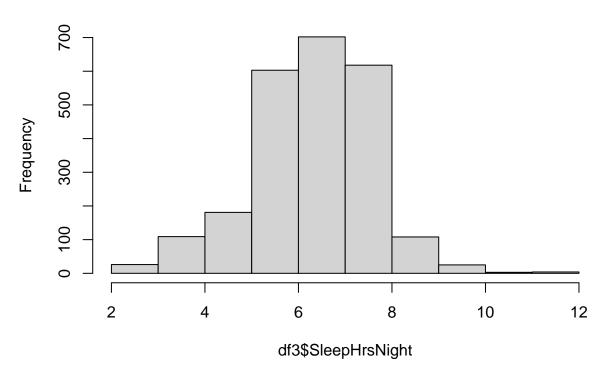
2023-11-21

### (1) Data cleaning

```
rm(list = ls())
gc()
           used (Mb) gc trigger (Mb) max used (Mb)
## Ncells 469578 25.1 1011221 54.1
                                    660860 35.3
## Vcells 877810 6.7
                       8388608 64.0 1800812 13.8
set.seed(123)
library(NHANES)
df <- NHANES[NHANES$Age >= 18 & NHANES$Age < 60, ]</pre>
# colSums(is.na(df)) / nrow(df)
df <- df[, which(colSums(is.na(df)) / nrow(df) < 0.3)]</pre>
df <- df[!duplicated(df), ]</pre>
# colSums(is.na(df)) / nrow(df)
# df$BPSysAve
library(dplyr)
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
      filter, lag
## The following objects are masked from 'package:base':
##
##
      intersect, setdiff, setequal, union
library(car)
## Loading required package: carData
## Attaching package: 'car'
## The following object is masked from 'package:dplyr':
##
##
      recode
df2 <- df %>% select(
  SleepHrsNight,
  BMI,
```

```
DirectChol,
  Age,
  Gender,
  Race1,
  TotChol,
  BPDiaAve,
  BPSysAve,
  AlcoholYear,
  Poverty,
  HomeRooms,
  SexNumPartnLife,
  SexNumPartYear,
  DaysMentHlthBad
)
df3 <- na.omit(df2)
\#df3\$SleepHrsNight \leftarrow df3\$SleepHrsNight * 60
#df3 <- df3[, -which(names(df3) %in% "SleepHrsNight")]
# cor(df3$BPSysAve, df3$BPDiaAve)
psych::describe(df3)
##
                   vars
                            n
                                mean
                                        sd median trimmed
                                                             mad
                                                                   min
                                                                           max
## SleepHrsNight
                      1 2379
                                6.81
                                     1.31
                                             7.00
                                                     6.87
                                                           1.48
                                                                  2.00
                                                                         12.00
## BMI
                      2 2379
                               28.78
                                     6.79
                                            27.52
                                                     28.10
                                                            5.95 15.02
                                                                         69.00
## DirectChol
                      3 2379
                                1.34
                                     0.41
                                             1.27
                                                     1.30
                                                           0.39
                                                                  0.39
                                                                          3.83
                      4 2379
## Age
                               38.65 11.58
                                            39.00
                                                     38.60 14.83 18.00
                                                                         59.00
                                             2.00
                      5 2379
                                                     1.55
## Gender*
                               1.54 0.50
                                                           0.00 1.00
                                                                          2.00
## Race1*
                      6 2379
                                3.43 1.16
                                             4.00
                                                     3.56 0.00 1.00
                                                                          5.00
## TotChol
                      7 2379
                                5.06 1.05
                                             4.99
                                                     5.00 1.04
                                                                  1.53
                                                                         13.65
## BPDiaAve
                      8 2379
                              71.25 11.63
                                            71.00
                                                    71.33 10.38
                                                                  0.00
                                                                        116.00
                      9 2379 117.55 14.40 116.00
## BPSysAve
                                                   116.59 13.34 78.00
                                                                        226.00
                     10 2379
## AlcoholYear
                               68.91 93.00
                                            24.00
                                                     49.33 35.58
                                                                  0.00
                                                                        364.00
## Poverty
                     11 2379
                                2.79 1.69
                                             2.71
                                                     2.83 2.42
                                                                  0.00
                                                                          5.00
## HomeRooms
                     12 2379
                                6.02 2.24
                                             6.00
                                                     5.88
                                                           1.48
                                                                  1.00
                                                                         13.00
## SexNumPartnLife
                     13 2379
                               15.97 63.17
                                             6.00
                                                     8.52 5.93
                                                                  0.00 2000.00
## SexNumPartYear
                     14 2379
                                1.37 2.76
                                             1.00
                                                     1.00
                                                           0.00
                                                                  0.00
                                                                         69.00
## DaysMentHlthBad
                     15 2379
                                4.42 7.98
                                             0.00
                                                     2.35 0.00
                                                                  0.00
                                                                         30.00
                     range skew kurtosis
##
                                             se
## SleepHrsNight
                     10.00 -0.30
                                      0.64 0.03
                     53.98 1.23
                                      2.65 0.14
## BMI
## DirectChol
                      3.44 1.14
                                      2.57 0.01
                     41.00 0.02
## Age
                                     -1.160.24
## Gender*
                      1.00 -0.15
                                     -1.98 0.01
                                      0.06 0.02
## Race1*
                      4.00 -1.10
## TotChol
                     12.12 0.88
                                      3.24 0.02
## BPDiaAve
                    116.00 -0.36
                                      3.11 0.24
## BPSysAve
                    148.00 1.12
                                      3.93 0.30
                    364.00 1.70
## AlcoholYear
                                      2.16 1.91
                      5.00 0.03
## Poverty
                                     -1.480.03
## HomeRooms
                     12.00 0.64
                                      0.43 0.05
## SexNumPartnLife 2000.00 19.57
                                    497.14 1.30
                                    250.92 0.06
## SexNumPartYear
                     69.00 13.35
## DaysMentHlthBad
                     30.00 2.19
                                      3.88 0.16
```

# Histogram of df3\$SleepHrsNight



```
# colSums(is.na(df2)) / nrow(df2)
fit0 <-
  lm(SleepHrsNight ~ .,
      data = df3
#data type
df3$Gender <- ifelse(df3$Gender == "male", 0, 1)</pre>
df3 <- df3 %>%
  mutate(
     Race1 = case_when(
        Race1 == 'Black' ~ 1,
       Race1 == 'Hispanic' ~ 2,
       Race1 == 'Mexican' ~ 3,
       Race1 == 'White' ~ 4,
        Race1 == 'Other' ~ 5,
        {\tt TRUE} \ \hbox{$^\sim$ NA\_integer\_} \ \# \ {\tt Default} \ \ {\tt value} \ \ {\tt if} \ \ {\tt none} \ \ {\tt of} \ \ {\tt the} \ \ {\tt conditions} \ \ {\tt are} \ \ {\tt met}
     )
  )
```

### (2) Baseline characteristics

```
Hmisc::describe(df3)
## df3
##
## 15 Variables 2379 Observations
## -----
## SleepHrsNight
  n missing distinct Info Mean Gmd .05
2379 0 11 0.94 6.807 1.417 4
##
                       .90
    .25
          .50
7
                  .75
                 8
                          8
##
     6
## lowest : 2 3 4 5 6, highest: 8 9 10 11 12
## Value 2
                3
                     4 5
                              6 7
## Frequency 3 23 109 181 603 702 618 108 25 3 4
## Proportion 0.001 0.010 0.046 0.076 0.253 0.295 0.260 0.045 0.011 0.001 0.002
## BMI
     n missing distinct Info
2379 0 1139 1
                               Mean
                                      Gmd
                                             .05
                                                     .10
                        1 28.78
.90 .95
                              28.78 7.297
     2379
                                             20.15
                                                    21.39
                 .75
##
           .50
    . 25
    23.97 27.52
                32.20 37.47 41.46
##
## lowest : 15.02 15.80 15.98 16.51 16.70, highest: 62.80 63.30 63.91 67.83 69.00
## DirectChol
         missing distinct Info Mean Gmd .05
0 99 0.999 1.34 0.4424 0.80
     n missing distinct
                                                     .10
    2379
                                                     0.88
                  .75 .90
     . 25
           .50
                                .95
##
         1.27 1.55 1.86 2.07
##
     1.06
##
## lowest : 0.39 0.41 0.52 0.54 0.57, highest: 3.41 3.44 3.59 3.72 3.83
## Age
                        Info Mean
                                             .05
##
      n missing distinct
                                      Gmd
                                                    .10
##
     2379 0 42 0.999 38.65
                                    13.37
                                              21
                                                      23
                  .75
                        .90
     . 25
            .50
                                .95
##
      29
                   48
                          55
            39
## lowest : 18 19 20 21 22, highest: 55 56 57 58 59
## Gender
    n missing distinct
                        Info
                                \operatorname{\mathtt{Sum}}
                                      Mean
##
     2379 0 2
                         0.746
                                1102 0.4632 0.4975
## -----
  n missing distinct Info Mean Gmd 2379 0 5 0.77 3.427 1.127
##
##
```

```
## lowest : 1 2 3 4 5, highest: 1 2 3 4 5
##
        1 2 3 4 5
## Value
## Frequency 318 160 271 1447 183
## Proportion 0.134 0.067 0.114 0.608 0.077
## -----
    n missing distinct Info Mean Gmd .05 .10 2379 0 212 1 5.057 1.15 3.54 3.83 .25 .50 .75 .90 .95 4.32 4.99 5.69 6.36 6.83
##
##
## lowest: 1.53 2.43 2.59 2.69 2.74, highest: 9.31 9.34 9.90 12.28 13.65
## -----
## BPDiaAve
  n missing distinct Info Mean Gmd .05
2379 0 84 0.999 71.25 12.62 53
##
                                              .10
##
                                                 58
                 .75 .90 .95
78 85 89
    . 25
           .50
##
           71
##
     64
##
## lowest: 0 20 21 22 25, highest: 108 109 110 114 116
## -----
## BPSysAve
## n missing distinct Info Mean
                                   Gmd .05
                                              .10
    2379 0 99 0.999 117.6 15.47
##
                                         98.0
                                                101.8
    . 25
           .50
                .75
                      .90 .95
## 108.0 116.0 125.0 134.0 142.0
## lowest : 78 83 84 85 86, highest: 184 191 202 209 226
## -----
## AlcoholYear
  n missing distinct Info Mean Gmd .05 .10 2379 0 56 0.993 68.91 90.19 0 0
##
    . 25
           .50 .75
24 104
                 .75 .90 .95
##
                       208
##
     4
                              260
## lowest : 0 1 2 3 4, highest: 260 300 312 360 364
## Poverty
                                   Gmd .05
  n missing distinct Info Mean
##
                                               .10
    2379 0 398 0.989 2.794 1.932 0.329 0.658
##
    .25
           .50
                 .75
                      .90
                             .95
   1.225 2.710 4.710 5.000 5.000
##
## lowest : 0.00 0.02 0.03 0.04 0.05, highest: 4.95 4.96 4.97 4.99 5.00
## HomeRooms
##
   n missing distinct Info Mean
                                   Gmd .05 .10
    2379 0 13 0.978 6.024 2.459
                                          3
                                                 4
        .50 .75 .90 .95
6 7 9 10
    .25
##
     4
##
## lowest : 1 2 3 4 5, highest: 9 10 11 12 13
##
```

```
## Value 1 2 3 4 5 6 7
## Frequency 25 34 168 408 441 438 331
                 2 3 4 5 6 7 8 9
                                            213 134
                                                      93
## Proportion 0.011 0.014 0.071 0.172 0.185 0.184 0.139 0.090 0.056 0.039 0.018
## Value
            12
                 13
                 26
## Frequency
            26
## Proportion 0.011 0.011
## -----
## SexNumPartnLife
       n missing distinct Info Mean
                                              .05
                                        Gmd
                                                     .10
##
     2379
         0 81 0.996
                              15.97
                                      21.68
                                               1
                                                      1
                  .75 .90
      .25
            .50
                                .95
##
                   15
       3
                           30
                                  50
##
## lowest: 0 1 2 3 4, highest: 600 800 999 1000 2000
## SexNumPartYear
                                              .05
     n missing distinct
                        Info
                               Mean
                                                     .10
##
     2379
                  22
                         0.683
                               1.374
                                      1.258
                                               0
             0
                                                      0
                  .75
##
      .25
            .50
                         .90
                                .95
##
       1
             1
                    1
                           2
## lowest : 0 1 2 3 4, highest: 19 20 30 50 69
## DaysMentHlthBad
      n missing distinct
                        Info
                               Mean
                                        Gmd
                                              . 05
                                                     .10
##
          0 28
                       0.842
                                4.422
                                       6.829
                                               0
                                                       0
     2379
                  .75
      .25
            .50
                         .90
                                 .95
       0
             0
                    5
                           15
## lowest : 0 1 2 3 4, highest: 25 26 27 29 30
```

# (3) linear regression model

```
model1 = lm(df3$SleepHrsNight ~ df3$BMI, data = df3)
summary(model1)

##
## Call:
## lm(formula = df3$SleepHrsNight ~ df3$BMI, data = df3)
##
## Residuals:
## Min 1Q Median 3Q Max
## -4.8366 -0.8209 0.1606 1.1457 5.2593
##
## Coefficients:
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 7.089190 0.116862 60.663 <2e-16 ***
## df3$BMI -0.009790 0.003953 -2.477 0.0133 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1</pre>
```

```
##
## Residual standard error: 1.309 on 2377 degrees of freedom
## Multiple R-squared: 0.002574,
                                           Adjusted R-squared: 0.002155
## F-statistic: 6.135 on 1 and 2377 DF, p-value: 0.01332
par(mfrow = c(2, 3)) #read more from ?plot.lm
plot(model1, which = 1)
plot(model1, which = 2)
plot(model1, which = 3)
plot(model1, which = 4)
plot(model1, which = 5)
plot(model1, which = 6)
        Residuals vs Fitted
                                                Normal Q-Q
                                                                                   Scale-Location
                                                                        (Standardized residuals)
                                     Standardized residuals
     9
Residuals
                                         \alpha
                                                                                      ഗവ അ
                                                                             0.
                                         0
                                         ņ
                        00
                                                                             0.0
     တု
                                         4
                                                              2
        6.4
                        6.8
                                                                 3
                                                                                6.4
                                                                                        6.6
                                                                                                6.8
               Fitted values
                                                Theoretical Quantiles
                                                                                       Fitted values
                                          Residuals vs Leverage Cook's dist vs Leverage h_{ii}/(1
          Cook's distance
     90.0
                                     Standardized residuals
Cook's distance
                                                                         Cook's distance
                                                                             0.04
    0.04
    0.02
                                                                             0.02
                                                           o
9670
     0.00
                                                                             0.00
         0
            500
                     1500
                                            0.000
                                                  0.005
                                                         0.010 0.015
                                                                                  0
                                                                                       0.005
                                                                                              0.01
                                                                                                    0.015
                                                                                       Leverage hii
               Obs. number
                                                    Leverage
par(mfrow = c(1, 1)) # reset
## multiple linear regression##
m_initial = lm(SleepHrsNight ~ BMI + Age + Gender + factor(Race1), df3)
summary(m initial)
##
## Call:
## lm(formula = SleepHrsNight ~ BMI + Age + Gender + factor(Race1),
##
        data = df3)
##
## Residuals:
                   10
                       Median
                                       3Q
                                               Max
```

## -4.9314 -0.8178 0.1258 1.0506 5.3685

```
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
                            0.165453 41.862 < 2e-16 ***
## (Intercept)
                  6.926204
## BMI
                 -0.006542
                            0.003986
                                     -1.641
                                             0.10086
                 ## Age
## Gender
                 0.190406
                            0.053607
                                     3.552 0.00039 ***
## factor(Race1)2 0.219456
                            0.126253
                                       1.738 0.08230
## factor(Race1)3 0.463251
                            0.107923
                                      4.292 1.84e-05 ***
## factor(Race1)4 0.364311
                            0.081381
                                       4.477 7.94e-06 ***
## factor(Race1)5 0.346075
                            0.121784
                                       2.842 0.00453 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.298 on 2371 degrees of freedom
## Multiple R-squared: 0.02277,
                                  Adjusted R-squared: 0.01988
## F-statistic: 7.892 on 7 and 2371 DF, p-value: 1.734e-09
m_knrisk = lm(
 SleepHrsNight ~ BMI + Age + Gender + factor(Race1) + TotChol + BPDiaAve +
   BPSysAve + AlcoholYear + DaysMentHlthBad,
 df3
)
summary(m_knrisk)
##
## Call:
## lm(formula = SleepHrsNight ~ BMI + Age + Gender + factor(Race1) +
      TotChol + BPDiaAve + BPSysAve + AlcoholYear + DaysMentHlthBad,
##
      data = df3)
##
##
## Residuals:
##
      Min
               10 Median
                              3Q
                                     Max
  -4.9890 -0.8396 0.0721 0.9860
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  7.0320813 0.2778091 25.313 < 2e-16 ***
## BMI
                  -0.0044747 0.0040584
                                       -1.103 0.270326
## Age
                  -0.0094332 0.0024860 -3.794 0.000152 ***
## Gender
                  0.2375920 0.0557852
                                        4.259 2.13e-05 ***
## factor(Race1)2
                 0.2194679 0.1252138
                                        1.753 0.079775 .
## factor(Race1)3 0.4198626 0.1074580
                                        3.907 9.60e-05 ***
## factor(Race1)4
                  0.3457651 0.0809536
                                        4.271 2.02e-05 ***
## factor(Race1)5
                  0.3059503 0.1211322
                                        2.526 0.011610 *
## Tot.Chol
                   0.0047497 0.0266203
                                        0.178 0.858404
## BPDiaAve
                   0.0005694 0.0027009
                                        0.211 0.833058
## BPSysAve
                  ## AlcoholYear
                   0.0004989
                            0.0002951
                                        1.691 0.091045 .
## DaysMentHlthBad -0.0263313  0.0033210  -7.929  3.38e-15 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.281 on 2366 degrees of freedom
## Multiple R-squared: 0.0491, Adjusted R-squared: 0.04427
```

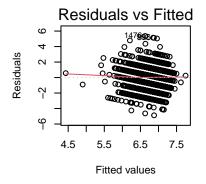
```
## F-statistic: 10.18 on 12 and 2366 DF, p-value: < 2.2e-16
m full = lm(
 SleepHrsNight ~ BMI + Age + Gender + factor(Race1) + TotChol + BPDiaAve +
   BPSysAve + AlcoholYear + DaysMentHlthBad + HomeRooms + SexNumPartnLife +
   SexNumPartYear + Poverty,
 df3
)
summary(m_full)
##
## Call:
## lm(formula = SleepHrsNight ~ BMI + Age + Gender + factor(Race1) +
      TotChol + BPDiaAve + BPSysAve + AlcoholYear + DaysMentHlthBad +
##
      HomeRooms + SexNumPartnLife + SexNumPartYear + Poverty, data = df3)
##
## Residuals:
##
      Min
              1Q Median
                             3Q
                                    Max
## -4.8773 -0.8413 0.0550 0.9634 5.3687
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                  6.7900913  0.2880350  23.574  < 2e-16 ***
## (Intercept)
## BMI
                 -0.0040314 0.0040533 -0.995 0.320044
## Age
                 0.2295409 0.0559260
## Gender
                                       4.104 4.19e-05 ***
## factor(Race1)2  0.2329616  0.1249975  1.864  0.062483 .
## factor(Race1)4  0.3135085  0.0815958  3.842  0.000125 ***
## factor(Race1)5 0.2899386 0.1211140
                                        2.394 0.016746 *
                  0.0053548 0.0265885 0.201 0.840408
## TotChol
## BPDiaAve
                  0.0006679 0.0026998 0.247 0.804627
## BPSysAve
                 -0.0005452 0.0022628 -0.241 0.809634
## AlcoholYear
                  0.0003952 0.0002967
                                       1.332 0.182986
## DaysMentHlthBad -0.0247441 0.0033503 -7.386 2.09e-13 ***
## HomeRooms
                  0.0213263 0.0127462
                                       1.673 0.094431 .
## SexNumPartnLife -0.0009946 0.0004243 -2.344 0.019168 *
## SexNumPartYear
                  0.0149274 0.0097588 1.530 0.126243
## Poverty
                  0.0372512 0.0173927
                                        2.142 0.032314 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.278 on 2362 degrees of freedom
## Multiple R-squared: 0.05601,
                                Adjusted R-squared: 0.04962
## F-statistic: 8.759 on 16 and 2362 DF, p-value: < 2.2e-16
vif(m full)
##
                     GVIF Df GVIF<sup>(1/(2*Df))</sup>
## BMI
                 1.104174 1
                                   1.050797
                 1.296882 1
## Age
                                   1.138807
## Gender
                 1.133022 1
                                   1.064435
## factor(Race1)
                1.208657 4
                                  1.023972
## TotChol
                1.133282 1
                                  1.064557
```

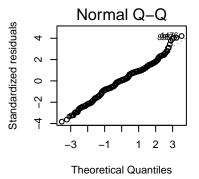
1.198704

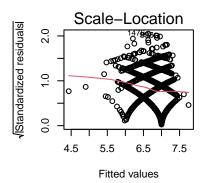
## BPDiaAve

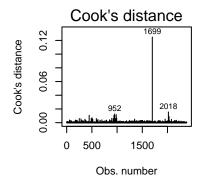
1.436892 1

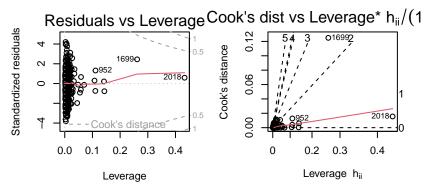
```
## BPSysAve
                                       1.243234
                   1.545631
## AlcoholYear
                   1.108683
                              1
                                       1.052940
## DaysMentHlthBad 1.041358
                                       1.020469
## HomeRooms
                   1.182949
                                       1.087635
## SexNumPartnLife 1.046533
                                       1.023002
## SexNumPartYear 1.053685
                                       1.026491
## Poverty
                   1.261580
                                       1.123201
par(mfrow = c(2, 3)) #read more from ?plot.lm
plot(m_full, which = 1)
plot(m_full, which = 2)
plot(m_full, which = 3)
plot(m_full, which = 4)
plot(m full, which = 5)
plot(m_full, which = 6)
```

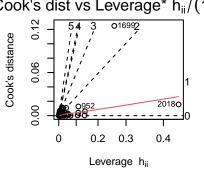






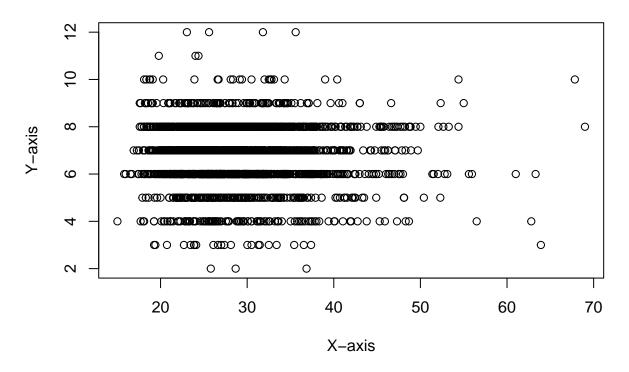






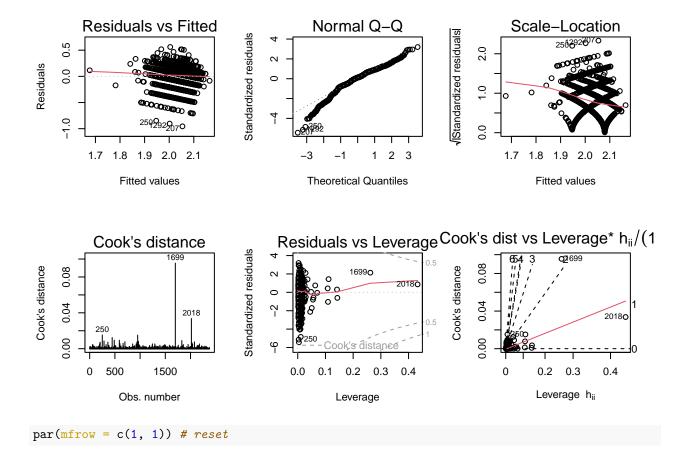
```
par(mfrow = c(1, 1)) # reset
plot(
  df3$BMI,
  df3$SleepHrsNight,
  main = "Scatter Plot with Linear Regression Line",
  xlab = "X-axis",
  ylab = "Y-axis"
```

## **Scatter Plot with Linear Regression Line**



```
#log x
df3\$logBMI = log(df3\$BMI + 1)
df3$logSleepHrsNight = log(df3$SleepHrsNight + 1)
df3$logDaysMentHlthBad = log(df3$DaysMentHlthBad + 1)
df3$invTotChol = 1 / df3$TotChol
df3$sqrtDaysMentHlthBad = sqrt(df3$DaysMentHlthBad)
df3$sqBMI = (df3$BMI - mean(df3$BMI)) ^ 2
m_logfull_2 = lm(
  logSleepHrsNight ~ Age + Gender + factor(Race1) + logBMI + invTotChol +
   BPDiaAve + BPSysAve + AlcoholYear + sqrtDaysMentHlthBad + HomeRooms + SexNumPartnLife +
   SexNumPartYear + Poverty,
  df3
)
summary(m_logfull_2)
##
## Call:
## lm(formula = logSleepHrsNight ~ Age + Gender + factor(Race1) +
       logBMI + invTotChol + BPDiaAve + BPSysAve + AlcoholYear +
##
       sqrtDaysMentHlthBad + HomeRooms + SexNumPartnLife + SexNumPartYear +
##
##
       Poverty, data = df3)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
                                             Max
  -0.95516 -0.09798 0.01973 0.12503 0.56082
##
```

```
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                       2.091e+00 7.094e-02 29.476 < 2e-16 ***
                      -1.567e-03 3.540e-04 -4.427 9.99e-06 ***
## Age
## Gender
                       3.130e-02 7.727e-03
                                            4.050 5.28e-05 ***
## factor(Race1)2
                       3.462e-02 1.719e-02 2.014 0.04416 *
## factor(Race1)3
                       6.283e-02 1.482e-02 4.239 2.33e-05 ***
                       4.723e-02 1.121e-02 4.212 2.63e-05 ***
## factor(Race1)4
                                           2.705 0.00688 **
## factor(Race1)5
                      4.506e-02 1.666e-02
## logBMI
                      -2.052e-02 1.776e-02 -1.156 0.24797
## invTotChol
                      -1.352e-02 8.866e-02 -0.152 0.87885
## BPDiaAve
                      1.927e-04 3.715e-04
                                            0.519 0.60410
## BPSvsAve
                      -5.826e-05 3.116e-04 -0.187 0.85168
                       6.167e-05 4.089e-05 1.508 0.13167
## AlcoholYear
## sqrtDaysMentHlthBad -1.748e-02 2.215e-03 -7.891 4.55e-15 ***
## HomeRooms
                       3.031e-03 1.755e-03
                                            1.727 0.08428 .
## SexNumPartnLife
                     -1.467e-04 5.844e-05 -2.511 0.01211 *
## SexNumPartYear
                     1.880e-03 1.344e-03 1.399 0.16203
## Poverty
                       6.249e-03 2.396e-03
                                             2.608 0.00917 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1759 on 2362 degrees of freedom
## Multiple R-squared: 0.06159,
                                  Adjusted R-squared: 0.05523
## F-statistic: 9.689 on 16 and 2362 DF, p-value: < 2.2e-16
par(mfrow = c(2, 3)) #read more from ?plot.lm
plot(m_logfull_2, which = 1)
plot(m_logfull_2, which = 2)
plot(m_logfull_2, which = 3)
plot(m_logfull_2, which = 4)
plot(m_logfull_2, which = 5)
plot(m_logfull_2, which = 6)
```



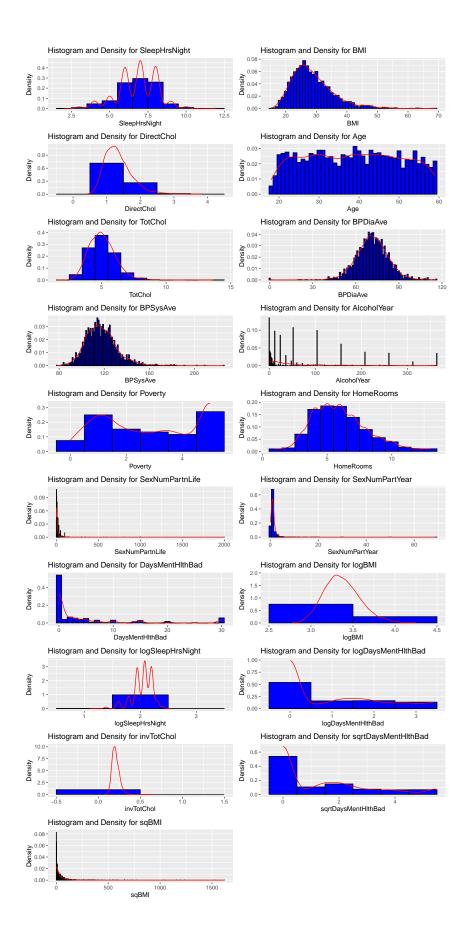
## (4) Diagnosis: 10-fold CV

```
library(caret)
## Loading required package: ggplot2
## Loading required package: lattice
splitIndex <-
  createDataPartition(df3$SleepHrsNight, p = 0.7, list = FALSE)
trainData <- df3[splitIndex, ]</pre>
testData <- df3[-splitIndex, ]</pre>
predictions <- predict(m_logfull_2, newdata = testData)</pre>
mse <- mean((testData$SleepHrsNight - predictions) ^ 2)</pre>
control <-
  trainControl(method = "cv", number = 10) # 10-fold cross-validation
cv_model <-
  train(
    SleepHrsNight ~ .,
    data = df3,
    method = "lm",
    trControl = control
```

```
cv_model
## Linear Regression
## 2379 samples
     20 predictor
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 2141, 2140, 2141, 2141, 2142, 2142, ...
## Resampling results:
##
##
     RMSE
                Rsquared MAE
##
     0.1900161 0.979765 0.1266116
## Tuning parameter 'intercept' was held constant at a value of TRUE
(cv_results <- cv_model$results)</pre>
                                                 RMSESD RsquaredSD
     intercept
                    RMSE Rsquared
                                        MAE
## 1
          TRUE 0.1900161 0.979765 0.1266116 0.03595476 0.005748305 0.00897214
```

#### (4) Diagnosis: Normality Assumption

```
library(ggplot2)
library(patchwork)
# Initializes an empty patchwork object
plot_list <- list()</pre>
# Draw a histogram for each numeric variable (except Race1 and Gender) and add it to the list
for (var in names(df3)) {
  if (is.numeric(df3[[var]]) && !(var %in% c("Race1", "Gender"))) {
    p \leftarrow ggplot(df3, aes(x = .data[[var]])) +
      geom_histogram(
        aes(y = after_stat(density)),
        binwidth = 1,
        fill = "blue",
        color = "black"
      geom_density(col = "red") +
      ggtitle(paste("Histogram and Density for", var)) +
      xlab(var) +
      ylab("Density")
    plot_list[[length(plot_list) + 1]] <- p</pre>
}
# Use patchwork to put all the charts together
combined_plot <- wrap_plots(plot_list, ncol = 2)</pre>
print(combined_plot)
```



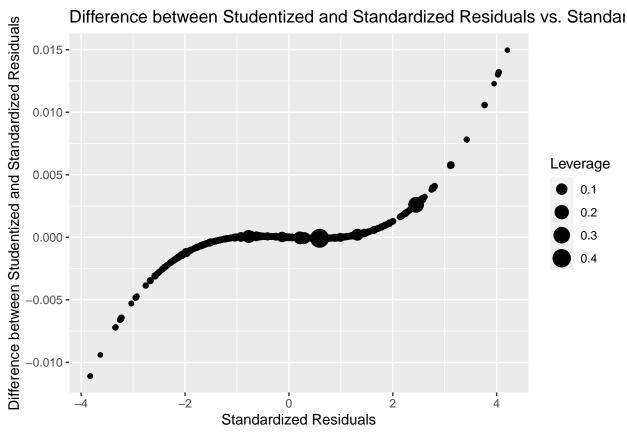
```
df3 <- data.frame(df3)</pre>
library(dplyr)
# Shapiro-Wilk normality test is performed for each numerical variable in df3
results <- sapply(df3, function(x) {
  if (is.numeric(x)) {
    shapiro_test <- shapiro.test(x)</pre>
    return(c(shapiro_test$statistic, shapiro_test$p.value))
    return(c(NA, NA))
  }
})
# Convert the result to a data box and name the column
results df <- as.data.frame(t(results))</pre>
names(results_df) <- c("W", "p.value")</pre>
# Add a variable name as a new column
results_df$Variable <- rownames(results_df)</pre>
# Rearrange the order of columns
results_df <- results_df[, c("Variable", "W", "p.value")]</pre>
# Calculate the corrected P-value (for example, using Bonferroni correction)
results_df$p.adjusted <-
  p.adjust(results_df$p.value, method = "bonferroni")
print(results_df)
                                                            p.value
                                   Variable
                                                     W
                                                                       p.adjusted
                              SleepHrsNight 0.9354644 6.065754e-31 1.273808e-29
## SleepHrsNight
## BMI
                                        BMI 0.9301559 5.692561e-32 1.195438e-30
## DirectChol
                                 DirectChol 0.9405789 6.876212e-30 1.444005e-28
                                        Age 0.9582706 1.360245e-25 2.856515e-24
## Age
## Gender
                                     Gender 0.6346474 1.545071e-57 3.244648e-56
```

```
## Race1
                                     Race1 0.7427298 1.802728e-51 3.785730e-50
## TotChol
                                   TotChol 0.9663542 3.785914e-23 7.950419e-22
## BPDiaAve
                                  BPDiaAve 0.9726214 6.250883e-21 1.312685e-19
## BPSvsAve
                                  BPSvsAve 0.9484045 3.946229e-28 8.287082e-27
## AlcoholYear
                               AlcoholYear 0.7403964 1.270928e-51 2.668949e-50
## Poverty
                                   Poverty 0.8951549 1.570942e-37 3.298979e-36
## HomeRooms
                                 HomeRooms 0.9553923 2.237881e-26 4.699550e-25
## SexNumPartnLife
                           SexNumPartnLife 0.1509787 1.499112e-73 3.148134e-72
## SexNumPartYear
                            SexNumPartYear 0.2545353 5.992229e-71 1.258368e-69
## DaysMentHlthBad
                           DaysMentHlthBad 0.6076574 8.193380e-59 1.720610e-57
## logBMI
                                    logBMI 0.9877235 1.946304e-13 4.087239e-12
## logSleepHrsNight
                          logSleepHrsNight 0.8984084 4.408251e-37 9.257327e-36
## logDaysMentHlthBad
                        logDaysMentHlthBad 0.7729598 2.157265e-49 4.530256e-48
## invTotChol
                                invTotChol 0.9572292 7.005059e-26 1.471062e-24
## sqrtDaysMentHlthBad sqrtDaysMentHlthBad 0.7619387 3.557376e-50 7.470490e-49
## sqBMI
                                     sqBMI 0.4152373 3.203569e-66 6.727494e-65
```

# Standardized residuals, Studentized residuals

```
# Regular residuals
residual_1 <- fit0$residuals
# Standardized residuals</pre>
```

```
residual_2 <- rstandard(fit0)</pre>
# Studentized residuals
residual 3 <- rstudent(fit0)</pre>
# Externally studentized residuals
# Note: Externally studentized residuals are the same as studentized residuals in most cases
residual 4 <- rstudent(fit0)</pre>
# Creating a data frame to summarize these residuals
residual_summary <- data.frame(</pre>
  Residuals = c("Regular", "Standardized", "Studentized", "Externally Studentized"),
 Mean = c(mean(residual_1), mean(residual_2), mean(residual_3), mean(residual_4)),
 SD = c(sd(residual_1), sd(residual_2), sd(residual_3), sd(residual_4)),
 Min = c(min(residual_1), min(residual_2), min(residual_3), min(residual_4)),
 Max = c(max(residual_1), max(residual_2), max(residual_3), max(residual_4))
# Display the summary
print(residual_summary)
##
                  Residuals
                                     Mean
                                                 SD
                                                          Min
## 1
                    Regular 7.060476e-17 1.273554 -4.878636 5.368822
## 2
               Standardized 1.960572e-04 1.000639 -3.826002 4.207084
## 3
                Studentized 1.585968e-04 1.001202 -3.837105 4.222048
## 4 Externally Studentized 1.585968e-04 1.001202 -3.837105 4.222048
# Load necessary library
library(ggplot2)
# Assuming fit0 is your linear model
\# fit0 \leftarrow lm(SleepMinNight \sim ., data = df3)
# Calculate standardized and studentized residuals
residual_2 <- rstandard(fit0)</pre>
residual_3 <- rstudent(fit0)</pre>
# Calculate leverage values
leverage_values <- hatvalues(fit0)</pre>
# Create a data frame for plotting
plot_data <- data.frame(</pre>
 Standardized_Residuals = residual_2,
 Difference = residual_3 - residual_2,
 Leverage = leverage_values
)
# Create the plot
ggplot(plot_data, aes(x = Standardized_Residuals, y = Difference)) +
  geom_point(aes(size = Leverage)) +
  ggtitle("Difference between Studentized and Standardized Residuals vs. Standardized Residuals") +
  xlab("Standardized Residuals") +
  ylab("Difference between Studentized and Standardized Residuals")
```



```
# Display the plot
print(ggplot)
## function (data = NULL, mapping = aes(), ..., environment = parent.frame())
##
       UseMethod("ggplot")
## }
## <bytecode: 0x4e12680>
## <environment: namespace:ggplot2>
# Load necessary library
library(ggplot2)
# Assuming fit0 is your linear model
\# fit0 \leftarrow lm(SleepMinNight \sim ., data = df3)
# Calculate studentized and externally studentized residuals
residual_3 <- rstudent(fit0)</pre>
residual_4 <- rstudent(fit0) # Externally studentized residuals are typically the same as studentized
# Regular residuals
residual_1 <- fit0$residuals</pre>
# Create a data frame for plotting
plot_data <- data.frame(</pre>
 Studentized_Residuals = residual_3,
 Difference = residual_4 - residual_3,
```

```
Residual_Squared = residual_1^2
)
# Create the plot
ggplot(plot_data, aes(x = Studentized_Residuals, y = Difference)) +
  geom_point(aes(size = Residual_Squared)) +
  ggtitle("Difference between Externally Studentized and Studentized Residuals vs. Studentized Residual
  xlab("Studentized Residuals") +
  ylab("Difference between Externally Studentized and Studentized Residuals")
Difference between Externally Studentized and Studentized Residua
          Difference between Externally Studentized and Studentized Residuals vs
     0.050 -
     0.025 -
                                                                              Residual_Squared
                                                                                  10
     0.000
                                                                                  20
    -0.025 -
     -0.050 -
                          <u>-</u>2
                                        ò
                               Studentized Residuals
# Display the plot
print(ggplot)
## function (data = NULL, mapping = aes(), ..., environment = parent.frame())
## {
##
       UseMethod("ggplot")
## }
## <bytecode: 0x4e12680>
## <environment: namespace:ggplot2>
# Load necessary library
library(ggplot2)
# Assuming fit0 is your linear model
# fit0 <- lm(SleepMinNight ~ ., data = df3)</pre>
```

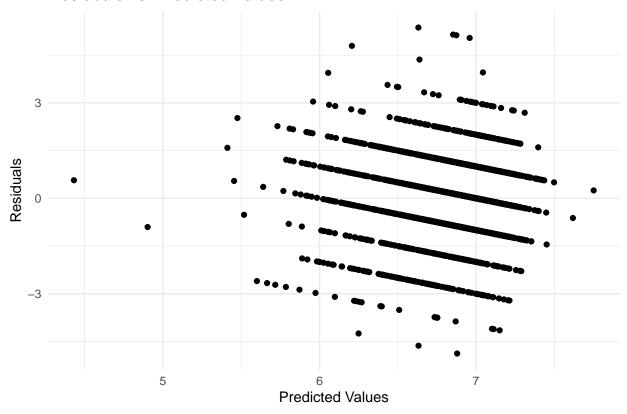
# Calculate regular residuals

```
residual_1 <- fit0$residuals

# Get predicted values from the model
predicted_values <- predict(fit0)

# Create the plot
ggplot() +
    geom_point(aes(x = predicted_values, y = residual_1)) +
    ggtitle("Residuals vs. Predicted Values") +
    xlab("Predicted Values") +
    ylab("Residuals") +
    theme_minimal()</pre>
```

#### Residuals vs. Predicted Values



```
# Display the plot
print(ggplot)
```

```
## function (data = NULL, mapping = aes(), ..., environment = parent.frame())
## {
## UseMethod("ggplot")
## }
## <bytecode: 0x4e12680>
## <environment: namespace:ggplot2>
# Load necessary library
library(ggplot2)
# Assuming fit0 is your linear model
```

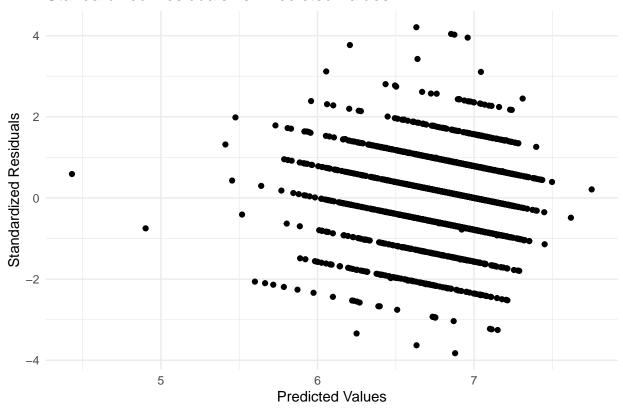
```
# fit0 <- lm(SleepMinNight ~ ., data = df3)

# Calculate different types of residuals
residual_2 <- rstandard(fit0)
residual_3 <- rstudent(fit0)
residual_4 <- rstudent(fit0) # Externally studentized residuals

# Get predicted values from the model
predicted_values <- predict(fit0)

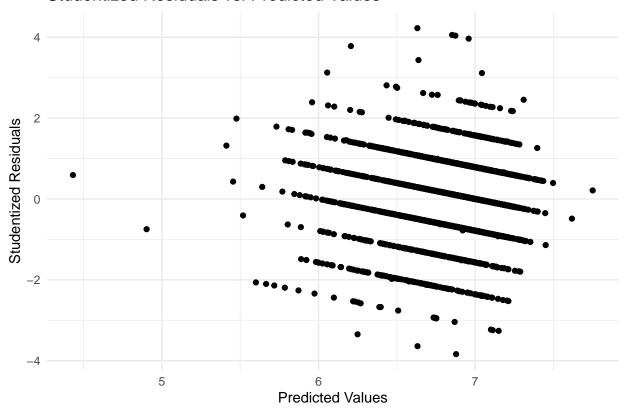
# Plot for Standardized Residuals
ggplot() +
    geom_point(aes(x = predicted_values, y = residual_2)) +
    ggtitle("Standardized Residuals vs. Predicted Values") +
    xlab("Predicted Values") +
    ylab("Standardized Residuals") +
    theme_minimal()</pre>
```

#### Standardized Residuals vs. Predicted Values



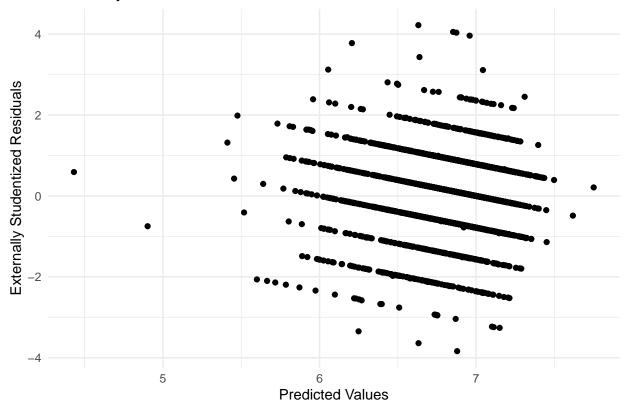
```
# Plot for Studentized Residuals
ggplot() +
  geom_point(aes(x = predicted_values, y = residual_3)) +
  ggtitle("Studentized Residuals vs. Predicted Values") +
  xlab("Predicted Values") +
  ylab("Studentized Residuals") +
  theme_minimal()
```

### Studentized Residuals vs. Predicted Values



```
# Plot for Externally Studentized Residuals
ggplot() +
  geom_point(aes(x = predicted_values, y = residual_4)) +
  ggtitle("Externally Studentized Residuals vs. Predicted Values") +
  xlab("Predicted Values") +
  ylab("Externally Studentized Residuals") +
  theme_minimal()
```

#### Externally Studentized Residuals vs. Predicted Values



## (5) Model Selection

```
step(fit0)
```

```
## Start: AIC=1185.54
## SleepHrsNight ~ BMI + DirectChol + Age + Gender + Race1 + TotChol +
##
      BPDiaAve + BPSysAve + AlcoholYear + Poverty + HomeRooms +
##
       SexNumPartnLife + SexNumPartYear + DaysMentHlthBad
##
                     Df Sum of Sq
##
                                     RSS
## - DirectChol
                      1
                            0.003 3857.0 1183.5
## - TotChol
                      1
                            0.069 3857.0 1183.6
## - BPSysAve
                            0.093 3857.1 1183.6
                      1
## - BPDiaAve
                      1
                            0.098 3857.1 1183.6
## - BMI
                      1
                            1.435 3858.4 1184.4
## - AlcoholYear
                            2.773 3859.7 1185.2
## <none>
                                  3857.0 1185.5
## - SexNumPartYear
                      1
                            3.823 3860.8 1185.9
## - HomeRooms
                      1
                            4.571 3861.5 1186.4
## - Poverty
                      1
                           7.466 3864.4 1188.1
## - SexNumPartnLife 1
                           8.973 3865.9 1189.1
## - Race1
                           32.638 3889.6 1197.6
## - Gender
                      1
                           23.929 3880.9 1198.2
## - Age
                           28.718 3885.7 1201.2
```

```
## - DaysMentHlthBad 1 89.039 3946.0 1237.8
##
## Step: AIC=1187.2
## SleepHrsNight ~ BMI + Age + Gender + Race1 + TotChol + BPDiaAve +
         BPSysAve + AlcoholYear + Poverty + HomeRooms + SexNumPartnLife +
##
          SexNumPartYear + DaysMentHlthBad
##
## Call:
## lm(formula = SleepHrsNight ~ BMI + Age + Gender + Race1 + TotChol +
          BPDiaAve + BPSysAve + AlcoholYear + Poverty + HomeRooms +
##
          SexNumPartnLife + SexNumPartYear + DaysMentHlthBad, data = df3)
##
## Coefficients:
         (Intercept)
                                              BMI
                                                                      Age
                                                                                           Gender
            6.8656069
                                  -0.0040545
                                                            -0.0107790
                                                                                    0.2153535
##
                                      TotChol
                                                              BPDiaAve
                  Race1
                                                                                      BPSysAve
            0.0766796
                                                           0.0003656
##
                                   0.0095890
                                                                                    -0.0007014
         AlcoholYear
                                      Poverty
                                                             HomeRooms SexNumPartnLife
            0.0003533 0.0303914
                                                             0.0198583
                                                                                   -0.0010323
##
     SexNumPartYear DaysMentHlthBad
##
            0.0146137 -0.0253312
library(olsrr)
##
## Attaching package: 'olsrr'
## The following object is masked from 'package:datasets':
##
##
ols_step_forward_p(m_full, penter = 0.1, details = F)
##
##
                                                  Selection Summary
## -
##
               Variable
                                                               Adj.
                                         R-Square R-Square
                                                                               C(p)
## Step
                    Entered
                                                                                                  AIC
                                                                                                                  RMSE

      1
      DaysMentHlthBad
      0.0242
      0.0238
      66.5525
      7985.6561
      1.2951

      2
      Gender
      0.0311
      0.0303
      51.4035
      7970.8875
      1.2908

      3
      Age
      0.0373
      0.0361
      37.8570
      7957.5830
      1.2869

      4
      factor(Race1)
      0.0471
      0.0443
      15.3744
      7941.2801
      1.2815

      5
      Poverty
      0.0507
      0.0475
      8.3826
      7934.2917
      1.2793

      6
      SexNumPartnLife
      0.0525
      0.0489
      5.7740
      7931.6716
      1.2783

      7
      HomeRooms
      0.0536
      0.0496
      4.9984
      7930.8847
      1.2779

##
##
##
##
##
##
##
ols_step_forward_p(m_full, penter = 0.05, details = F)
##
##
                                                  Selection Summary
               Variable
                                                               Adj.
               Entered R-Square R-Square C(p)
## Step
                                                                                               AIC
                                                                                                               RMSE
```

```
      0.0242
      0.0238
      66.5525

      0.0311
      0.0303
      51.4035

##
           DaysMentHlthBad
                                                                     7985.6561
                                                                                   1.2951
      1
##
      2
           Gender
                                                                     7970.8875
                                                                                   1.2908
                                  0.0373
                                             0.0361 37.8570
##
      3 Age
                                                                     7957.5830 1.2869
                                  0.0471
##
      4
           factor(Race1)
                                              0.0443 15.3744
                                                                     7941.2801
                                                                                   1.2815
##
                                  0.0507
                                              0.0475
                                                         8.3826
                                                                     7934.2917
                                                                                   1.2793
      5
           Poverty
##
      6
           SexNumPartnLife
                                  0.0525
                                              0.0489
                                                         5.7740
                                                                     7931.6716
                                                                                   1.2783
ols_mallows_cp(model = m_logfull_2, fullmodel = m_full) # Mallows' Cp
```

## [1] -2306.233