



## ← Subarray Sums Divisible by K



JAVA | 2 approaches | Fully explained

sourin\_bruh 2068 Sep 21, 2022

### Please Upvote :D

#### 1. Brute force approach (TLE):

Java

```

class Solution {
    public int subarraysDivByK(int[] nums, int k) {
        // check all possible subarrays,
        // take their sum, increment the count if divisible by k
        int total = 0;
        for (int i = 0; i < nums.length; i++) {
            int sum = 0;
            for (int j = i; j < nums.length; j++) {
                sum += nums[j];
                if (sum % k == 0) {
                    total++;
                }
            }
        }

        return total;
    }
}

// O(n ^ 2), SC: O(1)

```

#### 2. Optimal approach (using hashmap):

We will be using a hashmap to store **remainders** of the running sum of our array at each index.

The logic behind this is that if we encounter a remainder which was already encountered before, it means that the *sum of the subarray from from the index right next to that point to our current point is divisible by*

25



Say at index  $i$  , we got a remainder  $x$  , after that we got the same remainder  $x$  at index  $j$  .

It means that the sum of the subarray from index  $i + 1$  to  $j$  is divisible by  $k$  (or we can say that the sum of the subarray from index  $i + 1$  to  $j$  yields a remainder  $0$  when divided by  $k$  ).

Say sum till index  $i$  is  $s_1$  and sum till index  $j$  is  $s_2$  .

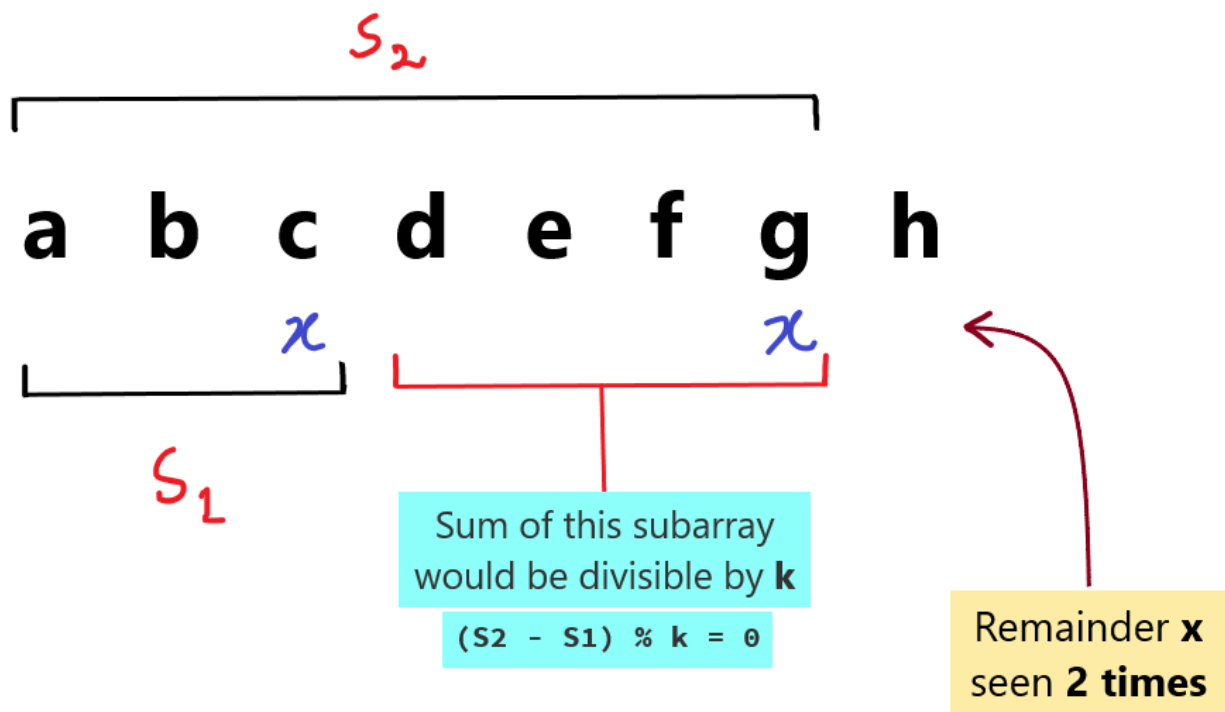
We observed that:

Remainder at index  $i$  = Remainder at index  $j$

$$s_2 \% k = s_1 \% k$$

$$\Rightarrow s_2 \% k - s_1 \% k = 0$$

$$\Rightarrow (s_2 - s_1) \% k = 0$$

$$\Rightarrow (\text{Sum of subarray from } i + 1 \text{ to } j) \% k = 0$$


Say the frequency of a remainder  $x$  is  $3$  .

It means that at  $3$  points, remainder  $3$  was encountered.

So if we draw a subarray from the next index of all those  $3$  points to our current index, we will get a sum divisible by  $k$  , so we will add that  $3$  to our answer.

At the end we will increment  $3$  to  $4$  (the count of  $x$  ) because our current index is one more point where we have encountered  $x$  .

So next time we encounter  $x$  again, we will be able to draw  $4$  subarrays from  $4$  points and add  $4$  to our answer.

We are currently here and we encountered remainder  $x$  again

a b c d e f g h i j k l

x

x

x

x

Remainder  $x$  encountered 3 times already, so we are able to get 3 subarrays till our current index

Sum of these 3 subarrays are divisible by  $k$

### Code:

Java

```
class Solution {
    public int subarraysDivByK(int[] nums, int k) {
        // map to store the remainders and number of times they've been encountered
        Map<Integer, Integer> map = new HashMap<>();
        // our sum is initially 0, and 0 is also divisible by k
        // there would be a case when remainder would actually be zero
        // so the array from the beginning to that index is our candidate subarray
        // so to address that case, so we put <0, 1> initially
        map.put(0, 1);
        int runningSum = 0, ans = 0;
        for (int n : nums) {
            runningSum += n;           // add the element to the running sum
            int rem = runningSum % k;  // get the remainder by k of our running sum
            if (rem < 0) {              // in case remainder < 0,
                rem += k;               // add divisor (k) to make it +ve
            }
            // if we already encountered the remainder, we add the frequency map
            // that frequency is nothing but the number of subarrays whose sum till that index is divisible by k
            ans += map.getOrDefault(rem, 0);
            // after that, we increment the frequency of that remainder,
            // because we have encountered it again so the number of subarrays is incremented by 1
            map.put(rem, 1 + map.getOrDefault(rem, 0));
        }

        return ans;    // return the answer
    }
}
```

25

☆

🔍

```
// TC: O(n), SC: O(n)
```

### Clean solution:

Java

```
class Solution {
    public int subarraysDivByK(int[] nums, int k) {
        Map<Integer, Integer> map = new HashMap<>();
        map.put(0, 1);
        int runningSum = 0, ans = 0;
        for (int n : nums) {
            runningSum += n;
            int rem = runningSum % k;
            if (rem < 0) {
                rem += k;
            }
            ans += map.getOrDefault(rem, 0);
            map.put(rem, 1 + map.getOrDefault(rem, 0));
        }

        return ans;
    }
}
```

↑ 25 ↓ [Share](#) [Favorite](#) ...



Comments (1)

[Previous](#)

[Next](#)

[Solution || 100% 100% Pref...](#)

[Day 19 || Explanation with Diagram ...](#) [Sort by: Best](#) →

Type comment here... (Markdown supported)

[Code](#) [Link](#) [@](#)

[Preview](#)

[Comment](#)



racemus

Jan 20, 2023

Thanks. It makes me understand why it works.

↑ 0 ↓ [Show 1 Replies](#) [Reply](#)

↑ 25 ↓ [Share](#) [Favorite](#) [Comment](#)

