FAN Liangdong

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Interests: Graph Theory, Combinatorics, Extremal Graph Theory

Education

Shanghai University

Shanghai, China

Bachelor of Mathematics and Applied Mathematics

Sept 2022 – present

- **GPA**: 3.76/4.0
- Core Course: Analysis I (90), Analysis II (99), Advanced Algebra I (94), Advanced Algebra II (100), Advanced Algebra III (98), Probability and Statistics(94), Real Analysis(92), Topology(92), Analytic Geometry(95), Differential Geometry(92)
- Supplementary Reading: Bondy, J.A., & Murty, U.S.R. (1976). Graph Theory with Applications. Macmillan.

Publications

[1] <u>L.D. Fan</u>, L.Y. Kang, J.D. Wu, Spectral extremal graphs of planar graphs with fixed size, arXiv:2410.00310. Under review in *European Journal of Combinatorics*

Research Experience

Spectral Extremal Graphs of Planar Graphs with Fixed Size

Jul 2024 - Oct 2024

Shanghai, China

• Abstract:

- Tait and Tobin [J. Combin. Theory Ser. B 126 (2017) 137–161] determined the unique spectral extremal graph over all outerplanar graphs and the unique spectral extremal graph over all planar graphs when the number of vertices is sufficiently large. In this paper we consider the spectral extremal problems of outerplanar graphs and planar graphs with fixed number of edges. We prove that the outerplanar graph on $m \geq 64$ edges with the maximum spectral radius is S_m , where S_m is a star with m edges. For planar graphs with m edges, our main result shows that the spectral extremal graph is $K_2 \vee \frac{m-1}{2} K_1$ when m is odd and sufficiently large, and $K_1 \vee (S_{\frac{m-2}{2}} \cup K_1)$ when m is even and sufficiently large. Additionally, we obtain spectral extremal graphs for path, circle and matching in outerplanar graphs and spectral extremal graphs for path, circle and complete graph on 4 vertices in planar graphs.

Spectral Extremal Graphs in Planar Graphs

Lead author | Supervisor: Prof. Living Kang

Oct 2024 - present

Researcher | Supervisor: Prof. Liying Kang

Shanghai, China

- Current Progress:
 - For sufficiently large n, the maximum spectral radius and the unique extremal graph were determined for all planar graphs on n vertices that do not contain Fan_k as a subgraph, where $Fan_k = K_1 \vee P_{k-1}$.
 - The conjecture by Boots and Royle, and independently by Cao and Vince, positing that for $n \ge 9$, the planar graph with the maximum spectral radius is $P_2 \lor P_{n-2}$, held for n greater than 10^9 .

Honors and Awards

First Prize in the Shanghai University Qian Weichang College Undergraduate	2024
Research and Innovation Forum	
Shanghai University Top Academic Scholarship	2024
Shanghai University Top Academic Scholarship	2023
National Encouragement Scholarship	2024

Skills

Technologies: Python, C++, SPSS, MT_FX