

$$x \cdot y = k = L^2 \Rightarrow \sqrt{x \cdot y} = L$$

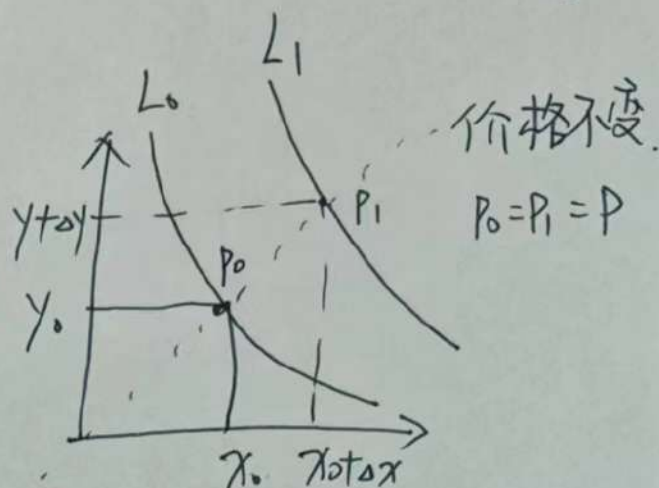
①

价格 $p = \frac{y}{x}$ x 用 y 计价

$$L_0 = \sqrt{x_0 \cdot y_0}$$

添加流动性 Δx 和 Δy

$$L_1 = \sqrt{(x_0 + \Delta x)(y_0 + \Delta y)}$$



$$\text{求 } \Delta L = L_1 - L_0 = \Delta x \cdot \bar{P} = \frac{\Delta y}{\bar{P}}$$

$$\text{解: } x = \frac{y}{p} \Rightarrow x \cdot y = \frac{y^2}{p} \Rightarrow L^2 = \frac{y^2}{p} \Rightarrow L = \frac{y}{\bar{p}}$$

$$y = xP \Rightarrow L = \frac{xP}{\bar{P}} = x\bar{P}$$

用 x 表示:

$$\Delta L = L_1 - L_0 = (x_0 + \Delta x)\bar{P}_1 - x_0\bar{P}_0$$

因为 $P_0 = P_1$

$$\Delta L = (x_0 + \Delta x)\bar{P}_0 - x_0\bar{P}_0 = \Delta x\bar{P}_0$$

用 y 表示:

$$\Delta L = L_1 - L_0 = \frac{y_0 + \Delta y}{\bar{P}_1} - \frac{y_0}{\bar{P}_0}$$

因为 $P_0 = P_1$

$$\Delta L = \frac{y_0 + \Delta y}{\bar{P}_0} - \frac{y_0}{\bar{P}_0} = \frac{\Delta y}{\bar{P}_0}$$

案例:

(2)

初始LP: 100 DAI: 1 ETH.

$$x \cdot y = k \Rightarrow 100 \cdot 1 = 100.$$

$$P_E = 100 \text{ DAI/ETH}$$

$$\text{总价值} = 100 \text{ DAI} + 1 \text{ ETH} = 200 \text{ U}$$

ETH涨价: 120 DAI: 0.83 ETH

$$x \cdot y = k \Rightarrow 120 \cdot 0.83 = 100$$

$$P_E = \frac{120}{0.83} = 144.58 \text{ DAI/ETH}$$

$$\text{总价值} = 120 \text{ DAI} + 0.83 \text{ ETH} = 240 \text{ U}$$

如果不做LP:

$$\text{总价值} = 100 \text{ DAI} + 1 \text{ ETH} = 100 + 144.58 = 244.58$$

$$\text{少赚 } 244.58 - 240 = 4.58 \text{ U}$$

ETH降价: 80 DAI: 1.25 ETH

$$x \cdot y = k \Rightarrow 80 \cdot 1.25 = 100$$

$$P_E = \frac{80}{1.25} = 64 \text{ DAI/ETH}$$

$$\text{总价值} = 80 \text{ DAI} + 1.25 \text{ ETH} = 160 \text{ U}$$

如果不做LP:

$$\text{总价值} = 100 \text{ DAI} + 1 \text{ ETH} = 164 \text{ U}$$

$$\text{少亏 } 164 - 160 = 4 \text{ U}$$

token x (ETH). token y (DAI)

(3)

x : 池子里 ETH 的数量

y : 池子里 DAI 的数量

$P = \frac{y}{x}$: ETH 用 DAI 计价的价格. 例: $P = \frac{1000 \text{ DAI}}{10 \text{ ETH}} = 100 \text{ DAI/ETH}$

由 $\sqrt{xy} = L$ 和 $P = \frac{y}{x}$ 可以得出 $\begin{cases} y = \frac{L^2}{x} \Rightarrow y = L\sqrt{P} \\ x = \frac{y}{P} \Rightarrow x = \frac{L}{\sqrt{P}} \end{cases}$

$$IL(d) = \frac{\text{做LP的损失}}{h_{\text{odd}}} = \frac{V_1 - V_{\text{odd}}}{V_{\text{odd}}}$$

V_1 : 在 t_1 时刻, 池子里 token 的价值

V_{odd} : 在 t_1 时刻, 如果不做 LP, token 的价值

P_0 : 在 t_0 时的价格. $P_0 = \frac{x_0}{y_0}$

P_1 : 在 t_1 时的价格. $P_1 = \frac{x_1}{y_1}$

$$V_1 = y_1 + x_1 \cdot P_1 = L\sqrt{P_1} + \frac{L}{\sqrt{P_1}} \cdot P_1 = 2L\sqrt{P_1}$$

$$V_{\text{odd}} = y_0 + x_0 P_1 = L\sqrt{P_0} + \frac{L}{\sqrt{P_0}} \cdot P_1$$

规定 $P_1 = P_0 \cdot d$

$$V_{\text{odd}} = L\sqrt{P_0} + \frac{L}{\sqrt{P_0}} \cdot P_0 d = (1+d)L\sqrt{P_0}$$

$$IL(d) = \frac{V_1 - V_{\text{odd}}}{V_{\text{odd}}} = \frac{2L\sqrt{P_0 d} - (1+d)L\sqrt{P_0}}{(1+d)L\sqrt{P_0}} = \frac{2\sqrt{d} - (1+d)}{1+d} = \frac{2\sqrt{d}}{1+d} - 1$$