

## Unsigned integer multiplication done by shifting and adding

Start with the operands at the top of two columns. Repeatedly divide the left column's value by 2 (integer division) and multiply the right column's value by 2, until the left column's value reaches one. Omit all rows in which the left column's value is even. Then add the remaining rows of the right column. For example ( $36 * 26$ ):

Here are the columns formed by halving left value and doubling right value until left column reaches 1:

26	36
13	72
6	144
3	288
1	576

Omit all rows where left column is even then add the right column's values:

26	36
13	72
6	144
3	288
1	576
	----
	936

( $36 * 26 = 936$ )

Why does this work? Here's the same example shown in binary:

11010	100100	
1101	1001000	$72_{10}$
110	10010000	
11	100100000	$288_{10}$
1	1001000000	$576_{10}$
	-----	
	1110101000	$936_{10}$

Showing the binary multiplication (it's the same algorithm as for decimal multiplication):

100100
11010
-----
000000
1001000
00000000
100100000
1001000000
-----
1110101000

Notice when the appropriate bit of the lower operand is 0, the row in the resulting addition is all zero bits, so it can be omitted. The sum of the non-zero rows is the product.