1. 语言和文法

文法 (grammar)

表达语言构成规则的形式化方法

 $G=(V_N, V_T, S, P)$

V_N:非终结符集

V_T:终结符集

S:文法开始符号

P:产生式 $A \rightarrow \alpha$

由文法产生语言 (3型)

Regular Grammar

例:设文法 $G_1 = (\{S\}, \{a,b\}, S,P)$,其中P为:

- $(0) S \rightarrow aS$
- $(1) S \rightarrow a$
- $(2) S \rightarrow b$

答: $L(G_1) = \{a^i(a \mid b) \mid i >= 0\}$

由文法产生语言 (2型)

例: 设文法
$$G_2 = (\{S\}, \{a,b\}, P,S)$$
, 其中P为: (0) $S \rightarrow aSb$ (1) $S \rightarrow ab$

答: $L(G_2)=\{a^nb^n|n>=1\}$

由语言构造文法 - 题型

• 构造形如a^{mi}bⁿⁱ的语言的文法

• $a^{i}b^{j}$, $(i \ge 2j, j \ge 1)$ $a^{i-2j}a^{2j}b^{j}$

由语言构造文法(续)

例:设 $L_2=\{a^ib^jc^k\mid i,j,k>=1$ 且 $a,b,c\in V_T\}$,试构造生成 L_2 的文法 G_2 。

答: (0) S → aS | aB

(1) $B \rightarrow bB \mid bC$

(2) $C \rightarrow cC \mid c \quad L2R$

- $(0) S \rightarrow ABC$
- $(1) A \rightarrow aA \mid a$
- (2) B \rightarrow bB | b
- (3) $C \rightarrow cC \mid c$ T2B

构造无e产生式的上下文无关文法

- 无8产生式的上下文无关文法要满足条件
 - 若P中含S → ε ,则S不出现在任何产生式右部,其中S为文法的开始符号;
 - P中不再含有其它任何ε产生式。

例题

设
$$G_1$$
=({S},{a,b},P,S),其中
P: (0) S $\rightarrow \epsilon$ (1) S \rightarrow aSbS (2) S \rightarrow bSaS

答案:

$$(1) V_0 = \{S\}$$

(2) P':
$$S\rightarrow abS \mid aSbS \mid abb \mid ab$$
 $S\rightarrow baS \mid bSaS \mid bSa \mid ba$ $S'\rightarrow \epsilon \mid S$

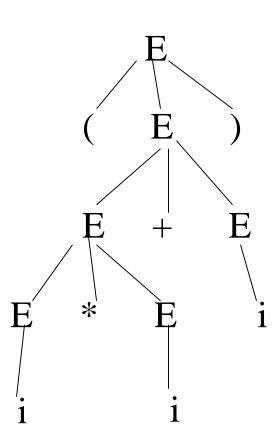
(3)
$$G_1' = (\{S', S\}, \{a, b\}, P', S')$$

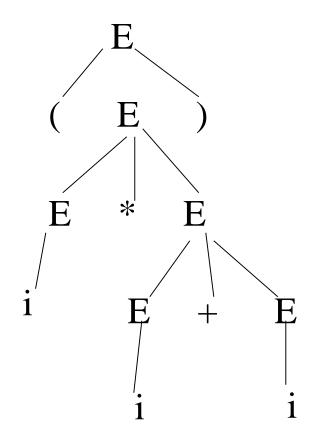
二义性文法

$$E \rightarrow E + E \mid E * E \mid (E) \mid i$$

$$(i * i + i)$$

非二义性文法 $E \rightarrow T \mid E + T$ $T \rightarrow F \mid T * F$ $F \rightarrow (E) \mid i$





2. 词法分析

Theme of this Chapter

Regular Expression Finite Automata Regular Grammar

NFA-DFA-DFA_{min}

Subset Construction algorithm

$$(1)I_0 = \varepsilon - closure(S_0), I_0 \in Q$$

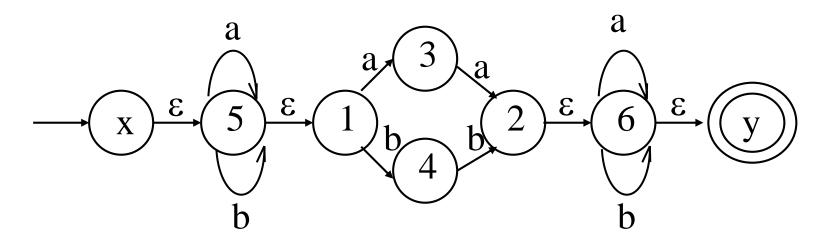
(2) For each I_i , $I_i \in Q$,

let $I_t = \varepsilon$ -closure(move(I_i ,a))

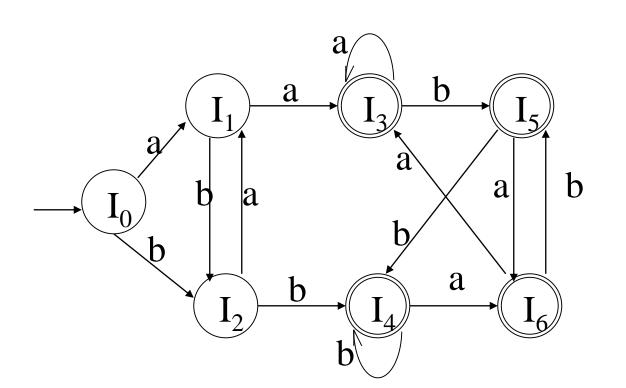
if $I_t \notin Q$, then put I_t into Q

(3)Repeat step (2), until there is no new state to put into Q

(4)Let $F=\{I \mid I \in Q, and I \cap Z <>\Phi\}$

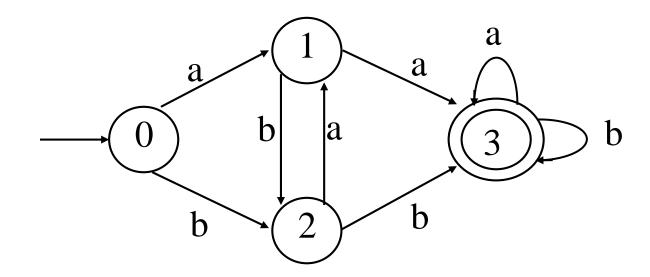


Ι	а	b
$I_0 = \{x, 5, 1\}$	$I_1 = \{5,3,1\}$	$I_2 = \{5,4,1\}$
$I_1 = \{5,3,1\}$	$I_3 = \{5,3,2,1,6,y\}$	
$I_2 = \{5,4,1\}$	$I_1 = \{5,3,1\}$	$I_4 = \{5,4,1,2,6,y\}$
1 -	$I_3 = \{5,3,2,1,6,y\}$	
$I_4 = \{5,4,2,1,6,y\}$		$I_4 = \{5,4,1,2,6,y\}$
$I_5 = \{5,1,4,6,y\}$	$I_6 = \{5,3,1,6,y\}$	$I_4 = \{5,4,1,2,6,y\}$
$I_6 = \{5,3,1,6,y\}$	$I_3 = \{5,3,2,1,6,y\}$	$I_4 = \{5,1,4,6,y\}$



$$\Pi_0 = \{ \{0,1,2\}, \{3,4,5,6\} \}$$

$$\Pi_1 = \{ \{1\}, \{0\}, \{2\}, \{3,4,5,6\} \}$$



FA

Write grammer for the following languages over the alphabet $\Sigma = \{0, 1\}$:

- (1) All strings that contain an odd number of 1's.
- (2) All strings which do not contain the substring 01.

3. 语法分析

To Avoid Backtracking

No left recursion (direct & indirect)

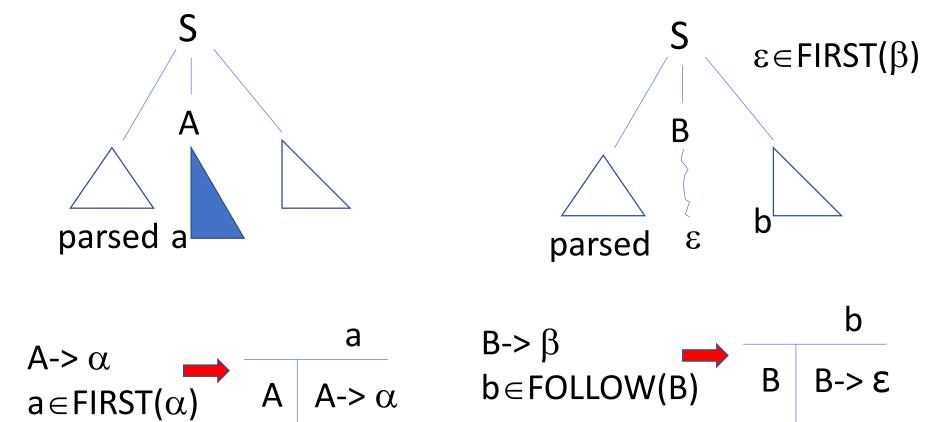
```
P \rightarrow P\alpha | \beta = >
P \rightarrow \beta P' P' \rightarrow \alpha P' | \epsilon
```

- No common prefixes extract common left factor
- No ambiguity
 rewrite the grammar
 operator: precedence & associativity
 else dangling

Compute First & Follow Set

• FIRST(α) $\alpha = \alpha_1 \alpha_2 \dots \alpha_n$ $FIRST(\alpha) = FIRST(\alpha_1), \ \epsilon \notin FIRST(\alpha_1)$ $(FIRST(\alpha_1)-\{\epsilon\}) \cup (FIRST(\alpha_2)-\{\epsilon\}) \dots$ \cup FIRST (α_{ν}) $\varepsilon \in FIRST(\alpha_i)$ (1\leq i < k), $\varepsilon \notin FIRST(\alpha_k)$ $\varepsilon \in FIRST(\alpha)$ if $\varepsilon \in FIRST(\alpha_i)$ ($1 \le i \le n$) FOLLOW(N) $A - > \alpha N\beta$ Add FIRST(β)-{ ϵ } If $\varepsilon \in FIRST(\beta)$, or A-> α N, Add FOLLOW(A)

Construct Predictive Parsing Table



LL(1) Grammar?

- Construct parsing table
 look for multidefined entries
- Look at FIRST & FOLLOW sets

```
G is LL(1) \Leftrightarrow
```

whenever there exists $A - > \alpha | \beta$ in G,

- (1) $FIRST(\alpha) \cap FIRST(\beta) = \emptyset$
- (2) At most one of α and β derive the ϵ , if $\beta \Rightarrow \epsilon$, then FIRST(α) \cap FOLLOW(A)= \varnothing
- // Left recursion, common prefixes, ambiguious grammar

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid id$$

1.
$$E \rightarrow TE'$$

2. E'
$$\rightarrow$$
 +TE'

3. E'
$$\rightarrow \epsilon$$

4.
$$T \rightarrow FT'$$

$$5. T' \rightarrow *FT'$$

6. T'
$$\rightarrow \epsilon$$

7.
$$F \rightarrow id$$

8.
$$F \rightarrow (E)$$

First(E`)=
$$\{+, \epsilon\}$$

First(T`)=
$$\{*, \epsilon\}$$

Follow(E)= Follow(E`)=
$$\{$$
), $\$$ $\}$

Follow(T)= Follow(T`)=
$$\{+,),\$$$

Follow(F)=
$$\{*,+,),\$\}$$

	id	+	*	()	\$
Е	E→TE'			E→TE'		
E'		E'→+TE'			E'→ε	E'→ε
T	T→FT'			T→FT'		
T'		T'→ε	T'→*FT'		T'→ε	T'→ε
F	$F \rightarrow id$			F →(E)		

LR Parsing

SLR(1): FOLLOW

LR(1):

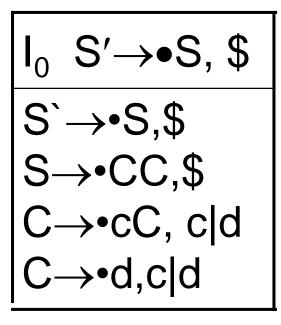
LALR(1)

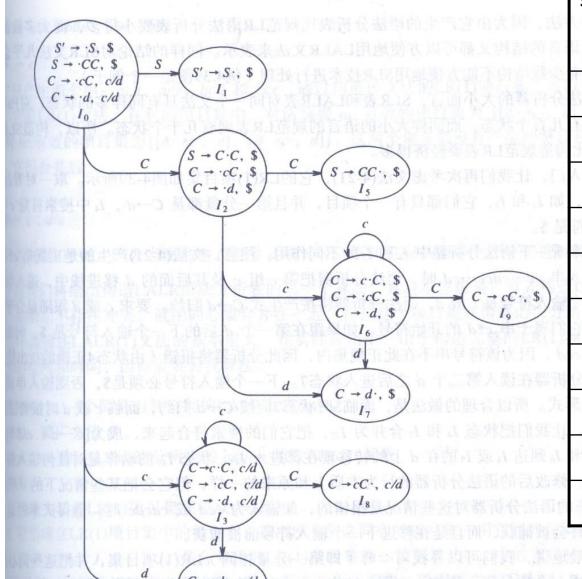
```
Closure(I) repeat { for each item [A \rightarrow \alpha^{\bullet}B\beta,a] in I add all [B \rightarrow^{\bullet} \gamma,b] for all b \in FIRST(\beta a) to I (if not already in I); } until (no more items can be added to I);
```

1.
$$S \rightarrow S$$

2.
$$S \rightarrow CC$$

3.
$$C \rightarrow cC|d$$





				_	
state		Action	1	go	oto
	С	d	\$	S	С
0	S ₃	S ₄		1	2
1			acc		
2	S ₆	S ₇			5
3	S ₃	S ₄			8
4	r ₃	r ₃			
5			r ₁		
6	S ₆	S ₇			9
建建 7			r ₃		
8	r ₂	r ₂			
9			r ₂		

IO:
$$E' \rightarrow \bullet E$$

$$E \rightarrow \bullet E + E$$

$$E \rightarrow \bullet E * E$$

I1:
$$E' \rightarrow E \bullet$$

$$E \rightarrow E + E$$

$$E \rightarrow E^{\bullet} * E$$

I2:
$$E \rightarrow (\bullet E)$$

$$E \rightarrow E + E$$

$$E \rightarrow E * E$$

$$E \rightarrow \bullet(E)$$

$$E \rightarrow \bullet id$$

I4:
$$E \rightarrow E + \bullet E$$

 $E \rightarrow \bullet E + E$

I5:
$$E \rightarrow E^* \bullet E$$

$$E \rightarrow E + E$$

$$E \rightarrow E * E$$

I6:
$$E -> (E \bullet)$$

$$E \rightarrow E + E$$

$$E \rightarrow E \bullet * E$$

I7:
$$E -> E + E -$$

$$E \rightarrow E + E$$

$$E \rightarrow E \bullet * E$$

I8:
$$E -> E * E -$$

$$E \rightarrow E + E$$

$$E \rightarrow E^{\bullet} * E$$

I9:
$$E -> (E)$$
•

I ₁ :	E'->E•
	E->E• +E
	E->E• *E

l ₈ :	E->E*E●
	E->E• +E
	F->F● *F

			Actio	on			goto
	id	+	*	()	\$	Е
0	S ₃			S2			1
1		S4	S5			acc	
2	S_3			S2			6
3		r ₄	r4		r4	r4	
4	S_3			S2			7
5	S_3			S ₂		r_1	8
6		S ₄	S ₅		S ₉		
7		r ₁ /S ₄	S ₅ /r ₁		r_1	r_1	
8		r ₂ /S ₄	r ₂ /S ₅		r_2	r_2	
9		r ₃	r ₃		r ₃	r_3	

id+id*id 0,1,4,7 E+E *id\$
Id+id+id 0,1,4,7 E+E +id\$

I ₇ :	E->E+E∙
	E->E• +E
	E->E• *E

l ₈ :	E->E*E●
	E->E• +E
	F->F• *F

r ₁ /S ₄	S ₅ /r ₁
r ₂ /S ₄	r ₂ /S ₅

Specify precedence & associativity

		Action					goto
	id	+	*	()	\$	Е
0	S_3			S2			1
1		S4	S5			acc	
2	S_3			S2			6
3		r ₄	r4		r4	r4	
4	S_3			S2			7
5	S_3			S ₂		r_1	8
6		S ₄	S ₅		S ₉		
7		r_1	S ₅		$r_{\scriptscriptstyle 1}$	r_1	
Ø		r_2	r ₂		r_2	r_2	
9		r ₃	r ₃		r_3	r ₃	

4. 语法制导翻译

E.g. Annotated parse tree for 3*5+4 n

产生式	语义规则	
1) $L \to E \mathbf{n}$	L.val = E.val	
$2) E \to E_1 + T$	$E.val = E_1.val + T.val$	L.val = 19
$3) E \to T$	E.val = T.val	
$4) T \to T_1 * F$	$T.val = T_1.val \times F.val$	E.val = 19 n
$5) T \to F$	T.val = F.val	
$6) F \to (E)$	F.val = E.val	E.val = 15 + $T.val = 4$
7) $F \to \mathbf{digit}$	$F.val = \mathbf{digit}.lexval$	
• 3*5+4n	$T.val = 3$ $\begin{vmatrix} F.val = 3 \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$	3
	algit.lexval =	= 3

lexval, val: synthesized attribute

• E.g. Syntax-directed definition with inherited attribute L.in

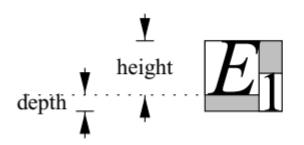
Production	Semantic rules
$D \rightarrow T L$	L.in=T.type
T →int	T.type= integer
T →real	T.type=real
$L \rightarrow L^{(1)}$,id	L (1).in=L.in addtype(id .entry, L.in)
$L \rightarrow id$	addtype(id.entry, L.in)

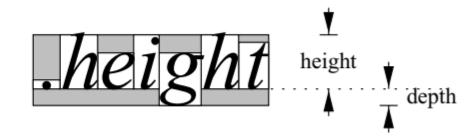
real id1,id2,id3 T.type=real ____ L.in=real L.in=real, id3 real id2 L.in=real id1

in: inherited attribute

type: synthesized attribute

SDT for L-attributed SDD ----Typesetting Box





Production

Semantic Rules

$$S \rightarrow B$$

$$B.ps=10$$

$$B \rightarrow B_1 B_2$$

$$B_1.ps=B.ps$$

$$B_2.ps = 0.7*B.ps$$

B.ht=
$$max(B_1.ht,B_2.ht-0.25*B.ps)$$

$$B.dp=max(B_1.dp,B_2.dp+0.25*B.ps)$$

$$B \rightarrow text$$

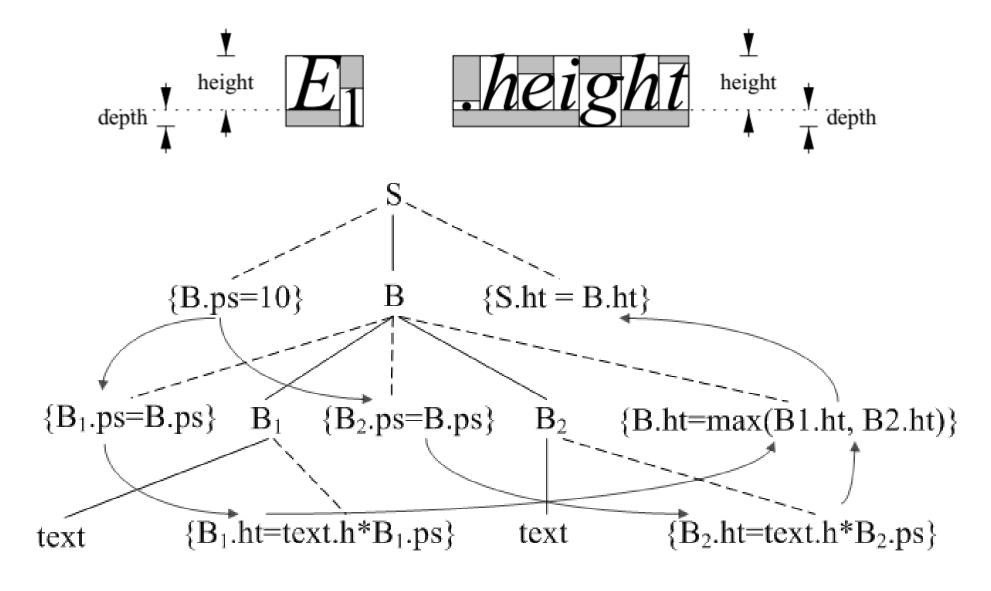
SDT

$$S \rightarrow \{B.ps=10\}B\{S.ht=B.ht\}$$

 $B \rightarrow \{B_1.ps=B.ps\}B_1\{B_2.ps=B.ps\}B_2\{B.ht=max(B_1.ht,B_2.ht)\}$
 $B \rightarrow text \{B.ht=text.h*B.ps\}$

- -Inherited attribute B.ps: the point size of block B
- -Synthesized attribute B.ht: the height of box B
- -Synthesized attribute B.dp: the depth of box B

A Simplified Version of Example 5.18



5. 中间代码生成

```
S \rightarrow id = E; { gen(top.get(id.lexeme) '=' E.addr); }
    L = E; { gen(L.array.base'['L.addr']''='E.addr); }
E \rightarrow E_1 + E_2 \quad \{ E.addr = \mathbf{new} \ Temp(); \}
                    qen(E.addr'='E_1.addr'+'E_2.addr); }
     id \{E.addr = top.get(id.lexeme); \}
     L 	 \{ E.addr = \mathbf{new} \ Temp() \}
                   gen(E.addr'=' L.array.base'[' L.addr']'); }
L \rightarrow id [E] \{L.array = top.get(id.lexeme);
                    L.type = L.array.type.elem;
                    L.addr = \mathbf{new} \ Temp();
                     gen(L.addr'='E.addr'*'L.type.width); 
     L_1 [E] \{L.array = L_1.array;
                    L.type = L_1.type.elem;
                    t = \mathbf{new} \ Temp();
                     L.addr = \mathbf{new} \ Temp();
                     gen(t'='E.addr'*'L.type.width);
                     qen(L.addr'='L_1.addr'+'t);
```

```
L \rightarrow id [E]
                     \{L.array = top.get(id.lexeme);
                                                                       c+a[i][j]
                       L.type = L.array.type.elem;
                       L.addr = new Temp();
                       gen(L.addr'='E.addr'*'L.type.width); }
       L_1 [ E ]
                    \{L.array = L_1.array;
                                                               E \rightarrow E_1 + E_2
                                                                               \{E.addr = \mathbf{new} \ Temp();
                       L.type = L_1.type.elem;
                      t = \mathbf{new} \ Temp();
                                                                                 gen(E.addr'='E_1.addr'+'E_2.addr);
                       L.addr = new \ Temp();
                       gen(t'='E.addr'*'L.type.width):
                                                                     id
                                                                               \{E.addr = top.get(id.lexeme); \}
                       gen(L.addr'='L_1.addr'+'t); \}
                                                                     L
                                                                                \{ E.addr = \mathbf{new} \ Temp(); 
                                                                                 gen(E.addr'=' L.array.base'[' L.addr']'); }
                         E.addr = t_5
    E.addr = c
                                               E.addr = t_4
         С
                                              L.array = a
                                               L.type = integer
                                               L.addr = t_3
                  L.array = a
                    L.type = array(3, integer)
                                                      E.addr = j
                   L.addr = t_1
                                                                                             t_5 = c + t_4
                                 E.addr = i
   a.type
   = array(2, array(3, integer))
```

图 6-24 表达式 c + a[i][j]

Backpatching for Boolean Expressions

```
B \rightarrow !B_1
                              \{B.truelist = B_1.falselist;
                                 B.falselist = B_1.truelist; }
4) B \rightarrow (B_1)
                              \{B.truelist = B_1.truelist;
                                 B.falselist = B_1.falselist; }
     B \to E_1 \text{ rel } E_2
                              \{ B.truelist = makelist(nextinstr); \}
                          99 B.falselist = makelist(nextinstr + 1);
                             /or gen('if' E_1.addr rel.op E_2.addr'goto _');
                             /o/ gen('goto 0'); }
                              nextinstr. 102
                           99 { B.truelist = makelist(nextinstr);
     B \to \mathbf{true}
                             /vo:gen('goto ');}
     B \to \mathbf{false}
                              \{ B.falselist = makelist(nextinstr); \}
                                 gen('goto Q'); \}
8)
     M \to \epsilon
                              \{ M.instr = nextinstr; \}
```

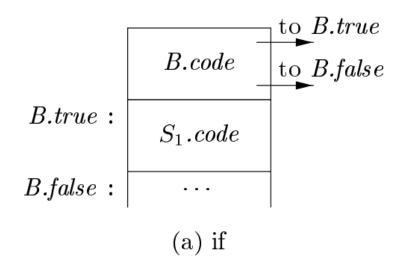
```
1) B \rightarrow B_1 \mid M_1B_2 \mid B_2 \mid B_1B_2 \mid B_1B_2 \mid B_1B_2 \mid B_1B_2 \mid B_2B_2 \mid 
M.Mtr: 150
               2) B \rightarrow B_1 \&\& M_{\bullet}B_2 { backpatch(B_1.truelist, M.instr); } B.truelist = <math>B_2.truelist; B_2.truelist; B_3.truelist = B_2.truelist; B.falselist = merge(B_1.falselist, B_2.falselist); }
                 x < 100 \mid | x > 200 \&\& x ! = y
                                                          if x < 100 goto ₫
                                                                                                                                                                                                                                                                                                                                      B.f = \{103, \overline{105}\}
         100:
                                                goto <a>Q√02</a>
         101:
                                                                                                                                                                                                                                                                                                                                                        M.i = 102
                                             if x > 200 goto 
arrange^{\frac{1}{2}} = \frac{4}{3}

         102:
                                                                                                                                                                                                                                     B.t = \{100\}
                                                                                                                                                                                                                                                                                                                                                                                                                                           B.t = \{104\}
                                                          goto 🗹
                                                                                                                                                                                          B.f = \{101\}
         103:
                                                                                                                                                                                                                                                                                                                                                                                                                                          B.f = \{103, 105\}
         104: if x != y goto x < 100
                                                                                                                                                                                                                                                                                                                                                                                                                                                      M.i = 104
          105:
                                                             goto 🗓 /03
                                                                                                                                                                                                                                                                                                                                         B.t = \{102\}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              B.t = \{104\}
                                                                                                                                                                                                                                                                                                                                       B.f = \{103\}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            B.f = \{105\}
                                                                                                                                                                                                                                                                                                                                                           > 200
```

Figure 6.44: Annotated parse tree for $x < 100 \mid \mid x > 200 \&\& x ! = y$

```
1) S \to \mathbf{if}(B) M S_1 \{ backpatch(B.truelist, M.instr); \}
                          S.nextlist = merge(B.falselist, S_1.nextlist); 
2) S \rightarrow \mathbf{if}(B) M_1 S_1 N \text{ else } M_2 S_2
                        { backpatch(B.truelist, M_1.instr);
                          backpatch(B.falselist, M_2.instr);
                          temp = merge(S_1.nextlist, N.nextlist);
                          S.nextlist = merge(temp, S_2.nextlist);
3) S \rightarrow while M_1 (B) M_2 S_1
                        { backpatch(S_1.nextlist, M_1.instr);
                          backpatch(B.truelist, M_2.instr);
                          S.nextlist = B.falselist;
                          emit('goto' M_1.instr); \}
4) S \rightarrow \{L\} { S.nextlist = L.nextlist; }
5) S \to A; { S.nextlist = null; }
6) M \to \epsilon { M.instr = nextinstr; }
7) N \rightarrow \epsilon
                       \{ N.nextlist = makelist(nextinstr); \}
                          emit('goto _'); }
8) L \rightarrow L_1 M S { backpatch(L_1.nextlist, M.instr);
                          L.nextlist = S.nextlist; }
9) L \rightarrow S
                       \{L.nextlist = S.nextlist;\}
```

$$S \rightarrow \mathbf{if}(B) M S_1 \{ backpatch(B.truelist, M.instr); \\ S.nextlist = merge(B.falselist, S_1.nextlist); \}$$



```
S \rightarrow \mathbf{if}(B) M_1 S_1 N \mathbf{else} M_2 S_2
\{ backpatch(B.truelist, M_1.instr); \\ backpatch(B.falselist, M_2.instr); \\ temp = merge(S_1.nextlist, N.nextlist); \\ S.nextlist = merge(temp, S_2.nextlist); \}
```

B.code $S_1.code$ $S_1.code$ $S_2.code$ \ldots

(b) if-else

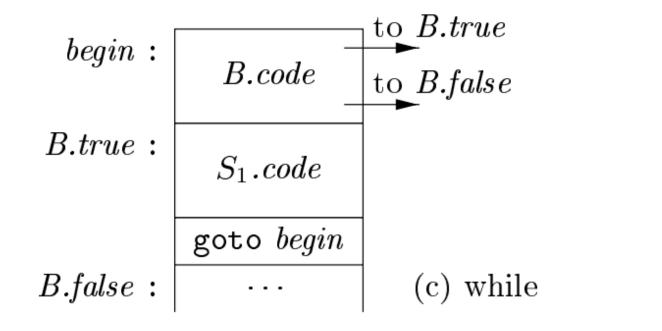
```
S \rightarrow while M_1 (B) M_2 S_1

{ backpatch(S_1.nextlist, M_1.instr);

backpatch(B.truelist, M_2.instr);

S.nextlist = B.falselist;

gen('goto' M_1.instr); }
```



```
S \rightarrow \mathbf{if} (B) S_1
                                B.true = newlabel()
                                 B.false = S_1.next = S.next
                                 S.code = B.code \mid | label(B.true) \mid | S_1.code
S \rightarrow \mathbf{if} (B) S_1 \mathbf{else} S_2 \mid B.true = newlabel()
                                B.false = newlabel()
                                 S_1.next = S_2.next = S.next
                                 S.code = B.code
                               || label(B.true) || S_1.code
|| gen('goto' S.next)
|| label(B.false) || S_2.code
 S \rightarrow \mathbf{if}(B) M S_1 \{ backpatch(B.truelist, M.instr); \}
                           S.nextlist = merge(B.falselist, S_1.nextlist);}
 S \rightarrow \mathbf{if}(B) M_1 S_1 N \mathbf{else} M_2 S_2
                         { backpatch(B.truelist, M_1.instr);
                            backpatch(B.falselist, M_2.instr);
                            temp = merge(S_1.nextlist, N.nextlist);
                            S.nextlist = merge(temp, S_2.nextlist);
```

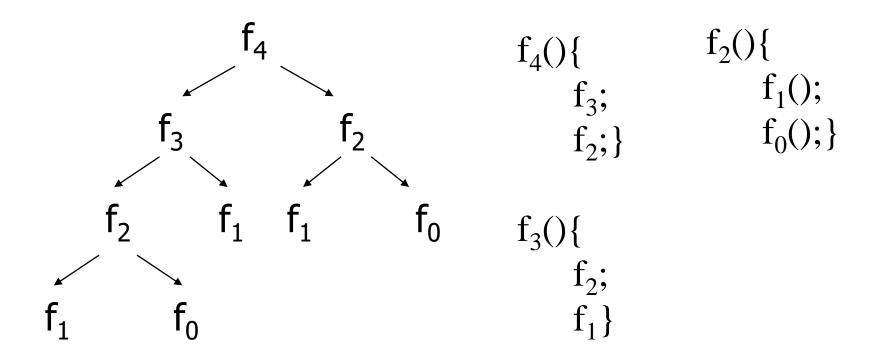
Translate the following program fragment into three-address-code using short circuit code and back-patching techniques.

```
while (a==r || a>b) {
    if (r==s)
        y=y+c;
    else
        y=y-d;
}
```

6.运行时环境

Activation Trees

A tree to depict the control flow enters and leaves activation of a procedure



An Example

```
#include <stdio.h>
 int i,j;
 int main()
    int k,l;
    cin>>l; //assume I=3
    k=p(I);
    cout<<k;
```

```
int p(int m)
    int t;
    if (m==0 || m==1)
      return(1);
    else {
      t=m*p(m-1);
      return(t); } }
```

+19	•••	
+18	K+12(SPp(2))	
+17	Returned value from P(2)	
+16	t	
+15	Formal Parameter m	2
+14	Number of Parameter	1
+13	Returned address	
+12	K+6(SPp(3))	
+11	Returned value from P(3)	
+10	t	

+9	Formal	3
	Parameter m	
+8	Number of	1
	Parameter	
+7	Returned address	
+6	K+2(SPmain)	
+5	Returned value from main	
+4	1	3
+3	k	
+2	K(SP0)	
+1	j	
K	i	

7.代码优化

Optimization of Basic Blocks

- Constant folding
 - Evaluate constant expressions at compile time and replace the constant expressions by their values
- Common subexpression elimination
- Copy propagation
- Dead code elimination

An Example

A source code

$$A: = 2*Pi*(R+r);$$

$$B:=A;$$

$$B:=2*Pi*(R+r)*(R-r)$$

$$(1)$$
Pi:=3.14

$$(2)T1:=2*Pi$$

$$(3)T2:=R+r$$

$$(4)A:=T1*T2$$

$$(5)B:=A$$

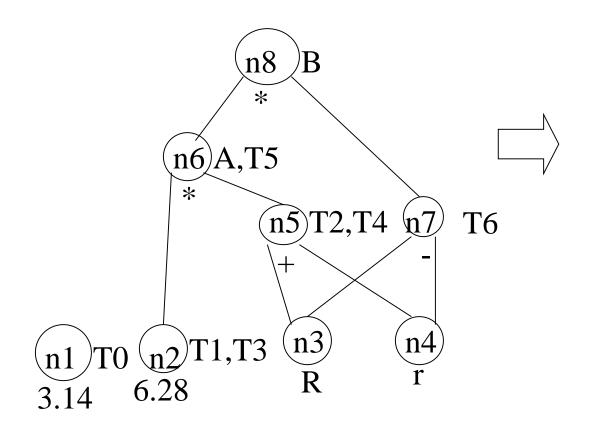
$$(6)T3:=2*Pi$$

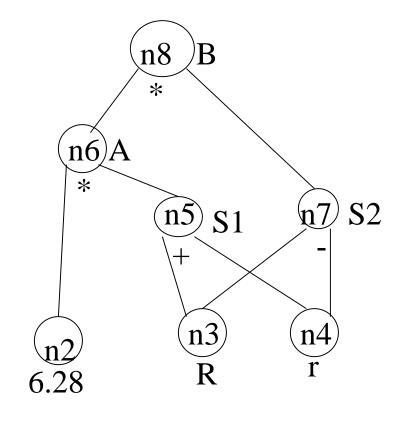
$$(7)T4:=R+r$$

$$(8)T5:=T3*T4$$

$$(9)T6:=R-r$$

$$(10)B:=T5*T6$$





- (1) S1=R+r
- (2) S2=R-r
- (3) A=6.28*S1
- (4) B=6.28*A