The Ideal Continual Learner: An Agent That Never Forgets

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Continual Learning: Problem Setup

$$\mathcal{G}_t \coloneqq \operatorname*{argmin}_{w \in \mathcal{W}} L_t(w; D_t)$$

- L_t : Loss function of task t
- D_t: Data for task t
- W: Search space
- \mathcal{G}_t : The set of global minimizers
- Tasks 1, ..., T are presented sequentially
- Goal: learn a model \widehat{w}_T that solves all tasks
- Challenge ("Catastrophic Forgetting"): model \widehat{w}_T may perform poorly on previous tasks

Methods to Prevent Forgetting

Regularization-based, e.g.,

$$\min_{\mathbf{w}\in\mathcal{W}} L_t(\mathbf{w}; D_t) + \delta \cdot \left| |\mathbf{w} - \widehat{\mathbf{w}}_{t-1}| \right|_2$$

- *Memory-based*, e.g., rehearsal: train with current data and part of previous data
- Expansion-based: tasks ↑ ⇒ parameters ↑,
 only train on new parameters

These methods greatly improved empirical performance in the deep learning context!

Theory that can explain their empirical success has been few and far between!!!

The Ideal Continual Learner (ICL)

With $\mathcal{K}_t \coloneqq \mathcal{W}$, **ICL** is a method that solves $\mathcal{K}_t \coloneqq \operatorname*{argmin} L_t(w; D_t)$ $\underset{w \in \mathcal{K}_{t-1}}{\mathcal{H}_t}$

sequentially, for t = 1, 2, ..., T.

ICL Never Forgets by Design

Suppose $\bigcap_{t=1}^T \mathcal{G}_t \neq \emptyset$. Then:

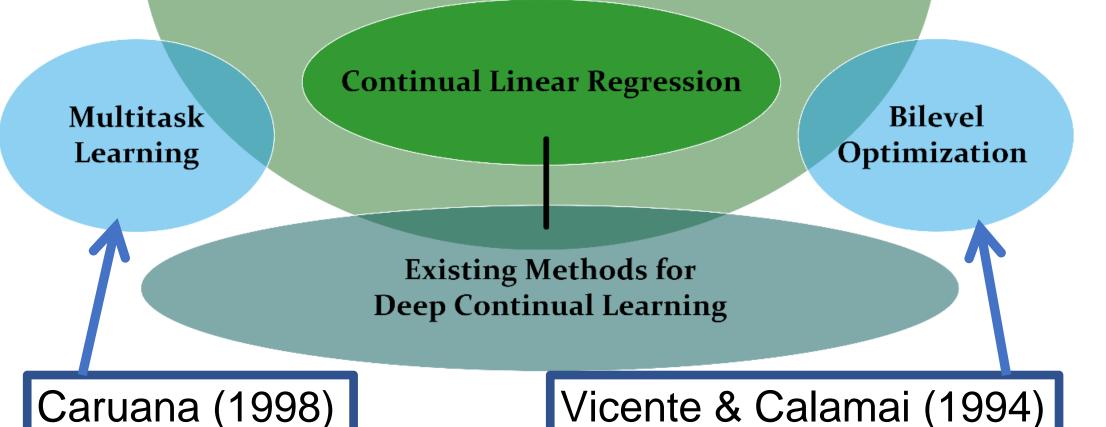
Bunch & Nielsen (1978)

- / ICL is sufficient to prevent forgetting
- The storage consumption of ICL is minimal to prevent catastrophic forgetting

Witsenhausen (1968)

Oja (1982), Yang (1995) Chamon et al. (2022) Incremental SVD Streaming PCA Subspace Tracking Constrained Learning Continual Matrix Factorization Continual Matrix Factorization

The Ideal Continual Learner



Take-Away Messages from ICL

History & Future (Figure in the middle)
Connections of ICL to other topics shed light
on historical remarks & research avenues

All Roads Lead to Rome

ICL can be viewed as a regularizationbased, memory-based (projection-based), or expansion-based method. Put differently, these methods, designed via engineering insights, are all Ideal Continual Learners.

Rehearsal is an Ideal Continual Learner

We prove the first generalization guarantee for rehearsal, a highly performant memory-based method

Wider Networks ⇒ Less Forgetting

By analyzing ICL, we rigorously show, for the first time, that wider neural networks forget less catastrophically.

Conclusion & Limitation

- ICL is the first general theoretical framework that never forgets by design
- Implementing ICL is challenging, but approximating it is possible

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