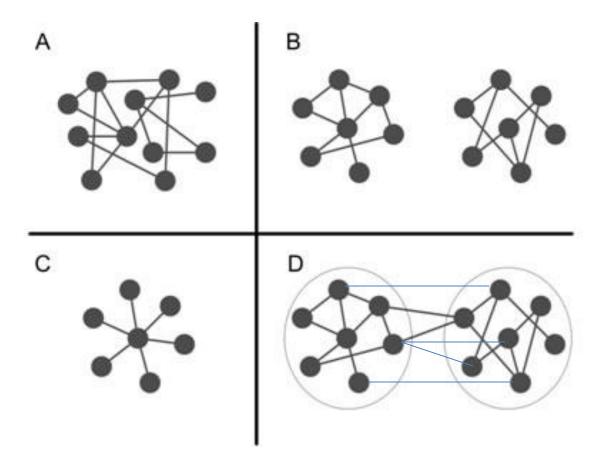
SNA

Cohesion, geodesic distance

Cohesion

- Don't confuse the measure with the construct
- Many ways to define or theoretically conceive of cohesion
- What is the mechanism that would relate cohesion to the outcome of interest?
- Define cohesion consistent with this mechanism
- For each way, we can then devise an operational measurement

Cohesion



Cohesions

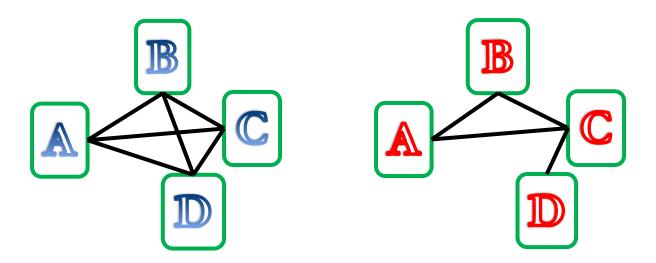
- Network>Cohesion>Density
- Network>Cohesion>Reachability
- Network>Cohesion>No. of Geodesics
 - Geodesics?
- Network>Cohesion>Point Connectivity

More functions...

- Network>Cohesion>Density>Density of subgroups
- Network>Network properties>Reciprocity
 - For directional network
- Network>Cohesion>E-I index

- An index of the degree of dyadic connection in a group
 - Binary data
 - The ration of the number of adjacencies that are present divided by the number of all possible pairs

• The density of a binary network is the total number of ties divided by the total number of possible ties



- Valued data
 - The sum of the values of all ties divided by the number of possible ties
 - The average strength of ties of across all possible (not all actual) ties

Density by group

- Identify subgroups in a network
- Calculate the density, sum or average value within and between groups in a network or matrix.

Density by groups

Open KNOKBUR

Create an attribute file (##d ##h)

- Group 1: governmental agencies: coun, educ, mayr 2 out of 3 links present
- Group 2: non-governmental agencies : comm, indu, news
- Group 3: welfare specialists: wro, uway, welf, west

Density in UCINET and Gephi

Try Network>Cohesion>Overall Density

Try Network>Cohesion>Density by group

KNOKBUR

You gonna need attribute data

##D#, ##H

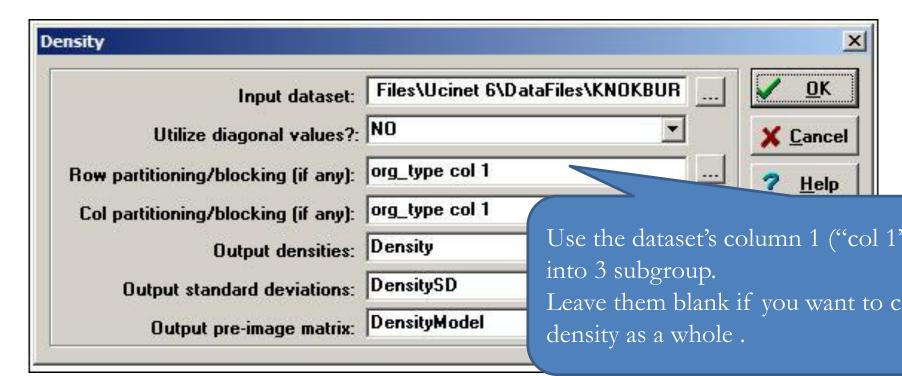
Also show the attributes using NetDraw

Do the same exercise with friendship data

- Exercise/unpack KRACK-HIGH-TECH
 - Open KRACKAD and KRACKFR from NetDraw
 - Use UCINET to compare the density between friendship and advice seeking density
 - Network>cohesion>density (overall)
 - * by group? (Please use the old procedure, I have run into all kinds of problems with the "New")

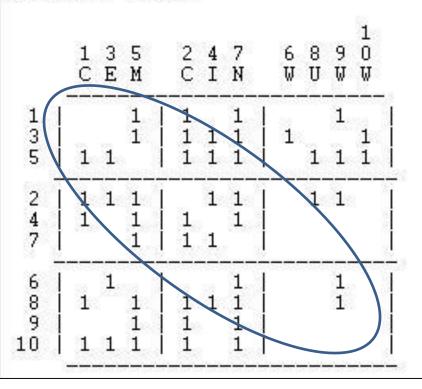
Within group density

- Network>Cohesion>Density
 - To calculate the density of whole populations, or of partitions
 - We can use an attribute or partition to divide the cases



Columr Block	n Old Code	Members:
1	1	COUN EDUC MAYR
2	2	COMM INDU NEWS
3	3	WRO UWAY WELF WEST

Relation: KNOKI



This shows the way you partitioned the cases. "Old Code" is from column 1.

The three sub-groups and the connections WITHIN them.

Density / average value within blocks

		1	2	3
1	1	0.6667	0.8889	0.5000
2	2		1.0000	
3	3	0.5833	0.6667	0.1667

Standard Deviations within blocks

		1 1	2 2	3
2	1 2 3	0.4714	0.3143 0.0000 0.4714	0.3727

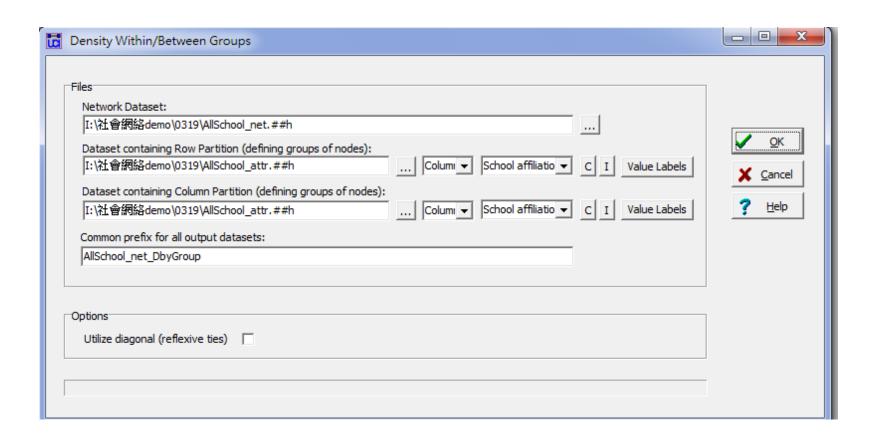
The density withinand between-blocks.

The SD within- and between-blocks.

Exercise, apply density analysis on NTNU data

Simplified NTNU

Save into excel file then open with Gephi



Density by groups

Number of ties/Sum of tie-strengths

```
0 1 2 3 4 5 6 7 8

10 0.000 1.000 1.000 0.000 0.000 0.000 0.000 0.000 0.000
21 1.000 138.000 35.000 19.000 25.000 14.000 19.000 0.000 16.000
32 0.000 36.000 79.000 21.000 16.000 6.000 30.000 4.000 47.000
43 0.000 10.000 25.000 118.000 17.000 9.000 9.000 6.000 85.000
54 0.000 4.000 1.000 12.000 59.000 12.000 15.000 2.000 14.000
65 1.000 20.000 14.000 12.000 36.000 30.000 24.000 5.000 12.000
76 0.000 7.000 11.000 11.000 11.000 16.000 61.000 2.000 15.000
87 0.000 11.000 6.000 2.000 5.000 4.000 1.000 19.000 10.000
98 0.000 3.000 9.000 16.000 1.000 4.000 1.000 7.000 11.000
```

Density (prop of ties) / Average tie strength

```
1 2 3 4 5 6 7 8 9
0 1 2 3 4 5 6 7 8
```

1 0 0.000 0.009 0.010 0.000 0.000 0.000 0.000 0.000 0.000 2 1 0.009 0.197 0.052 0.032 0.042 0.027 0.050 0.000 0.008 3 2 0.000 0.053 0.132 0.038 0.029 0.013 0.086 0.020 0.026 4 3 0.000 0.017 0.045 0.255 0.035 0.022 0.029 0.034 0.054 5 4 0.000 0.007 0.002 0.025 0.128 0.029 0.049 0.011 0.009 6 5 0.013 0.039 0.029 0.029 0.086 0.088 0.090 0.033 0.009 7 6 0.000 0.019 0.031 0.036 0.036 0.060 0.335 0.018 0.015 8 7 0.000 0.051 0.030 0.011 0.028 0.026 0.009 0.339 0.018 9 8 0.000 0.002 0.005 0.010 0.001 0.003 0.001 0.012 0.002

Reachability

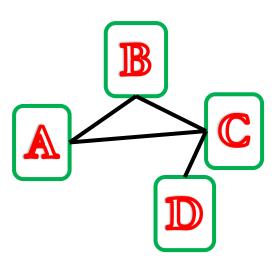
• An actor is reachable by another if there exists any set of connections by which we can trace from the source to the target actor, **regardless of how many others fall between them.**

Reachability of Knoke "I" and "M" relations

```
Matrix #1
Matrix #2
 10
```

(Geodesic) Distance

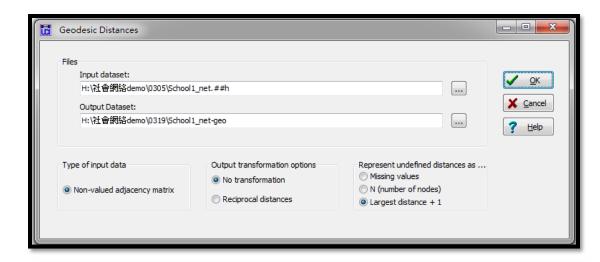
- The distance between two nodes is the length of the shortest path.
- Isolates?



Distance

- Choose input, choose output.
- Use default settings.
- Suggestion:

 save the text
 file for average
 and frequencies.



	Actor1	Actor2	Actor3	Actor4	Actor5	Actor6	Actor7
Actor1	0	2	2	1	1	2	3
Actor2	2	0	1	2	1	2	3
Actor3	2	3	0	2	1	2	3
Actor4	1	1	1	0	1	1	2
Actor5	1	2	1	1	0	1	2
Actor6	1	1	1	1	1	0	1
Actor7	2	2	2	1	1	1	0

Geodesic distances for Knoke information exchange

Geode	es:	ic	D:	is	tar	106	8	Ś		
	1 C	2 C	3 E	4 I	5 M	6 W	7 N	0 8	9 W	1 0 W
1 2 3 4 5 6 7 8 9	0121132121	1 0 1 1 1 2 1 1 1	2102112221	2110121122	1 1 1 0 2 1 1 1	3 2 1 3 2 0 3 3 3 2	1 1 1 1 1 0 1 1	2122132022	1 1 2 2 1 1 2 1 0 2	2 2 1 2 2 2 2 0

Compare 6 to 4 and 4 to 6, are they symmetrical

Save the output file and open it with netdraw Reverse the value?

Who is close to the CEO? Krack-high-tech

Distance in a valued graph: tie strength

- How to measure distance with valued data?
- The distance between two actors is defined as the strength of the weakest link in the shortest path.
 - If A sends 6 units to B, B sends 4 units to C, the strength of the path from A to C (assuming A to B to C is the shortest path) is 4.
 - Wolf/fn (first save the data into separate file, then use the OLD procedure)

No. of Geodesics

- Counts the number of different geodesic paths connecting each pair of nodes.
- Binary dataset only, or UCINET will warn you.
- What does the mean?

	Actor1	Actor2	Actor3	Actor4	Actor5	Actor6	Actor7	Actor8
Actor1	1	1	2	1	1	2	2	1
Actor2	1	1	1	1	1	1	1	2
Actor3	1	2	1	1	1	1	1	2
Actor4	1	1	1	1	1	1	1	2
Actor5	1	2	1	1	1	1	1	2
Actor6	1	1	1	1	1	1	1	1
Actor7	3	2	3	1	1	1	1	1
Actor8	0	0	0	0	0	0	0	1

Who can influence the CEO? Krack-high-tech

Number of geodesic paths for Knoke information exchange

# 0	f G	eo	ies	sio	= I	Pa:	ths	S		
	1 C	2 C	3 E	4 I	5 M	6 W	7 N	8 U	9 W	1 0 W
	-	-	-	-	-	-	-	-		
1 2 3 4 5 6 7 8 9	1 9 3 1 1 2	1 1 1 1 1 1 1 1 1	2112112221	3111121134	1 1 1 1 1 1 1 1 1 1	2112112221	1 1 1 1 1 1 1 1	2122162122	1 1 3 3 1 1 2 1 3	1211111111

Next: Run on WOLFN data

Flow

- Complementing geodesic paths
- Taking into account ALL connections between pairs of actors, not just the most efficient ones.
- Network>Cohesion>Maximum Flow
 - How many different actors in the NEIGHBORHOOD of a source leads to pathways to a target.

Flow

- "If I need to send a message to you, and there is only one other person to whom I can send this for retransmission, my connection is weak— even if the person I send it to may have many ways of reaching you.
- If, on the other hand, there are four people to whom I can send my message, each of whom has one or more ways of retransmitting my message to you, then my connection is stronger."

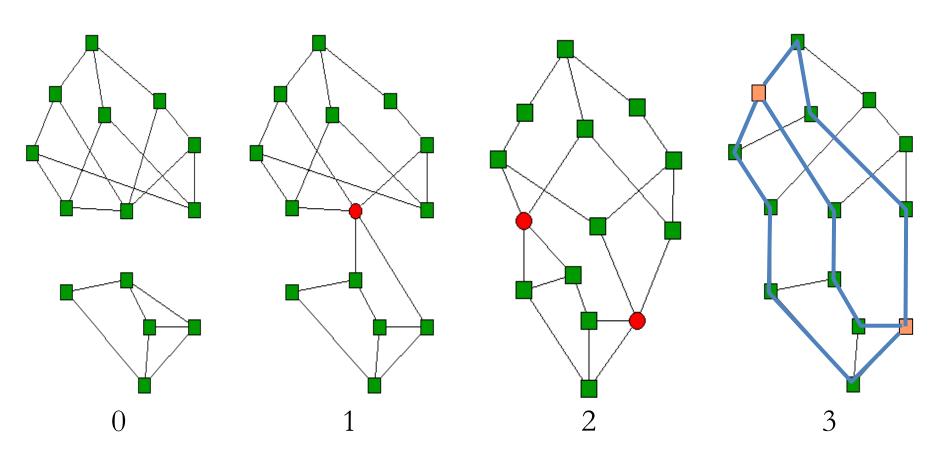
Maximum flow for Knoke information network

	1 C	2 C	3 E	4 I	5 M	6 W	7 N	8 U	9 W	1 0 W
1 2 3 4 5 6 7 8 9 10	0554533535	4064833635	13303333333	4550533535	4764033635	- 1 1 1 1 1 1 1 1 1 1 1	4764830635	22222222022	4554533505	2222222220

Who can influence the CEO? Krack-high-tech

Global Connectivity

•Networks are structurally cohesive if they remain connected even when nodes are removed



Node/point connectivity

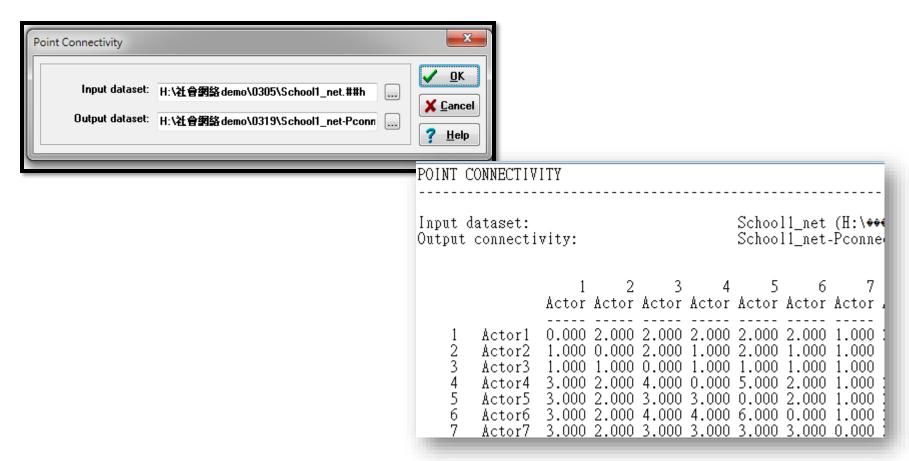
- The minimum number of nodes that need to be removed to disrupt the path between any two pair of nodes.
- Equal to the maximum number of **node** independent path between any two pair of nodes.

Point/local connectivity

- NETWORK>COHESION>POINT CONNECTIVITY PURPOSE Compute the local point connectivity between all pairs of nodes in a network.
 - **DESCRIPTION** The local (point) connectivity of two non-adjacent vertices is the number of vertices that need to be deleted so that no path connects them, this is equal to the maximum number of vertex disjoint paths connecting them.
- NOTE: This procedure only operates on the first matrix in a dataset.
- Hint: data > unpack

Point Connectivity

 Compute the local point connectivity between all pairs of nodes in a network



Local connectivity: the minimum # of nodes need to be removed to disconnect a pair of nodes

	1 C	2 C	3 E	4 I	5 M	6 W	7 N	N 8	9 W	1 0 W
	-	-	-	-	-	-	-	-	-	-
1	5	5	3	4	5	1	6	4	4	3
2	5	8	3	5	8	1	6	5	3	4
3	3	3	4	4	3	1	4	3	3	3
4	5	5	3	5	5	1	5	4	3	4
5	5	8	3	5	8	1	6	5	3	5
6	1	1	1	1	1	1	2	1	2	1
7	5	6	3	5	6	1	6	4	2	3
8	5	5	3	5	5	ī	5	5	4	4
9	3	3			3	1	3	3	3	3
			3	3						5
10	4	5	3	4	5	1	4	4	3	5

Flow

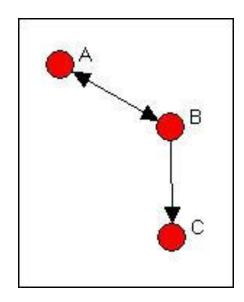
- Complementing geodesic paths
- Taking into account ALL connections between pairs of actors, not just the most efficient ones.
- Network>Cohesion>Maximum Flow
 - How many different actors in the NEIGHBORHOOD of a source leads to pathways to a target.

Flow

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- If, on the other hand, there are four people to whom I can send my message, each of whom has one or more ways of retransmitting my message to you, then my connection is stronger."

Reciprocity in directional network

- Four possible dyadic relationships with directed data
- A network that has a predominance of **null or reciprocated ties** over asymmetric connections may be a more "equal" or "stable" network than **one with a predominance of asymmetric connections**



Reciprocity

- Network>Cohesion>Reciprocity
- Method
 - Arc-based:
 - "Hybrid"

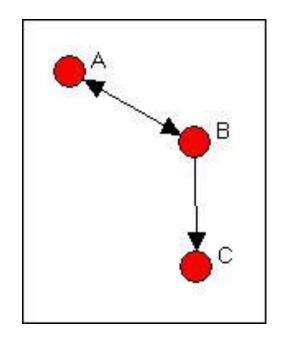
- Dyad-based

All actual pairs (A, B), (B, C) > 1/2

AB, BA, BC, CB, CA, AC > 1/3

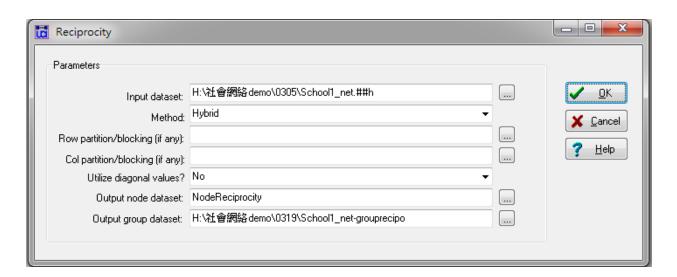
All actual ties
AB, BA, BC, CB, CA, AC > 2/3

Consider all possible pairs Is less sensible in a large network, why?

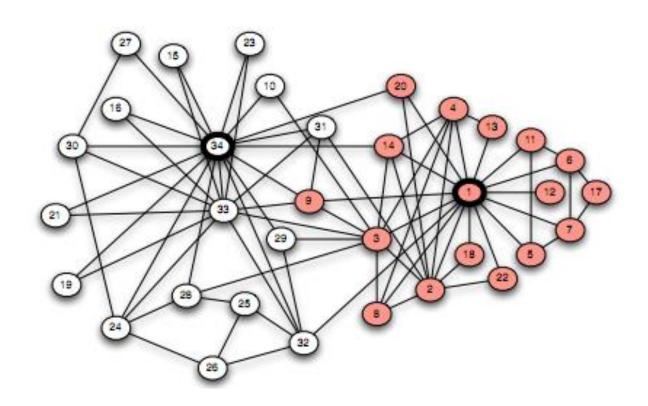


Reciprocity

- Calculate the amount of ties that are reciprocated in a network.
- Use default settings.
- Suggestion: save the text file for detail info.



E-I: Group External vs. Internal ties



E-I: Group External vs. Internal ties

- Takes the number of external group ties, subtracts the number of internal ties, and divides by the total number of ties
- The lower the E-I, the higher the degree of closure
- Range from -1 (all ties are internal; homophile or closure) to +1 (all ties are external)
- Directions of ties are ignored

E-I index

- Units of analysis
 - Entire population
 - Each sub-group
 - Individual

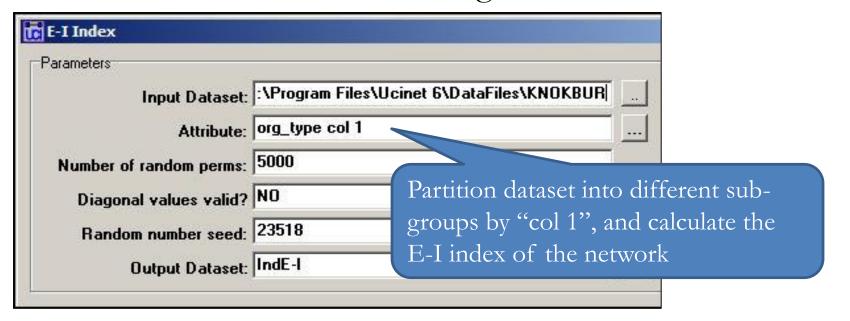
External and internal ties

- Network>Cohesion>E-I index
 - Given a partition of a network into a number of mutually exclusive groups, then
 - the E-I index is the number of ties external to the groups minus the number of ties that are internal to the group divided by the total number of ties.

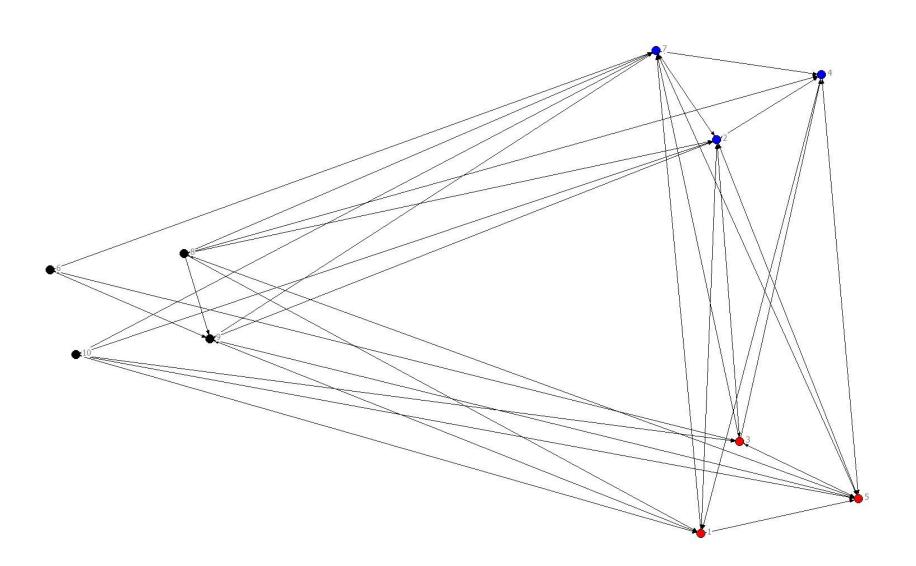
You can also try
Network>Cohesion>Homophily
more about this later

E-I Index

- Network>Cohesion>E-I Index
- Compare the numbers of ties within groups and between groups.
 - The directions of ties are ignored



E-I



		1 Freq	2 Pot	3 Possib	4 Densit
	Internal External	50.000	0 781	24.000 66.000	0.758
3	E-I	36.000	0.563	42.000	0.467

Max possible external ties: 66.000 Max possible internal ties: 24.000

E-I Index: 0.563

Expected value for E-I index is: 0.467

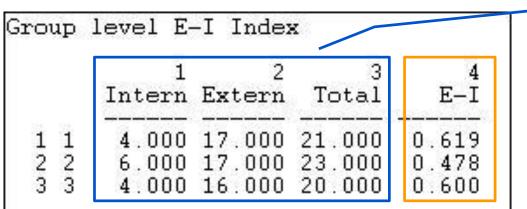
the expected value under a random distribution (given the size of the group and the overall density)

Max possible E-I given density & group sizes: 1.000 Min possible E-I given density & group sizes: 0.250

Re-scaled E-I index: -0.167

Re-scaled E-I Index by the demographic constraints and overall density.

Permutation Test Number of iterations = 5000					P=.20	P=.203, not significant		
	1 Obs	2 Min	3 Avg	4 Max	5 SD	P >= 0b P	7 ' <= Ob	
1 Internal 2 External 3 E-I	0.219 0.781 0.563	0.625 0.156 0.250	0.733 0.267 0.467	0.844 0.375 0.688	0.039 0.039 0.078	0.000	0.000 1.000 0.953	



Raw counts of ties within and between each group.

Individual Level E-I Index

	1	2	3	4
	Inter	Exter	Total	E-I
1 2 3 4 5 6 7 8 9 10	1.000 2.000 1.000 2.000 2.000 1.000 2.000 1.000 2.000	6.000 6.000 5.000 4.000 6.000 2.000 7.000 5.000 4.000 5.000	7.000 8.000 6.000 6.000 8.000 3.000 9.000 6.000 5.000	0.714 0.500 0.667 0.333 0.500 0.333 0.556 0.667 0.333

E-I Index for each group.

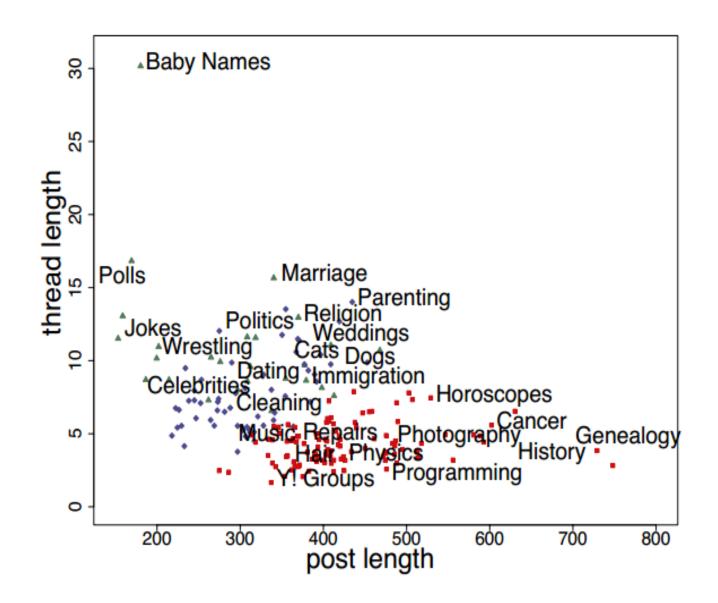
Exercise I

- Use <u>Friendship data</u> and do the following analyses
- 1. Run density within Gender and Club
- 2. Run E-I Index on both attributes and see if there exists homophily by either attribute
- 3. Identify the most outward/Inward looking group and individuals
- 4. Which gender is more outward looking?

Exercise II

- Apply E-I index analysis on Krack High Tech, and Try both level (column 3) and department (column 4)
 - The procedure only runs on the first spreadsheet
 - Run on report-to network and check the E-I value

Yahoo Answers (YA)



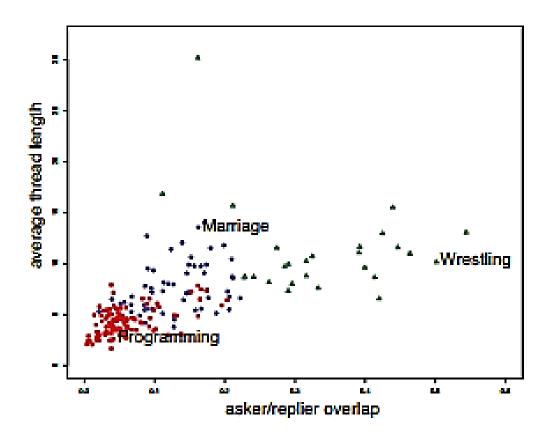


Figure 2: Clustering of categories by thread length and overlap between askers and repliers

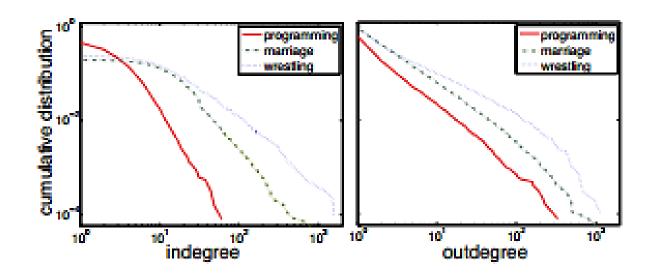


Figure 3: Distributions of indegree (number of users one has received answers from) and outdegree (number of users one has answered)

Table 1: Summary statistics for selected QA networks

Category	Nodes	Edges	Avg.	Mutual	SCC
			deg.	edges	
Wrestling	9,959	56,859	7.02	1,898	13.5%
Program.	12,538	18,311	1.48	0	0.01%
Marriage	45,090	164,887	3.37	179	4.73%

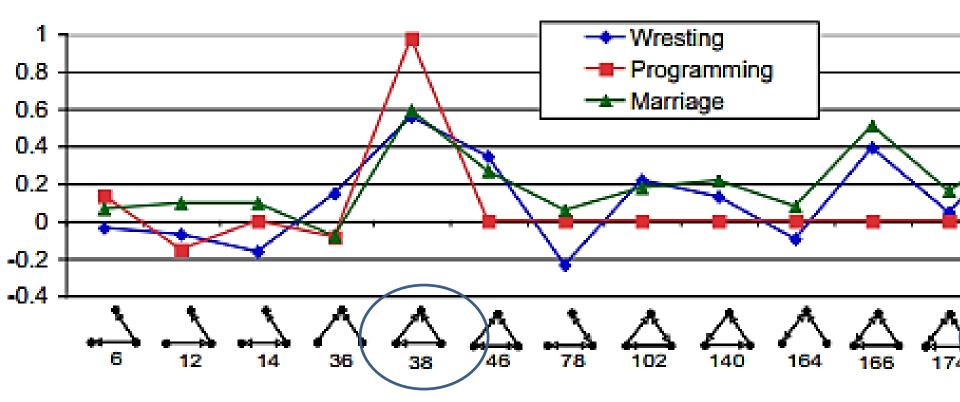


Figure 5: Motif profiles of selected categories