

# Kinetic model of *Escherichia coli* central metabolism

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## Documentation

Pierre Millard<sup>1,2,3</sup>, Kieran Smallbone<sup>1,2</sup> and Pedro Mendes<sup>1,2,4</sup>

<sup>1</sup>MCISB, Manchester Institute of Biotechnology, University of Manchester, M17DN, Manchester, UK.

<sup>2</sup>School of Computer Science, University of Manchester, Manchester, UK.

<sup>3</sup>LISBP, Université de Toulouse, CNRS, INRA, INSA, Toulouse, France.

<sup>4</sup>Center for Quantitative Medicine and Dept. Cell Biology, UConn Health, Farmington CT 06030, USA.

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## 1. Model overview

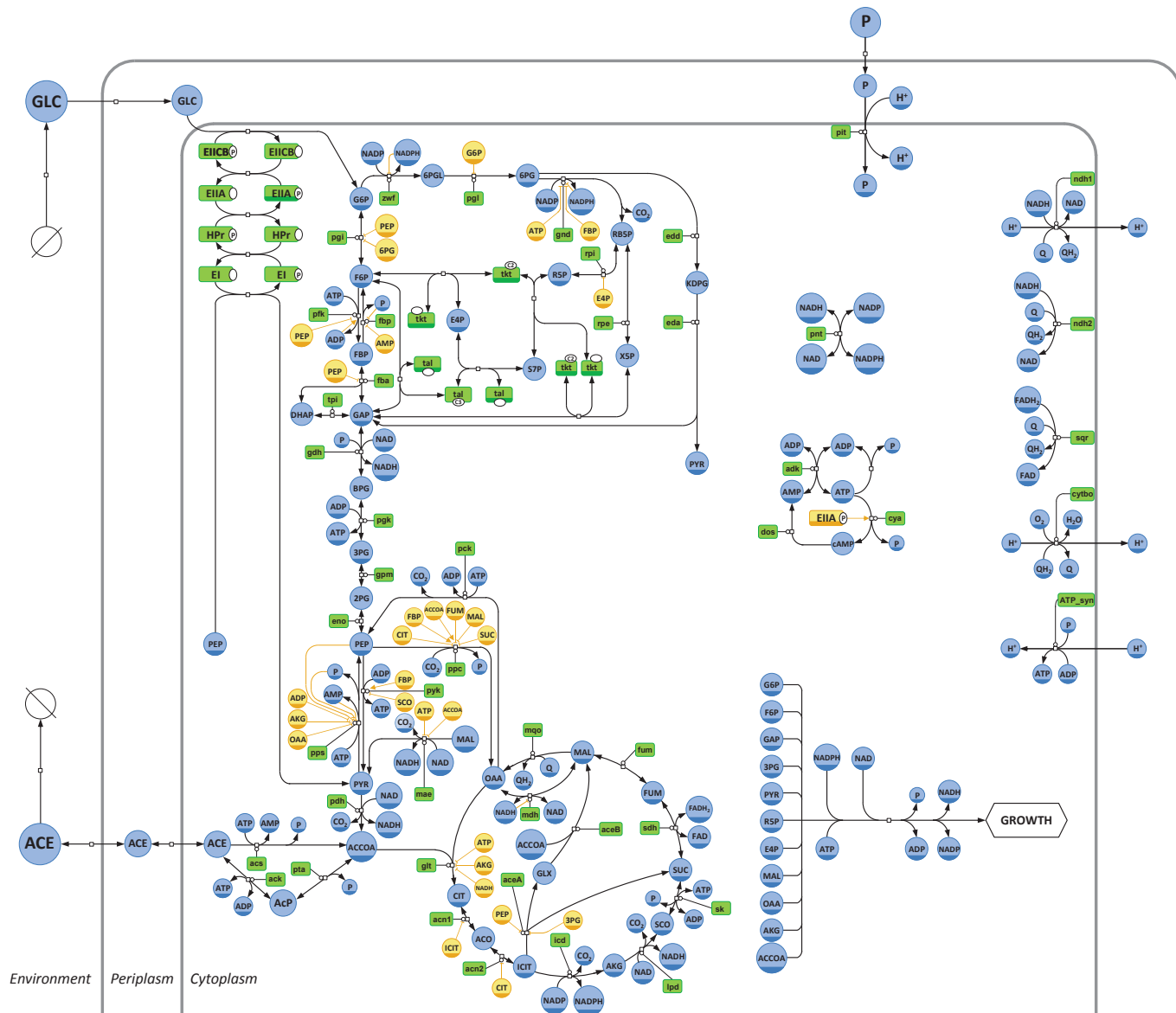
The model developed in this work represents the central metabolic network of the bacterium *Escherichia coli*. It should be noted that when developing a model, certain criteria must be decided, such as the level of detail and the boundaries within which the model can be expected to be valid. The current model simulates the metabolic operation of *E. coli* K-12 MG1655 during exponential growth phase, under aerobic condition and glucose limitation ( $\mu = 0.1 \text{ h}^{-1}$ ). It may allow simulation of other scenarios by changing the enzyme activities to reflect the altered conditions, and/or implementing additional pathways known to be active in the other scenarios.

This model comprises three compartments: the environment and the cell which is divided in two compartments (cytoplasm and periplasm). The periplasmic volume represents 20% of the cell volume [1]. The model contains 77 species and 68 reactions constitutive of the central carbon and energy pathways of *E. coli* (Figure 1):

- transport reactions between the environment and the periplasm
- glucose phosphotransferase system (PTS)
- glycolytic and gluconeogenic pathways (EMP)
- pentose phosphate pathway (PP)
- Entner-Doudoroff pathway (ED)
- anaplerotic reactions (AR)
- tricarboxylic acids cycle (TCA)
- glyoxylate shunt (GS)
- acetate metabolism
- oxidative phosphorylation (OP)
- synthesis of biomass

The following sections describe:

- all the reactions included in the model
- the system of ODEs
- the laws for conserved moieties
- the rate laws for each reaction
- the value of all kinetic parameters



**Figure 1.** Central metabolic network of *E. coli* implemented in the model. The model comprises three compartments: the environment, the periplasm and the cytoplasm. Metabolites are shown in blue (reactants) and orange (regulators). Enzymes are shown in green. Black and orange arrows denote reactions and regulatory interactions, respectively. The diagram adopts the conventions of the Systems Biology Graphical Notation process description [2].

## 2. Model units

Model units are millimole (mmol) for amounts, litre (L) for volumes, and second (s) for time. Experimental data used for parameter estimation were converted into intracellular units (mM for concentrations and mM/s for fluxes) assuming a cytosolic volume of  $1.77 \times 10^{-3}$  L/g<sub>DW</sub> [3].

## 3. Reactions

Table S1 lists the reactions implemented in the model. It also includes the types of kinetic equations describing each reaction and the effectors considered. When the equation was taken or adapted from the literature, the corresponding reference is given. All the equations can be found in section 5. This model is available in SBML and COPASI formats in Supplementary data and can be downloaded from the Biomed models database (<http://www.ebi.ac.uk/biomodels/>) with identifier < MODEL1515110000 >.

**Table S1.** Reactions implemented in the model. When equations were taken from the literature, references are given in the *Rate law* column.

The following abbreviations are used: MA: Mass action; MM: Michaelis-Menten; MWC: Monod-Wyman-Changeux; OBB: Ordered Bi Bi; OUB: Ordered Uni Bi; PPTB: Ping Pong Ter Bi; PPUBBU: Ping Pong Uni Bi Bi Uni; RBB: Random Bi Bi; RBT: Random Bi Ter; RUB: Random Uni Bi. The signs (+) and (-) denotes a positive and a negative control of reaction rates by their effectors, respectively.

<i>Sub-system</i>	<i>Reaction name</i>	<i>EC number</i>	<i>Reaction</i>	<i>Effector(s)</i>	<i>Rate law</i>	<i>Comment</i>
-	GLC_feed	-	$\text{S} \rightarrow \text{GLC}_{\text{env}}$	-	Constant flux	Glucose inflow into the environment
-	ACE_OUT	-	$\text{ACE}_{\text{env}} \rightarrow \text{S}$	-	MA	Acetate output from the environment
Exchange reactions	XCH_GLC	-	$\text{GLC}_{\text{env}} \leftrightarrow \text{GLC}_{\text{per}}$	-	MM	Additional information are given after the table
	XCH_P	-	$\text{P}_{\text{env}} \leftrightarrow \text{P}_{\text{per}}$	-	MM	
	XCH_ACE	-	$\text{ACE}_{\text{per}} \leftrightarrow \text{ACE}_{\text{env}}$	-	MM	
Glucose uptake	PTS_0	2.7.3.9	$\text{ei} + \text{PEP} \leftrightarrow \text{eiP} + \text{PYR}$	-	MA [4]	-
	PTS_1	2.7.1.199	$\text{hpr} + \text{eiP} \leftrightarrow \text{hprP} + \text{ei}$	-	MA [4]	-
	PTS_2	2.7.1.199	$\text{eiia} + \text{hprP} \leftrightarrow \text{eiiaP} + \text{hpr}$	-	MA [4]	-
	PTS_3	2.7.1.199	$\text{eiicb} + \text{eiiaP} \leftrightarrow \text{eiicbP} + \text{eiia}$	-	MA [4]	-
	PTS_4	2.7.1.199	$\text{GLC}_{\text{per}} + \text{eiicbP} \leftrightarrow \text{G6P} + \text{eiicb}$	-	MA [4]	-
Phosphate uptake	PIT	-	$\text{P}_{\text{per}} + \text{H}^+_{\text{per}} \leftrightarrow \text{P}_{\text{cyt}} + \text{H}^+_{\text{cyt}}$	$\text{H}^+_{\text{per}}$ (+)	MM	-
Glycolysis & gluconeogenesis	PGI	5.3.1.9	$\text{G6P} \leftrightarrow \text{F6P}$	PEP (-), PGN (-)	MM, adapted from [5]	With inhibition by PGN [6, 7]
	PFK	2.7.1.11	$\text{ATP} + \text{F6P} \leftrightarrow \text{ADP} + \text{FDP}$	PEP (-)	MWC [5]	-
	FBP	3.1.3.11	$\text{FDP} \rightarrow \text{F6P} + \text{P}$	AMP (-), P (-)	MWC [5]	-
	FBA	4.1.2.13	$\text{FDP} \leftrightarrow \text{DAP} + \text{GAP}$	PEP (-)	OUB [5]	-
	TPI	5.3.1.1	$\text{DAP} \leftrightarrow \text{GAP}$	-	MM [5]	-
	GDH	1.2.1.12	$\text{GAP} + \text{NAD} + \text{P} \leftrightarrow \text{BPG} + \text{NADH}$	-	RBT [5]	-
	PGK	2.7.2.3	$\text{ADP} + \text{BPG} \leftrightarrow \text{ATP} + \text{PGA3}$	-	RBB [5]	-
	GPM	5.4.2.11/12	$\text{PGA3} \leftrightarrow \text{PGA2}$	-	MM [5]	-
	ENO	4.2.1.11	$\text{PGA2} \leftrightarrow \text{PEP}$	-	MM [5]	-
	PYK	2.7.1.40	$\text{ADP} + \text{PEP} \rightarrow \text{ATP} + \text{PYR}$	SUCCOA (-), FDP (+)	MWC [5]	-
	PPS	2.7.9.2	$\text{ATP} + \text{PYR} \leftrightarrow \text{AMP} + \text{PEP} + \text{P}$	ADP (-), AKG (-), OAA (-), AMP (-), P (-), PEP (-)	PPUBBU [5]	-
	PDH	1.2.1.-	$\text{COA} + \text{NAD} + \text{PYR} \leftrightarrow \text{ACCOA} + \text{NADH} + \text{HCO}^{3-}$	-	PPTB [5]	-
PP pathway	ZWF	1.1.1.49	$\text{G6P} + \text{NADP} \leftrightarrow \text{GL6P} + \text{NADPH}$	NADPH (-)	RBT [5]	-
	PGL	3.1.1.31	$\text{GL6P} \leftrightarrow \text{PGN}$	G6P (-)	MM [5]	-
	GL6P_HYDRO	-	$\text{GL6P} \leftrightarrow \text{PGN}$	-	MA [5]	Spontaneous hydrolysis of GL6P
	GND	1.1.1.44	$\text{NADP} + \text{PGN} \leftrightarrow \text{NADPH} + \text{RU5P} + \text{HCO}^{3-}$	FDP (-), ATP (-), NADPH (-)	RBT, adapted from [5]	Inhibition by PEP was removed (no experimental evidence)
	RPE	5.1.3.1	$\text{RU5P} \leftrightarrow \text{X5P}$	-	MM [5]	-
	RPI	5.3.1.6	$\text{RU5P} \leftrightarrow \text{R5P}$	E4P (-)	MM [5]	-
	X5P_GAP_TKT	2.2.1.1	$\text{tkt} + \text{X5P} \leftrightarrow \text{GAP} + \text{tktC2}$	-	MA [5]	-
	F6P_E4P_TKT	2.2.1.1	$\text{E4P} + \text{tktC2} \leftrightarrow \text{F6P} + \text{tkt}$	-	MA [5]	-
	S7P_R5P_TKT	2.2.1.1	$\text{R5P} + \text{tktC2} \leftrightarrow \text{S7P} + \text{tkt}$	-	MA [5]	-
	F6P_GAP_TAL	2.2.1.2	$\text{GAP} + \text{talC3} \leftrightarrow \text{F6P} + \text{tal}$	-	MA [5]	-
	S7P_E4P_TAL	2.2.1.2	$\text{S7P} + \text{tal} \leftrightarrow \text{E4P} + \text{talC3}$	-	MA [5]	-

ED pathway	EDD	4.2.1.12	PGN $\leftrightarrow$ KDPG	-	MM [5]	-
	EDA	4.1.2.14	KDPG $\leftrightarrow$ GAP + PYR	-	OUB [5]	-
Anaplerotic reactions	PPC	4.1.1.31	PEP + HCO <sup>3-</sup> $\leftrightarrow$ OAA + P	ACCOA (+), CIT (-), FDP (+), FUM (-), MAL (-), SUC (-), ASP (+), CYS (-)	MWC [5]	-
	PCK	4.1.1.49	ATP + OAA $\leftrightarrow$ ADP + PEP + HCO <sup>3-</sup>	-	RBT [5]	-
	MAD	1.1.1.39	MAL + NAD $\rightarrow$ NADH + PYR + HCO <sup>3-</sup>	ATP (-), ACCOA (-), COA (-), ASP (+)	MWC [5]	-
TCA cycle	GLT	2.3.3.1	ACCOA + OAA $\leftrightarrow$ CIT + COA	ATP (-), AKG (-), NADH (-)	MWC [5]	-
	ACN_1	4.2.1.3	CIT $\leftrightarrow$ ACO	ICIT (-)	MM [5]	-
	ACN_2	4.2.1.3	ACO $\leftrightarrow$ ICIT	CIT (-)	MM [5]	-
	ICD	1.1.1.42	ICIT + NADP $\leftrightarrow$ AKG + NADPH + HCO <sup>3-</sup>	-	MWC [5]	-
	ACEK_1	3.1.3.-	ATP + icd $\leftrightarrow$ ADP + icdP	-	MA [5]	-
	ACEK_2	3.1.3.-	icdP $\leftrightarrow$ icd + P	-	MA [5]	-
	LPD	1.2.4.2	COA + AKG + NAD $\rightarrow$ NADH + SUCCOA + HCO <sup>3-</sup>	-	MWC [5]	-
	SK	6.2.1.5	ADP + SUCCOA + P $\leftrightarrow$ ATP + COA + SUC	-	RBT [5]	-
	SDH	1.3.5.1	Q + SUC $\leftrightarrow$ FUM + QH <sub>2</sub>	-	RBB [5]	-
	FUMA	4.2.1.2	FUM $\leftrightarrow$ MAL	-	MM [5]	-
	MQO	1.1.5.4	MAL + Q $\leftrightarrow$ OAA + QH <sub>2</sub>	-	MM [5]	-
	MDH	1.1.1.37	QH <sub>2</sub> + OAA $\leftrightarrow$ MAL + Q	-	OBB [5]	-
Glyoxylate shunt	ACEA	4.1.3.1	ICIT $\leftrightarrow$ GLX + SUC	PEP (-), PGA3 (-)	RUB [5]	-
	ACEB	2.3.3.9	ACCOA + GLX $\leftrightarrow$ COA + MAL	-	RBB [5]	-
Acetate metabolism	PTA	2.3.1.8	ACCOA + P $\leftrightarrow$ COA + ACP	-	MM [8]	-
	ACK	2.7.2.1	ACP + ADP $\leftrightarrow$ ACE <sub>per</sub> + ATP	-	MM [8]	-
	ACS	6.2.1.1	ACE <sub>per</sub> + ATP + COA $\rightarrow$ ACCOA + AMP + 2 * P	-	MM [8]	-
Oxidative phosphorylation	NDHI	1.6.5.3	NADH + Q + 4 * H <sup>+</sup> <sub>cyt</sub> $\leftrightarrow$ NAD + QH <sub>2</sub> + 4 * H <sup>+</sup> <sub>per</sub>	H <sup>+</sup> <sub>per</sub> (-)	MA	Additional information are given after the table
	NDHII	1.6.5.9	NADH + Q $\leftrightarrow$ NAD + QH <sub>2</sub>	-	MA	
	SQR	1.3.5.1	FADH <sub>2</sub> + Q $\leftrightarrow$ FAD + QH <sub>2</sub>	-	MA	
	CYTBO	1.10.3.10	2 * QH <sub>2</sub> + 8 * H <sup>+</sup> <sub>cyt</sub> + O <sub>2</sub> $\leftrightarrow$ 2 * Q + 8 * H <sup>+</sup> <sub>per</sub> + 2 * H <sub>2</sub> O	H <sup>+</sup> <sub>per</sub> (-)	MA	
	ATP_SYN	3.6.3.14	ADP + P + 4 * H <sup>+</sup> <sub>per</sub> $\leftrightarrow$ ATP + 4 * H <sup>+</sup> <sub>cyt</sub>	H <sup>+</sup> <sub>per</sub> (+)	MA	
Additional reactions for nucleotides and redox cofactors	PNT	1.6.1.1/2/3	NAD + NADPH $\leftrightarrow$ NADH + NADP	-	MA	Additional information are given after the table
	ADK	2.7.4.3	AMP + ATP $\leftrightarrow$ 2 * ADP	-	MA	
	ATP_NGAM	-	ATP $\leftrightarrow$ ADP + P	-	MA	
	CYA	4.6.1.1	ATP $\leftrightarrow$ cAMP + 2 * P	eiiaP (+)	MA	
	DOS	3.1.4.53	cAMP $\leftrightarrow$ AMP	-	MA	
Biomass synthesis	GROWTH	-	116 * G6P + 204 * E4P + 845 * PGA3 + 1010 * OAA + 610 * AKG + 1601 * PYR + 507 * R5P + 293 * PEP + 73 * GAP + 40 * F6P + 10169 * NADPH + 2118 * ACCOA + 2004 * NAD + 30508 * ATP $\rightarrow$ 10169 * NADP + 2118 * COA + 2004 * NADH + 30508 * ADP + 30508 * P	-	Random ordered	Additional information are given after the table

All the rate laws are given in section 5. Details on the equations taken from the literature can be found in the original paper given in reference. Information on the modelling of some processes is detailed hereafter.

- *Exchange reactions*

Three reactions enable the transport of glucose (XCH\_GLC), acetate (XCH\_ACE) and phosphate (XCH\_P) between the environment and the periplasm. Diffusion through the outer membrane is modelled as a saturable, porin-facilitated diffusion process [9], using reversible Michaelis-Menten kinetics. The same (arbitrary) values for  $V_{\max}$  and  $K_m$  of 100 mM/s and 10 mM were taken for all compounds.

- *Oxidative phosphorylation*

Oxidative phosphorylation is used by *E. coli* to generate ATP. In aerobic condition, electrons are transferred from NADH and FADH<sub>2</sub> to O<sub>2</sub>. This process generates an H<sup>+</sup> gradient across the cytoplasmic membrane, which is then used to drive ATP synthesis. The main components of oxidative phosphorylation are two NADH dehydrogenases (NDHI and NDHII), the succinate dehydrogenase complex (SQR), the cytochrome bo oxidase (CYTBO) and the ATP synthase (ATP\_SYN) [10]. *E. coli* also has two other cytochromes (bd1 and bd2) which are expressed under oxygen-limited condition and starvation for carbon and/or phosphate [11-13], respectively, and were not included in the model since they are not significantly active in exponential growth on glucose in aerobic condition. NDHI and NDHII catalyse the transfer of electrons from NADH to the quinone pool (Q) in the cytoplasmic membrane. In contrast to NDHII, NDHI also generates a proton gradient by translocating H<sup>+</sup> from cytoplasm to periplasm, with an H<sup>+</sup>/e<sup>-</sup> ratio of 2 [10]. SQR is a complex of 4 proteins (SDHA, B, C and D). SDHA is a part of the TCA cycle (reaction SDH) and oxidizes succinate to fumarate by reducing FAD to FADH<sub>2</sub>. Further transfer of electrons from FADH<sub>2</sub> to Q (reaction SQR) occurs via the three other proteins. CYTBO couples the two-electron oxidation of ubiquinol (QH<sub>2</sub>) with the four-electron reduction of molecular oxygen to water. It also functions as a proton pump, with an H<sup>+</sup>/e<sup>-</sup> ratio of 2 [10]. Finally, the proton gradient is used by the ATP synthase to generate ATP by translocating H<sup>+</sup> from the periplasm to the cytoplasm, with an H<sup>+</sup>/ATP ratio of 4 [14].

Oxidative phosphorylation was modelled using reversible mass action kinetics. Although the oxidative phosphorylation reactions have no specific feedback regulation, experimental evidences show that kinetics of H<sup>+</sup> pumps (NDHI and CYTBO) and ATP\_SYN strongly depends on the H<sup>+</sup> gradient. As the H<sup>+</sup> gradient increases, the reaction rate through NDHI and CYTBO decreases in a sigmoidal fashion. In opposite, a strongly sigmoidal increase of the rate of ATP synthesis with the increase of H<sup>+</sup> gradient was observed. We considered the dependence of reaction rates on the H<sup>+</sup> gradient using the relation proposed by [15].

*E. coli* maintains a cytoplasmic pH within a narrow range, approximately 7.4 to 7.8, when grown over a large range of environmental pH from pH 5 to 9 [16-18]. Thus, the cytosolic concentration of  $H^+$  ions was fixed at  $3.16 \times 10^{-5}$  mM (pH=7.5, [18]).

- *Transport of phosphate*

Phosphate enters in the cytoplasm via the PIT transporter. Transport is energised by the proton gradient with a  $H^+/P$  ratio of 1 and can be abolished with uncouplers or respiration inhibitors, thus the reaction rate was modelled as function of the  $H^+$  gradient, similarly to reactions of oxidative phosphorylation involved in the production of the  $H^+$  gradient.

- *Additional reactions for nucleotides and redox cofactors*

Various processes strongly impact the balance of AMP, ADP, ATP and cAMP pools and had to be considered to fit the experimental data. Several reactions of non-growth associated processes which consume ATP were lumped in the reaction ATP\_NGAM. Adenylate kinase (reaction ADK) catalyzes the reversible conversion of AMP and ATP to two molecules of ADP. Adenylate cyclase (CYA) catalyzes the synthesis of cAMP from ATP and is activated by the phosphorylated form of EIIA enzyme of the PTS. Finally, cAMP can be hydrolyzed into AMP by the cAMP phosphodiesterase (DOS).

The reversible reduction of NADP by NADH is catalysed by two transhydrogenases [19] lumped into the reaction PNT and modelled using reversible mass action kinetics.

- *Biomass synthesis*

In contrast to previous models where growth was function of extracellular glucose levels, we assumed that the growth rate is controlled by the intracellular concentration of the cell building blocks (G6P, E4P, PGA3, OAA, AKG, PYR, R5P, PEP, GAP, F6P, NADPH, ACCOA, NAD, ATP). Thus, we defined an overall pseudo-reaction to describe cellular growth in terms of the required metabolic precursors, with the stoichiometric coefficients taken from the biomass function published in [20] (after unit conversion from mmol/g<sub>DW</sub>/h to mmol/L<sub>cytoplasm</sub>/s). The kinetic equation for growth is:

$$\mu = V_{max} \cdot \prod_i \frac{S_i}{S_i + K_m^{S_i}}$$

where  $S_i$  represents the concentration of the building block  $i$  and  $K_m^{S_i}$  represents the saturation of the growth rate with respect to the concentration of the metabolite  $i$ .



## 4. ODEs system

The differential equations, which describe the progression of the variables over time as a function of the system's rates, balance the:

- concentrations of extracellular metabolites (glucose, phosphate and acetate)
- concentrations of intracellular metabolites
- phosphorylation states of PTS proteins
- states of transaldolases and transketolases

### Metabolites:

$$d(\text{ACCOA})/dt = v_{\text{PDH}} - v_{\text{GLT}} - v_{\text{ACEB}} - 2118 * v_{\text{GROWTH}} + v_{\text{ACS}} - v_{\text{PTA}}$$

$$d(\text{ACO})/dt = v_{\text{ACN}_1} - v_{\text{ACN}_2}$$

$$d(\text{ACE})/dt = v_{\text{ACK}} - v_{\text{ACS}} - v_{\text{XCH\_ACE1}}$$

$$d(\text{ACEp})/dt = (v_{\text{XCH\_ACE1}} - v_{\text{XCH\_ACE2}}) * \text{vol\_cyt}/\text{vol\_per}$$

$$d(\text{ACEx})/dt = v_{\text{XCH\_ACE2}} * \text{vol\_per}/\text{vol\_env} - v_{\text{ACE\_OUT}}$$

$$d(\text{ACP})/dt = v_{\text{PTA}} - v_{\text{ACK}}$$

$$d(\text{ADP})/dt = 2 * v_{\text{ADK}} - v_{\text{ATP\_SYN}} - v_{\text{PGK}} + v_{\text{PFK}} - v_{\text{PYK}} + v_{\text{PCK}} - v_{\text{SK}} + v_{\text{ACEK}_1} - v_{\text{ACK}} + 30508 * v_{\text{GROWTH}}$$

$$d(\text{AKG})/dt = v_{\text{ICD}} - v_{\text{LPD}} - 610 * v_{\text{GROWTH}}$$

$$d(\text{AMP})/dt = v_{\text{DOS}} - v_{\text{ADK}} + v_{\text{PPS}} + v_{\text{ACS}}$$

$$d(\text{ATP})/dt = v_{\text{ATP\_SYN}} - v_{\text{CYA}} - v_{\text{ADK}} + v_{\text{PGK}} - v_{\text{PFK}} + v_{\text{PYK}} - v_{\text{PCK}} - v_{\text{PPS}} + v_{\text{SK}} - v_{\text{ACEK}_1} - v_{\text{ACS}} + v_{\text{ACK}} - 30508 * v_{\text{GROWTH}}$$

$$d(\text{BPG})/dt = v_{\text{GDH}} - v_{\text{PGK}}$$

$$d(\text{CAMP})/dt = v_{\text{CYA}} - v_{\text{DOS}}$$

$$d(\text{CIT})/dt = v_{\text{GLT}} - v_{\text{ACN}_1}$$

$$d(\text{DAP})/dt = v_{\text{FBA}} - v_{\text{TPI}}$$

$$d(\text{E4P})/dt = v_{\text{S7P\_E4P\_TAL}} - v_{\text{F6P\_E4P\_TKT}} - 204 * v_{\text{GROWTH}}$$

$$d(\text{F6P})/dt = v_{\text{PGI}} - v_{\text{PFK}} + v_{\text{F6P\_E4P\_TKT}} + v_{\text{F6P\_GAP\_TAL}} + v_{\text{FBP}} - 40 * v_{\text{GROWTH}}$$

$$d(\text{FAD})/dt = v_{\text{SQR}} - v_{\text{SDH}}$$

$$d(\text{FADH}_2)/dt = v_{\text{SDH}} - v_{\text{SQR}}$$

$$d(\text{FDP})/dt = v_{\text{PFK}} - v_{\text{FBA}} - v_{\text{FBP}}$$

$$d(\text{FUM})/dt = v_{\text{SDH}} - v_{\text{FUMA}}$$

$$d(\text{G6P})/dt = v_{\text{PTS}_4} - v_{\text{PGI}} - v_{\text{ZWF}} - 116 * v_{\text{GROWTH}}$$

$$d(\text{GAP})/dt = v_{\text{FBA}} + v_{\text{TPI}} - v_{\text{GDH}} + v_{\text{X5P\_GAP\_TKT}} - v_{\text{F6P\_GAP\_TAL}} + v_{\text{EDA}} - 73 * v_{\text{GROWTH}}$$

$$d(\text{GL6P})/dt = v_{\text{ZWF}} - v_{\text{PGL}} - v_{\text{GL6P\_HYDRO}}$$

$$d(\text{GLCp})/dt = (v_{\text{GLC\_XCH}} - v_{\text{PTS}_4}) * \text{vol\_cyt}/\text{vol\_per}$$

$$d(\text{GLCx})/dt = (v_{\text{GLC\_feed}} - v_{\text{GLC\_XCH}}) * \text{vol\_per}/\text{vol\_env}$$

$$d(GLX)/dt = v\_ACEA - v\_ACEB$$

$$d(Hp)/dt = (4 * v\_NDHI + 8 * v\_CYTBO - 4 * v\_ATP\_SYN - v\_PIT) * vol\_cyt/vol\_per$$

$$d(ICIT)/dt = v\_ACN\_2 - v\_ICD - v\_ACEA$$

$$d(KDPG)/dt = v\_EDD - v\_EDA$$

$$d(MAL)/dt = v\_FUMA - v\_MAD + v\_MDH - v\_MQO + v\_ACEB$$

$$d(NAD)/dt = v\_MDH - v\_PNT - v\_GDH - v\_MAD - v\_PDH - v\_LPD - 2004 * v\_GROWTH$$

$$d(NADH)/dt = v\_GDH + v\_MAD + v\_PDH + v\_LPD - v\_MDH + v\_NADH\_req + v\_PNT - 2004 * v\_GROWTH$$

$$d(NADP)/dt = v\_PNT - v\_GND - v\_ZWF - v\_ICD + 10169 * v\_GROWTH$$

$$d(NADPH)/dt = v\_GND + v\_ZWF + v\_ICD - v\_PNT - 10169 * v\_GROWTH$$

$$d(OAA)/dt = v\_PPC - v\_PCK - v\_GLT + v\_MQO - v\_MDH - 1010 * v\_GROWTH$$

$$d(Pp)/dt = (v\_P\_XCH - v\_PIT) * vol\_cyt/vol\_per$$

$$d(Pc)/dt = v\_FBP - v\_GDH + v\_PPC + v\_PPS - v\_SK + v\_ACEK\_2 - v\_ATP\_SYN + 2 * v\_CYA + 2 * v\_ACS - v\_PTA + v\_ATP\_MAINTENANCE + 30508 * v\_GROWTH + v\_PIT$$

$$d(PEP)/dt = v\_ENO - v\_PYK - v\_PPC + v\_PCK + v\_PPS - v\_PTS\_0 - 293 * v\_GROWTH$$

$$d(PGA2)/dt = v\_GPM - v\_ENO$$

$$d(PGA3)/dt = v\_PGK - v\_GPM - 845 * v\_GROWTH$$

$$d(PGN)/dt = v\_PGL - v\_GND - v\_EDD$$

$$d(PYR)/dt = v\_PYK - v\_PPS + v\_MAD - v\_PDH + v\_EDA + v\_PTS\_0 - 1601 * v\_GROWTH$$

$$d(Q)/dt = v\_MDH + 2 * v\_CYTBO - v\_SQR - v\_NDHI - v\_NDHII - v\_MQO$$

$$d(QH_2)/dt = v\_SQR + v\_NDHI + v\_NDHII + v\_MQO - v\_MDH - 2 * v\_CYTBO$$

$$d(R5P)/dt = v\_RPI - v\_S7P\_R5P\_TKT - 507 * v\_GROWTH$$

$$d(RU5P)/dt = v\_GND - v\_RPE - v\_RPI$$

$$d(S7P)/dt = v\_S7P\_R5P\_TKT - v\_S7P\_E4P\_TAL$$

$$d(SUC)/dt = v\_SK - v\_SDH + v\_ACEA$$

$$d(SUCCOA)/dt = v\_LPD - v\_SK$$

$$d(X5P)/dt = v\_RPE - v\_X5P\_GAP\_TKT$$

### Proteins:

$$d(ei)/dt = v\_PTS\_1 - v\_PTS\_0$$

$$d(eiia)/dt = v\_PTS\_3 - v\_PTS\_2$$

$$d(eiiaP)/dt = v\_PTS\_2 - v\_PTS\_3$$

$$d(eiicb)/dt = v\_PTS\_4 - v\_PTS\_3$$

$$d(eiicbP)/dt = v\_PTS\_3 - v\_PTS\_4$$

$$d(eiP)/dt = v\_PTS\_0 - v\_PTS\_1$$

$$d(hpr)/dt = v\_PTS\_2 - v\_PTS\_1$$

$$d(hprP)/dt = v\_PTS\_1 - v\_PTS\_2$$

$$d(icd)/dt = v\_ACEK\_2 - v\_ACEK\_1$$

$$d(\text{icdP})/dt = v\_ACEK\_1 - v\_ACEK\_2$$

$$d(\text{tal})/dt = v\_F6P\_GAP\_TAL - v\_S7P\_E4P\_TAL$$

$$d(\text{talC3})/dt = v\_S7P\_E4P\_TAL - v\_F6P\_GAP\_TAL$$

$$d(\text{tkt})/dt = v\_S7P\_R5P\_TKT - v\_X5P\_GAP\_TKT + v\_F6P\_E4P\_TKT$$

$$d(\text{tkc2})/dt = v\_X5P\_GAP\_TKT - v\_F6P\_E4P\_TKT - v\_S7P\_R5P\_TKT$$

## 5. Rate laws

This section contains the rate laws for each reaction.

$$v_{ACEA} = \frac{V_{max} \cdot \left( ICIT - \frac{GLX \cdot SUC}{K_{eq}} \right)}{K_{mICIT} \left( 1 + \frac{ICIT}{K_{mICIT}} \left( 1 + \frac{PEP}{K_{dPEPicit}} \right) + \frac{SUC}{K_{dSUC}} \left( 1 + \frac{ICIT}{K_{dICITsuc}} \right) + \frac{KmSUC}{K_{dSUC}} \cdot \frac{GLX}{K_{mGLX}} \cdot \left( 1 + \frac{PEP}{K_{dPEPgls}} \right) + \frac{GLX}{K_{mGLX}} \cdot \frac{SUC}{K_{dSUC}} + \frac{PEP}{K_{dPEP}} + \frac{PGA3}{K_{dPGA3}} \right)}$$

$$v_{ACEB} = \frac{V_{max} \cdot \left( ACCOA \cdot GLX - \frac{COA \cdot MAL}{K_{eq}} \right)}{K_{mACCOA} \cdot K_{mGLX} \left( 1 + \frac{ACCOA}{K_{mACCOA}} \cdot \left( 1 + \frac{GLX}{K_{mGLX}} \right) + \left( 1 + \frac{COA}{K_{mCOA}} \right) \cdot \left( 1 + \frac{MAL}{K_{mMAL}} \right) - 1 \right)}$$

$$v_{ACEK\_1} = k \cdot \left( ATP \cdot icd - \frac{ADP \cdot icdP}{K_{eq}} \right)$$

$$v_{ACEK\_2} = k \cdot \left( icdP - \frac{icd \cdot P}{K_{eq}} \right)$$

$$v_{ACK} = \frac{V_{max} \cdot \left( ACP \cdot ADP - \frac{ACEX \cdot ATP}{K_{eq}} \right)}{K_{mACP} \cdot K_{mADP} \left( 1 + \frac{ACP}{K_{mACP}} + \frac{ACEX}{K_{mACE}} \right) \cdot \left( 1 + \frac{ADP}{K_{mADP}} + \frac{ATP}{K_{mATP}} \right)}$$

$$v_{ACE\_OUT} = D \cdot ACEX$$

$$v_{ACN1} = \frac{V_{max} \cdot \left( CIT - \frac{ACO}{K_{eq}} \right)}{K_{mCIT} \left( 1 + \frac{CIT}{K_{mCIT}} + \frac{ACO}{K_{mACO}} + \frac{ICIT}{K_{mICIT}} \right)}$$

$$v_{ACN2} = \frac{V_{max} \cdot \left( ACO - \frac{ICIT}{K_{eq}} \right)}{K_{mACO} \left( 1 + \frac{ACO}{K_{mACO}} + \frac{ICIT}{K_{mICIT}} + \frac{CIT}{K_{mCIT}} \right)}$$

$$v_{ACS} = \frac{V_{max} \cdot ACEX \cdot ATP \cdot COA}{K_{mACE} \cdot K_{mATP} \cdot K_{mCOA} \left( 1 + \frac{ACEX}{K_{mACE}} \right) \cdot \left( 1 + \frac{ATP}{K_{mATP}} \right) \cdot \left( 1 + \frac{COA}{K_{mCOA}} \right)}$$

$$v_{ADK} = k \cdot \left( AMP \cdot ATP - \frac{ADP^2}{K_{eq}} \right)$$

$$v_{ATP\_NGAM} = V_{max} \cdot \left( ATP - \frac{ADP \cdot P}{K_{eq}} \right)$$

$$v_{ATP\_SYN} = \frac{V_{max} \cdot \left( \frac{\ln \left( \frac{H_{out}}{H_{in}} \right)}{\ln 10} \right)^4}{1 + \left( \frac{\ln \left( \frac{H_{out}}{H_{in}} \right)}{\ln 10} \right)^4} \cdot \left( ADP \cdot P - \frac{ATP}{K_{eq}} \right)$$

$$v_{CYA} = \frac{k \cdot \left( ATP - \frac{CAMP \cdot P^2}{K_{eq}} \right) \cdot e_{iiaP}}{e_{iiaP} + K_{aeiiaP}}$$

$$v_{CYTBO} = \frac{V_{max}}{1 + \left( \frac{\ln \left( \frac{H_{out}}{H_{in}} \right)}{\ln 10} \right)^2} \cdot \left( QH2^2 \cdot O2 - \frac{Q^2}{K_{eq}} \right)$$

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$$\begin{aligned}
v_{GPM} &= \frac{V_{max} \cdot \left( PGA3 - \frac{PGA2}{K_{eq}} \right)}{K_m PGA3} \\
&= \frac{PGA3}{1 + \frac{PGA3}{K_m PGA3} + \frac{PGA2}{K_m PGA2}} \\
v_{GROWTH} &= \frac{V_{max} \cdot G6P \cdot E4P \cdot PGA3 \cdot OAA \cdot AKG \cdot PYR \cdot R5P \cdot PEP \cdot GAP \cdot F6P \cdot NADPH \cdot ACCOA \cdot NAD \cdot ATP}{K_m G6P \cdot K_m E4P \cdot K_m PGA3 \cdot K_m OAA \cdot K_m AKG \cdot K_m PYR \cdot K_m R5P \cdot K_m PEP \cdot K_m GAP \cdot K_m F6P \cdot K_m NADPH \cdot K_m ACCOA \cdot K_m NAD \cdot K_m ATP} \\
&\quad \cdot \left( \left( 1 + \frac{G6P}{K_m G6P} \right) \cdot \left( 1 + \frac{E4P}{K_m E4P} \right) \cdot \left( 1 + \frac{PGA3}{K_m PGA3} \right) \cdot \left( 1 + \frac{OAA}{K_m OAA} \right) \cdot \left( 1 + \frac{AKG}{K_m AKG} \right) \cdot \left( 1 + \frac{PYR}{K_m PYR} \right) \cdot \left( 1 + \frac{R5P}{K_m R5P} \right) \right. \\
&\quad \cdot \left. \left( 1 + \frac{PEP}{K_m PEP} \right) \cdot \left( 1 + \frac{GAP}{K_m GAP} \right) \cdot \left( 1 + \frac{F6P}{K_m F6P} \right) \cdot \left( 1 + \frac{NADPH}{K_m NADPH} \right) \cdot \left( 1 + \frac{ACCOA}{K_m ACCOA} \right) \cdot \left( 1 + \frac{NAD}{K_m NAD} \right) \cdot \left( 1 + \frac{ATP}{K_m ATP} \right) \right) \\
v_{ICD} &= \frac{icd \cdot kcat \cdot \left( ICIT \cdot NADP - \frac{AKG \cdot NADPH}{K_{eq}} \right)}{K_m ICIT \cdot K_m NADP} \\
&= \left( 1 + \frac{ICIT}{K_m ICIT} \right) \cdot \left( 1 + \frac{NADP}{K_m NADP} \right) + \left( 1 + \frac{AKG}{K_m AKG} \right) \cdot \left( 1 + \frac{NADPH}{K_m NADPH} \right) - 1 \\
v_{LPD} &= \frac{V_{max} \cdot COA \cdot AKG \cdot NAD \cdot \left( 1 - \frac{AKG}{K_d AKG} \right)}{K_m COA \cdot K_m AKG \cdot K_m NAD} \\
&= \left( \frac{COA}{K_m COA} \cdot \frac{AKG}{K_m AKG} + \frac{COA}{K_m COA} \cdot \frac{NAD}{K_m NAD} + \frac{AKG}{K_m AKG} \cdot \frac{NAD}{K_m NAD} + \frac{COA}{K_m COA} \cdot \frac{AKG}{K_m AKG} \cdot \frac{NAD}{K_m NAD} \right. \\
&\quad \left. - \frac{AKG}{K_d AKG} \cdot \left( \frac{COA}{K_m COA} \cdot \frac{AKG}{K_m AKG} + \frac{AKG}{K_m AKG} \cdot \frac{NAD}{K_m NAD} + \alpha \cdot \frac{COA}{K_m COA} \cdot \frac{AKG}{K_m AKG} \cdot \frac{NAD}{K_m NAD} \right) \right) \\
v_{MAE} &= \frac{V_{max} \cdot n \cdot MAL \cdot NAD}{K_m MAL \cdot K_m NAD} \cdot \frac{\frac{MG}{K_m MG} + \frac{MN}{K_m MN}}{1 + \frac{K_m NAD}{K_m NAD} \cdot \frac{MAL}{K_m MAL} + \frac{NAD}{K_m NAD} + \frac{MAL}{K_m MAL} \cdot \frac{NAD}{K_m NAD}} \cdot \frac{\frac{MG}{K_m MG} + \frac{MN}{K_m MN}}{1 + \frac{MG}{K_m MG} + \frac{MN}{K_m MN}} \\
&\quad + L0 \cdot \left( \frac{\left( 1 + \frac{ASP}{K_{eff} ASP} \right) \cdot \left( 1 + \frac{MG}{K_m MG} + \frac{MN}{K_m MN} \right) \cdot \left( 1 + \frac{ATP}{K_{eff} ATP} \right) \cdot \left( 1 + \frac{ACCOA}{K_{eff} ACCOA} + \frac{COA}{K_{eff} COA} \right) \cdot \left( 1 + \frac{K_m NAD}{K_m NAD} \cdot \frac{MAL}{K_m MAL} + \frac{NAD}{K_m NAD} + \frac{MAL}{K_m MAL} \cdot \frac{NAD}{K_m NAD} \right)}{\left( 1 + \frac{ASP}{K_{eff} ASP} \right) \cdot \left( 1 + \frac{MG}{K_m MG} + \frac{MN}{K_m MN} \right) \cdot \left( 1 + \frac{ATP}{K_{eff} ATP} \right) \cdot \left( 1 + \frac{ACCOA}{K_{eff} ACCOA} + \frac{COA}{K_{eff} COA} \right) \cdot \left( 1 + \frac{K_m NAD}{K_m NAD} \cdot \frac{MAL}{K_m MAL} + \frac{NAD}{K_m NAD} + \frac{MAL}{K_m MAL} \cdot \frac{NAD}{K_m NAD} \right)} \right)^n \\
v_{MDH} &= \frac{V_{max} \cdot \left( NADH \cdot OAA - \frac{MAL \cdot NAD}{K_{eq}} \right)}{K_i NADH \cdot K_m OAA} \\
&= \left( 1 + \frac{K_m NAD}{K_i NAD} \cdot \frac{MAL}{K_m MAL} + \frac{NAD}{K_i NAD} + \frac{MAL}{K_m MAL} \cdot \frac{NAD}{K_i NAD} + \frac{NADH}{K_i NADH} + \frac{K_m NAD}{K_i NAD} \cdot \frac{MAL}{K_m MAL} \cdot \frac{NADH}{K_i NADH} + \frac{K_m NADH}{K_i NADH} \cdot \frac{OAA}{K_m OAA} + \frac{K_m NADH}{K_i NADH} \cdot \frac{NAD}{K_i NAD} \cdot \frac{OAA}{K_m OAA} \right. \\
&\quad \left. + \frac{MAL \cdot NAD \cdot OAA}{K_i NAD \cdot K_i OAA \cdot K_m MAL} + \frac{NADH}{K_i NADH} \cdot \frac{OAA}{K_m OAA} + K_{eq} \cdot \frac{K_i NADH \cdot K_m OAA}{K_i NAD \cdot K_m MAL} \cdot \frac{MAL}{K_i NAD} \cdot \frac{NADH}{K_m MAL} \cdot \frac{OAA}{K_m NADH} \cdot \frac{OAA}{K_i OAA} \right) \\
v_{MQO} &= \frac{V_{max} \cdot \left( MAL \cdot Q - \frac{OAA \cdot QH2}{K_{eq}} \right)}{K_m MAL \cdot K_m Q} \\
&= \left( 1 + \frac{MAL}{K_m MAL} \right) \cdot \left( 1 + \frac{Q}{K_m Q} \right) + \left( 1 + \frac{OAA}{K_m OAA} \right) \cdot \left( 1 + \frac{QH2}{K_m QH2} \right) - 1 \\
v_{NDH1} &= \frac{V_{max}}{1 + \left( \frac{\ln \left( \frac{H_{out}}{H_{in}} \right)}{\ln 10} \right)^2} \cdot \left( NADH \cdot Q - \frac{NAD \cdot QH2}{K_{eq}} \right) \\
v_{NDH2} &= V_{max} \cdot \left( NADH \cdot Q - \frac{NAD \cdot QH2}{K_{eq}} \right) \\
v_{PCK} &= \frac{V_{max} \cdot \left( MgATP \cdot OAA - \frac{HCO3 \cdot MgADP \cdot PEP}{K_{eq}} \right)}{K_m ATP \cdot K_m OAA} \\
&= \frac{HCO3}{1 + \frac{HCO3}{K_m HCO3} + \frac{HCO3}{K_m HCO3} \cdot \frac{ADP}{K_m ADP} + \frac{MgADP}{K_m ADP} + \frac{MgATP}{K_m ATP} + \frac{OAA}{K_m OAA} + \frac{MgATP}{K_m ATP} \cdot \frac{OAA}{K_m OAA} + \frac{HCO3}{K_m HCO3} \cdot \frac{PEP}{K_m PEP} + \frac{PEP}{K_m PEP} + \frac{HCO3}{K_m HCO3} \cdot \frac{MgADP}{K_m ADP} \cdot \frac{PEP}{K_m PEP} + \frac{MgADP}{K_m ADP} \cdot \frac{PEP}{K_m PEP}} \\
&\quad \cdot \left( COA \cdot NAD \cdot PYR - \frac{ACCOA \cdot NADH \cdot HCO3}{K_{eq}} \right) \\
&\quad \frac{K_m COA \cdot K_m NAD \cdot K_m PYR}{\left( \frac{ACCOA}{K_m ACCOA} + \frac{NADH}{K_m NADH} + \frac{ACCOA}{K_m ACCOA} \cdot \frac{NADH}{K_m NADH} + \frac{COA}{K_m COA} \cdot \frac{NADH}{K_m NADH} + \frac{ACCOA}{K_m ACCOA} \cdot \frac{COA}{K_m COA} \cdot \frac{NADH}{K_m NADH} + \frac{NAD}{K_m NAD} \cdot \frac{NADH}{K_m NADH} + \frac{COA}{K_m COA} \cdot \frac{NAD}{K_m NAD} \cdot \frac{NADH}{K_m NADH} \right. \\
&\quad \left. + \frac{ACCOA}{K_m ACCOA} \cdot \frac{PYR}{K_m PYR} + \frac{ACCOA}{K_m ACCOA} \cdot \frac{COA}{K_m COA} \cdot \frac{PYR}{K_m PYR} + \frac{COA}{K_m COA} \cdot \left( 1 + \frac{NAD}{K_m NAD} \right) \cdot \frac{PYR}{K_m PYR} + \frac{NAD}{K_m NAD} \cdot \left( 1 + \frac{COA}{K_m COA} + \frac{PYR}{K_m PYR} \right) \right) \\
v_{PDH} &= \frac{HCO3}{1 + \frac{HCO3}{K_m HCO3}}
\end{aligned}$$

$$\begin{aligned}
& \frac{V_{\max} \cdot n \cdot \left( MgATP \cdot F6P - \frac{MgADP \cdot FDP}{K_{eq}} \right)}{KirF6P \cdot KmrATPMg} \\
vPFK = & \frac{\left( 1 + \frac{KmrFDP}{KirFDP} \cdot \frac{MgADP}{KmrADP} + \frac{KmrF6P}{KirF6P} \cdot \frac{MgATP}{KmrATPMg} + \frac{KmrFDP}{KirFDP} \cdot \frac{MgADP}{KmrADP} \cdot \frac{F6P}{KirF6P} + \frac{MgATP}{KmrATPMg} \cdot \frac{F6P}{KirF6P} + \frac{MgADP}{KirADP} \cdot \frac{MgATP}{KmrATPMg} \cdot \frac{F6P}{KirF6P} \right.}{\left( 1 + \frac{ATP - MgATP}{KirATP} \right) \cdot \frac{F6P}{KirF6P} + \frac{FDP}{KirFDP} + \frac{MgADP}{KmrADP} \cdot \frac{FDP}{KirFDP} + \frac{KmrF6P}{KirF6P} \cdot \frac{MgATP}{KmrATPMg} \cdot \frac{FDP}{KirFDP} + W_r \cdot \frac{KmrF6P}{KirF6P} \cdot \frac{MgADP}{KirADP} \cdot \frac{MgATP}{KmrATPMg} \cdot \frac{FDP}{KmrFDP}} \\
& \left( 1 + L_0 \cdot \left( \left( 1 + \frac{MgADP}{K_{eff}ADP} + \frac{PEP}{K_{eff}PEP} \right) \cdot \left( 1 + \frac{KmtFDP}{KitFDP} \cdot \frac{MgADP}{KmtADP} + \frac{KmtF6P}{KitF6P} \cdot \frac{MgATP}{KmtATPMg} + \frac{KmtFDP}{KitFDP} \cdot \frac{MgADP}{KmtADP} \cdot \frac{F6P}{KitF6P} + \frac{MgATP}{KmtATPMg} \cdot \frac{F6P}{KitF6P} + \frac{MgADP}{KitADP} \cdot \frac{MgATP}{KmtATPMg} \cdot \frac{F6P}{KitF6P} \right) \right. \right. \\
& \left. \left. + \left( 1 + \frac{ATP - MgATP}{KitATP} \right) \cdot \frac{F6P}{KitF6P} + \frac{FDP}{KitFDP} + \frac{MgADP}{KmtADP} \cdot \frac{FDP}{KitFDP} + \frac{KmtF6P}{KitF6P} \cdot \frac{MgATP}{KmtATPMg} \cdot \frac{FDP}{KitFDP} + W_t \cdot \frac{KmtF6P}{KitF6P} \cdot \frac{MgADP}{KitADP} \cdot \frac{MgATP}{KmtATPMg} \cdot \frac{FDP}{KmtFDP} \right) \right) \right)^n \\
& \left( 1 + \frac{MgADP}{K_{eff}ADP} + \frac{PEP}{K_{eff}PEP} \right) \cdot \left( 1 + \frac{KmrFDP}{KirFDP} \cdot \frac{MgADP}{KmrADP} + \frac{KmrF6P}{KirF6P} \cdot \frac{MgATP}{KmrATPMg} + \frac{KmrFDP}{KirFDP} \cdot \frac{MgADP}{KmrADP} \cdot \frac{F6P}{KirF6P} + \frac{MgATP}{KmrATPMg} \cdot \frac{F6P}{KirF6P} + \frac{MgADP}{KirADP} \cdot \frac{MgATP}{KmrATPMg} \cdot \frac{F6P}{KirF6P} \right. \\
& \left. + \left( 1 + \frac{ATP - MgATP}{KirATP} \right) \cdot \frac{F6P}{KirF6P} + \frac{FDP}{KirFDP} + \frac{MgADP}{KmrADP} \cdot \frac{FDP}{KirFDP} + \frac{KmrF6P}{KirF6P} \cdot \frac{MgATP}{KmrATPMg} \cdot \frac{FDP}{KirFDP} + W_r \cdot \frac{KmrF6P}{KirF6P} \cdot \frac{MgADP}{KirADP} \cdot \frac{MgATP}{KmrATPMg} \cdot \frac{FDP}{KmrFDP} \right) \right) \\
vPGI = & \frac{\frac{V_{\max} \cdot \left( G6P - \frac{F6P}{K_{eq}} \right)}{KmG6P}}{1 + \frac{F6P}{KmF6P} + \frac{G6P}{KmG6P} + \frac{PEP}{KmPEP} + \frac{PGN}{KmPGN}} \\
vPGK = & \frac{\frac{V_{\max} \cdot \left( MgADP \cdot BPG - \frac{MgATP \cdot PGA3}{K_{eq}} \right)}{KmADPMg \cdot KmBPG}}{1 + \frac{MgADP}{KmADPMg} + \frac{BPG}{KmBPG} + \frac{MgADP}{KmADPMg} \cdot \frac{BPG}{KmBPG} + \frac{MgATP}{KmATPMg} + \frac{PGA3}{KmPGA3} + \frac{MgATP}{KmATPMg} \cdot \frac{PGA3}{KmPGA3}} \\
vPGL = & \frac{\frac{V_{\max} \cdot \left( GL6P - \frac{PGN}{K_{eq}} \right)}{KmGL6P}}{1 + \frac{GL6P}{KmGL6P} + \frac{PGN}{KmPGN} + \frac{G6P}{KiG6P}} \\
vPIT = V_{\max} \cdot & \left( \frac{\left( \ln \left( \frac{H_{out}}{H_{in}} \right) \right)^2}{\ln 10} \cdot \frac{P_p}{KmP_p + P_p} - \frac{\left( \ln \left( \frac{H_{out}}{H_{in}} \right) \right)^2}{\ln 10} \cdot \frac{P}{KmP + P} \right) \\
vPNT = k \cdot & \left( NAD \cdot NADPH - \frac{NADH \cdot NADP}{K_{eq}} \right) \quad V_{\max} \cdot n \cdot \left( PEP \cdot HCO_3 - \frac{OAA \cdot P}{K_{eq}} \right) \\
vPPC = & \frac{\frac{KdrPEP \cdot KmrHCO_3}{1 + \frac{KmrPEP}{KdrPEP} \cdot \frac{HCO_3}{KmrHCO_3} + \frac{KmrOAA}{KdrOAA} \cdot \frac{P}{KmrP} + \frac{OAA}{KdrOAA} + \frac{P}{KmrP} \cdot \frac{OAA}{KdrOAA} + \frac{HCO_3}{KmrHCO_3} \cdot \frac{PEP}{KdrPEP} + \frac{PEP}{KdrPEP}}}{\left( \left( 1 + \frac{KmtPEP}{KdtPEP} \cdot \frac{HCO_3}{KmtHCO_3} + \frac{KmtOAA}{KdtOAA} \cdot \frac{P}{KmtP} + \frac{OAA}{KdtOAA} + \frac{P}{KmtP} \cdot \frac{OAA}{KdtOAA} + \frac{HCO_3}{KmtHCO_3} \cdot \frac{PEP}{KdtPEP} + \frac{PEP}{KdtPEP} \right) \right. \\
& \left. \cdot \left( 1 + \frac{ACCOA}{K_{eff}ACCOA} + \frac{FDP}{K_{eff}FDP} + \frac{FDP}{K_{eff}FDP} \cdot \frac{ACCOA}{K_{eff}FDP} \right) \cdot \left( 1 + \frac{ASP}{K_{eff}ASP} + \frac{CYS}{K_{eff}CYS} + \frac{CIT}{K_{eff}CIT} + \frac{FUM}{K_{eff}FUM} + \frac{MAL}{K_{eff}MAL} + \frac{SUC}{K_{eff}SUC} \right) \right) \right)^n \\
& \left( 1 + L_0 \cdot \left( \left( 1 + \frac{KmrPEP}{KdrPEP} \cdot \frac{HCO_3}{KmrHCO_3} + \frac{KmrOAA}{KdrOAA} \cdot \frac{P}{KmrP} + \frac{OAA}{KdrOAA} + \frac{P}{KmrP} \cdot \frac{OAA}{KdrOAA} + \frac{HCO_3}{KmrHCO_3} \cdot \frac{PEP}{KdrPEP} + \frac{PEP}{KdrPEP} \right) \right. \right. \\
& \left. \left. \cdot \left( 1 + \frac{ACCOA}{K_{eff}ACCOA} + \frac{FDP}{K_{eff}FDP} + \frac{FDP}{K_{eff}FDP} \cdot \frac{ACCOA}{K_{eff}FDP} \right) \cdot \left( 1 + \frac{ASP}{K_{eff}ASP} + \frac{CYS}{K_{eff}CYS} + \frac{CIT}{K_{eff}CIT} + \frac{FUM}{K_{eff}FUM} + \frac{MAL}{K_{eff}MAL} + \frac{SUC}{K_{eff}SUC} \right) \right) \right) \\
vPPS = & \frac{\frac{V_{\max} \cdot \left( MgATP \cdot PYR - \frac{AMP \cdot PEP \cdot P \cdot MG}{K_{eq}} \right)}{KmATPMg \cdot KmPYR}}{\left( \frac{MgATP}{KmATPMg} + \alpha \cdot \frac{P}{KdP} \cdot \frac{MgATP}{KmATPMg} + \alpha \cdot \frac{AMP}{KdAMP} \cdot \frac{MgATP}{KmATPMg} + \alpha \cdot \frac{P}{KdP} \cdot \frac{AMP}{KdAMP} \cdot \frac{MgATP}{KmATPMg} + \frac{\alpha \cdot \frac{MG}{KdMg} \cdot \frac{P}{KmP} \cdot \frac{AMP}{KdAMP} \cdot \frac{MgATP}{KdATPMgPPS}}{W \cdot \left( 1 + \frac{MG}{KdMg} \right)} \right. \\
& + \frac{MgATP}{KmATPMg} \cdot \frac{AKG}{K_{eff}AKG} + \frac{\left( 1 + \frac{MG}{KdMg} \right) \cdot \frac{AKG}{K_{eff}AKG} \cdot \frac{PEP}{KmPEP}}{W} + \frac{MgATP}{KmATPMg} \cdot \frac{OAA}{K_{eff}OAA} + \frac{\left( 1 + \frac{MG}{KdMg} \right) \cdot \frac{OAA}{K_{eff}OAA} \cdot \frac{PEP}{KmPEP}}{W} + \frac{MG}{KdMg} \cdot \frac{P}{KmP} \cdot \frac{AMP}{KdAMP} \\
& + \frac{\alpha \cdot \frac{P}{KdP} \cdot \frac{AMP}{KdAMP} \cdot \frac{PEP}{KmPEP}}{W} + \frac{\alpha \cdot \frac{AMP}{KdAMP} \cdot \frac{PEP}{KmPEP} \cdot \frac{MG}{KdMg} \cdot \frac{P}{KmP} \cdot \frac{AMP}{KdAMP} \cdot \frac{PEP}{KmPEP}}{W} + \frac{\alpha \cdot \left( 1 + \frac{MG}{KdMg} \right) \cdot \left( \frac{KmAMP}{KdAMP} \cdot \frac{P}{KmP} \cdot \frac{PEP}{KmPEP} + \frac{AMP}{KdAMP} \cdot \frac{PEP}{KmPEP} \right)}{W} \\
& + \left( 1 + \frac{MG}{KdMg} \right) \cdot \frac{PYR}{KmPYR} + \frac{MgATP}{KmATPMg} \cdot \frac{PYR}{KmPYR} + \frac{\frac{KdADPMg}{KdMg} \cdot \frac{P}{KmP} \cdot \frac{MgADP}{K_{eff}ADP} \cdot \frac{AMP}{KdAMP}}{W \cdot \left( 1 + \frac{MG}{KdMg} \right)} + \frac{ADP - MgADP}{K_{eff}ADP} \cdot \frac{PYR}{KmPYR} + \frac{\frac{KdATPMg}{KdMg} \cdot \frac{P}{KmP} \cdot \frac{AMP}{KdAMP} \cdot \frac{MgATP}{K_{eff}ATP}}{W \cdot \left( 1 + \frac{MG}{KdMg} \right)} \\
& + \frac{ATP - MgATP}{K_{eff}ATP} \cdot \frac{PYR}{KmPYR} + \frac{\left( 1 + \frac{MG}{KdMg} \right) \cdot \frac{PEP}{KmPEP}}{W} + \alpha \cdot \left( 1 + \frac{MG}{KdMg} \right) \cdot \frac{PEP}{KdPEP} \cdot \frac{PYR}{KmPYR} + \frac{\left( 1 + \frac{MG}{KdMg} \right) \cdot \frac{PYR}{KdPYR} \cdot \frac{PEP}{KmPEP}}{W} \right) \\
vPTA = & \frac{\frac{V_{\max} \cdot \left( ACCOA \cdot P - \frac{ACP \cdot COA}{K_{eq}} \right)}{KiACCOA \cdot KmP}}{1 + \frac{ACCOA}{KiACCOA} + \frac{P}{KiP} + \frac{ACP}{KiACP} + \frac{COA}{KiCOA} + \frac{ACCOA \cdot P}{KiACCOA \cdot KmP} + \frac{ACP \cdot COA}{KmACP \cdot KiCOA}}
\end{aligned}$$

$$\begin{aligned}
v_{PTS\_0} &= \frac{kF \cdot ei \cdot PEP^2}{KmPEP^2 + PEP^2} - \frac{kR \cdot eiP \cdot PYR^2}{KmPYR^2 + PYR^2} \\
v_{PTS\_1} &= kF \cdot hpr \cdot eiP - kR \cdot hprP \cdot ei \\
v_{PTS\_2} &= kF \cdot hprP \cdot eiia - kR \cdot hpr \cdot eiiaP \\
v_{PTS\_3} &= kF \cdot eiicb \cdot eiiaP - kR \cdot eiia \cdot eiicbP \\
v_{PTS\_4} &= \frac{kF \cdot eiicbP \cdot GLC_x}{KmGLC + GLC_x} - \frac{kR \cdot eiicb \cdot G6P}{KmG6P + G6P} \\
v_{PYK} &= \frac{V_{max} \cdot n \cdot PEP \cdot MgADP}{KirPEP \cdot KmrADPMg} \\
&\cdot \frac{1 + \frac{KmrPEP}{KirPEP} \cdot \frac{MgADP}{KmrADPMg} + \frac{MgATP}{KirATP} + \frac{MgADP}{KmrADPMg} \cdot \frac{PEP}{KirPEP} + \frac{KmrADPMg}{KmrADPMg} \cdot \left(1 + \frac{ADP - MgADP}{KirADP}\right) \cdot \frac{PEP}{KirPEP} + \frac{PYR}{KirPYR} + \frac{MgATP}{KirPyrATP} \cdot \frac{PYR}{KirPYR}}{\left(1 + L0 \cdot \left( \left(1 + \frac{KmtPEP}{KitPEP} \cdot \frac{MgADP}{KmtADPMg} + \frac{MgATP}{KitATP} + \frac{MgADP \cdot PEP}{KmtPEP \cdot KmtADPMg} + \left(1 + \frac{ADP - MgADP}{KitADP}\right) \cdot \frac{PEP}{KitPEP} + \frac{PYR}{KitPYR} + \frac{MgATP}{KitPyrATP} \cdot \frac{PYR}{KitPYR}\right) \cdot \left(1 + \frac{SUCCOA}{KeflSUCCOA} + \frac{MgATP \cdot SUCCOA}{KeflATP \cdot KeflSUCCOA}\right) \right) \cdot \left(1 + \frac{KmrPEP}{KirPEP} \cdot \frac{MgADP}{KmrADPMg} + \frac{MgATP}{KirATP} + \frac{MgADP}{KmrADPMg} \cdot \frac{PEP}{KirPEP} + \left(1 + \frac{ADP - MgADP}{KirADP}\right) \cdot \frac{PEP}{KirPEP} + \frac{PYR}{KirPYR} + \frac{MgATP}{KirPyrATP} \cdot \frac{PYR}{KirPYR}\right) \cdot \left(1 + \frac{FDP}{KefrFDP} + \frac{G6P}{KefrG6P} + \frac{GL6P}{KefrGL6P} + \frac{R5P}{KefrR5P} + \frac{RU5P}{KefrRU5P} + \frac{S7P}{KefrS7P} + \frac{X5P}{KefrX5P}\right) \right)} \\
v_{RPE} &= \frac{V_{max} \cdot \left(RU5P - \frac{X5P}{Keq}\right)}{KmRU5P} \\
&\cdot \frac{1 + \frac{RU5P}{KmRU5P} + \frac{X5P}{KmX5P}}{1 + \frac{RU5P}{KmRU5P} + \frac{R5P}{KmR5P} + \frac{E4P}{KmE4P}} \\
v_{S7P\_E4P\_TAL} &= kcat \cdot \left(S7P \cdot tal - \frac{E4P \cdot talC3}{Keq}\right) \\
v_{S7P\_R5P\_TKT} &= kcat \cdot \left(R5P \cdot tktC2 - \frac{S7P \cdot tkt}{Keq}\right) \\
v_{SDH} &= \frac{V_{max} \cdot \left(SUC \cdot Q - \frac{FUM \cdot QH2}{Keq}\right)}{KefSUC \cdot KmQ} \\
&\cdot \frac{1 + \frac{FUM}{KefFUM} + \frac{KmSUC}{KefSUC} \cdot \frac{Q}{KmQ} + \frac{KmFUM}{KefFUM} \cdot \frac{QH2}{KmQH2} + \frac{FUM}{KefFUM} \cdot \frac{QH2}{KmQH2} + \frac{SUC}{KefSUC} + \frac{SUC}{KefSUC} \cdot \frac{Q}{KmQ}}{V_{max} \cdot \left(ADP \cdot SUCCOA \cdot P - \frac{ATP \cdot COA \cdot SUC}{Keq}\right)} \\
v_{SK} &= \frac{1 + \frac{ADP}{KmADP} \cdot \left(1 + \frac{SUCCOA}{KmSUCCOA}\right) \cdot \left(1 + \frac{P}{KmP}\right) + \left(1 + \frac{ATP}{KmATP}\right) \cdot \left(1 + \frac{COA}{KmCOA}\right) \cdot \left(1 + \frac{SUC}{KmSUC}\right) - 1}{V_{max} \cdot \left(DAP - \frac{GAP}{Keq}\right)} \\
v_{SQR} &= V_{max} \cdot \left(FADH2 \cdot Q - \frac{FAD \cdot QH2}{Keq}\right) \\
v_{TPI} &= \frac{V_{max} \cdot \left(DAP - \frac{GAP}{Keq}\right)}{KmDAP} \\
&\cdot \frac{1 + \frac{DAP}{KmDAP} + \frac{GAP}{KmGAP}}{v_{X5P\_GAP\_TKT} = kcat \cdot \left(tkt \cdot X5P - \frac{GAP \cdot tktC2}{Keq}\right)} \\
v_{XCH\_GLC} &= \frac{V_{max} \cdot \left(\frac{GLC_x}{KmGLC} - \frac{GLC_p}{KmGLC}\right)}{1 + \frac{GLC_x}{KmGLC} + \frac{GLC_p}{KmGLC}} \\
v_{XCH\_P} &= \frac{V_{max} \cdot \left(\frac{Px}{KmP} - \frac{Pp}{KmP}\right)}{1 + \frac{Px}{KmP} + \frac{Pp}{KmP}} \\
v_{XCH\_ACE1} &= \frac{V_{max} \cdot \left(\frac{ACE}{KmACE} - \frac{ACE_p}{KmACE}\right)}{1 + \frac{ACE}{KmACE} + \frac{ACE_p}{KmACE}} \\
v_{XCH\_ACE2} &= \frac{V_{max} \cdot \left(\frac{ACE_p}{KmACE} - \frac{ACE_x}{KmACE}\right)}{1 + \frac{ACE_p}{KmACE} + \frac{ACE_x}{KmACE}} \\
v_{ZWF} &= \frac{V_{max} \cdot \left(G6P \cdot NADP - \frac{GL6P \cdot NADPH}{Keq}\right)}{KdG6P \cdot KmNADP} \\
&\cdot \frac{1 + \frac{G6P}{KdG6P} + \frac{KmG6P}{KdG6P} \cdot \frac{NADP}{KmNADP} + \frac{G6P}{KdG6P} \cdot \frac{NADP}{KmNADP} + \frac{KmGL6P}{KdGL6P} \cdot \frac{NADPH}{KmNADPH} + \frac{GL6P}{KdGL6P} \cdot \frac{NADPH}{KmNADPH}}{15}
\end{aligned}$$

## 6. Conservation laws

The following equations describe the conservation laws of conserved moieties:

$$\text{tal}_{\text{total}} = \text{tal} + \text{talC3}$$

$$\text{tk}_{\text{total}} = \text{tk} + \text{tkC2}$$

$$\text{icd}_{\text{total}} = \text{icd} + \text{icdP}$$

$$\text{ei}_{\text{total}} = \text{ei} + \text{eiP}$$

$$\text{eiia}_{\text{total}} = \text{eiia} + \text{eiiaP}$$

$$\text{eiicb}_{\text{total}} = \text{eiicb} + \text{eiicbP}$$

$$\text{hpr}_{\text{total}} = \text{hpr} + \text{hprP}$$

$$\text{Q}_{\text{total}} = \text{Q} + \text{QH}_2$$

$$\text{NAD}_{\text{total}} = \text{NAD} + \text{NADH}$$

$$\text{NADP}_{\text{total}} = \text{NADP} + \text{NADPH}$$

$$\text{FAD}_{\text{total}} = \text{FAD} + \text{FADH}_2$$

$$\text{AxP}_{\text{total}} = \text{AMP} + \text{ADP} + \text{ATP} + \text{cAMP}$$

## 7. Concentrations of cofactors and conserved moieties

Concentrations of cofactors, metal ions and conserved moieties were taken from the literature and are given in table S2.

**Table S2.** Initial intracellular concentrations of cofactors, metal ions and conserved moieties.

Specie	Concentration (mM)	Comment
$\text{HCO}_3^-$	1.4	saturation concentration in water at 298 K, 1 atm, pH=7.5
$\text{O}_2$	0.21	saturation concentration in water at 298 K, 1 atm
$\text{H}^+_{\text{cytoplasm}}$	$3.16 \times 10^{-5}$	from [18], $\text{pH}_{\text{cytoplasm}} = 7.5$
$\text{Mg}^{2+}$	1	from [21]
$\text{Mn}^{2+}$	0.3	from [22]
Asp	1.17	from [23]
Cys	0.085	from [23]
CoA	0.5	from [24]
$\text{AxP}_{\text{total}}$	4.28	from [23]
$\text{ICD}_{\text{total}}$	0.043	from [25]
$\text{Q}_{\text{total}}$	1	from [24]
$\text{TAL}_{\text{total}}$	0.006	from [26]
$\text{TKT}_{\text{total}}$	0.007	from [27]
$\text{NAD}_{\text{total}}$	1.57	from [3], in agreement with [28]
$\text{NADP}_{\text{total}}$	0.257	from [3]
$\text{FAD}_{\text{total}}$	1	arbitrary



## 8. Magnesium complexes

The following functions were used to estimate the concentrations of magnesium complexes taking part as substrates in particular enzyme reactions:

$$MgADP = \frac{Mg \cdot ADP}{KdADPMg + Mg}$$

$$MgATP = \frac{Mg \cdot ATP}{KdATPMg + Mg}$$

$$MgFDP = \frac{Mg \cdot FDP}{KdFDPMg + Mg}$$

where MgADP, MgATP and MgFDP are the concentrations of magnesium complexes, ATP, ADP and FDP are the concentrations of free metabolites, Mg is the concentration of free magnesium ions, and KdADPMg, KdATPMg and KdFDPMg are the respective dissociation constants.

## 9. Model calibration

This section outlines the followed model calibration strategy and lists the values of all the parameters.

To the extent possible, values of the biochemical parameters were taken from the literature. This was the case for 56% of the parameters (253/449, Table S3). Parameters not available in the literature, which do not have a real biochemical meaning (e.g. Michaelis constants of the biomass function), or for which biochemical estimates are generally not indicative of cellular conditions (e.g. Vmax) were estimated to reproduce in the best possible way various experimental data obtained from a unique *E. coli* strain (the model strain K-12 MG1655 wild-type) grown in a unique reference condition (M9 minimal medium, dilution rate = 0.1 h<sup>-1</sup>, temperature = 37°C, pH = 7.0, pO<sub>2</sub> > 20%). This was critical to prevent biases during parameter estimation since fluxes and metabolite concentrations depends on environmental conditions and strains [29-32]. Experimental data used for parameter estimation were steady state reaction rates and metabolite concentrations [23, 33-35] and time-course concentrations of intracellular metabolites in response to a glucose pulse [23] (S1 Dataset). A total of 276 data points was used to estimate the remaining 196 parameters. Parameter estimation problem was formulated as a constrained optimization problem:

$$\begin{aligned} & \text{minimize } f(p) \\ & \text{subject to } g(p) \geq c \end{aligned}$$

where  $p$  is the parameter vector,  $f$  is the objective function which evaluates the deviation between the simulated and measured data,  $g(p)$  is the constraint function vector, and  $c$  is the constraint vector. The objective function  $f$  is defined as the sum of squared weighted errors:

$$f(p) = \sum_i \left( \frac{x_i - y_i(p)}{\sigma_i} \right)^2$$

where  $x_i$  is the experimental value of the data point  $i$  with standard deviation  $\sigma_i$ , and  $y_i(p)$  is the corresponding simulated value.

Constraints were defined on estimated parameters ( $10^{-4} \text{ mM} \leq K_M \leq 10^3 \text{ mM}$ ;  $10^{-2} \text{ mM/s} \leq V_{max} \leq 10^3 \text{ mM/s}$ ;  $10^{-4} \leq K_{eq} \leq 10^6$ ) to ensure they are kept within a biologically reasonable range.

The objective function was minimized with the Particle Swarm Optimization algorithm [36] (with a swarm size of 50 and 20,000 iterations), using the Condor-COPASI system [37] on a pool of 2500 CPU cores. Values of all the parameters (and the corresponding reference for values taken from the literature) are listed in Table S3. The experimental and fitted data are provided in S1 Dataset.

**Table S3.** Parameters of the kinetic model.

<i>Reaction</i>	<i>Equation</i>	<i>Parameter</i>	<i>Value</i>	<i>Unit</i>	<i>Source</i>
ACEA	[5]	KdICITsuc	0.0049	mM	Estimated
		KdPEP	1.05	mM	[38]
		KdPEPgIx	0.0312	mM	Estimated
		KdPEPicit	0.164	mM	Estimated
		KdPGA3	0.8	mM	[38]
		KdSUC	0.53	mM	[38]
		Keq	8.8	1	[38]
		KmGLX	0.13	mM	[38]
		KmICIT	0.063	mM	[38]
		KmSUC	0.59	mM	[38]
		Vmax	1.53	mM/s	Estimated
ACEB	[5]	Keq	230000	1	[39]
		KmACCOA	0.009	mM	[40]
		KmCOA	10	mM	[5]
		KmGLX	0.021	mM	[40]
		KmMAL	15.1	mM	Estimated, in agreement with the value of 10 estimated in [5]
		Vmax	0.353	mM/s	Estimated
ACEK_1	[5]	k	1.25	mM/s	Estimated
		Keq	888	1	Estimated
ACEK_2	[5]	k	0.0332	mM/s	Estimated
		Keq	2000	1	Estimated
ACK	[8]	Keq	174	1	[8]
		KmACE	7	mM	[41]
		KmACP	0.16	mM	[41]
		KmADP	0.5	mM	[41]
		KmATP	0.07	mM	[41]
		Vmax	7.23	mM/s	Estimated
ACN_1	[5]	Keq	0.385	1	Estimated
		KmACO	0.02	mM	[42]
		KmCIT	0.063	mM	Estimated
		KmICIT	9.31	mM	Estimated
		Vmax	9.72	mM/s	Estimated
ACN_2	[5]	Keq	3.5	1	Estimated, in agreement with the value of 2.615 estimated in [5]
		KmACO	0.02	mM	[42]
		KmCIT	0.063	mM	Estimated
		KmICIT	9.31	mM	Estimated
		Vmax	9.87	mM/s	Estimated
ACS	[8]	KmACE	0.07	mM	[43]
		KmATP	0.1	mM	[44]
		KmCOA	0.01	mM	Estimated
		Vmax	7.3	mM/s	Estimated
ADK	see Section 3	k	0.242	mM/s	Estimated
		Keq	0.963	1	Estimated, in agreement with the experimental range of 0.20-1.45 [23]
ATP_NGAM	see Section 3	Keq	3.63	mM	Estimated
		Vmax	1.3	1/s	Estimated
ATP_SYN	see Section 3	Keq	49.8	1	Estimated
		Vmax	109	mM/s	Estimated
CYA	see Section 3	k	0.0041	1/s	Estimated
		KaeiiaP	0.181	mM	Estimated
		Keq	2590	?	Estimated
CYTBO	see Section 3	Keq	12.07	1	Estimated
		Vmax	8.54	mM/s	Estimated
DOS	see Section 3	k	0.0083	1/s	Estimated
		Keq	674	1	Estimated

EDA	[5]	Keq	0.5	mM	[45]
		KmGAP	86.7	mM	Estimated
		KmKDPG	0.06	mM	[46]
		KmPYR	10	mM	[47]
		Vmax	0.0775	mM/s	Estimated
EDD	[5]	Keq	1000	1	[48]
		KmKDPG	0.318	mM	Estimated, in agreement with the value of 1 estimated in [5]
		KmPGN	0.6	mM	[48]
		Vmax	0.111	mM/s	Estimated
ENO	[5]	Keq	3	1	[49]
		KmPEP	0.1	mM	[50]
		KmPGA2	0.1	mM	[50]
		Vmax	11.7	mM/s	Estimated
F6P_E4P_TKT	[5]	kcat	40	mM/s/mM_enz	Estimated, in agreement with the value of 69 estimated in [5]
		Keq	0.5	1	[51]
F6P_GAP_TAL	[5]	kcat	120	mM/s/mM_enz	Estimated, in agreement with the value of 70 estimated in [5]
		Keq	0.11	1	[27]
FBA	[5]	Keq	0.19	mM	[52]
		KmDAP	0.13	mM	[53]
		KmFDP	0.12	mM	[53]
		KmGAP	0.13	mM	[54]
		KiPEP	0.5	mM	[55]
		Vmax	21.7	mM/s	Estimated
FBP	[5]	KdFDPMg	5.81	mM	Estimated, in agreement with the value of 10 estimated in [5]
		KirAMP	0.0012	mM	[56]
		KirAMPFDP	0.256	mM	[56]
		KirF6P	1.12	mM	[56]
		KirF6PMg	0.385	mM	[57]
		KirFDP	1.35	mM	Estimated, in agreement with the value of 1.116 estimated in [5]
		KirFDPMg	0.76	mM	[56-59]
		KirFDPMgMg	0.356	mM	[56-59]
		KirP	3.16	mM	[57]
		KirPF6P	6.6	mM	[57]
		KirPF6PMg	48.4	mM	[57]
		KirPMg	0.856	mM	[57]
		KitAMP	0.000255	mM	[56-59]
		KitAMPFDP	690	mM	[56-59]
		KitF6P	0.304	mM	[57]
		KitF6PMg	315	mM	[57]
		KitFDP	0.043	mM	Estimated
		KitFDPMg	0.00642	mM	[56-59]
		KitFDPMgMg	100	mM	[56-59]
		KitP	0.642	mM	[57]
		KitPF6P	0.00689	mM	[56-59]
		KitPF6PMg	16.5	mM	[57]
		KitPMg	539	mM	[57]
		KmrFDP	0.064	?	Estimated
		KmrMg	0.039	?	[56-59]
		KmtFDP	1.0e-05	?	[56-59]
		KmtMg	55	?	[57]
		L0	0.000815	?	[56-59]
		n	4	?	[60]
		Vmax	0.216	?	Estimated
FUMA	[5]	Keq	5	1	[61]
		KmFUM	0.6	mM	[61]
		KmMAL	0.7	mM	[62]
		Vmax	53.3	mM/s	Estimated

GDH	[5]	Keq	20	l/mmol	[49]
		KmBPG	0.2	mM	[63]
		KmGAP	2.47	mM	Estimated
		KmNAD	0.011	mM	Estimated, in agreement with the value of 0.045 estimated in [5]
		KmNADH	3.7	mM	Estimated
		KmP	0.017	mM	Estimated
		Vmax	8.67	mM/s	Estimated
GLT	[5]	KdACCOA0	0.7	mM	[64]
		KdcsCIT	7.38	mM	Estimated
		KdcsCOA	0.00175	mM	Estimated
		KdcsOAA	0.155	mM	Estimated, in agreement with the value of 0.05 estimated in [5]
		Keq	8300	1	[65]
		Ki1AKG	0.015	mM	[65]
		Ki1NADH	0.00033	mM	[65]
		Ki2AKG	0.256	mM	[65]
		Ki2NADH	0.0504	mM	[65]
		KiATP	0.58	mM	[65]
		KmACCOA0	0.12	mM	[64]
		KmcsCIT	1.16	mM	Estimated
		KmcsCOA	0.0001	mM	Estimated
		KmOAA0	0.00123	mM	Estimated
		Vmax	57	mM/s	Estimated
GND	see Section 3	KdHCO3	59	mM	Estimated, in agreement with the value of 100 estimated in [5]
		KdHCO3NADPH	9.72	mM	Estimated
		KdNADP	0.117	mM	[66]
		KdNADPH	0.0034	mM	[67]
		KdRu5P	0.044	mM	[67]
		KefATP	0.065	mM	[67]
		KefFbP	0.013	mM	[67]
		KefNADPATP	0.14	mM	[67]
		KefNADPFbP	0.0052	mM	[67]
		Keq	50	mM	[67]
		KmHCO3	6.4	mM	Estimated, in agreement with the value of 3 estimated in [5]
		KmNADP	0.049	mM	[68], in agreement with the value of 0.015 estimated in [5]
		KmNADPH	68.4	mM	Estimated, in agreement with the value of 100 estimated in [5]
		KmPGN	0.093	mM	[68]
		KmRU5P	45.2	mM	Estimated, in agreement with the value of 100 estimated in [5]
		Vmax	4.08	mM/s	Estimated
GPM	[5]	Keq	0.565	1	Estimated, in agreement with the value of 0.55 estimated in [5]
		KmPGA2	1.91	mM	Estimated
		KmPGA3	0.115	mM	Estimated, in agreement with the value of 0.19 estimated in [5]
		Vmax	11	mM/s	Estimated
GROWTH	see Section 3	KmG6P	1.21		Estimated
		KmF6P	0.366		Estimated
		KmGAP	0.0249		Estimated
		KmR5P	0.0212		Estimated
		KmE4P	1.63		Estimated
		KmPGA3	0.0765		Estimated
		KmPEP	0.458		Estimated
		KmPYR	0.00464		Estimated
		KmOAA	0.0248		Estimated
		KmAKG	5.12		Estimated
		KmACCOA	0.0494		Estimated
		KmNADPH	3.598		Estimated
		KmNAD	2.822		Estimated
		KmATP	0.0468		Estimated
		Vmax	9.74		Estimated

ICD	[5]	kcat	2460	1/s	Estimated
		Keq	28.2	1	Estimated, in agreement with the value of 25.3 estimated in [5]
		KmAKG	0.038	mM	[69]
		KmICIT	0.011	mM	[69]
		KmNADP	0.006	mM	[69]
		KmNADPH	0.000683	mM	Estimated
LPD	[5]	alpha	16.4	?	Estimated
		KdAKG	14.9	mM	Estimated
		KmAKG	0.02	?	[70]
		KmCOA	0.076	?	[71]
		KmNAD	0.098	?	[70]
		Vmax	0.0684	?	Estimated
MAD	[5]	KefrACCOA	1.83	mM	Estimated, higher than 0.57 [5]
		KefrASP	0.362	mM	[5]
		KefrATP	89	mM	[5]
		KefrCOA	0.268	mM	[5]
		KeftACCOA	0.197	mM	[5]
		KeftASP	0.583	mM	[5]
		KeftATP	0.26	mM	[5]
		KeftCOA	0.268	mM	[5]
		KirNAD	0.636	mM	Estimated
		KitNAD	0.99	mM	Estimated
		KmrMAL	0.213	mM	Estimated
		KmrMg	0.192	mM	Estimated
		KmrMn	0.273	mM	Estimated
		KmrNAD	1.37	mM	Estimated
		KmtMAL	0.093	mM	[5]
		KmtMg	2.38	mM	Estimated
		KmtMn	0.41	mM	Estimated
		KmtNAD	0.108	mM	[5]
		L0	19.9	?	[5]
		n	4	?	[5]
		Vmax	6.64	?	Estimated
MDH	[5]	Keq	100000	1	[72]
		KiNAD	0.0233	mM	Estimated
		KiNADH	0.000197	mM	Estimated
		KiOAA	2.46	mM	[72]
		KmMAL	0.86	mM	[72]
		KmNAD	0.64	mM	[72]
		KmNADH	0.003	mM	[72]
		KmOAA	0.001	mM	[72]
		Vmax	6.11	mM/s	Estimated
MQO	[5]	Keq	9	1	[73]
		KmMAL	0.435	mM	[73]
		KmOAA	75.8	mM	Estimated, in agreement with the value of 50 estimated in [5]
		KmQ	0.0414	mM	[73]
		KmQH2	8.78	mM	Estimated
		Vmax	4.62	mmol/s	Estimated
NDHI	see Section 3	Keq	27.6	1	Estimated
		Vmax	23.1	mM/s	Estimated
NDHII	see Section 3	Keq	27.6	1	Estimated
		Vmax	30.8	mM/s	Estimated
PCK	[5]	Keq	1.88	mM	[49]
		KmADP	0.05	mM	[74]
		KmATP	0.06	mM	[74]
		KmHCO3	2.63	mM	Estimated, in agreement with the value of 3 estimated in [5]
		KmOAA	0.67	mM	[74]
		KmPEP	0.07	mM	[74]
		Vmax	8.09	mM/s	Estimated

PDH	[5]	Keq	3140	1	Estimated
		KmACCOA	10.2	mM	[5]
		KmCOA	0.005	mM	[5]
		KmHCO <sub>3</sub>	0.00545	mM	Estimated
		KmNAD	0.01	mM	[5]
		KmNADH	6.64	mM	Estimated
		KmPYR	2	mM	[5]
		Vmax	961	mM/s	Estimated
PFK	[5]	K <sub>fr</sub> ADP	0.0735	mM	[5]
		K <sub>fr</sub> PEP	20	mM	[5]
		K <sub>ft</sub> ADP	9	mM	[5]
		K <sub>ft</sub> PEP	0.26	mM	[5]
		Keq	2000	1	Estimated
		K <sub>r</sub> ADP	55	mM	[5]
		K <sub>r</sub> ATP	2.5e-05	mM	[5]
		K <sub>r</sub> F6P	1.846	mM	[5]
		K <sub>r</sub> FDP	0.046	mM	[5]
		K <sub>t</sub> ADP	80	mM	[5]
		K <sub>t</sub> ATP	0.014	mM	[5]
		K <sub>t</sub> F6P	0.0086	mM	[5]
		K <sub>t</sub> FDP	50.5	mM	[5]
		K <sub>mr</sub> ADP	0.69	mM	[5]
		K <sub>mr</sub> ATPMg	8.12e-05	mM	[5]
		K <sub>mr</sub> F6P	2.05e-05	mM	[5]
		K <sub>mr</sub> FDP	10	mM	[5]
		K <sub>mt</sub> ADP	2	mM	[5]
		K <sub>mt</sub> ATPMg	3.34	mM	[5]
		K <sub>mt</sub> F6P	33	mM	[5]
		K <sub>mt</sub> FDP	10	mM	[5]
		L0	14.09	?	[5]
		n	4	?	[5]
		Vmax	0.185	?	Estimated
		W <sub>r</sub>	0.0237	1	Estimated, in agreement with the value of 0.08 estimated in [5]
		W <sub>t</sub>	0.147	1	Estimated
PGI	see Section 3	Keq	0.36	1	[23]
		K <sub>m</sub> F6P	0.147	mM	[75]
		K <sub>m</sub> G6P	0.28	mM	[75]
		K <sub>i</sub> PEP	2	mM	[55]
		K <sub>i</sub> PGN	0.516	mM	Estimated, in agreement with the value of 0.2 estimated in [5]
		Vmax	2.32	mM/s	Estimated
PGK	[5]	Keq	100	1	[49]
		K <sub>m</sub> ADPMg	0.0854	mM	Estimated, in agreement with the value of 0.2 estimated in [5]
		K <sub>m</sub> ATPMg	3.48	mM	Estimated
		K <sub>m</sub> BPG	0.0113	mM	Estimated, in agreement with the value of 0.018 estimated in [5]
		K <sub>m</sub> PGA3	2.457	mM	Estimated, in agreement with the value of 1.28 estimated in [5]
		Vmax	16.1	mM/s	Estimated
PGL	[5]	Keq	42.7	1	[5]
		K <sub>i</sub> G6P	2	mM	Estimated
		K <sub>m</sub> GL6P	0.023	mM	[5]
		K <sub>m</sub> PGN	10	mM	[5]
		Vmax	11	mM/s	Estimated
PIT	[5]	Keq	12.2	1	Estimated
		K <sub>m</sub> P <sub>per</sub>	0.025	mM	[76]
		K <sub>m</sub> P <sub>cyt</sub>	0.1	mM	Estimated
		Vmax	7.15	mM/s	Estimated
PNT	see Section 3	k	2.5	mM/s	Estimated
		Keq	0.182	1	Estimated

PPC	[5]	KdrOAA	4.35	mM	[5]
		KdrPEP	655	mM	[5]
		KdtOAA	17.9	mM	Estimated
		KdtPEP	0.0122	mM	[5]
		KefrACCOA	0.14	mM	[5]
		KefrASP	0.389	mM	Estimated
		KefrCIT	34.4	mM	[5]
		KefrCYS	0.000449	mM	Estimated
		KefrFDP	10	mM	[5]
		KefrFDPACCOA	0.0156	mM	Estimated
		KefrFUM	2.75	mM	[5]
		KefrMAL	0.23	mM	[5]
		KefrSUC	23	mM	[5]
		KeftACCOA	1.28	mM	Estimated
		KeftASP	27.5	mM	Estimated
		KeftCIT	0.522	mM	Estimated
		KeftCYS	0.977	mM	Estimated
		KeftFDP	13.2	mM	Estimated
		KeftFDPACCOA	47.8	mM	Estimated
		KeftFUM	9.76	mM	Estimated
		KeftMAL	0.737	mM	Estimated
		KeftSUC	107	mM	Estimated
		Keq	150	1	Estimated
		KmrHCO3	0.0022	mM	[5]
		KmrOAA	13	mM	Estimated
		KmrP	0.663	mM	Estimated
		KmrPEP	3.2	mM	[5]
		KmtHCO3	0.0022	mM	[5]
		KmtOAA	6.81	mM	Estimated, in agreement with the value of 6.6 estimated in [5]
		KmtP	0.285	mM	Estimated, in agreement with the range of 0.0013-2.1 estimated in [5]
		KmtPEP	5.12	mM	[5]
		L0	6.37E-06	?	[5]
		n	4	?	[5]
		Vmax	21.4	?	Estimated
PPS	[5]	alpha	38900	?	Estimated
		KdADPMg	1.28	?	[5]
		KdAMP	1480	?	[5]
		KdATPMg	0.085	?	[5]
		KdATPMgPPS	0.0549	?	[5]
		KdMg	36.9	mM	[5]
		KdP	346	?	[5]
		KdPEP	95.7	?	[5]
		KdPYR	2740	?	[5]
		KefADP	0.0283	?	[5]
		KefAKG	0.274	?	[5]
		KefATP	0.000628	?	[5]
		KefOAA	0.796	?	[5]
		Keq	2.00E+05	mmol <sup>2</sup> /l <sup>2</sup>	[5]
		KmAMP	0.000384	?	[5]
		KmATPMg	0.0549	?	[5]
		KmP	85	?	[5]
		KmPEP	20.7	?	[5]
		KmPYR	0.229	?	[5]
		Vmax	0.0164	?	Estimated
		W	10	?	[5]
PTA	[8]	Keq	0.005	1	Estimated
		KiACCOA	0.2	mM	[77]
		KiACP	0.2	mM	[77]
		KiCOA	0.029	mM	[77]
		KiP	13.5	mM	[77]
		KmACP	0.7	mM	[77]
		KmP	6.1	mM	Estimated
		Vmax	2.7	mM/s	Estimated



PTS_0	[4]	kF	12000	?	[4]
		KmPEP	0.6	mM	Estimated, in agreement with the experimental range of 0.2-0.4 [4]
		KmPYR	1	mM	Estimated, in agreement with the experimental range of 1.5-3 [4]
		kR	8000	?	[4]
PTS_1	[4]	k1	200000	l/(mmol*s)	[4]
		k2	8000	l/(mmol*s)	[4]
PTS_2	[4]	k1	61000	l/(mmol*s)	[4]
		k2	47000	l/(mmol*s)	[4]
PTS_3	[4]	k1	11000	l/(mmol*s)	[4]
		k2	4000	l/(mmol*s)	[4]
PTS_4	[4]	kF	4000	?	[4]
		KmG6P	2125	mM	Estimated
		KmGLC	0.02	mM	[4]
		kR	1.0e-05	?	[4]
PYK	[5]	KefrFDP	0.39	mM	[5]
		KeftATP	4.26	mM	[5]
		KeftSUCCOA	9.67	mM	[5]
		KirADP	0.47	mM	[5]
		KirATP	84	mM	[5]
		KirPEP	0.184	mM	[5]
		KirPYR	13.2	mM	[5]
		KirPyrATP	202.6	mM	[5]
		KitADP	0.196	mM	[5]
		KitATP	0.0448	mM	[5]
		KitPEP	0.405	mM	[5]
		KitPYR	0.294	mM	[5]
		KitPyrATP	13.26	mM	[5]
		KmrADPMg	0.358	mM	[5]
		KmrPEP	6.47E-07	mM	[5]
		KmtADPMg	0.0475	mM	[5]
		KmtPEP	0.1	mM	[5]
		L0	50	1	Estimated, in agreement with the value of 25.3 estimated in [5]
		n	4	1	[5]
		Vmax	0.747	mM/s	Estimated
RPE	[5]	Keq	1.5	1	[78]
		KmRUSP	0.872	mM	[78]
		KmX5P	0.893	mM	[78]
		Vmax	6	mM/s	Estimated
RPI	[5]	Keq	0.33	1	[78]
		KmE4P	0.67	mM	[79]
		KmR5P	3.1	mM	[80]
		KmRUSP	4.4	mM	[80]
		Vmax	8	mM/s	Estimated
S7P_E4P_TAL	[5]	kcat	100	l/(mmol*s)	Estimated, in agreement with the value of 35 estimated in [5]
		Keq	26.6	1	[5]
S7P_R5P_TKT	[5]	kcat	200	l/(mmol*s)	Estimated, in agreement with the value of 131 estimated in [5]
		Keq	0.33	1	[5]
SDH	[5]	KefFUM	0.067	mM	[81]
		KefSUC	0.0322	mM	Estimated
		Keq	2250	1	[82]
		KmFUM	1.36	mM	Estimated
		KmQ	0.00161	mM	Estimated, in agreement with the value of 0.002 estimated in [5]
		KmQH2	0.006	mM	Estimated, in agreement with the value of 0.0045 estimated in [5]
		KmSUC	0.806	mM	Estimated
		Vmax	1.56	mM/s	Estimated

SK	[5]	Keq	1.16	1	Estimated
		KmADP	0.00868	mM	Estimated
		KmATP	0.102	mM	Estimated, in agreement with the value of 0.07 estimated in [5]
		KmCOA	0.255	mM	Estimated
		KmP	0.915	mM	Estimated, in agreement with the value of 0.7 estimated in [5]
		KmSUC	0.8	mM	Estimated
		KmSUCCOA	0.0085	mM	Estimated
		Vmax	76.8	mM/s	Estimated
SQR	see Section 3	Keq	0.94	1	Estimated
		Vmax	3.42	mM/s	Estimated
TPI	[5]	Keq	0.27	1	Estimated
		KmDAP	0.01	mM	[5]
		KmGAP	1.89	mM	Estimated
		Vmax	24.2	mM/s	Estimated
XSP_GAP_TKT	[5]	kcat	40	l/(mmol*s)	Estimated
		Keq	1	1	[5]
ZWF	[5]	KdG6P	0.192	mM	[5]
		KdGL6P	0.02	mM	[5]
		Keq	6.00E+10	1	[5]
		KmG6P	0.119	mM	Estimated, in agreement with the value of 0.156 estimated in [5]
		KmGL6P	0.329	mM	Estimated, in agreement with the value of 0.122 estimated in [5]
		KmNADP	0.0274	mM	[5]
		KmNADPH	0.0168	mM	[5]
		Vmax	0.266	mM/s	Estimated

## 10. Model validation

We first assessed the stability of the model by checking the stability of the Jacobian matrix under two different conditions, namely: the reference state condition (glucose limitation at a growth rate of  $0.1 \text{ h}^{-1}$ ), and glucose excess condition (by fixing extracellular glucose concentration at 10 mM). In both situations the model demonstrates stable steady states with strictly negative Jacobian eigenvalues.

Then, we evaluated the metabolic control analysis results by comparing the predicted flux control to observations. The model predictions were in line with the literature, as detailed in the manuscript.

Finally, we assessed the ability of the model to identify conserved functional couplings that are independent of gene expression. As detailed in the manuscript, we collected 778 flux data from some 266 experiments, where different *E. coli* K-12 wild-type and mutant strains were cultivated under different conditions (in batch, chemostat, or shake flask). It is important to note that these data were not used to calibrate the model, they were used only for validation purpose. This data set is very different from the data set used for parameter estimation, which were from a single *E. coli* strain grown in a unique condition. The 778 data used for validation (growth rates, glucose uptake rates, biomass yields, oxygen uptake rates, and fluxes through the TCA cycle) are provided in Dataset S2. The simulations and measurements are in excellent agreement (Figures 4, 5, and 6 of the manuscript), which indicates the model yielded fairly accurate predictions of the metabolic states that can be expressed by *E. coli* growing on glucose. All the

experimental data support the model-driven hypothesis that metabolic regulation is sufficient to maintain the tight coordination between these key metabolic processes.

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