Tut 11: More Hierarchical Clustering

May/June 2022

Hierarchical Clustering

1. (May 2020 Final Q3(b)) Given an appropriate example to explain why the Minkowski distance

$$M(oldsymbol{x},oldsymbol{y}) = \left(\sum_{i=1}^p |x_i - y_i|^r
ight)^{rac{1}{r}}, \quad oldsymbol{x}, \,\,\, oldsymbol{y} \in \mathbb{R}^p$$

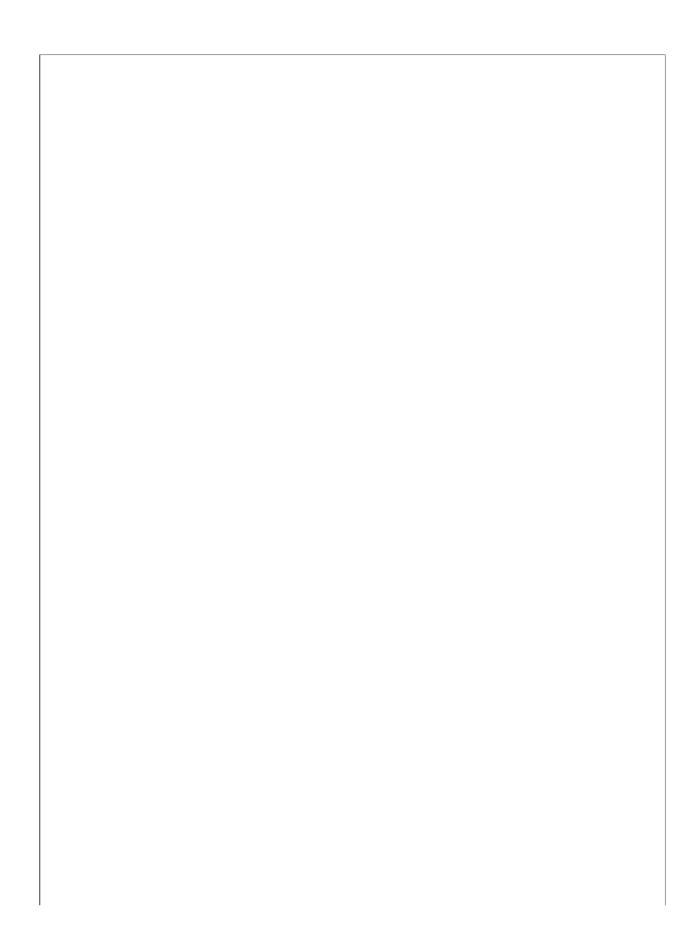
will no longer be a distance function when $r = \frac{1}{2}$. (2 marks)

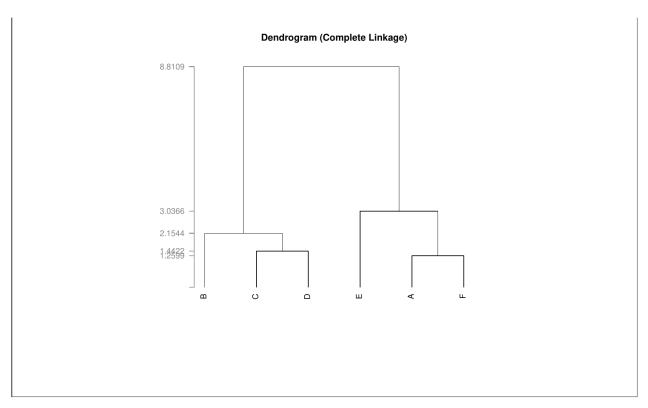
2. (May 2020 Final Q3(c)) Group the observations in Table 3.1 using hierarchical clustering and the **Minkowski distance** with r=3 (refer to part (b) for the definition of Minkowski distance) and **complete linkage** and draw the dendrogram formed by the hierarchical clustering.

Table 3.1: Unlabelled data.

| Obs | x_1 | x_2 | x_3 |
|----------|-------|-------|-------|
| A | 1 | 3 | 2 |
| В | 5 | 7 | 9 |
| С | 6 | 9 | 8 |
| D | 7 | 8 | 9 |
| ${ m E}$ | 2 | 3 | 5 |
| F | 1 | 4 | 3 |

(4 marks)



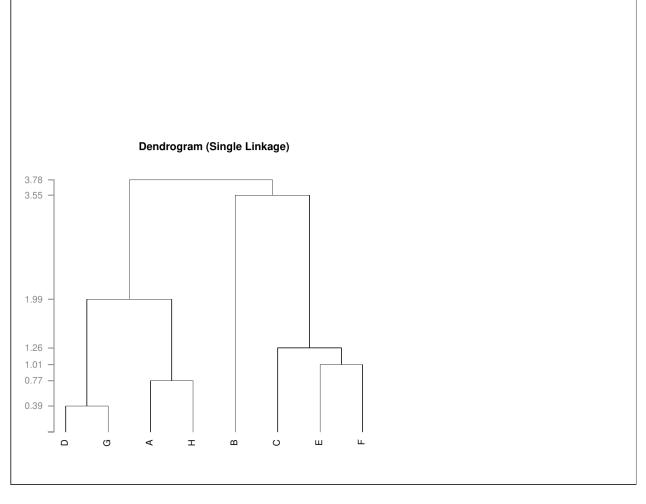


3. (Jan 2021 Final Q4(a). Hand calculation is possible but Excel/R is recommended) Group the observations in Table 4.1 using hierarchical clustering and the **Manhattan distance** and **single linkage** and draw the dendrogram formed by the hierarchical clustering.

Table 4.1: Unlabelled data.

| Obs | x_1 | x_2 |
|--------------|-------|-------|
| A | -2.68 | -2.02 |
| В | 3.06 | -0.83 |
| \mathbf{C} | 1.91 | 1.57 |
| D | -1.06 | -0.88 |
| \mathbf{E} | 0.49 | 2.42 |
| \mathbf{F} | 0.83 | 1.75 |
| G | -0.71 | -0.84 |
| Н | -2.01 | -1.92 |

(5 marks)



4. (Jan 2022 Final Q5(b)) Given the three-dimensional points in Table 5.2,

Table 5.2: Three-dimensional points.

| Label | x_1 | x_2 | x_3 |
|-------|-------|-------|-------|
| P_1 | 3.3 | 4.4 | 2.5 |
| P_2 | 2.4 | 3.1 | 2.1 |
| P_3 | 0.1 | 1.9 | 1.1 |
| P_4 | 0.3 | 2.4 | 1.5 |
| P_5 | -0.6 | 1.1 | 1.1 |
| P_6 | -2.9 | -0.1 | 0.1 |
| P_7 | 4.3 | 6.4 | 5.5 |
| P_8 | 3.4 | 5.1 | 5.1 |
| P_9 | 1.1 | 3.9 | 4.1 |

Use the k-means clustering method with **Manhattan distance** to cluster the given points into k = 3 clusters by using P_5 , P_4 , P_7 as the initial clusters, find the **stable cluster centres**. (8 marks)