worksheet_14

March 23, 2024

1 Worksheet 14

Name: **Bowen Li** UID: **U79057147**

1.0.1 Topics

• Naive Bayes

• Model Evaluation

1.0.2 Naive Bayes

Attribute A	Attribute B	Attribute C	Class	
Yes	Single	High	No	
No	Married	$\overline{\mathrm{Mid}}$	No	
No	Single	Low	No	
Yes	Married	High	No	
No	Divorced	$\overline{\mathrm{Mid}}$	Yes	
No	Married	Low	No	
Yes	Divorced	High	No	
No	Single	$\overline{\mathrm{Mid}}$	Yes	
No	Married	Low	No	
No	Single	Mid	Yes	

a) Compute the following probabilities:

- P(Attribute A = Yes | Class = No)
- P(Attribute B = Divorced | Class = Yes)
- $P(Attribute C = High \mid Class = No)$
- $P(Attribute C = Mid \mid Class = Yes)$

$$P(A = \text{Yes} \mid \text{Class} = \text{No}) = \frac{P(A = \text{Yes, Class} = \text{No})}{P(\text{Class} = \text{No})} = \frac{3/10}{7/10} = \boxed{\frac{3}{7}}$$

$$P(B = \text{Divorced} \mid \text{Class} = \text{Yes}) = \frac{P(B = \text{Divorced}, \, \text{Class} = \text{Yes})}{P(\text{Class} = \text{Yes})} = \frac{1/10}{3/10} = \boxed{\frac{1}{3}}$$

$$P(C = \text{High} \mid \text{Class} = \text{No}) = \frac{P(C = \text{High}, \, \text{Class} = \text{No})}{P(\text{Class} = \text{No})} = \frac{3/10}{7/10} = \boxed{\frac{3}{7}}$$

$$P(C = \text{Mid} \mid \text{Class} = \text{Yes}) = \frac{P(C = \text{Mid}, \text{Class} = \text{Yes})}{P(\text{Class} = \text{Yes})} = \frac{3/10}{3/10} = \boxed{1}$$

- b) Classify the following unseen records:
- (Yes, Married, Mid)
- (No, Divorced, High)
- (No, Single, High)
- (No, Divorced, Low)
- (Yes, Married, Mid)

 $P(\text{Class} = \text{Yes}|\text{Yes}, \text{Married}, \text{Mid}) \propto P(\text{Yes}, \text{Married}, \text{Mid}|\text{Class} = \text{Yes}) = P(\text{Yes}|\text{Class} = \text{Yes})P(\text{Married}|\text{Class})$

$$= 0 \cdot 0 \cdot 1 = 0$$

 $P(\text{Class} = \text{No}|\text{Yes}, \text{Married}, \text{Mid}) \propto P(\text{Yes}, \text{Married}, \text{Mid}|\text{Class} = \text{No}) = P(\text{Yes}|\text{Class} = \text{No})P(\text{Married}|\text{Class})$

$$=\frac{3}{7}\cdot\frac{4}{7}\cdot\frac{1}{7}>0$$

 $P(\text{Class} = \text{Yes}|\text{Yes}, \text{Married}, \text{Mid}) < P(\text{Class} = \text{No}|\text{Yes}, \text{Married}, \text{Mid}); \text{ so the class is } \boxed{\text{No.}}$

• (No, Divorced, High)

 $P(\text{Class} = \text{Yes}|\text{No, Divorced, High}) \propto P(\text{No, Divorced, High}|\text{Class} = \text{Yes}) = P(\text{No}|\text{Class} = \text{Yes})P(\text{Divorced}|\text{Class}) = P(\text{No}|\text{Class} = \text{Yes})P(\text{Divorced}|\text{Class}) = P(\text{No}|\text{Class} = \text{Yes})P(\text{Divorced}|\text{Class}) = P(\text{No}|\text{Class}) = P(\text{No}|\text{Class})$

$$=1\cdot\frac{1}{3}\cdot 0=0$$

 $P(\text{Class} = \text{No}|\text{No, Divorced, High}) \propto P(\text{No, Divorced, High}|\text{Class} = \text{No}) = P(\text{No}|\text{Class} = \text{No})P(\text{Divorced}|\text{Class}) = P(\text{No}|\text{Class}) = P$

$$=\frac{4}{7}\cdot\frac{1}{7}\cdot\frac{3}{7}>0$$

 $P(\text{Class} = \text{Yes}|\text{No, Divorced, High}) < P(\text{Class} = \text{No}|\text{No, Divorced, High}); so the class is No.}$

• (No, Single, High)

 $P(\text{Class} = \text{Yes}|\text{No, Single, High}) \propto P(\text{No, Single, High}|\text{Class} = \text{Yes}) = P(\text{No}|\text{Class} = \text{Yes})P(\text{Single}|\text{Class} = \text{Yes})P(\text{Single}|$

$$=1\cdot\frac{2}{3}\cdot 0=0$$

 $P(\text{Class} = \text{No}|\text{No, Single, High}) \propto P(\text{No, Single, High}|\text{Class} = \text{No}) = P(\text{No}|\text{Class} = \text{No})P(\text{Single}|\text{Class} = \text{No})P(\text{Single}|\text{Class}$

$$=\frac{4}{7}\cdot\frac{2}{7}\cdot\frac{3}{7}>0$$

P(Class = Yes|No, Single, High) < P(Class = No|No, Single, High); so the class is $\boxed{\text{No.}}$

• (No, Divorced, Low)

$$=1\cdot\frac{1}{3}\cdot0=0$$

$$P(\text{Class}=\text{No}|\text{No, Divorced, Low})\propto P(\text{No, Divorced, Low}|\text{Class}=\text{No})=P(\text{No}|\text{Class}=\text{No})P(\text{Divorced}|\text{Class}=\frac{4}{7}\cdot\frac{1}{7}\cdot\frac{3}{7}>0$$

 $P(\text{Class} = \text{Yes}|\text{No, Divorced, Low}) \propto P(\text{No, Divorced, Low}|\text{Class} = \text{Yes}) = P(\text{No}|\text{Class} = \text{Yes})P(\text{Divorced}|\text{Class})$

 $P(\text{Class} = \text{Yes}|\text{No, Divorced, Low}) < P(\text{Class} = \text{No}|\text{No, Divorced, Low}); \text{ so the class is } \boxed{\text{No.}}$

1.0.3 Model Evaluation

a) Write a function to generate the confusion matrix for a list of actual classes and a list of predicted classes

```
[1]: actual_class = ["Yes", "No", "No", "Yes", "No", "No", "Yes", "No", "No", "No"]
                  predicted_class = ["Yes", "No", "Yes", "No", "No", "No", "Yes", "
                       ∽"No"]
                  def confusion matrix(actual, predicted):
                                 n = len(actual)
                                 if n != len(predicted):
                                                 raise ValueError("Predictions don't match label length.")
                                  confusion_mat = [[0,0],[0,0]]
                                 for i in range(n):
                                                 if actual_class[i] == "Yes" and predicted_class[i] == "Yes":
                                                                 confusion_mat[0][0] += 1
                                                 elif actual_class[i] == "Yes" and predicted_class[i] == "No":
                                                                confusion_mat[0][1] += 1
                                                 elif actual_class[i] == "No" and predicted_class[i] == "Yes":
                                                                 confusion mat[1][0] += 1
                                                 else:
                                                                confusion mat[1][1] += 1
                                 return confusion_mat
                  print(confusion_matrix(actual_class, predicted_class))
```

[[2, 1], [3, 4]]

b) Assume you have the following Cost Matrix:

	predicted = Y	predicted = N
actual = Y	-1	5
actual = N	10	0

What is the cost of the above classification?

$$2(-1) + 1(5) + 3(10) + 4(0) = \boxed{33}$$

c) Write a function that takes in the actual values, the predictions, and a cost matrix and outputs a cost. Test it on the above example.

33

- d) Implement functions for the following:
- accuracy
- precision
- recall
- f-measure

and apply them to the above example.

```
[3]: def accuracy(actual, predicted):
    confusion_mat = confusion_matrix(actual, predicted)
    num_correct = 0
    for i in range(len(confusion_mat)):
        num_correct += confusion_mat[i][i]

    total = 0
    for row in confusion_mat:
        total += sum(row)
```

```
return num_correct / total

print("Accuracy:", accuracy(actual_class, predicted_class))

def precision(actual, predicted):
    confusion_mat = confusion_matrix(actual, predicted)
    return confusion_mat[0][0] / (confusion_mat[0][0] + confusion_mat[1][0])

print("Precision:", precision(actual_class, predicted_class))

def recall(actual, predicted):
    confusion_mat = confusion_matrix(actual, predicted)
    return confusion_mat[0][0] / (confusion_mat[0][0] + confusion_mat[0][1])

print("Recall:", recall(actual_class, predicted_class))

def f_measure(actual, predicted):
    p = precision(actual, predicted)
    r = recall(actual, predicted)
    return 2 * p * r / (p + r)

print("F-measure:", f_measure(actual_class, predicted_class))
```

Accuracy: 0.6 Precision: 0.4

F-measure: 0.5

1.1 Challenge (Midterm prep part 2)

In this exercise you will update your submission to the titanic competition.

- a) First let's add new numerical features / columns to the datasets that might be related to the survival of individuals.
- has_cabin should have a value of 0 if the cabin feature is nan and 1 otherwise
- family_members should have the total number of family members (by combining SibSp and Parch)
- title_type: from the title extracted from the name, we will categorize it into 2 types: common for titles that many passengers have, rare for titles that few passengers have. Map common to 1 and rare to 0. Describe what threshold you used to define common and rare titles and how you found it.
- fare_type: using Kmeans clustering on the fare column, find an appropriate number of clusters / groups of similar fares. Using the clusters you created, fare_price should be an ordinal variable that represents the expensiveness of the fare. For example if you split fare into 3 clusters (0 15, 15 40, and 40+) then the fare_price value should be 0 for fare values 0 15, 1 for 15 40, and 2 for 40+.
- Create an addition two numerical features of your invention that you think could be relevant

to the survival of individuals.

Note: The features must be numerical because the sklearn DecisionTreeClassifier can only take on numerical features.

Kaggle Username: lib250

```
1.1.1 Get Imports and Load Data
[4]: from sklearn.preprocessing import StandardScaler, MinMaxScaler
     from sklearn.model_selection import LeaveOneOut, cross_val_score
     from sklearn.decomposition import PCA
     from sklearn.pipeline import make_pipeline
     from sklearn.cluster import KMeans
     from sklearn.tree import DecisionTreeClassifier
     from sklearn.naive_bayes import GaussianNB
     from sklearn.neighbors import KNeighborsClassifier
     from sklearn.ensemble import VotingClassifier, HistGradientBoostingClassifier
     import numpy as np
     import pandas as pd
     import matplotlib.pyplot as plt
[5]: train_df = pd.read_csv('train.csv')
     test_df = pd.read_csv('test.csv')
     print(f"Training Set: {train_df.shape}")
     print(f"Testing Set: {test_df.shape}")
    Training Set: (891, 12)
```

Testing Set: (418, 11)

[6]: train_df.head()

```
[6]:
         PassengerId
                        Survived
                                    Pclass
     0
                     1
                                 0
                                          3
     1
                     2
                                 1
                                          1
     2
                     3
                                 1
                                          3
     3
                     4
                                 1
                                          1
     4
                     5
                                 0
                                          3
```

```
Name
                                                          Sex
                                                                Age SibSp \
0
                             Braund, Mr. Owen Harris
                                                         male
                                                               22.0
                                                                         1
  Cumings, Mrs. John Bradley (Florence Briggs Th... female 38.0
                                                                       1
1
2
                              Heikkinen, Miss. Laina
                                                                         0
                                                       female
                                                               26.0
3
        Futrelle, Mrs. Jacques Heath (Lily May Peel)
                                                       female 35.0
                                                                         1
4
                            Allen, Mr. William Henry
                                                         male 35.0
                                                                         0
```

	Parch	Ticket	Fare	${\tt Cabin}$	Embarked
0	0	A/5 21171	7.2500	NaN	S
1	0	PC 17599	71.2833	C85	C
2	0	STON/02. 3101282	7.9250	NaN	S
3	0	113803	53.1000	C123	S
4	0	373450	8.0500	NaN	S

1.1.2 Extract Features

Here we extract the numerical has_cabin, family_members, title_type, and fare_type features as described in the instructions.

We additionally extract is_child as an indicator where 1 indicates a person 18 or under and 0 indicates an adult. This could be useful since children have priority in terms of lifeboat access. We extract is_woman for the same reason.

We also enumerate the deck as the first letter of the cabin number indicates where physically on the ship the person's cabin is located. Spatial information could be useful as proximity to danger and safe zones on the ship could affect survival rate.

Extract Title Here, we get all the titles in the dataset and count how frequently they appear. We consider the 3 most frequent titles, Mr., Miss. and Mrs. to be common titles while the rest Master. onwards to be uncommon, since there's a big dip in frequency after Mrs..

```
[7]: def extract_title(name):
    strs = name.split()
    for s in strs:
        if '.' in s:
            return s

titles = train_df["Name"].copy().apply(extract_title)
```

```
[8]: titles.value_counts()
```

```
[8]: Mr.
                      517
     Miss.
                      182
     Mrs.
                      125
     Master.
                       40
     Dr.
                        7
     Rev.
                        6
                        2
     Mlle.
     Major.
                        2
                        2
      Col.
     Countess.
                        1
      Capt.
                        1
     Ms.
                        1
     Sir.
                        1
     Lady.
                        1
     {\tt Mme.}
                        1
```

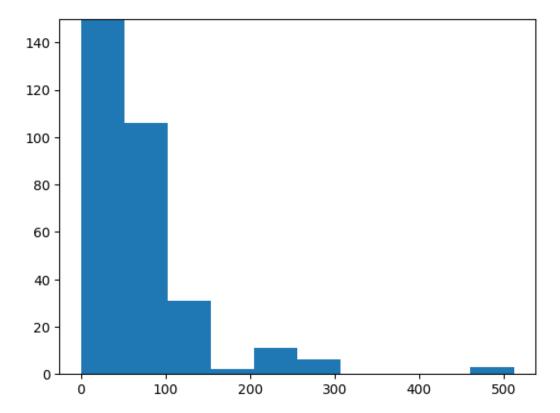
Don. 1
Jonkheer. 1
Name: Name, dtype: int64

```
[9]: common_titles = ['Mr.', 'Miss.', 'Mrs.', 'Ms.']
[10]: def has_common_title(name):
    title = extract_title(name)
    if title in common_titles:
        return 1
    return 0
```

Extract Fare Type Here we perform K-means clustering to bucket the fares. We first plot a histogram of all the fares and can see that they roughly concentrate into 3 groups. We have a local peak at around 0-50, 200-250, and the last bin at around 500 (The value of the first bin is much larger than the bounds of the graph, we limit the y-axis to better see the smaller values).

As such we can use K-means to collect the fares into 3 buckets, potentially representing a lower, middle, and upper economic class.

```
[11]: plt.hist(train_df["Fare"])
    plt.ylim(0,150)
    plt.show()
```



```
[12]: fare_array = train_df["Fare"].to_numpy().reshape((-1, 1))
      fare kmeans = KMeans(n_clusters=3, random_state=0, n_init="auto").

→fit(fare_array)
[13]: fare_kmeans.cluster_centers_
[13]: array([[ 82.92256875],
             [279.308545],
             [ 15.3602868 ]])
[14]: | sorted_idx = np.argsort(fare_kmeans.cluster_centers_.flatten())
      ordered fare centers = np.zeros(3, dtype=int)
      ordered_fare_centers[sorted_idx] = np.arange(3)
      ordered fare centers
[14]: array([1, 2, 0])
     Process Data and Extract Features
[15]: def extract_features(df):
        y = None
        if "Survived" in df.columns:
          y = df["Survived"].to numpy().copy()
        df["Age"].fillna(df["Age"].mean(), inplace=True)
        df["Fare"].fillna(df["Fare"].mean(), inplace=True)
        df["is_child"] = (df["Age"] < 19).astype(int)</pre>
        df["is_woman"] = (df["Sex"].str.lower() == "female").astype(int)
        df["has_cabin"] = df["Cabin"].notna().astype(int)
        df["deck"] = (df["Cabin"].str[:1])
        df["deck"].fillna('N', inplace=True)
        df["family_members"] = df["SibSp"] + df["Parch"]
        df["title_type"] = df["Name"].apply(has_common_title)
        deck to num = {'N': 0, 'A': 1, 'B': 2, 'C': 3, 'D': 4, 'E': 5, 'F': 6, 'G': 11
       ⇔7, 'T': 8}
        df["deck"] = df["deck"].apply(lambda letter: deck to num[letter])
        fare_np = df["Fare"].to_numpy().reshape((-1, 1))
        fare_buckets_np = fare_kmeans.predict(fare_np)
        df["fare_type"] = pd.Series(fare_buckets_np).apply(lambda c:__
       ⇔ordered_fare_centers[c])
```

```
[16]: X_train, y_train = extract_features(train_df)
X_test, y_test = extract_features(test_df)
```

1.1.3 Decision Tree

b) Using a method covered in class, tune the parameters of a decision tree model on the titanic dataset (containing all numerical features including the ones you added above). Evaluate this model locally and report it's performance.

Note: make sure you are not tuning your parameters on the same dataset you are using to evaluate the model. Also explain how you know you are not overfitting to the training set.

The model is likely not overfitting to the training set as it performs relatively well on leave-one-out cross validation runs. We also select the minimum max_depth which gets us decent performance, which reduces the chances of overfitting.

```
[17]: def cross_val_acc(model, X, y):
    splits = LeaveOneOut()

    results = cross_val_score(model, X, y, cv=splits)
    return results.sum() / results.shape[0]

dt_test = DecisionTreeClassifier(random_state=0)
    cross_val_acc(dt_test, X_train, y_train)
```

[17]: 0.81818181818182

```
[18]: upper_max_depth = 20
lower_max_depth = 5

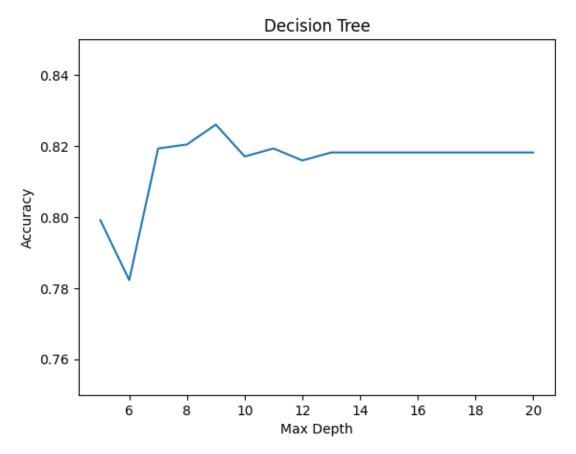
max_depth_vals = np.arange(lower_max_depth, upper_max_depth+1)

def apply_max_depth_DT(max_depth):
    model = DecisionTreeClassifier(random_state=0, max_depth=max_depth)
    return cross_val_acc(model, X_train, y_train)

vec_apply_depth = np.vectorize(apply_max_depth_DT)
```

```
[19]: md_acc = vec_apply_depth(max_depth_vals)
```

```
[20]: plt.plot(max_depth_vals, md_acc)
   plt.ylim(0.75, 0.85)
   plt.title("Decision Tree")
   plt.ylabel("Accuracy")
   plt.xlabel("Max Depth")
   plt.show()
```



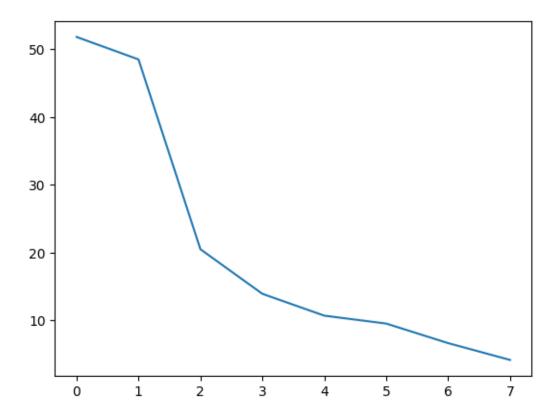
1.1.4 PCA and Naive Bayes

c) Try reducing the dimension of the dataset and create a Naive Bayes model. Evaluate this model.

We'll first check the singular values to get a sense of how the information gain falls off with each dimension. It seems to taper off at around 3-4 components.

```
[21]: pca_full = PCA(n_components=8)
    pca_full.fit(X_train)

plt.plot(pca_full.singular_values_)
    plt.show()
```



[22]: dim_reduce = PCA(n_components=4)

We'll initialize the Naive Bayes model with the priors since historically the Titanic had a recorded 37% survival rate.

```
[23]: naive_bayes = GaussianNB(priors=[.63,.37])
cross_val_acc(naive_bayes, X_train, y_train)
```

[23]: 0.7306397306397306

```
[24]: pca_nb = make_pipeline(dim_reduce, naive_bayes)
cross_val_acc(pca_nb, X_train, y_train)
```

[24]: 0.7755331088664422

Next we test if scaling helps, which it doesn't seem to.

```
[25]: scaler = StandardScaler()
standardized_pca_nb = make_pipeline(scaler, dim_reduce, naive_bayes)
cross_val_acc(standardized_pca_nb, X_train, y_train)
```

[25]: 0.7138047138047138

Visualize how Naive Bayes performs as we change the number of PCA components.

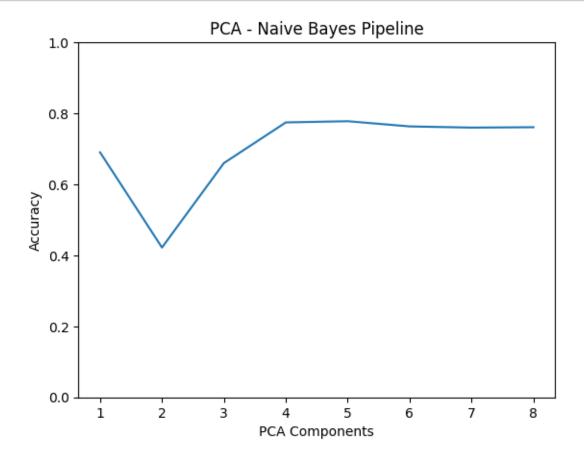
```
[26]: test_n_components = np.arange(1, 9)

def apply_pca_n(num_components):
    pca = PCA(n_components=num_components)
    model = make_pipeline(pca, GaussianNB(priors=[.37,.63]))
    return cross_val_acc(model, X_train, y_train)

vec_pca_n = np.vectorize(apply_pca_n)

[27]: pca_n_accuracies = vec_pca_n(test_n_components)

[28]: plt.plot(test_n_components, pca_n_accuracies)
    plt.ylim(0, 1)
    plt.title("PCA - Naive Bayes Pipeline")
    plt.ylabel("Accuracy")
    plt.xlabel("PCA Components")
    plt.show()
```

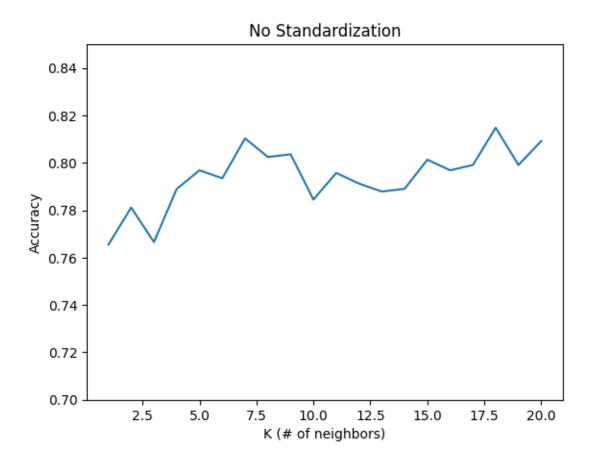


1.1.5 Ensemble

d) Create an ensemble classifier using a combination of KNN, Decision Trees, and Naive Bayes models. Evaluate this classifier.

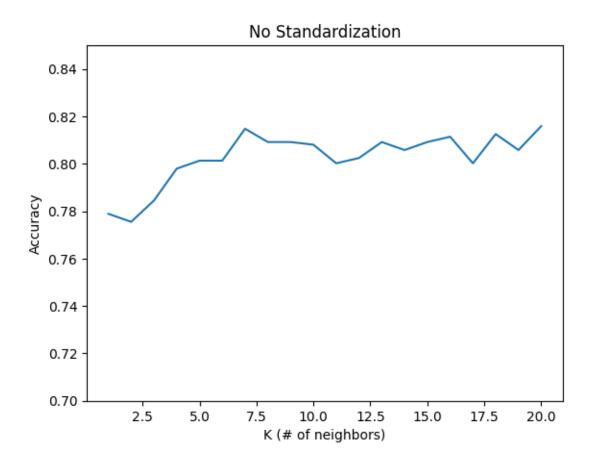
First let's search for the best KNN for this feature set. We test different values of k and different ways to standardize the features of the data.

```
[29]: def apply_knn_no_stand(k):
       model = KNeighborsClassifier(n_neighbors=k)
        return cross_val_acc(model, X_train, y_train)
      def apply_knn_stand(k):
        knn = KNeighborsClassifier(n_neighbors=k)
        model = make_pipeline(StandardScaler(), knn)
        return cross_val_acc(model, X_train, y_train)
      def apply_knn_minmax(k):
       knn = KNeighborsClassifier(n neighbors=k)
       model = make_pipeline(MinMaxScaler(), knn)
        return cross_val_acc(model, X_train, y_train)
      vec_knn_no_stand = np.vectorize(apply_knn_no_stand)
      vec_knn_stand = np.vectorize(apply_knn_stand)
      vec_knn_minmax = np.vectorize(apply_knn_minmax)
      k_vals = np.arange(1, 21)
[30]: knn_acc_none = vec_knn_no_stand(k_vals)
[31]: plt.plot(k_vals, knn_acc_none)
      plt.ylim(0.7, 0.85)
      plt.title("No Standardization")
      plt.ylabel("Accuracy")
      plt.xlabel("K (# of neighbors)")
      plt.show()
```



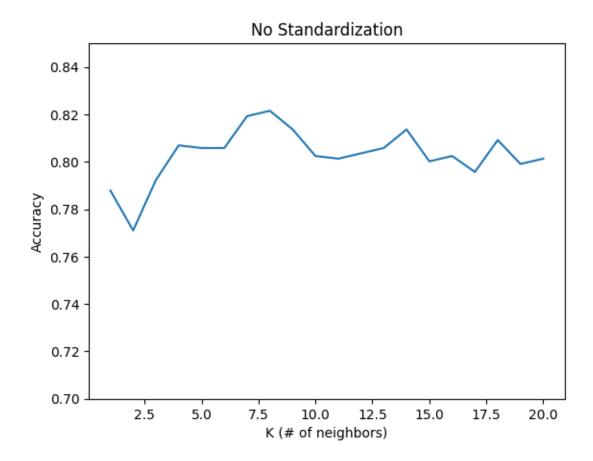
```
[32]: knn_acc_stand = vec_knn_stand(k_vals)

[33]: plt.plot(k_vals, knn_acc_stand)
    plt.ylim(0.7, 0.85)
    plt.title("No Standardization")
    plt.ylabel("Accuracy")
    plt.xlabel("K (# of neighbors)")
    plt.show()
```



```
[34]: knn_acc_minmax = vec_knn_minmax(k_vals)

[35]: plt.plot(k_vals, knn_acc_minmax)
    plt.ylim(0.7, 0.85)
    plt.title("No Standardization")
    plt.ylabel("Accuracy")
    plt.xlabel("K (# of neighbors)")
    plt.show()
```



Optimal here is 8 neighbors with MinMax standardization.

Check if PCA can help (doesn't seem like it).

```
[36]: 0.7946127946127947
```

```
[37]: best_dt = DecisionTreeClassifier(random_state=0, max_depth=9)
best_nb = make_pipeline(PCA(n_components=4), GaussianNB(priors=[.63, .37]))
best_knn = make_pipeline(MinMaxScaler(), KNeighborsClassifier(n_neighbors=8))
ensemble_model = VotingClassifier(
    estimators=[('dt', best_dt), ('nb', best_nb), ('knn', best_knn)],
    voting='hard'
)
```

```
[38]: for model, name in zip([best_dt, best_nb, best_knn, ensemble_model], ['Decision_\]

Tree', 'Naive Bayes', 'KNN', 'Ensemble']):

scores = cross_val_acc(model, X_train, y_train)

print("Accuracy: %0.2f (+/- %0.2f) [%s]" % (scores.mean(), scores.std(), \]

name))
```

```
Accuracy: 0.83 (+/- 0.00) [Decision Tree]
Accuracy: 0.78 (+/- 0.00) [Naive Bayes]
Accuracy: 0.82 (+/- 0.00) [KNN]
Accuracy: 0.82 (+/- 0.00) [Ensemble]
```

e) Update your kaggle submission using the best model you created (best model means the one that performed the best on your local evaluation)

It seems the best model was still the decision tree, so we'll go with that.

```
[39]: best_model = DecisionTreeClassifier(random_state=0, max_depth=9)
best_model.fit(X_train, y_train)
```

[39]: DecisionTreeClassifier(max_depth=9, random_state=0)

```
[40]: predictions = best_model.predict(X_test)
```

```
[41]: submission_df = test_df[["PassengerId"]].copy()
submission_df["Survived"] = predictions
submission_df
```

```
[41]:
                           Survived
            PassengerId
                     892
      1
                     893
                                   0
      2
                     894
                                   0
      3
                     895
                                   0
      4
                     896
                                   0
                                   0
      413
                    1305
      414
                    1306
                                   1
      415
                    1307
                                   0
      416
                    1308
                                   0
      417
                    1309
                                   1
```

[418 rows x 2 columns]

```
[42]: submission_df.to_csv('titanic_submission.csv', index=False)
```

The predictions scored 0.76315 on Kaggle under the username lib250.

1.2 Some useful code for the midterm

```
[43]: import seaborn as sns
      from sklearn.svm import SVC
      import matplotlib.pyplot as plt
      from sklearn.decomposition import PCA
      from sklearn.pipeline import make_pipeline
      from sklearn.metrics import confusion_matrix, accuracy_score
      from sklearn.datasets import fetch_lfw_people
      from sklearn.ensemble import BaggingClassifier
      from sklearn.model_selection import GridSearchCV, train_test_split
      sns.set()
      # Get face data
      faces = fetch_lfw_people(min_faces_per_person=60)
      # plot face data
      fig, ax = plt.subplots(3, 5)
      for i, axi in enumerate(ax.flat):
          axi.imshow(faces.images[i], cmap='bone')
          axi.set(xticks=[], yticks=[],
                  xlabel=faces.target_names[faces.target[i]])
      plt.show()
      # split train test set
      Xtrain, Xtest, ytrain, ytest = train_test_split(faces.data, faces.target,_
       →random_state=42)
      pca = PCA(n_components=150, whiten=True)
      svc = SVC(kernel='rbf', class weight='balanced')
      svcpca = make_pipeline(pca, svc)
      # Tune model to find best values of C and gamma using cross validation
      param_grid = {'svc__C': [1, 5, 10, 50],
                    'svc_gamma': [0.0001, 0.0005, 0.001, 0.005]}
      kfold = 10
      grid = GridSearchCV(svcpca, param_grid, cv=kfold)
      grid.fit(Xtrain, ytrain)
      print(grid.best_params_)
      # use the best params explicitly here
      pca = PCA(n_components=150, whiten=True)
      svc = SVC(kernel='rbf', class_weight='balanced', C=10, gamma=0.005)
      svcpca = make pipeline(pca, svc)
```

```
model = BaggingClassifier(svcpca, n_estimators=100).fit(Xtrain, ytrain)
yfit = model.predict(Xtest)
fig, ax = plt.subplots(6, 6)
for i, axi in enumerate(ax.flat):
   axi.imshow(Xtest[i].reshape(62, 47), cmap='bone')
   axi.set(xticks=[], yticks=[])
   axi.set_ylabel(faces.target_names[yfit[i]].split()[-1],
                   color='black' if yfit[i] == ytest[i] else 'red')
fig.suptitle('Predicted Names; Incorrect Labels in Red', size=14)
plt.show()
mat = confusion_matrix(ytest, yfit)
sns.heatmap(mat.T, square=True, annot=True, fmt='d', cbar=False,
            xticklabels=faces.target_names,
            yticklabels=faces.target_names)
plt.xlabel('true label')
plt.ylabel('predicted label')
plt.show()
print("Accuracy = ", accuracy_score(ytest, yfit))
```



eorge W Blackhorge W Buskhorge W Buskhorge W Buskhorge W Bus

Predicted Names; Incorrect Labels in Red

Bush	Bush	Bush	Koizumi	Koizumi	Powell
Bush	Bush	Bush	Bush	Bush	Bush
Powell	a Bush	Bush	Powell	Blair	Chave&umsfeld Bush
Bush	umsfelc	Blair	Bush	Chavez	Chave ⊉
Sharon	Bush Rumsfeld Bush	Koizumi	Blair	Bush	Bush
Sharon	Coizumi	Bush	Bush	Bush	Bush

Ariel Sharon	9	0	0	0	0	0	0	0
Colin Powell	1	59	2	6	0	1	0	0
Donald Rumsfeld	0	1	19	0	0	0	0	0
George W Bush	5	7	10	120	5	5	2	8
Gerhard Schroeder	0	0	0	0	16	0	0	0
Hugo Chavez	0	0	0	0	0	13	0	0
Junichiro Koizumi	0	0	0	0	0	0	10	0
Tony Blair	0	1	0	0	2	1	0	34
	Ariel Sharon	Colin Powell	Donald Rumsfeld	an George W Bush	ਨੂੰ Gerhard Schroeder	Hugo Chavez	Junichiro Koizumi	Tony Blair
	Colin Powell Donald Rumsfeld George W Bush Gerhard Schroeder Hugo Chavez Junichiro Koizumi	Colin Powell Donald Rumsfeld George W Bush Gerhard Schroeder Hugo Chavez Junichiro Koizumi Tony Blair 0	Colin Powell 1 59 Donald Rumsfeld 0 1 George W Bush 5 7 Gerhard Schroeder 0 0 Hugo Chavez 0 0 Junichiro Koizumi 0 0 Tony Blair 0 1	Colin Powell 1 59 2 Donald Rumsfeld 0 1 19 George W Bush 5 7 10 Gerhard Schroeder 0 0 0 Hugo Chavez 0 0 0 Junichiro Koizumi 0 0 0 Tony Blair 0 1 0	Colin Powell 1 59 2 6 Donald Rumsfeld 0 1 19 0 George W Bush 5 7 10 120 Gerhard Schroeder 0 0 0 0 Hugo Chavez 0 0 0 0 Junichiro Koizumi 0 0 0 0 Tony Blair 0 1 0 0 W Bray Bray Bray Bray Bray Bray Bray Bray	Colin Powell 1 59 2 6 0 Donald Rumsfeld 0 1 19 0 0 George W Bush 5 7 10 120 5 Gerhard Schroeder 0 0 0 0 16 Hugo Chavez 0 0 0 0 0 Junichiro Koizumi 0 0 0 0 0 Tony Blair 0 1 0 0 2	Colin Powell 1 59 2 6 0 1 Donald Rumsfeld 0 1 19 0 0 0 George W Bush 5 7 10 120 5 5 Gerhard Schroeder 0 0 0 0 16 0 Hugo Chavez 0 0 0 0 0 13 Junichiro Koizumi 0 1 0 0 2 1 Tony Blair 0 1 0 0 2 1 Hndo Chavez O D D D D D D D D D D D D D D D D D D	Colin Powell 1 59 2 6 0 1 0 Donald Rumsfeld 0 1 19 0 0 0 0 George W Bush 5 7 10 120 5 5 2 Gerhard Schroeder 0 0 0 0 0 16 0 0 Hugo Chavez 0 0 0 0 0 13 0 Junichiro Koizumi 0 1 0 0 2 1 0 Tony Blair 0 1 0 0 2 1 0

Accuracy = 0.8308605341246291