



# **COMP712: Classical Artificial Intelligence**

# Workshop: Constraint Satisfaction Problem (CSP)

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COMP712/Sudoku Backtracking Demo - Falmouth University 2023-2024 — 🖂 🗙								
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# Introduction

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We've learnt Constraint Satisfaction Problem (CSP) during the lecture. Now, you know that there are two popular ways of solving the CSP: the Backtracking algorithm (BT) and Constraint Propagation (CP). In this workshop, you will implement these two methods to solve Sudoku puzzles.

### **CSP**

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CSP is a powerful framework used in artificial intelligence and computer science to represent and solve problems where a set of variables must satisfy certain constraints. At its core, a CSP involves a collection of variables, each with a domain of possible values, and a set of constraints that limit the permissible combinations of values for these variables. The primary goal in a CSP is to find a solution that satisfies all the constraints simultaneously, adhering to the specified criteria without violating any constraints. The challenge in CSPs lies in efficiently exploring the solution space to identify valid assignments that meet all constraints, often employing algorithms like backtracking or constraint propagation to navigate the possibilities and arrive at a satisfactory solution.

### The Game

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The Sudoku puzzle is a popular and captivating example of a CSP. It consists of a 9x9 grid divided into nine 3x3 subgrids. The objective is to fill each cell in the grid with a digit from 1 to 9, ensuring that each row, column, and subgrid contains all digits exactly once. The clues provided at the beginning create constraints, restricting the potential values that can be placed in specific cells, thereby turning the puzzle into a classic CSP.

This puzzle perfectly encapsulates the fundamental components of a CSP: variables (the cells), domains (allowable digits), and constraints (the rules governing placement). Solving Sudoku involves deducing the valid assignment of digits that meets all constraints, typically leveraging CSP-solving techniques like backtracking or constraint propagation. The interplay of logical deduction and constraint satisfaction in Sudoku showcases the application of CSPs in solving complex, structured problems across various domains, offering a tangible and enjoyable demonstration of this computational concept.

# The Repository

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This repository contains the materials for COMP712 - CSP workshop.

https://github.falmouth.ac.uk/Daniel-Zhang/COMP712-CSP.git

There are 2 demos available:

This repository contains the materials for COMP712 - CSP workshop.

- demo\_sudoku\_bt.pyc : demo of solving Sudoku using Backtracking algorithm (BT)
- demo\_sudoku\_cp.pyc : demo of solving Sudoku using Constraint Propagation (CP)
- 2 predefined puzzles
- Press H for help

### **Code Structure**

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- bt\_sudoku.py: the template for the backtracking algorithm that you are going to implement.
- cp\_sudoku.py: the template for constraint propagation that you are going to implement.

The gui lib contains helper functions for visualisation. Some of them are:

- fillCell(v: Cell, s: int, force\_update=False): fills a specific cell v using the number s, update the board if force\_update is True
- clearCell(v: Cell, force\_update=False): clears a cell v and update the board if force\_update is True

- animateCell(c: Cell, colour='white'): changes the specified cell **c** 's background colour with colour, then resets it to the default colour
- getRow(row): returns a list of the numbers in the row
- getCol(col): returns a list of the numbers in the col
- getSubGrid(row, col): returns a list of the numbers in the sub-grid which the cell (row, col)
   belongs to, it will automatically calculate the grid position
- getDomain(row, col): combines getRow(), getCol(), and getSubGrid() that returns the
  possible options to fill for the specified cell (row, col)
- isValid(row, col, num): returns True if the number num can be filled at cell (row, col)

## Your Task

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# Task 1: implement backtracking algorithm (BT)

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- implement the Backtracking (BT) algorithm in bt\_sudoku.py
- you don't need to implement any GUI functionalities as long as the .solve() function was
  implemented properly. It should return either True or False to indicate the solvability of the
  Sudoku puzzle.
- play the demo\_sudoku\_bt.pyc after pressing F to turn on the constraint forward checking during BT search. Compare the searching behaviour to the routine without this functionality enabled.

# Task 2: implement constraint propagation (CP)

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- implement Constraint Propagation (CP) in cp\_sudoku.py
- you don't need to implement any GUI functionalities as long as the .solve() function was
  implemented properly. It should return either True or False to indicate the solvability of the
  Sudoku puzzle.
- play the demo\_sudoku.pyc after pressing B to turn on the backtracking if CP is stuck. Compare the behaviour to the one without this functionality turned on.

### Task 3: combine BT and CP

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- introduce CP into your BT implementation you don't need to do anything more other than checking the self.forward status between True and False
  - o By introducing CP into BT, it significantly reduces the search space during BT process
- introduce BT into your CP implementation you don't need to do anything more other than checking the self.backtrack status between True and False
  - o continue searching with BT if CP cannot proceed further to find a solution

#### Note

- 1. All the Sudoku puzzles generated by pressing the keyboard shortcuts are solvable.
- 2. Those loaded externally might not be solvable.

#### Your Code:

You can submit a pull request to the original repository to showcase your work if you like.

# **Further Reading**

- 1. Sudoku Online
- 2. Sudoku Difficulty Analysis
- 3. Mathematical Analysis of Sudoku
- 4. Sudoku as a CSP