



# Balancing handover areas among neighbouring cells in 3G networks

Evolutionary Algorithms  
Multiobjective optimization and design

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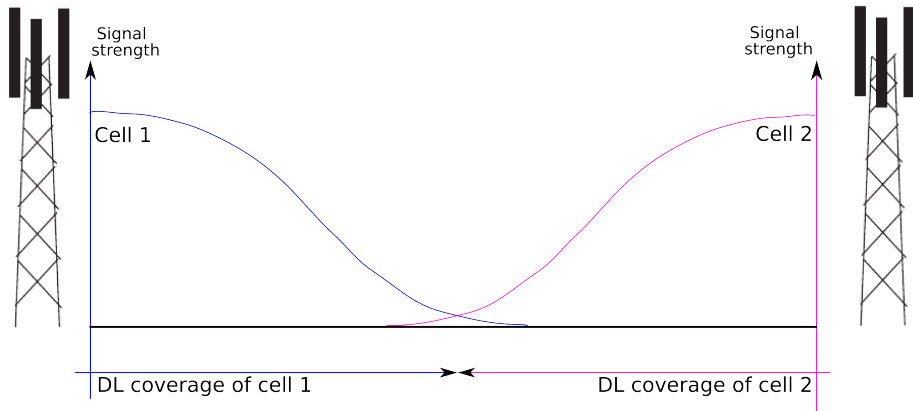
# Outline

- 1 The problem
  - ... description
  - ... structure
  - ... elements
- 2 Single-objective optimization
- 3 Multi-objective optimization
- 4 Concluding remarks
- 5 Appendix: parameter set-up

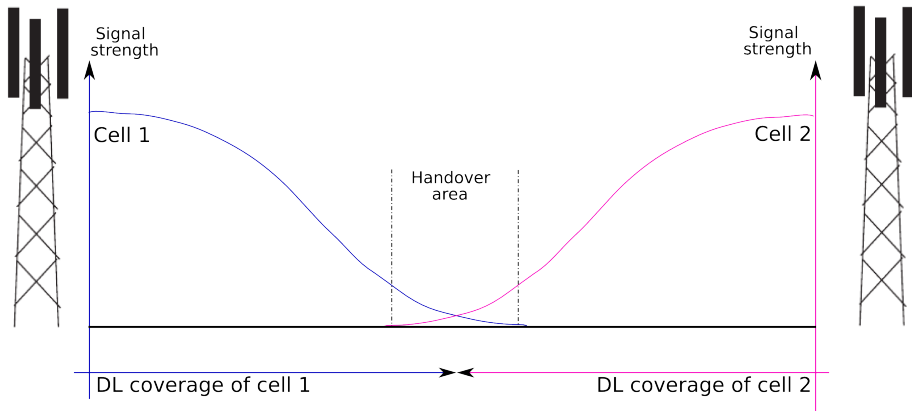
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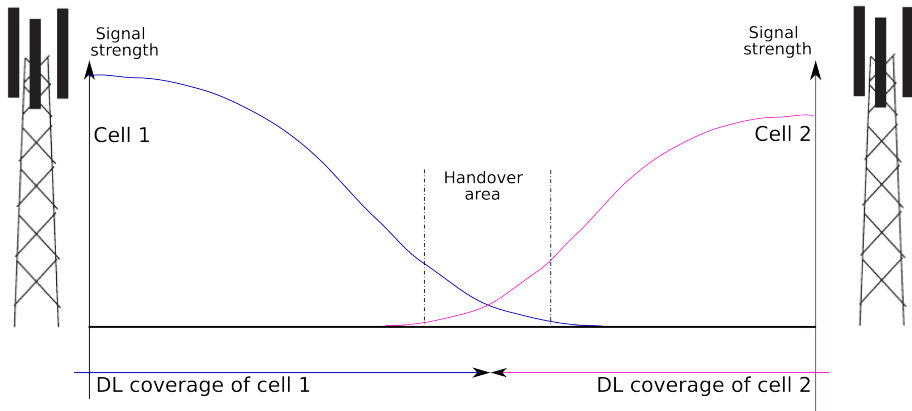
# Neighbour cells



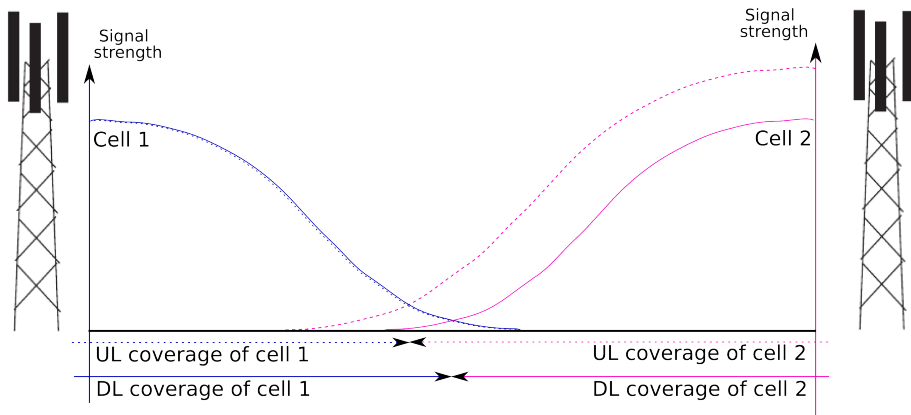
# Handover area



# Balancing handover area

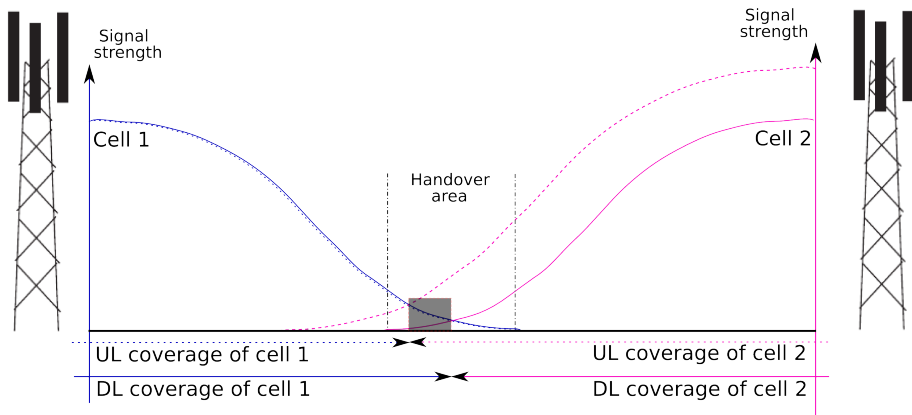


# Balancing UL-DL handover areas

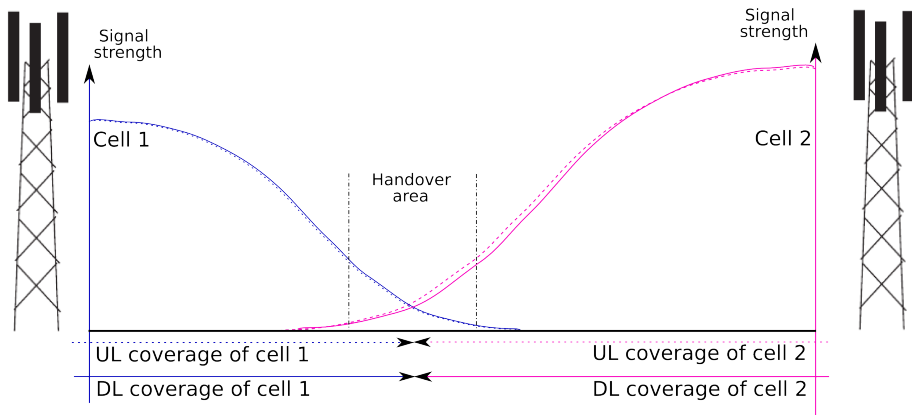




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# Adjacency Matrix

	CELL 1	CELL 2	CELL 3	CELL 4	CELL 5
CELL 1					
CELL 2					
CELL 3					
CELL 4					
CELL 5					

# Adjacency Matrix

	CELL 1	CELL 2	CELL 3	CELL 4	CELL 5
CELL 1	0	0	1	0	1
CELL 2	0	0	0	1	0
CELL 3	1	0	0	0	1
CELL 4	0	1	0	0	0
CELL 5	1	0	1	0	0

# Adjacency Matrix - symmetry

	CELL 1	CELL 2	CELL 3	CELL 4	CELL 5
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# Problem elements

- **Candidate solutions:** DL power setting for every cell.
- **Constraints:** solutions within  $[-2dB, +2dB]$  of current setting.
- Static problem.



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# Objective function

Minimize ...

... the difference between UL and DL areas among neighbour cells.

# Objective function

## Objective function

$$\min |\sum_{i=1}^{|V|} \sum_{j=i}^{|V|} a_{ij} ((UL(c_i) - UL(c_j)) - (DL(c_i) - DL(c_j)))|$$

- $c_i$   $i$ -th cell of the network,
- $DL(c_i)$  downlink power of the  $i$ -th cell,
- $UL(c_i)$  uplink power of the  $i$ -th cell.

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- Discrete search space
  - ▶ changes of  $0.1\text{ dBm}$ .
- Key parameters
  - ▶ initial temperature,
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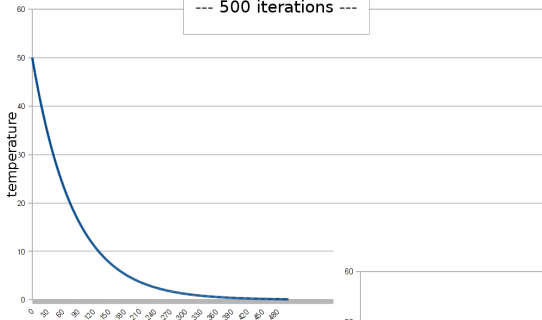
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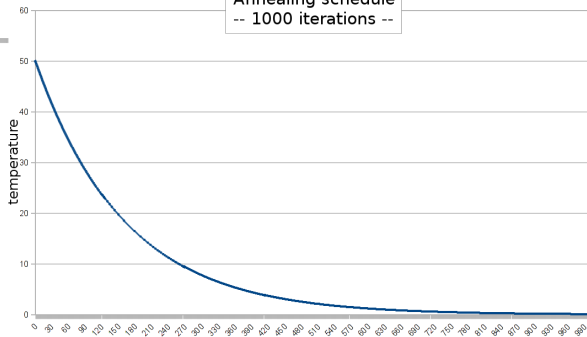
Annealing schedule

--- 500 iterations ---

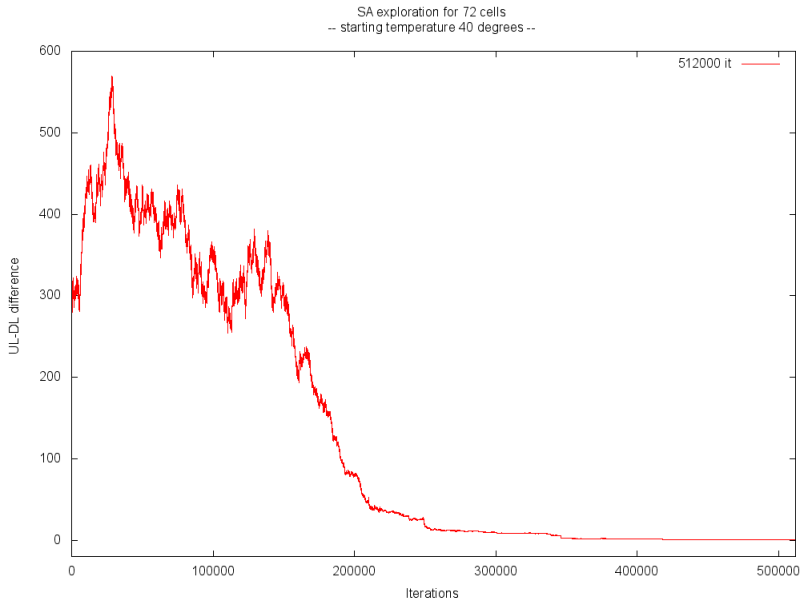


Annealing schedule

-- 1000 iterations --



# SA: Results





# Objective functions

## Minimize ...

... the difference between UL and DL areas among neighbour cells.

## Minimize ...

... the total DL power used.

# Objective functions

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- Continous search space.
- Key parameters
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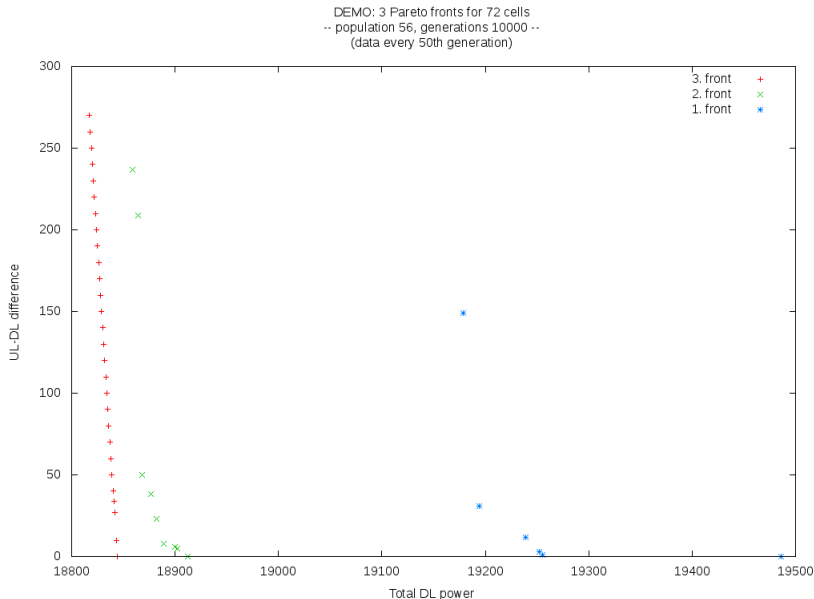
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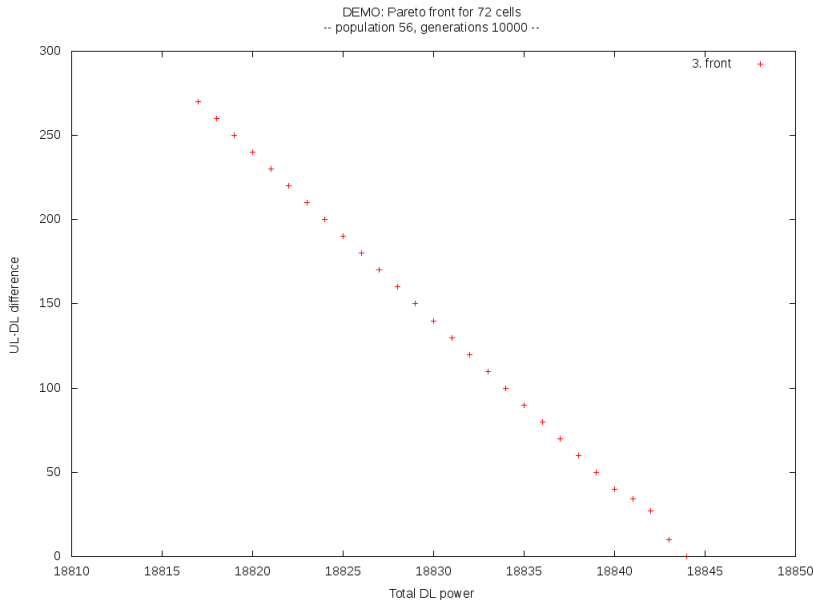
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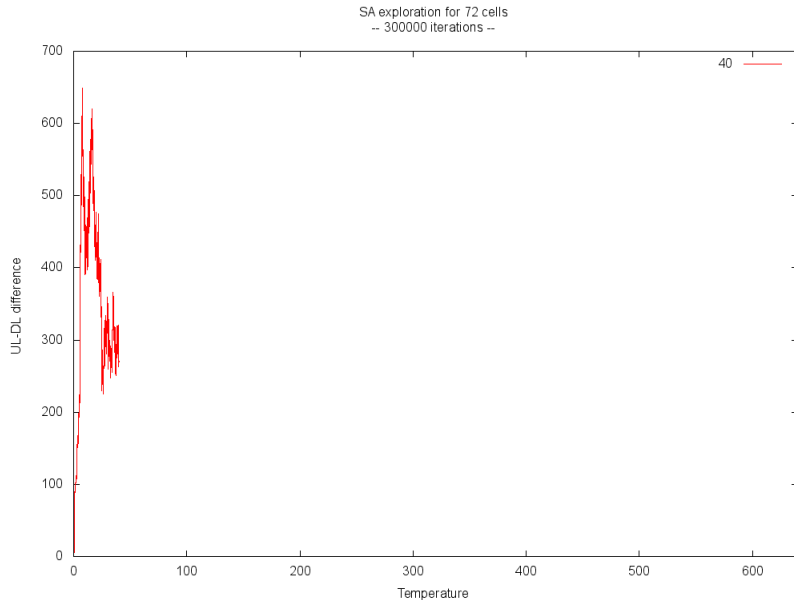
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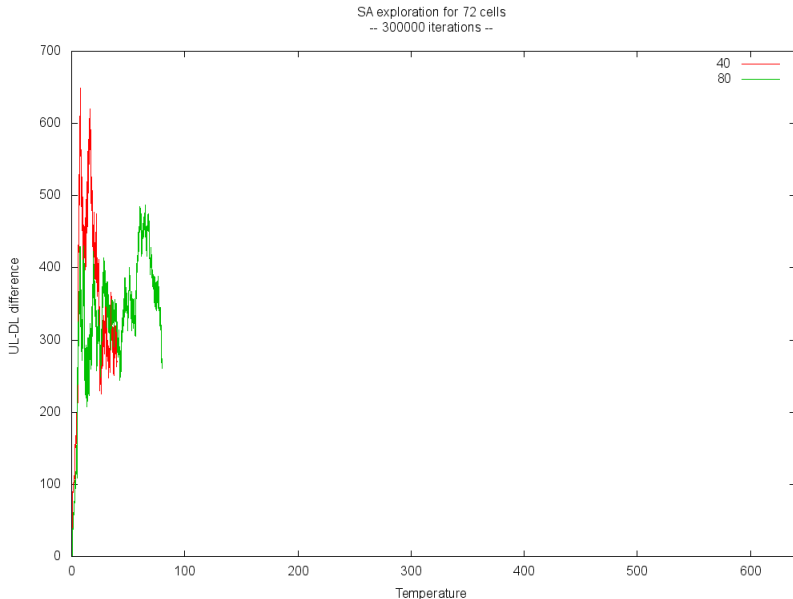
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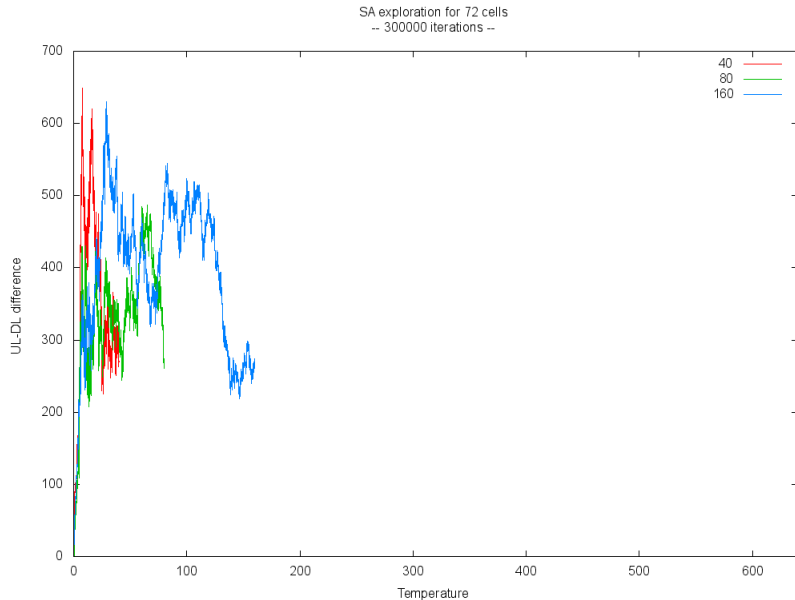
# SA: Starting temperature



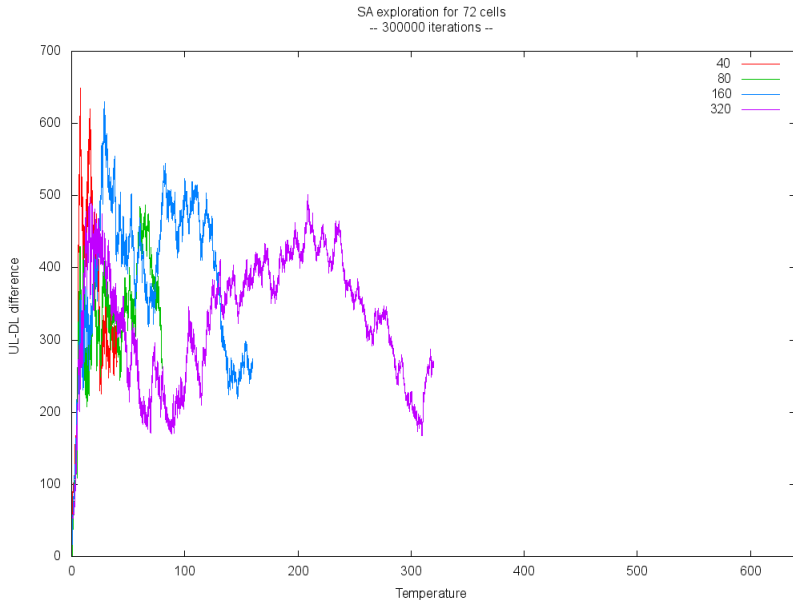
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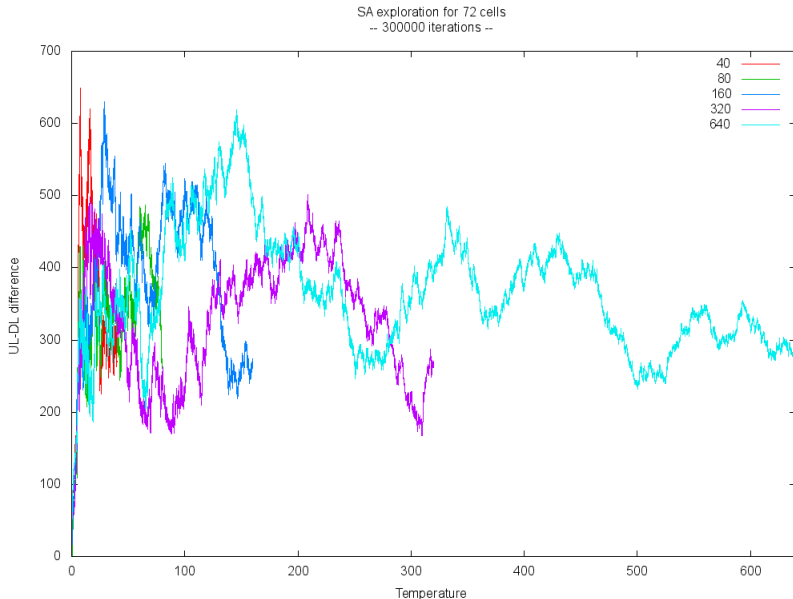
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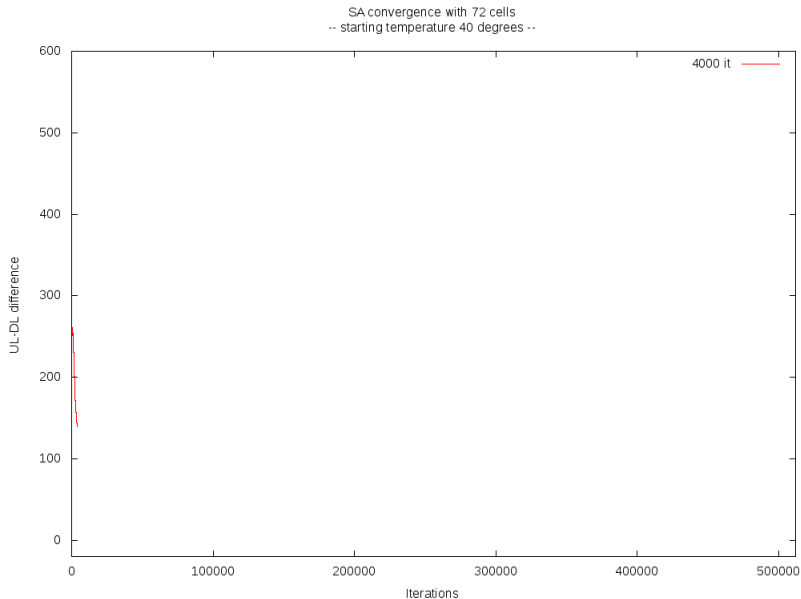
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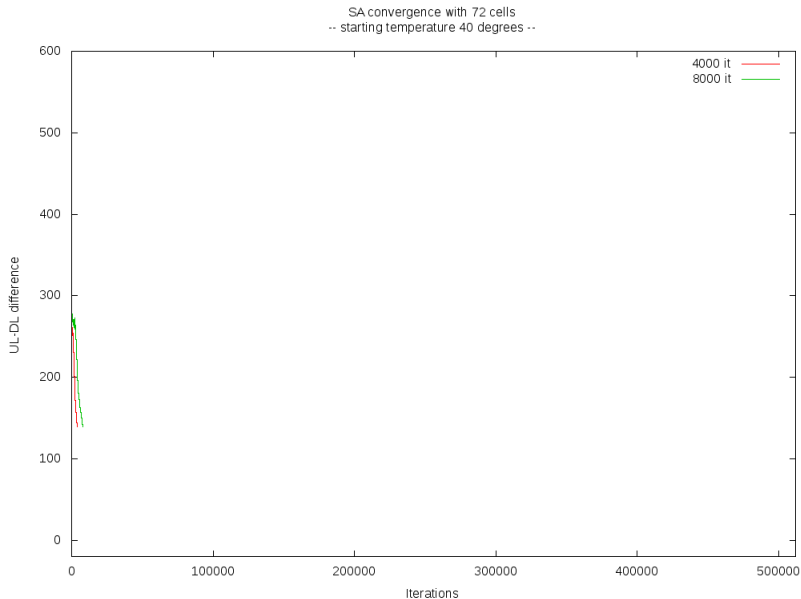
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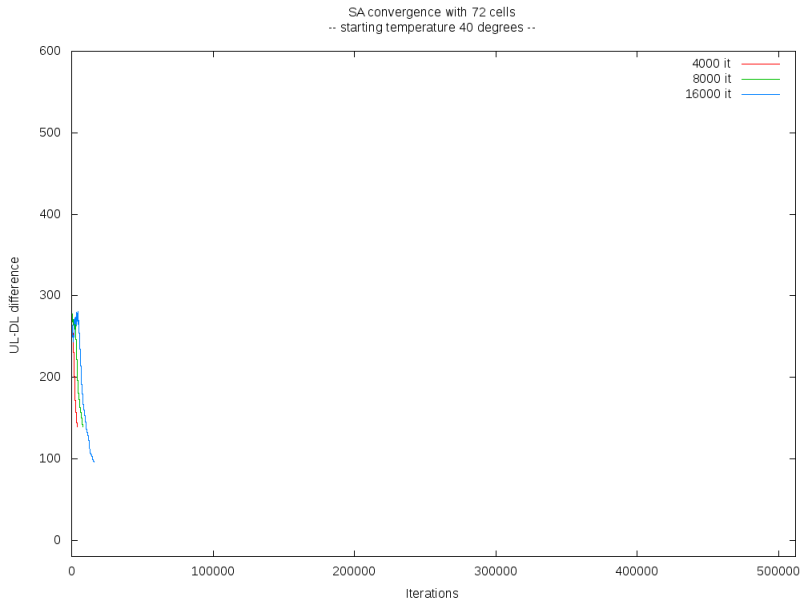
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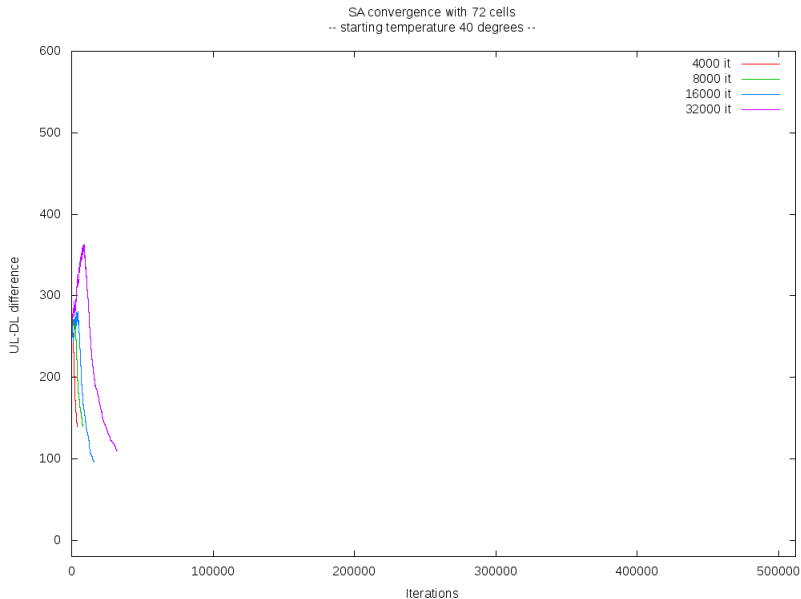


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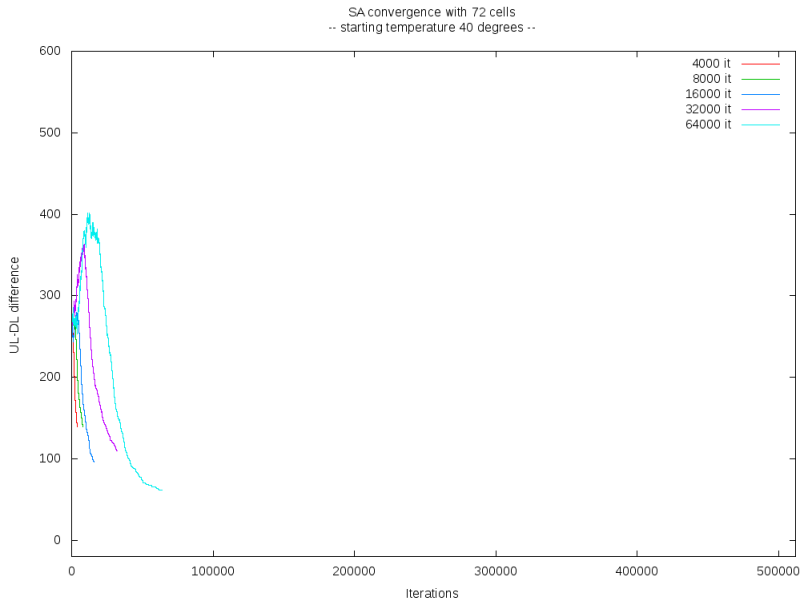




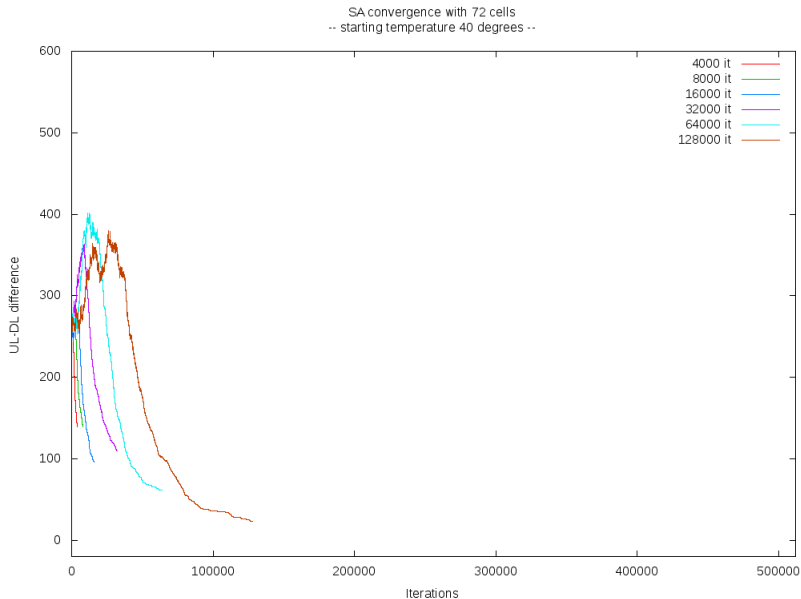
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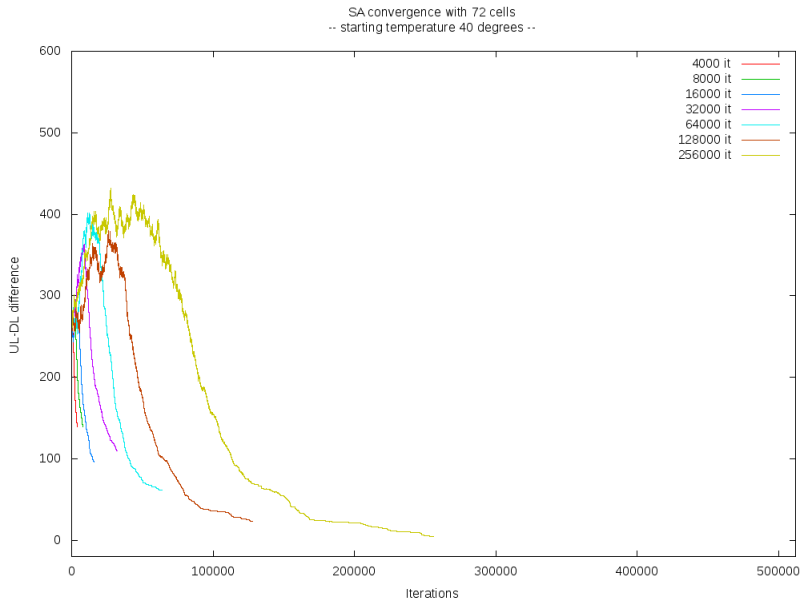
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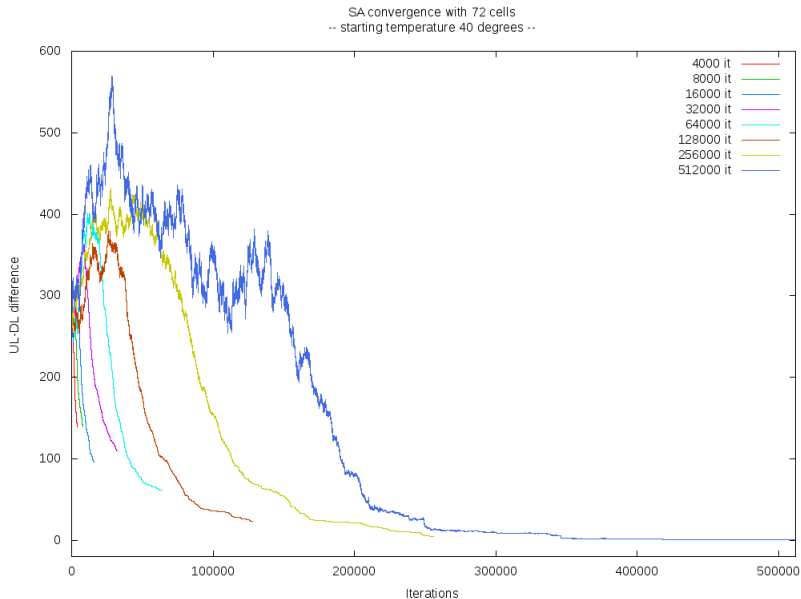
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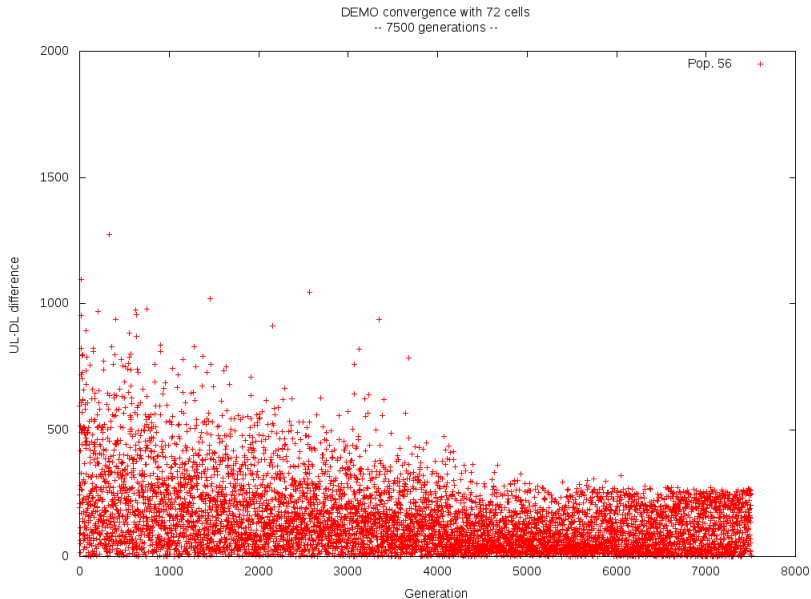
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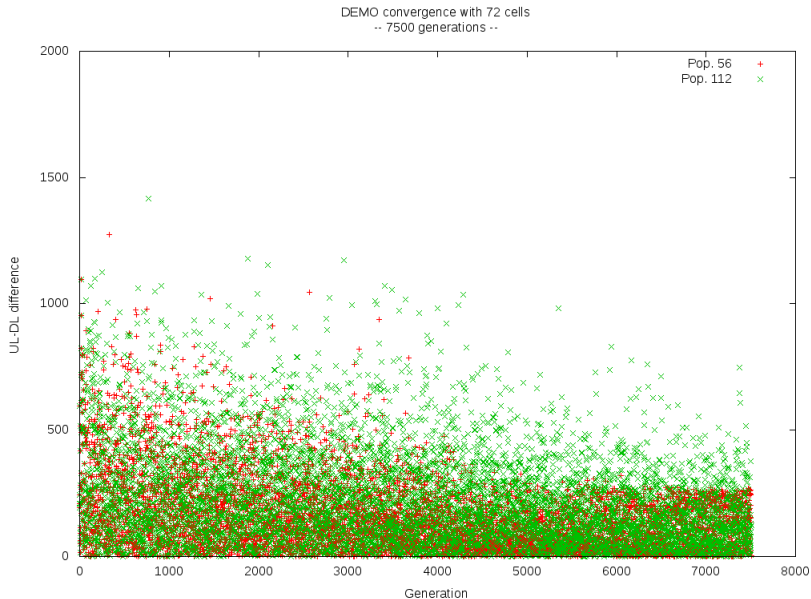
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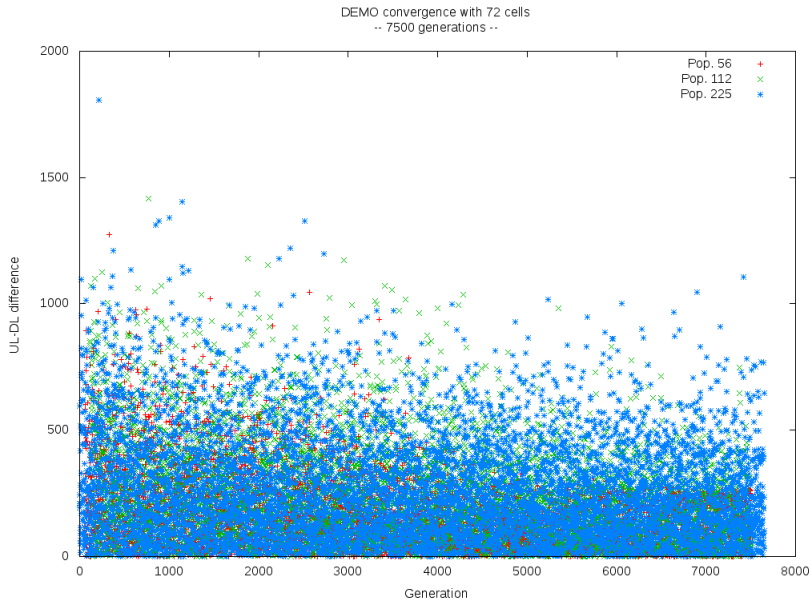
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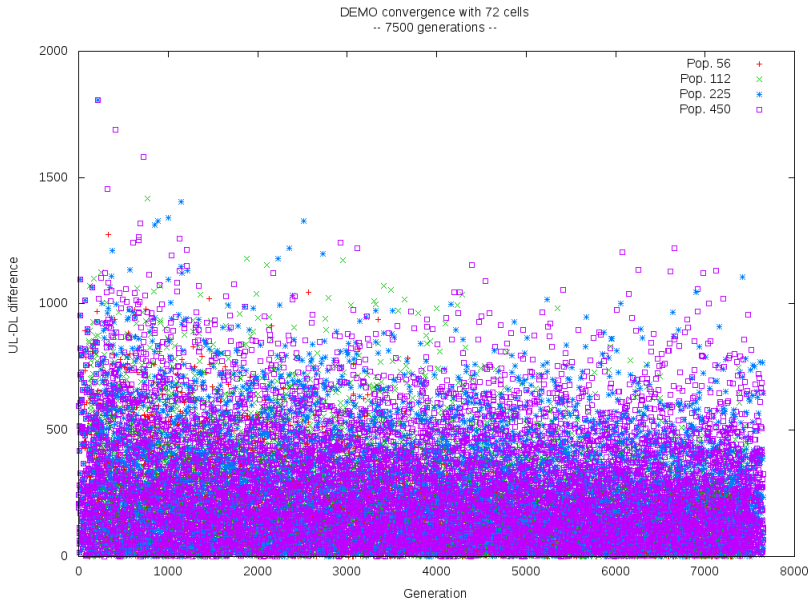


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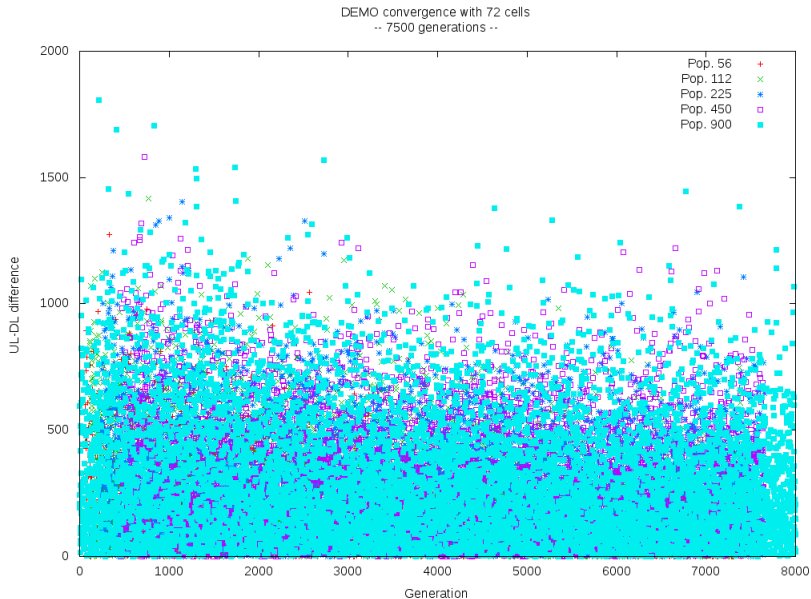




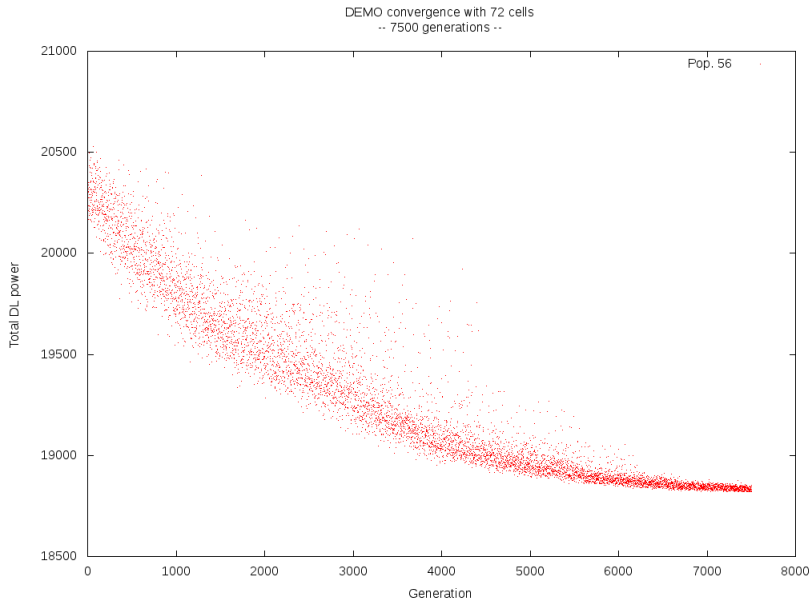
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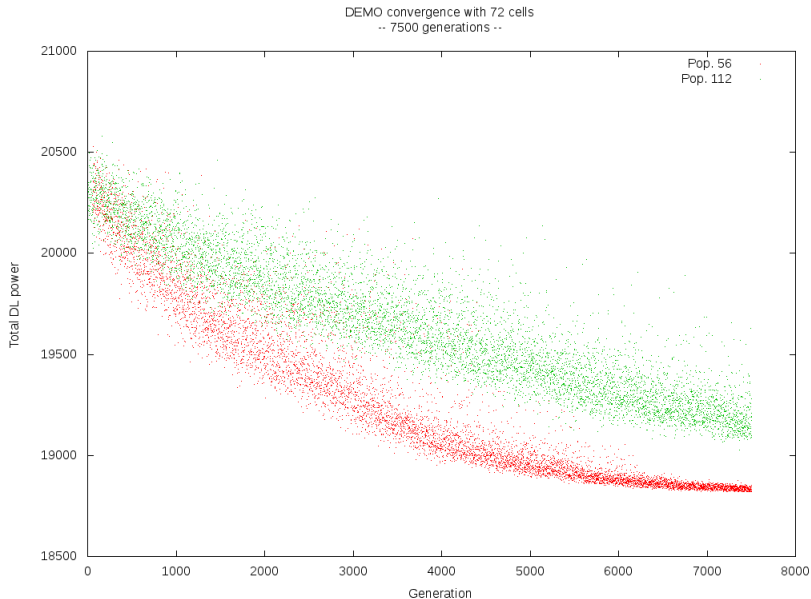
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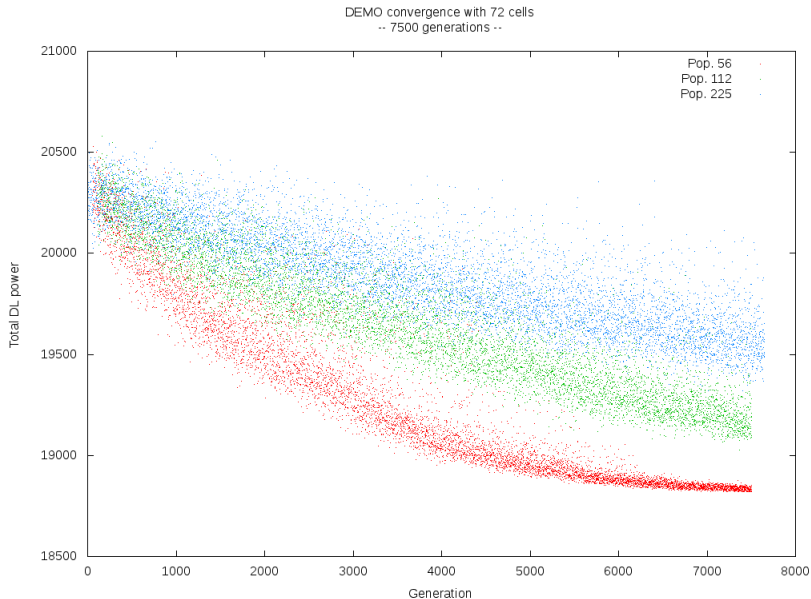
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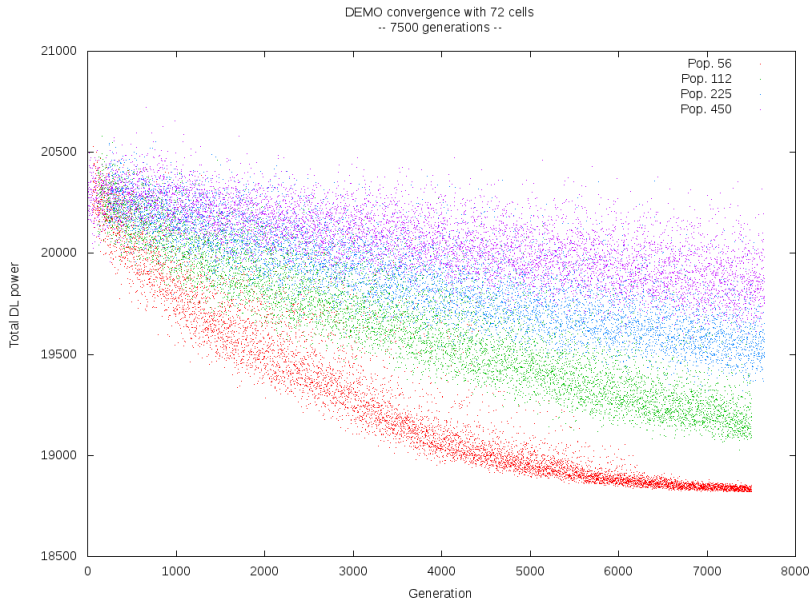
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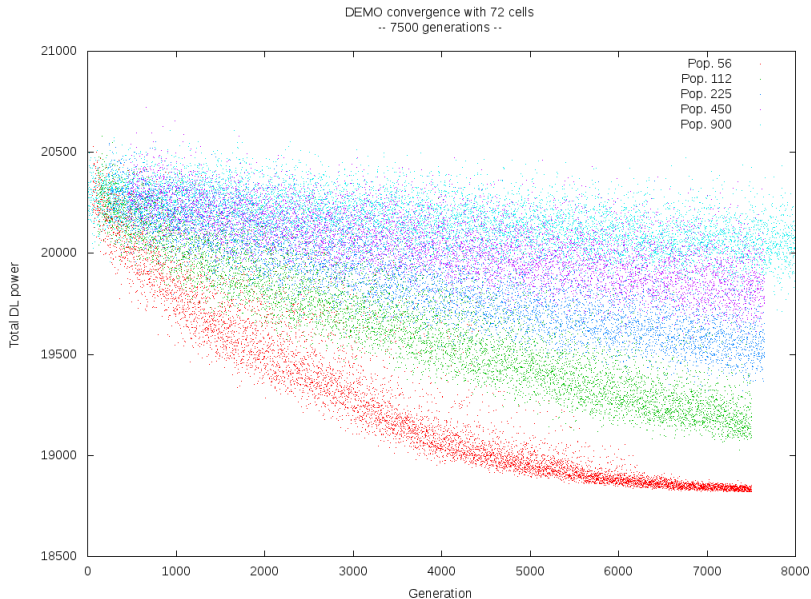
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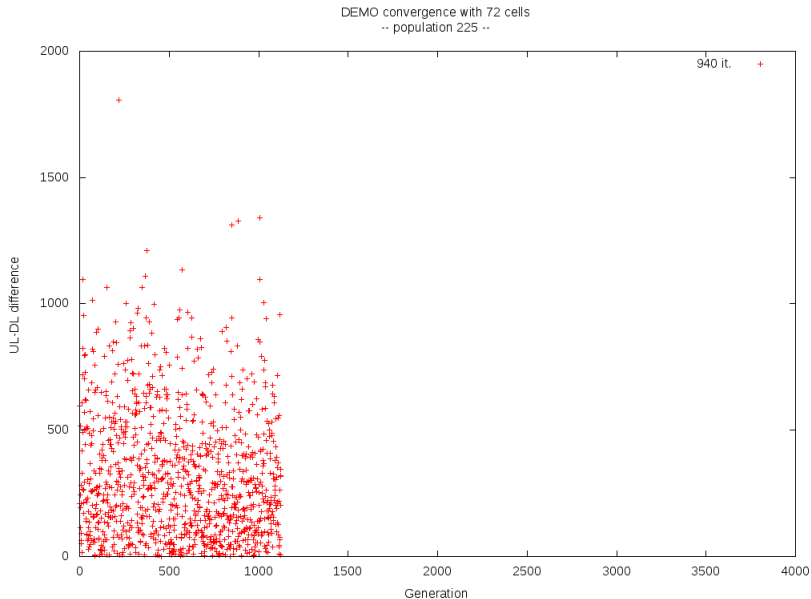
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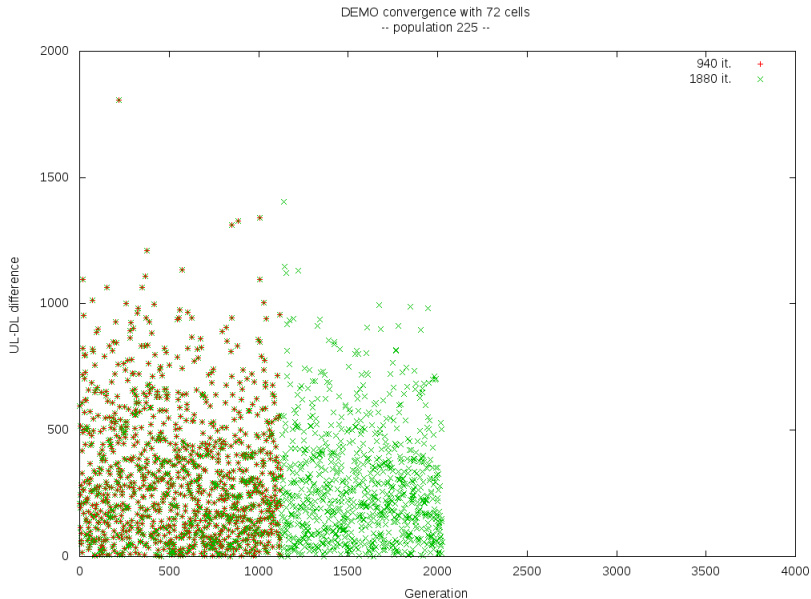


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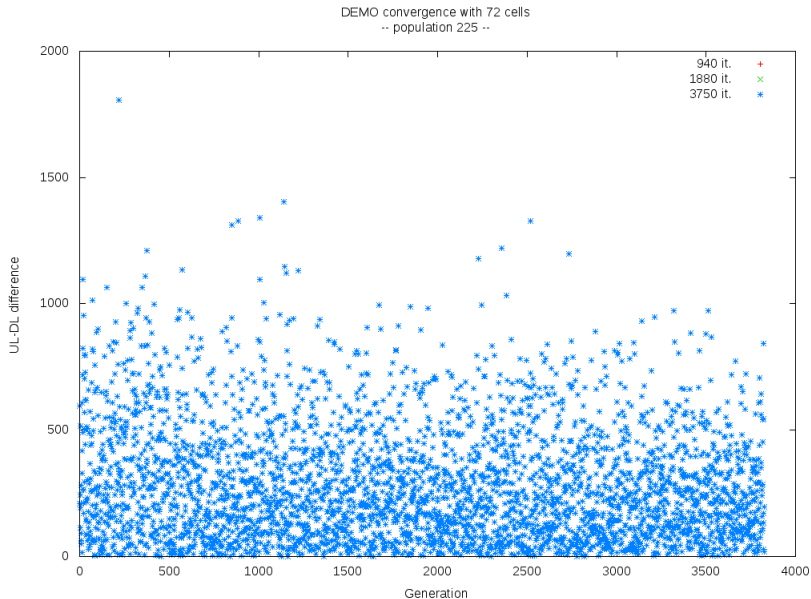




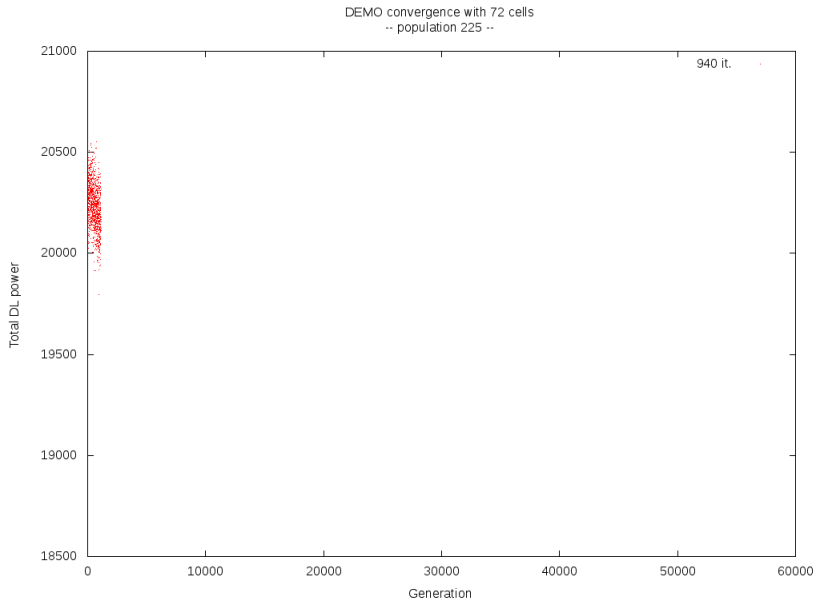
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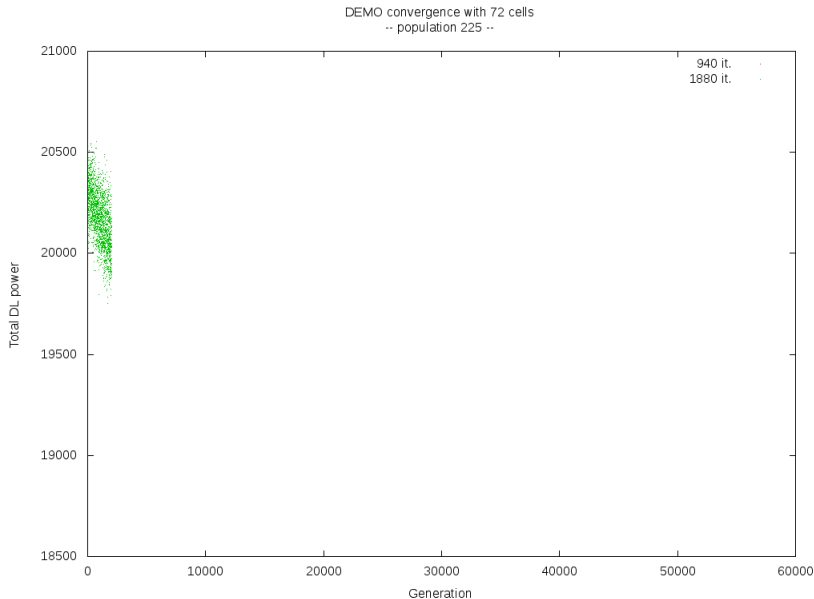
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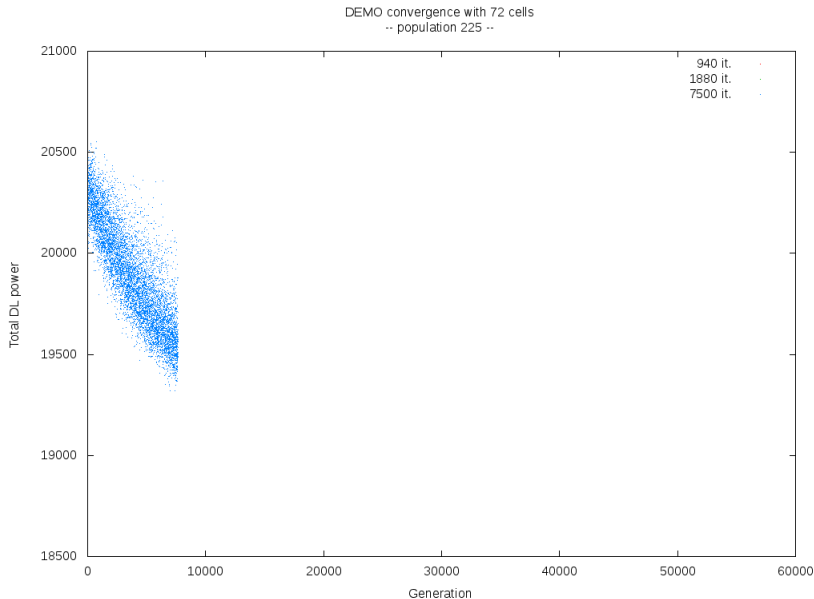
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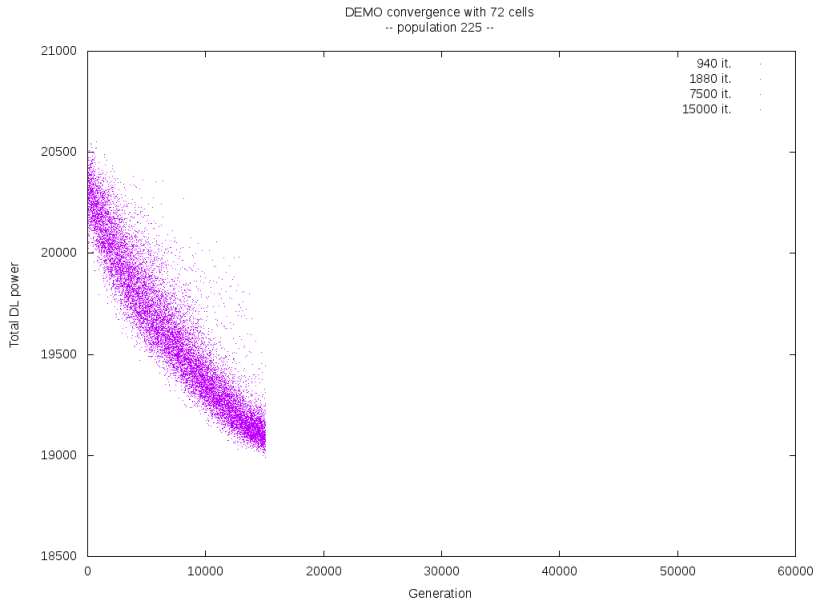
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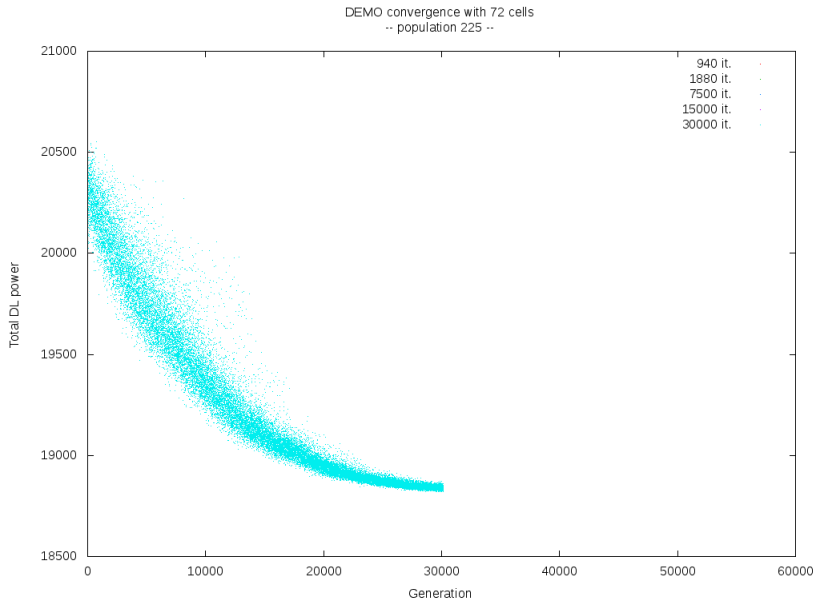
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