

Given an array of positive numbers, find the maximum sum of a subsequence with the constraint that no 2 numbers in the sequence should be adjacent in the array.

5, 5, 10, 100, 10, 5 -> 110 5,100, 5

1, 2, 3 -> 4

5, 10, 100, 5

elem of subsequence is not adjacent in array ?

input: arr, repeated? Y order? N, range of value ? $0 < . < 100,000$

output: int

corner case : input: None?Y []?Y only one elem? Y

idea: brute force

method:

1. for loop to scan elem of arr, find all possible combination of arr, get sum of them $tO(2^{**}N)$, $sO(2^{**}N)$

2. find max value of these sum of them $tO(2^{**}N)$, $sO(1)$

time $O(2^{**}N)$ space $O(2^{**}N)$

idea: dynamic program method

method:

1. $dp[i]$: until $arr[i]$, the max value of subsequence

2. $dp[i] = \max(dp[i - 1], dp[i - 2] + arr[i])$

3. $dp[0] = 5, dp[1] = 5$

time $O(n^{**}2)$ space $O(N)$

5, 5, 10, 100, 10, 5 -> 110 -> 5,100, 5

$dp[0] = 5$

$dp[1] = 5$

$dp[2] = \max(dp[1], dp[0] + arr[2]) = \max(5, 5 + 10) = 15$

$dp[3] = \max(dp[2], dp[1] + arr[3]) = \max(15, 5 + 100) = 105$

$dp[4] = \max(dp[3], dp[2] + arr[4]) = \max(105, 15 + 10) = 105$

$dp[5] = \max(dp[4], dp[3] + arr[5]) = \max(105, 105 + 5) = 110$

class MySolution:

```
def findMax(self, arr): # find the not adjacent biggest sum, output: int
```

```
    if not arr: # corner case
```

```
        return -1
```

```
    if len(arr) == 1:
```

```
        return arr[0]
```

```
    dp = [0] * len(arr)
```

```
    dp[0] = arr[0]
```

```
    dp[1] = arr[1]
```

```
    for i in range(2, len(arr)): # dp method to find max value
```

```
        dp[i] = max(dp[i - 1], dp[i - 2] + arr[i])
    return dp[-1]
```

test:

test case: None -> - 1 only one elem -> arr[0]

test case: [2,7,9,3,1]

```
dp[0] = 2
```

```
dp[1] = 7
```

```
dp[2] = max(dp[1], dp[0] + arr[2]) = max(7, 11) = 11
```

```
dp[3] = max(dp[2], dp[1] + arr[3]) = max(11, 7 + 3) = 11
```

```
dp[4] = max(dp[3], dp[2] + arr[4]) = max(11, 11 + 1) = 12
```

```
return dp[-1] = 12
```