

Report for Project5

Xiaozhi Li

October 6, 2017

Abstract

Project 5 using \LaTeX . In this project we will use EmitTeX to generate the HOL reports. All HOL source files are included in the HOL folder.

Acknowledgments: This report follows the hand book Certified Security by Design Using Higer Order Logic, and course instructions from CIS400-CSBD.

Contents

1	Executive Summary	3
2	Exercise 8.4.1	4
2.1	Problem Statement	4
2.2	HOL Code	4
2.3	Session Transcript	4
2.4	Explain Result	4
3	Exercise 8.4.2	5
3.1	Problem Statement	5
3.2	HOL Code	5
3.3	Session Transcript	6
3.4	Explain Result	6
4	Excercise 8.4.3	7
4.1	Problem Statement	7
4.2	HOL Code	7
4.3	Session Transcript	8
4.4	Explain Result	8
5	Appendix A: source code for 8.4.1, 8.4.2, and 8.4.3	9

Chapter 1

Executive Summary

All requirements for this project are satisfied. Specifically, we utilized HOL to prove the following theorems:

[conjSymAll]

$$\vdash \forall p \ q. \ p \wedge q \iff q \wedge p$$

[conjSymThm]

$$\vdash p \wedge q \iff q \wedge p$$

[problem1Thm]

$$\vdash p \Rightarrow (p \Rightarrow q) \Rightarrow (q \Rightarrow r) \Rightarrow r$$

All requirments of the project have been met, all theories and code compiled and ran within HOL and Latex.

Chapter 2

Exercise 8.4.1

2.1 Problem Statement

Our task is to prove the theorem $\vdash p \Rightarrow (p \Rightarrow q) \Rightarrow (q \Rightarrow r) \Rightarrow r$

2.2 HOL Code

```
(* 8-4-1 *)
val problem1Thm =
let
val th1 = ASSUME ``p:bool``
val th2 = ASSUME ``p ==> q``
val th3 = ASSUME ``q ==> r``
val th4 = MP th2 th1
val th5 = MP th3 th4
val th6 = DISCH (hd(hyp th3)) th5
val th7 = DISCH (hd(hyp th2)) th6

in
DISCH (hd(hyp th1)) th7
end
```

2.3 Session Transcript

```
> > > ##### ** Unicode trace now off
> *** Globals.show_assums now true ***
> ##### ** types trace now on
> ##### val problem1Thm =
    [] |- (p :bool) ==> (p ==> (q :bool)) ==> (q ==> (r :bool)) ==> r:
    thm
>
```

1

2.4 Explain Result

Hol is showing our theorem with no type errors, this means our tests have passed.

Chapter 3

Exercise 8.4.2

3.1 Problem Statement

For 8.4.2 we need to prove the theorem:

$$\vdash p \wedge q \iff q \wedge p$$

3.2 HOL Code

```

val conj1Thm =
let
val th2 =ASSUME ``p/\q``
val th3 =CONJUNCT1 th2
val th4 =CONJUNCT2 th2
val th5 =CONJ th4 th3
in
DISCH (hd(hyp th2)) th5
end;

val conj2Thm =
let
val th1 =ASSUME ``q/\p``
val th2 =CONJUNCT1 th1
val th3 =CONJUNCT2 th1

val th4 =CONJ th3 th2
in
DISCH (hd(hyp th1)) th4
end;

val conjSymThm =
IMP_ANTISYMRULE conj1Thm conj2Thm;

```

3.3 Session Transcript

```
> > > # # # # # # # ** types trace now on
> *** Globals.show_assums now true ***
> # # # # # # # ** Unicode trace now off
> # # # # # # # val conj1Thm =
  □ |- (p :bool) /\ (q :bool) ==> q /\ p:
  thm
> > # # # # # # # val conj2Thm =
  □ |- (q :bool) /\ (p :bool) ==> p /\ q:
  thm
> > > # val conjSymThm =
  □ |- (p :bool) /\ (q :bool) <=> q /\ p:
  thm
>
*** Emacs/HOL command completed ***
```

1

3.4 Explain Result

In 8.4.2, all of our theorem and theory have passed by HOL.

Chapter 4

Excercise 8.4.3

4.1 Problem Statement

For 8.4.3 we need to prove the therom:

$$\vdash \forall p \ q. \ p \wedge q \iff q \wedge p$$

4.2 HOL Code

Notice in 8.4.3 we are extending the code from 8.4.2:

```

val conj1Thm =
let
val th2 =ASSUME ``p/\q``
val th3 =CONJUNCT1 th2
val th4 =CONJUNCT2 th2
val th5 =CONJ th4 th3
in
DISCH (hd(hyp th2)) th5
end;

val conj2Thm =
let
val th1 =ASSUME ``q/\p``
val th2 =CONJUNCT1 th1
val th3 =CONJUNCT2 th1

val th4 =CONJ th3 th2
in
DISCH (hd(hyp th1)) th4
end;

val conjSymThm =
IMP_ANTISYM_RULE conj1Thm conj2Thm;
val conjSymAll=GENL [``p:bool``, ``q:bool``] conjSymThm;

```

4.3 Session Transcript

```

> > > # # # # # ** types trace now on
> *** Globals.show_assums now true ***
> # # # # # ** Unicode trace now off
> # # # # # val conj1Thm =
  [] |- (p :bool) /\ (q :bool) ==> q /\ p:
  thm
> > # # # # # val conj2Thm =
  [] |- (q :bool) /\ (p :bool) ==> p /\ q:
  thm
>
*** Emacs/HOL command completed ***

> # val conjSymThm =
  [] |- (p :bool) /\ (q :bool) <=> q /\ p:
  thm
> val conjSymAll =
  [] |- !(p :bool) (q :bool). p /\ q <=> q /\ p:
  thm
>

```

1

4.4 Explain Result

All tests from 8.4.3 have been passed in HOL.

Chapter 5

Appendix A: source code for 8.4.1, 8.4.2, and 8.4.3

The following code is from *proj5Script.sml*

```
(*****
(* Author: Xiaozhi Li *)
*****)

(*****
(* All HOL script files are ML modules, so we need to declare the file *)
(* example1Script as an ML structure. Do this with the "structure: command *)
(* as the very first executable line. The very last executable line is "end" *)
*****)

structure proj5Script = struct

  (*****
  (* Note: everything after new_theory must be part of a val assignment, when *)
  (* using Holmake. Otherwise, there will be compilation errors. If you don't *)
  (* want to assign an expression to a name, just use "val _ = <expression>" *)
  (* The "_" indicates that we don't want to have a name. *)
  *****)
  open HolKernel Parse boolLib bossLib;

  val _ = new_theory "proj5";
  (*****
  (* val problem1Thm *)
  (* [] |- p ==> (p ==> q) ==> (q ==> r) ==> r *)
  *****)

  (* 8-4-1 *)
  val problem1Thm =
  let
  val th1 = ASSUME 'p: bool'
  val th2 = ASSUME 'p ==> q'
  val th3 = ASSUME 'q ==> r'
  val th4 = MP th2 th1
  val th5 = MP th3 th4
  val th6 = DISCH (hd(hyp th3)) th5
  val th7 = DISCH (hd(hyp th2)) th6

  in
  DISCH (hd(hyp th1)) th7
  end
```

```
val _ = save_thm("problem1Thm", problem1Thm);
```

```
(* 8-4-2 *)
```

```
val conj1Thm =
let
val th2 = ASSUME ``p/\q``
val th3 = CONJUNCT1 th2
val th4 = CONJUNCT2 th2
val th5 = CONJ th4 th3
in
DISCH (hd(hyp th2)) th5
end;
```

```
val conj2Thm =
let
val th1 = ASSUME ``q/\p``
val th2 = CONJUNCT1 th1
val th3 = CONJUNCT2 th1

val th4 = CONJ th3 th2
in
DISCH (hd(hyp th1)) th4
end;
```

```
val conjSymThm =
IMP_ANTISYM_RULE conj1Thm conj2Thm;
```

```
val _ = save_thm("conjSymThm", conjSymThm);
```

```
(* **** *)
(* 8-4-3 *)
```

```
val conj1Thm =
let
val th2 = ASSUME ``p/\q``
val th3 = CONJUNCT1 th2
val th4 = CONJUNCT2 th2
val th5 = CONJ th4 th3
in
```

```
DISCH (hd(hyp th2)) th5
end;

val conj2Thm =
let
val th1 =ASSUME ‘‘q/\p‘‘
val th2 =CONJUNCT1 th1
val th3 =CONJUNCT2 th1

val th4 =CONJ th3 th2
in
DISCH (hd(hyp th1)) th4
end;

val conjSymThm =
IMP_ANTISYM_RULE conj1Thm conj2Thm;
val conjSymAll=GENL [‘‘p:bool‘‘, ‘‘q:bool‘‘] conjSymThm;

val _=save_thm("conjSymAll", conjSymAll)

val _=export_theory();

end (* structure *)
```