

## Domain Specific Languages and rewriting-based optimisations for performance-portable parallel programming

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## Examples of Domain Specific Languages

SQL

```
SELECT Book.title AS Title,
       count(*) AS Authors
  FROM Book
 JOIN Book_author
    ON Book.isbn = Book_author.isbn
 GROUP BY Book.title;
```

make

```
all: hello

hello: main.o factorial.o hello.o
        g++ main.o factorial.o hello.o -o hello

main.o: main.cpp
        g++ -c main.cpp

factorial.o: factorial.cpp
        g++ -c factorial.cpp

hello.o: hello.cpp
        g++ -c hello.cpp

clean:
        rm *o hello
```

HTML



VHDL

```
library IEEE;
use IEEE.std_logic_1164.all;
use IEEE.numeric_std.all; -- for the unsigned type

entity COUNTER is
  generic (
    WIDTH : in natural := 32);
  port (
    RST : in std_logic;
    CLK : in std_logic;
    LOAD : in std_logic;
    DATA : in std_logic_vector(WIDTH-1 downto 0);
    Q : out std_logic_vector(WIDTH-1 downto 0));
end entity COUNTER;

architecture RTL of COUNTER is
  signal CNT : unsigned(WIDTH-1 downto 0);
begin
  process(RST, CLK) is
  begin
    if RST = '1' then
      CNT <= (others => '0');
    elsif rising_edge(CLK) then
      if LOAD = '1' then
        CNT <= unsigned(DATA); -- type is converted to unsigned
      else
        CNT <= CNT + 1;
      end if;
    end if;
  end process;
  Q <= std_logic_vector(CNT); -- type is converted back to std_logic_vector
end architecture RTL;
```

shell scripts

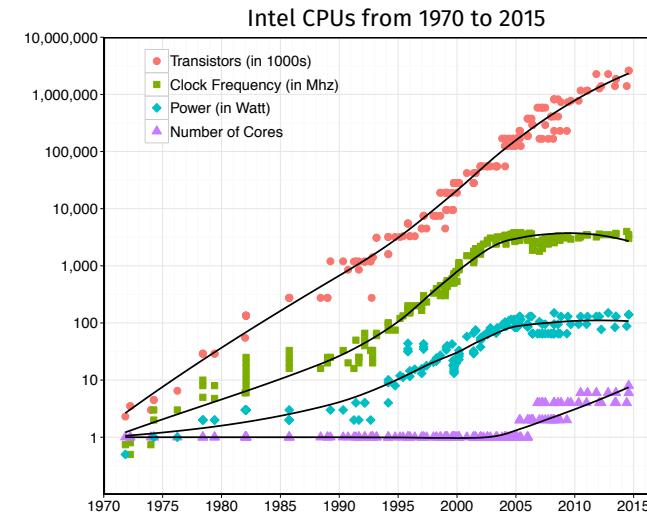
```
#!/bin/sh
if [ $(id -u) != "0" ]; then
  echo "You must be the superuser to
        run this script" >&2
  exit 1
fi
```

- Definition by Paul Hudak:  
“A programming language tailored specifically for an application domain”
- DSLs are *not* general purpose programming language
- Capture the semantics of a particular application domain
- Raise level of abstraction (often *declarative* not *imperative*)



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## Parallelism everywhere: The Many-Core Era



Inspired by Herb Sutter “The Free Lunch is Over:  
A Fundamental Turn Towards  
Concurrency in Software”

# Challenges of Parallel Programming

- Threads are the dominant parallel programming model for multi-core architectures
- Concurrently executing threads can modify shared data, leading to:
  - race conditions
  - need for mutual exclusion and synchronisation
  - deadlocks
  - non-determinism
- Writing correct parallel programs is extremely challenging

## Examples of Algorithmic Skeletons

map( <i>f</i> , <i>xs</i> )	→	$[f(x_1)   f(x_2)   f(x_3)   f(x_4)   f(x_5)   f(x_6)   f(x_7)   f(x_8)]$
zip(+, <i>xs</i> , <i>ys</i> )	→	$[x_1+y_1   x_2+y_2   x_3+y_3   x_4+y_4   x_5+y_5   x_6+y_6   x_7+y_7   x_8+y_8]$
reduce(+, 0, <i>xs</i> )	→	$x_1+x_2+x_3+x_4+x_5+x_6+x_7+x_8$

- Algorithmic Skeletons have a parallel semantics
- Every (parallel) execution order to compute the result is valid
- Complexity of parallelism is hidden by the skeleton

# Structured Parallel Programming aka: "Threads Considered Harmful"

- Dijkstra's: "GO TO" Considered Harmful led to structured programming
  - Raise the level of abstraction by capturing common patterns:
    - E.g. use '**if A then B else C**' instead of multiple **goto** statements
- Murray Cole at Edinburgh invented *Algorithmic Skeletons*:
  - special higher-order functions which describe the "computational skeleton" of a parallel algorithm
  - E.g. use **D\_C** indivisible split join **f** instead of a custom divide-and-conquer implementation with threads
- Algorithmic Skeletons are structured *parallel* programming and raise the level of abstraction over threads
  - No race conditions and no need for explicit synchronisation
  - No deadlocks
  - Deterministic

## DSLs for Parallel Programming with Algorithmic Skeletons

- There exist numerous implementations of algorithmic skeletons libraries
  - The Edinburgh Skeleton Library (**eSkel**): C, MPI
  - FastFlow and Muesli: C++, multi-core CPU, MPI, GPU
  - SkePU, **SkelCL**: C++, GPU
  - Accelerate: Haskell, GPU
  - ...
- Libraries from industry implementing similar concepts:
  - Intel's Threading Building Blocks (TBB)
  - Nvidia's Thrust Library

# SkelCL by Example

```
dotProduct A B = reduce (+) 0 ∘ zip (x) A B
```

```

#include <SkelCL/SkelCL.h>
#include <SkelCL/Zip.h>
#include <SkelCL/Reduce.h>
#include <SkelCL/Vector.h>

float dotProduct(const float* a, const float* b, int n) {
    using namespace skelcl;
    skelcl::init( 1_device.type(deviceType::ANY) );

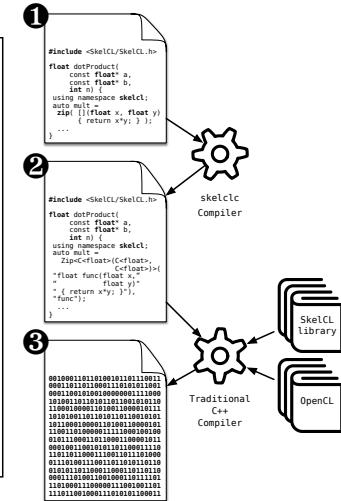
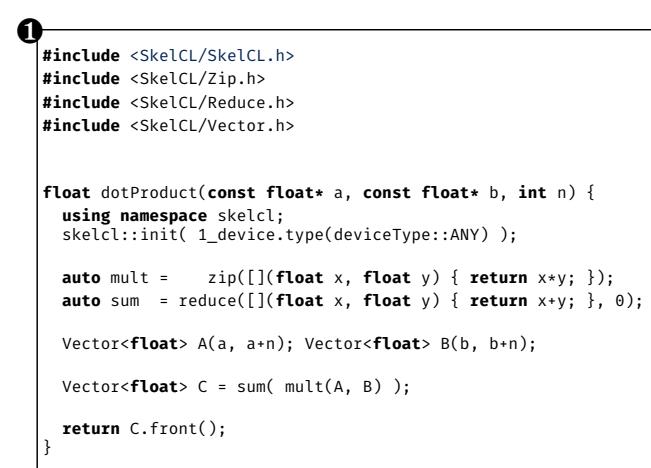
    auto mult = zip([](float x, float y) { return x*y; });
    auto sum = reduce([](float x, float y) { return x+y; }, 0);

    Vector<float> A(a, a+n); Vector<float> B(b, b+n);

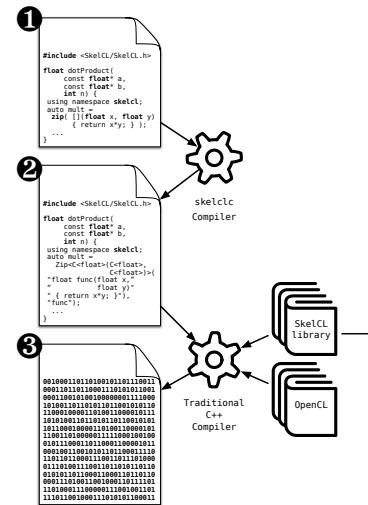
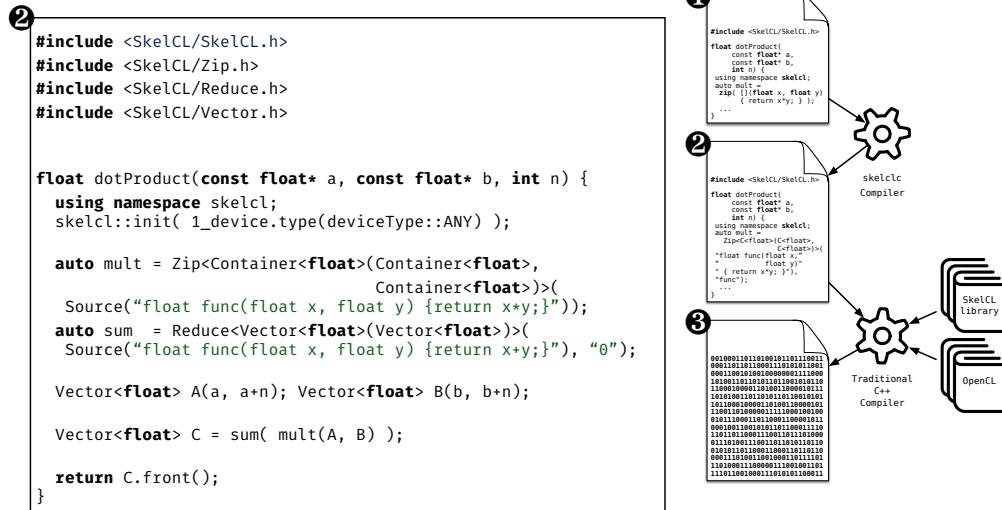
    Vector<float> C = sum( mult(A, B) );

    return C.front();
}

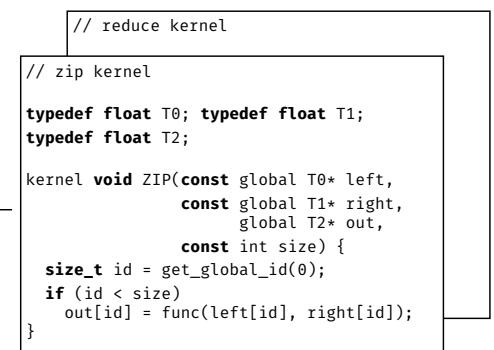
```



# From SkelCL to OpenCL

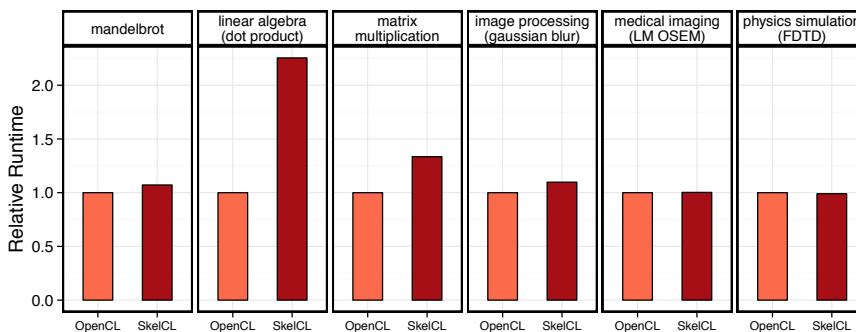


# From SkelCL to OpenCL



# Implementations of Algorithmic Skeletons in OpenCL

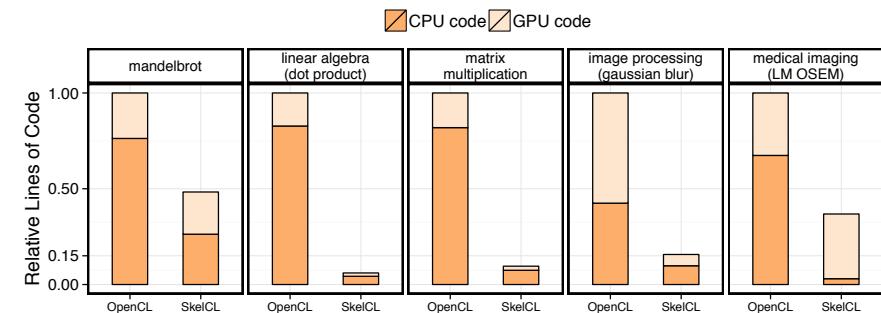
## SkelCL Evaluation – Performance



SkelCL performance close to native OpenCL code!

(Exception: dot product ... we will address this later)

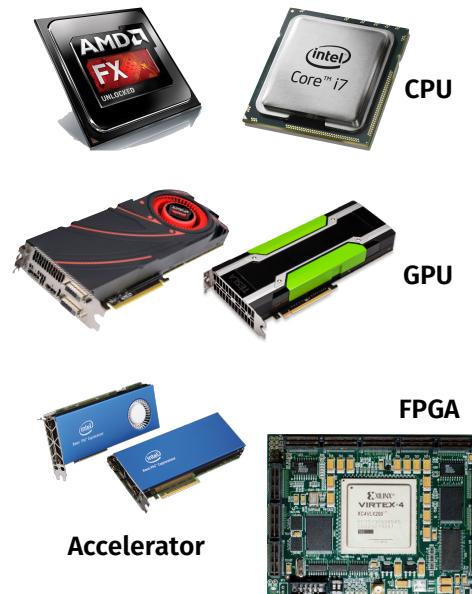
## SkelCL Evaluation – Productivity



SkelCL programs are significantly shorter!  
Common advantage of Domain Specific Languages!

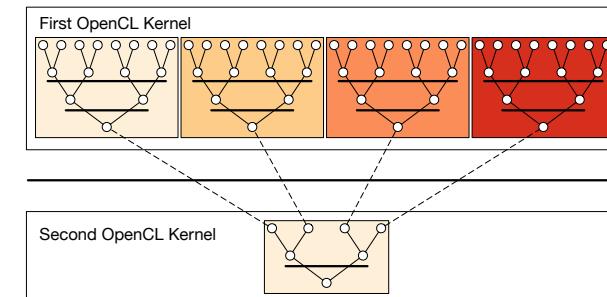
## The Performance Portability Problem

- Many different types: CPUs, GPUs, ...
- Parallel programming is hard
- Optimising is even harder
- Problem:**  
No portability of performance!



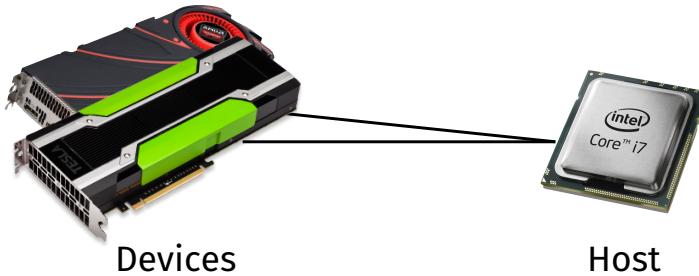
## Case Study: Parallel Reduction in OpenCL

- Summing up all values of an array (= *reduce* skeleton)
- Comparison of 7 implementations by Nvidia
- Investigating complexity and efficiency of optimisations



# OpenCL

- Parallel programming language for GPUs, multi-core CPUs
- Application is executed on the *host* and offloads computations to *devices*
- Computations on the device are expressed as *kernels*:
  - functions executed in parallel
- Usual problems of deadlocks, race conditions, ...



Devices

Host

## Unoptimised Implementation Parallel Reduction

```
kernel void reduce0(global float* g_idata, global float* g_odata,
                    unsigned int n, local float* l_data) {
    unsigned int tid = get_local_id(0);
    unsigned int i   = get_global_id(0);
    l_data[tid] = (i < n) ? g_idata[i] : 0;
    barrier(CLK_LOCAL_MEM_FENCE);
    // do reduction in local memory
    for (unsigned int s=1; s < get_local_size(0); s*= 2) {
        if ((tid % (2*s)) == 0) {
            l_data[tid] += l_data[tid + s];
        }
        barrier(CLK_LOCAL_MEM_FENCE);
    }
    // write result for this work-group to global memory
    if (tid == 0) g_odata[get_group_id(0)] = l_data[0];
}
```

```
kernel void reduce0(global float* g_idata, global float* g_odata,
                    unsigned int n, local float* l_data) {
    unsigned int tid = get_local_id(0);
    unsigned int i   = get_global_id(0);
    l_data[tid] = (i < n) ? g_idata[i] : 0;
    barrier(CLK_LOCAL_MEM_FENCE);
    // do reduction in local memory
    for (unsigned int s=1; s < get_local_size(0); s*= 2) {
        if ((tid % (2*s)) == 0) {
            l_data[tid] += l_data[tid + s];
        }
        barrier(CLK_LOCAL_MEM_FENCE);
    }
    // write result for this work-group to global memory
    if (tid == 0) g_odata[get_group_id(0)] = l_data[0];
}
```

- Multiple *work-items* (threads) execute the same *kernel* function
- *Work-items* are organised for execution in *work-groups*

## Avoid Divergent Branching

```
kernel void reduce1(global float* g_idata, global float* g_odata,
                    unsigned int n, local float* l_data) {
    unsigned int tid = get_local_id(0);
    unsigned int i   = get_global_id(0);
    l_data[tid] = (i < n) ? g_idata[i] : 0;
    barrier(CLK_LOCAL_MEM_FENCE);

    for (unsigned int s=1; s < get_local_size(0); s*= 2) {
        // continuous work-items remain active
        int index = 2 * s * tid;
        if (index < get_local_size(0)) {
            l_data[index] += l_data[index + s];
        }
        barrier(CLK_LOCAL_MEM_FENCE);
    }
    if (tid == 0) g_odata[get_group_id(0)] = l_data[0];
}
```

## Avoid Interleaved Addressing

```
kernel void reduce2(global float* g_idata, global float* g_odata,
                   unsigned int n, local float* l_data) {
    unsigned int tid = get_local_id(0);
    unsigned int i = get_global_id(0);
    l_data[tid] = (i < n) ? g_idata[i] : 0;
    barrier(CLK_LOCAL_MEM_FENCE);

    // process elements in different order
    // requires commutativity
    for (unsigned int s=get_local_size(0)/2; s>0; s>>=1) {
        if (tid < s) {
            l_data[tid] += l_data[tid + s];
        }
        barrier(CLK_LOCAL_MEM_FENCE);
    }
    if (tid == 0) g_odata[get_group_id(0)] = l_data[0];
}
```

## Increase Computational Intensity per Work-Item

```
kernel void reduce3(global float* g_idata, global float* g_odata,
                   unsigned int n, local float* l_data) {
    unsigned int tid = get_local_id(0);
    unsigned int i = get_group_id(0) * (get_local_size(0)*2)
                  + get_local_id(0);
    l_data[tid] = (i < n) ? g_idata[i] : 0;
    // performs first addition during loading
    if (i + get_local_size(0) < n)
        l_data[tid] += g_idata[i+get_local_size(0)];
    barrier(CLK_LOCAL_MEM_FENCE);

    for (unsigned int s=get_local_size(0)/2; s>0; s>>=1) {
        if (tid < s) {
            l_data[tid] += l_data[tid + s];
        }
        barrier(CLK_LOCAL_MEM_FENCE);
    }
    if (tid == 0) g_odata[get_group_id(0)] = l_data[0];
}
```

## Avoid Synchronisation inside a Warp

```
kernel void reduce4(global float* g_idata, global float* g_odata,
                   unsigned int n, local volatile float* l_data) {
    unsigned int tid = get_local_id(0);
    unsigned int i = get_group_id(0) * (get_local_size(0)*2)
                  + get_local_id(0);
    l_data[tid] = (i < n) ? g_idata[i] : 0;
    if (i + get_local_size(0) < n)
        l_data[tid] += g_idata[i+get_local_size(0)];
    barrier(CLK_LOCAL_MEM_FENCE);

    # pragma unroll 1
    for (unsigned int s=get_local_size(0)/2; s>32; s>>=1) {
        if (tid < s) { l_data[tid] += l_data[tid + s]; }
        barrier(CLK_LOCAL_MEM_FENCE); }

    // this is not portable OpenCL code!
    if (tid < 32) {
        if (WG_SIZE >= 64) { l_data[tid] += l_data[tid+32]; }
        if (WG_SIZE >= 32) { l_data[tid] += l_data[tid+16]; }
        if (WG_SIZE >= 16) { l_data[tid] += l_data[tid+ 8]; }
        if (WG_SIZE >=  8) { l_data[tid] += l_data[tid+ 4]; }
        if (WG_SIZE >=  4) { l_data[tid] += l_data[tid+ 2]; }
        if (WG_SIZE >=  2) { l_data[tid] += l_data[tid+ 1]; } }
    if (tid == 0) g_odata[get_group_id(0)] = l_data[0];
}
```

## Complete Loop Unrolling

```
kernel void reduce5(global float* g_idata, global float* g_odata,
                   unsigned int n, local volatile float* l_data) {
    unsigned int tid = get_local_id(0);
    unsigned int i = get_group_id(0) * (get_local_size(0)*2)
                  + get_local_id(0);
    l_data[tid] = (i < n) ? g_idata[i] : 0;
    if (i + get_local_size(0) < n)
        l_data[tid] += g_idata[i+get_local_size(0)];
    barrier(CLK_LOCAL_MEM_FENCE);

    if (WG_SIZE >= 256) {
        if (tid < 128) { l_data[tid] += l_data[tid+128]; }
        barrier(CLK_LOCAL_MEM_FENCE); }
    if (WG_SIZE >= 128) {
        if (tid <  64) { l_data[tid] += l_data[tid+ 64]; }
        barrier(CLK_LOCAL_MEM_FENCE); }

    if (tid < 32) {
        if (WG_SIZE >= 64) { l_data[tid] += l_data[tid+32]; }
        if (WG_SIZE >= 32) { l_data[tid] += l_data[tid+16]; }
        if (WG_SIZE >= 16) { l_data[tid] += l_data[tid+ 8]; }
        if (WG_SIZE >=  8) { l_data[tid] += l_data[tid+ 4]; }
        if (WG_SIZE >=  4) { l_data[tid] += l_data[tid+ 2]; }
        if (WG_SIZE >=  2) { l_data[tid] += l_data[tid+ 1]; } }
    if (tid == 0) g_odata[get_group_id(0)] = l_data[0];
}
```

## Fully Optimised Implementation

```

kernel void reduce6(global float* g_idata, global float* g_odata,
                   unsigned int n, local volatile float* l_data) {
    unsigned int tid = get_local_id(0);
    unsigned int i = get_group_id(0) * (get_local_size(0)*2)
                    + get_local_id(0);

    unsigned int gridSize = WG_SIZE * get_num_groups(0);
    l_data[tid] = 0;
    while (i < n) { l_data[tid] += g_idata[i];
                      if (i + WG_SIZE < n)
                          l_data[tid] += g_idata[i+WG_SIZE];
                      i += gridSize; }
    barrier(CLK_LOCAL_MEM_FENCE);

    if (WG_SIZE >= 256) {
        if (tid < 128) { l_data[tid] += l_data[tid+128]; }
        barrier(CLK_LOCAL_MEM_FENCE); }

    if (WG_SIZE >= 128) {
        if (tid < 64) { l_data[tid] += l_data[tid+ 64]; }
        barrier(CLK_LOCAL_MEM_FENCE); }

    if (tid < 32) {
        if (WG_SIZE >= 64) { l_data[tid] += l_data[tid+32]; }
        if (WG_SIZE >= 32) { l_data[tid] += l_data[tid+16]; }
        if (WG_SIZE >= 16) { l_data[tid] += l_data[tid+ 8]; }
        if (WG_SIZE >= 8) { l_data[tid] += l_data[tid+ 4]; }
        if (WG_SIZE >= 4) { l_data[tid] += l_data[tid+ 2]; }
        if (WG_SIZE >= 2) { l_data[tid] += l_data[tid+ 1]; }
    }

    if (tid == 0) g_odata[get_group_id(0)] = l_data[0];
}

```

## Case Study Conclusions

- Optimising OpenCL is complex
  - Understanding of target hardware required
- Program changes not obvious
- Is it worth it? ...

```

kernel
void reduce0(global float* g_idata,
             global float* g_odata,
             unsigned int n,
             local float* l_data) {
    unsigned int tid = get_local_id(0);
    unsigned int i = get_global_id(0);
    l_data[tid] = (i < n) ? g_idata[i] : 0;
    barrier(CLK_LOCAL_MEM_FENCE);

    for (unsigned int s=1;
         s < get_local_size(0); s*= 2) {
        if ((tid % (2*s)) == 0) {
            l_data[tid] += l_data[tid + s];
        }
        barrier(CLK_LOCAL_MEM_FENCE);
    }

    if (tid == 0)
        g_odata[get_group_id(0)] = l_data[0];
}

```

Unoptimized Implementation

```

kernel
void reduce6(global float* g_idata,
             global float* g_odata,
             unsigned int n,
             local volatile float* l_data) {
    unsigned int tid = get_local_id(0);
    unsigned int i =
        get_group_id(0) * (get_local_size(0)*2)
        + get_local_id(0);

    unsigned int gridSize =
        WG_SIZE * get_num_groups(0);
    l_data[tid] = 0;
    while (i < n) {
        l_data[tid] += g_idata[i];
        if (i + WG_SIZE < n)
            l_data[tid] += g_idata[i+WG_SIZE];
        i += gridSize; }
    barrier(CLK_LOCAL_MEM_FENCE);

    if (WG_SIZE >= 256) {
        if (tid < 128) {
            l_data[tid] += l_data[tid+128]; }
        barrier(CLK_LOCAL_MEM_FENCE); }

    if (WG_SIZE >= 128) {
        if (tid < 64) {
            l_data[tid] += l_data[tid+ 64]; }
        barrier(CLK_LOCAL_MEM_FENCE); }

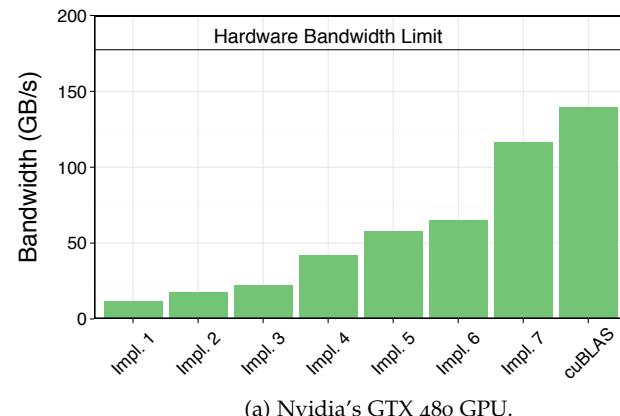
    if (tid < 32) {
        if (WG_SIZE >= 64) {
            l_data[tid] += l_data[tid+32]; }
        if (WG_SIZE >= 32) {
            l_data[tid] += l_data[tid+16]; }
        if (WG_SIZE >= 16) {
            l_data[tid] += l_data[tid+ 8]; }
        if (WG_SIZE >= 8) {
            l_data[tid] += l_data[tid+ 4]; }
        if (WG_SIZE >= 4) {
            l_data[tid] += l_data[tid+ 2]; }
        if (WG_SIZE >= 2) {
            l_data[tid] += l_data[tid+ 1]; }
    }

    if (tid == 0)
        g_odata[get_group_id(0)] = l_data[0];
}

```

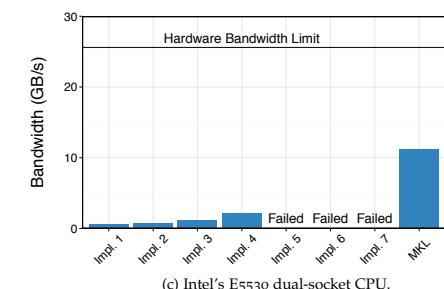
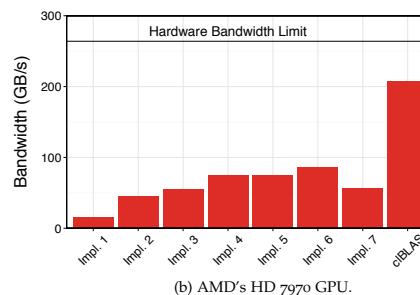
Fully Optimized Implementation

## Performance Results Nvidia



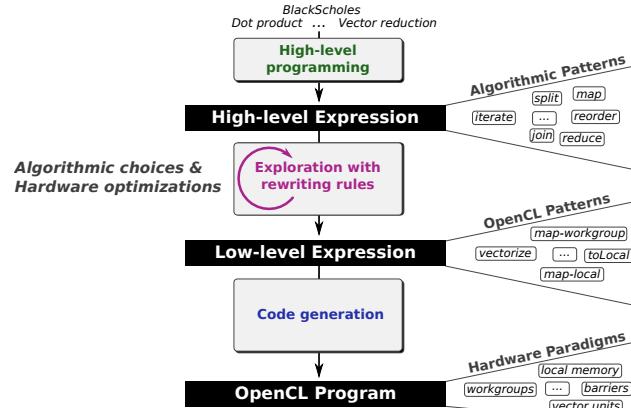
- ... Yes! Optimising improves performance by a factor of 10!
- Optimising is important, but ...

## Performance Results AMD and Intel



- ... unfortunately, optimisations in OpenCL are not portable!
- **Challenge:** how to achieving portable performance?

# Generating Performance Portable Code using Rewrite Rules



- Goal: automatic generation of *Performance Portable* code

Michel Steuwer, Christian Fensch, Sam Lindley, Christophe Dubach:  
*"Generating performance portable code using rewrite rules:  
from high-level functional expressions to high-performance OpenCL code."*  
ICFP 2015

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## Example Parallel Reduction ③

$$① \quad \text{vecSum} = \text{reduce } (+) \ 0$$

②

```
vecSum = reduce ∘ join ∘ map-workgroup (
  join ∘ toGlobal (map-local (map-seq id)) ∘ split 1 ∘
  join ∘ map-warp (
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 1 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 2 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 4 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 8 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 16 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 32 ∘
  ) ∘ split 64 ∘
  join ∘ map-local (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 64 ∘
  join ∘ toLocal (map-local (reduce-seq (+) 0)) ∘
  split (blockSize/128) ∘ reorder-stride 128 ∘
) ∘ split blockSize
```

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## Example Parallel Reduction ③

$$① \quad \text{vecSum} = \text{reduce } (+) \ 0$$

rewrite rules

code generation

②

```
vecSum = reduce ∘ join ∘ map-workgroup (
  join ∘ toGlobal (map-local (map-seq id)) ∘ split 1 ∘
  join ∘ map-warp (
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 1 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 2 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 4 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 8 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 16 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 32 ∘
  ) ∘ split 64 ∘
  join ∘ map-local (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 64 ∘
  join ∘ toLocal (map-local (reduce-seq (+) 0)) ∘
  split (blockSize/128) ∘ reorder-stride 128 ∘
) ∘ split blockSize
```

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```
kernel
void reduce6(global float* g_idata,
            global float* g_odata,
            unsigned int n,
            local volatile float* l_data) {
  unsigned int tid = get_local_id(0);
  unsigned int i =
    get_group_id(0) * (get_local_size(0)*2)
    + get_local_id(0);
  unsigned int gridSize =
    WG_SIZE * get_num_groups(0);
  l_data[tid] = 0;
  while (i < n) {
    l_data[tid] += g_idata[i];
    if (i + WG_SIZE < n)
      l_data[tid] += g_idata[i+WG_SIZE];
    i += gridSize;
    barrier(CLK_LOCAL_MEM_FENCE);

    if (WG_SIZE >= 256) {
      if (tid < 128) {
        l_data[tid] += l_data[tid+128];
        barrier(CLK_LOCAL_MEM_FENCE);
      }
    if (WG_SIZE >= 128) {
      if (tid < 64) {
        l_data[tid] += l_data[tid+64];
        barrier(CLK_LOCAL_MEM_FENCE);
      }
    if (tid < 32) {
      if (WG_SIZE >= 64) {
        l_data[tid] += l_data[tid+32];
        if (WG_SIZE >= 32) {
          l_data[tid] += l_data[tid+16];
        }
      if (WG_SIZE >= 16) {
        l_data[tid] += l_data[tid+8];
      }
      if (WG_SIZE >= 8) {
        l_data[tid] += l_data[tid+4];
      }
      if (WG_SIZE >= 4) {
        l_data[tid] += l_data[tid+2];
      }
      if (WG_SIZE >= 2) {
        l_data[tid] += l_data[tid+1];
      }
    }
    if (tid == 0)
      g_odata[get_group_id(0)] = l_data[0];
  }
```

## ① Algorithmic Primitives

$$\text{map}_{A,B,I} : (A \rightarrow B) \rightarrow [A]_I \rightarrow [B]_I$$

$$\text{zip}_{A,B,I} : [A]_I \rightarrow [B]_I \rightarrow [A \times B]_I$$

$$\text{reduce}_{A,I} : ((A \times A) \rightarrow A) \rightarrow A \rightarrow [A]_I \rightarrow [A]_1$$

$$\text{split}_{A,I} : (n : \text{size}) \rightarrow [A]_{n \times I} \rightarrow [[A]]_n$$

$$\text{join}_{A,I,J} : [[A]]_J \rightarrow [A]_{I \times J}$$

$$\begin{aligned} \text{iterate}_{A,I,J} : (n : \text{size}) \rightarrow ([A]_{I \times m} \rightarrow [A]_m) \rightarrow \\ [A]_{I^n \times J} \rightarrow [A]_J \end{aligned}$$

$$\text{reorder}_{A,I} : [A]_I \rightarrow [A]_I$$

# ① High-Level Programs

$scal = \lambda a. map (*a)$

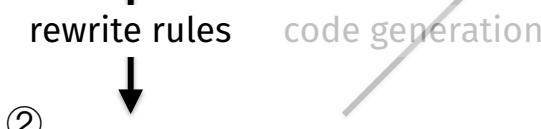
$asum = reduce (+) 0 \circ map abs$

$dot = \lambda xs ys. (reduce (+) 0 \circ map (*)) (zip xs ys)$

$gemv = \lambda mat xs ys \alpha \beta. map (+) ($   
 $zip (map (scal \alpha \circ dot xs) mat) (scal \beta ys) )$

# Example Parallel Reduction ③

①  $vecSum = reduce (+) 0$



②

```
vecSum = reduce ∘ join ∘ map-workgroup (
  join ∘ toGlobal (map-local (map-seq id)) ∘ split 1 ∘
  join ∘ map-warp (
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 1 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 2 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 4 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 8 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 16 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 32 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 64 ∘
    join ∘ map-local (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 64 ∘
    join ∘ toLocal (map-local (reduce-seq (+) 0)) ∘
    split (blockSize/128) ∘ reorder-stride 128
  ) ∘ split blockSize
```

# Example Parallel Reduction ③

①  $vecSum = reduce (+) 0$

↓ rewrite rules      code generation

②

```
vecSum = reduce ∘ join ∘ map-workgroup (
  join ∘ toGlobal (map-local (map-seq id)) ∘ split 1 ∘
  join ∘ map-warp (
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 1 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 2 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 4 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 8 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 16 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 32 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 64 ∘
    join ∘ map-local (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 64 ∘
    join ∘ toLocal (map-local (reduce-seq (+) 0)) ∘
    split (blockSize/128) ∘ reorder-stride 128
  ) ∘ split blockSize
```

# ② Algorithmic Rewrite Rules

- Provably correct rewrite rules
- Express algorithmic implementation choices

Split-join rule:

$$map f \rightarrow join \circ map (map f) \circ split n$$

Map fusion rule:

$$map f \circ map g \rightarrow map (f \circ g)$$

Reduce rules:

$$reduce f z \rightarrow reduce f z \circ reducePart f z$$

$$reducePart f z \rightarrow reducePart f z \circ reorder$$

$$reducePart f z \rightarrow join \circ map (reducePart f z) \circ split n$$

$$reducePart f z \rightarrow iterate n (reducePart f z)$$

```
kernel
void reduce6(global float* g_idata,
            global float* g_odata,
            unsigned int n,
            local volatile float* l_data) {
  unsigned int tid = get_local_id(0);
  unsigned int i =
    get_group_id(0) * (get_local_size(0)*2)
    + get_local_id(0);
  unsigned int gridSize =
    WG_SIZE * get_num_groups(0);
  l_data[tid] = 0;
  while (i < n) {
    l_data[tid] += g_idata[i];
    if (i + WG_SIZE < n)
      l_data[tid] += g_idata[i+WG_SIZE];
    i += gridSize; }
    barrier(CLK_LOCAL_MEM_FENCE);

  if (WG_SIZE >= 256) {
    if (tid < 128) {
      l_data[tid] += l_data[tid+128]; }
    barrier(CLK_LOCAL_MEM_FENCE); }
  if (WG_SIZE >= 128) {
    if (tid < 64) {
      l_data[tid] += l_data[tid+64]; }
    barrier(CLK_LOCAL_MEM_FENCE); }
  if (tid < 32) {
    if (WG_SIZE >= 64) {
      l_data[tid] += l_data[tid+32]; }
    if (WG_SIZE >= 32) {
      l_data[tid] += l_data[tid+16]; }
    if (WG_SIZE >= 16) {
      l_data[tid] += l_data[tid+ 8]; }
    if (WG_SIZE >= 8) {
      l_data[tid] += l_data[tid+ 4]; }
    if (WG_SIZE >= 4) {
      l_data[tid] += l_data[tid+ 2]; }
    if (WG_SIZE >= 2) {
      l_data[tid] += l_data[tid+ 1]; }
  }
  if (tid == 0)
    g_odata[get_group_id(0)] = l_data[0];
}
```

## ② OpenCL Primitives

### Primitive

*mapGlobal*

*mapWorkgroup*

*mapLocal*

*mapSeq*

*reduceSeq*

*toLocal*, *toGlobal*

*mapVec*,  
*splitVec*, *joinVec*

### OpenCL concept

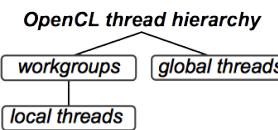
Work-items

Work-groups

Sequential implementations

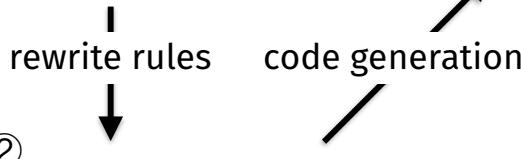
Memory areas

Vectorization



## Example Parallel Reduction ③

①  $\text{vecSum} = \text{reduce } (+) 0$



②

```

vecSum = reduce ∘ join ∘ map-workgroup (
  join ∘ toGlobal (map-local (map-seq id)) ∘ split 1 ∘
  join ∘ map-warp (
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 1 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 2 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 4 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 8 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 16 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 32 ∘
  ) ∘ join ∘ map-local (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 64 ∘
  join ∘ toLocal (map-local (reduce-seq (+) 0)) ∘
  split (blockSize/128) ∘ reorder-stride 128 ∘
  ) ∘ split blockSize
  
```

```

kernel
void reduce6(global float* g_idata,
             global float* g_odata,
             unsigned int n,
             local volatile float* l_data) {
    unsigned int tid = get_local_id(0);
    unsigned int i = get_group_id(0) * (get_local_size(0)*2)
                  + get_local_id(0);
    unsigned int gridSize =
      WG_SIZE * get_num_groups(0);
    l_data[tid] = 0;
    while (i < n) {
        l_data[tid] += g_idata[i];
        if (i + WG_SIZE < n)
            l_data[tid] += g_idata[i+WG_SIZE];
        i += gridSize; }
    barrier(CLK_LOCAL_MEM_FENCE);
}

if (WG_SIZE >= 256) {
    if (tid < 128) {
        l_data[tid] += l_data[tid+128]; }
    barrier(CLK_LOCAL_MEM_FENCE); }
if (WG_SIZE >= 128) {
    if (tid < 64) {
        l_data[tid] += l_data[tid+ 64]; }
    barrier(CLK_LOCAL_MEM_FENCE); }
if (tid < 32) {
    if (WG_SIZE >= 64) {
        l_data[tid] += l_data[tid+32]; }
    if (WG_SIZE >= 32) {
        l_data[tid] += l_data[tid+16]; }
    if (WG_SIZE >= 16) {
        l_data[tid] += l_data[tid+ 8]; }
    if (WG_SIZE >= 8) {
        l_data[tid] += l_data[tid+ 4]; }
    if (WG_SIZE >= 4) {
        l_data[tid] += l_data[tid+ 2]; }
    if (WG_SIZE >= 2) {
        l_data[tid] += l_data[tid+ 1]; } }
    if (tid == 0)
        g_odata[get_group_id(0)] = l_data[0];
}
  
```

## ② OpenCL Rewrite Rules

- Express low-level implementation and optimisation choices

### Map rules:

*map f*  $\rightarrow$  *map Workgroup f* | *mapLocal f* | *mapGlobal f* | *mapSeq f*

### Local/ global memory rules:

*mapLocal f*  $\rightarrow$  *toLocal (mapLocal f)*

*mapLocal f*  $\rightarrow$  *toGlobal (mapLocal f)*

### Vectorisation rule:

*map f*  $\rightarrow$  *join Vec*  $\circ$  *map (mapVec f)*  $\circ$  *splitVec n*

### Fusion rule:

*reduceSeq f z*  $\circ$  *mapSeq g*  $\rightarrow$  *reduceSeq (λ (acc, x). f (acc, g x)) z*

## Example Parallel Reduction ③

①  $\text{vecSum} = \text{reduce } (+) 0$



②

```

vecSum = reduce ∘ join ∘ map-workgroup (
  join ∘ toGlobal (map-local (map-seq id)) ∘ split 1 ∘
  join ∘ map-warp (
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 1 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 2 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 4 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 8 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 16 ∘
    join ∘ map-lane (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 32 ∘
  ) ∘ join ∘ map-local (reduce-seq (+) 0) ∘ split 2 ∘ reorder-stride 64 ∘
  join ∘ toLocal (map-local (reduce-seq (+) 0)) ∘
  split (blockSize/128) ∘ reorder-stride 128 ∘
  ) ∘ split blockSize
  
```

```

kernel
void reduce6(global float* g_idata,
             global float* g_odata,
             unsigned int n,
             local volatile float* l_data) {
    unsigned int tid = get_local_id(0);
    unsigned int i = get_group_id(0) * (get_local_size(0)*2)
                  + get_local_id(0);
    unsigned int gridSize =
      WG_SIZE * get_num_groups(0);
    l_data[tid] = 0;
    while (i < n) {
        l_data[tid] += g_idata[i];
        if (i + WG_SIZE < n)
            l_data[tid] += g_idata[i+WG_SIZE];
        i += gridSize; }
    barrier(CLK_LOCAL_MEM_FENCE);
}

if (WG_SIZE >= 256) {
    if (tid < 128) {
        l_data[tid] += l_data[tid+128]; }
    barrier(CLK_LOCAL_MEM_FENCE); }
if (WG_SIZE >= 128) {
    if (tid < 64) {
        l_data[tid] += l_data[tid+ 64]; }
    barrier(CLK_LOCAL_MEM_FENCE); }
if (tid < 32) {
    if (WG_SIZE >= 64) {
        l_data[tid] += l_data[tid+32]; }
    if (WG_SIZE >= 32) {
        l_data[tid] += l_data[tid+16]; }
    if (WG_SIZE >= 16) {
        l_data[tid] += l_data[tid+ 8]; }
    if (WG_SIZE >= 8) {
        l_data[tid] += l_data[tid+ 4]; }
    if (WG_SIZE >= 4) {
        l_data[tid] += l_data[tid+ 2]; }
    if (WG_SIZE >= 2) {
        l_data[tid] += l_data[tid+ 1]; } }
    if (tid == 0)
        g_odata[get_group_id(0)] = l_data[0];
}
  
```

### ③ Pattern based OpenCL Code Generation

- Generate OpenCL code for each OpenCL primitive

*mapGlobal f xs* →

```
for (int g_id = get_global_id(0); g_id < n;
     g_id += get_global_size(0)) {
    output[g_id] = f(xs[g_id]);
}
```

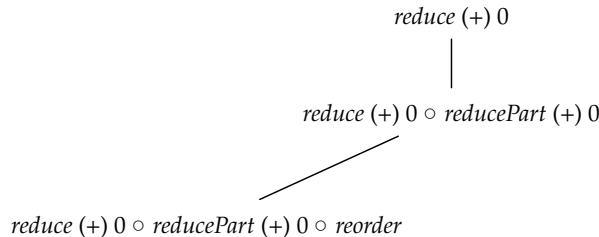
*reduceSeq f z xs* →

```
T acc = z;
for (int i = 0; i < n; ++i) {
    acc = f(acc, xs[i]);
}
```

:

:

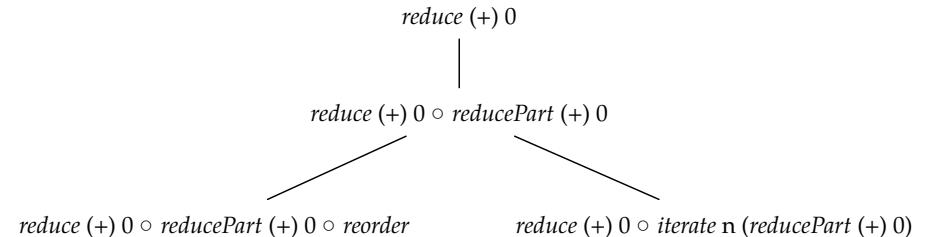
### Rewrite rules define a space of possible implementations



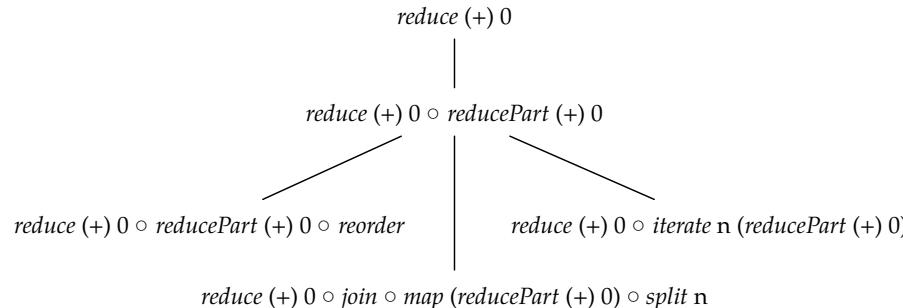
### Rewrite rules define a space of possible implementations

reduce (+) 0  
|  
reduce (+) 0 ○ reducePart (+) 0

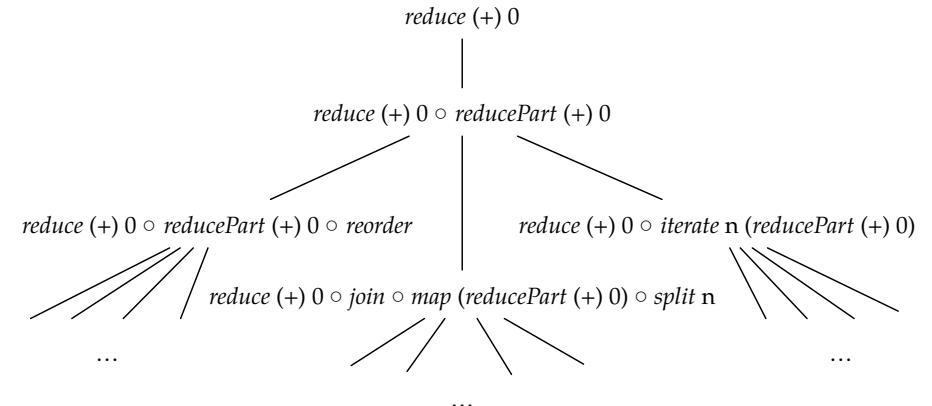
### Rewrite rules define a space of possible implementations



## Rewrite rules define a space of possible implementations



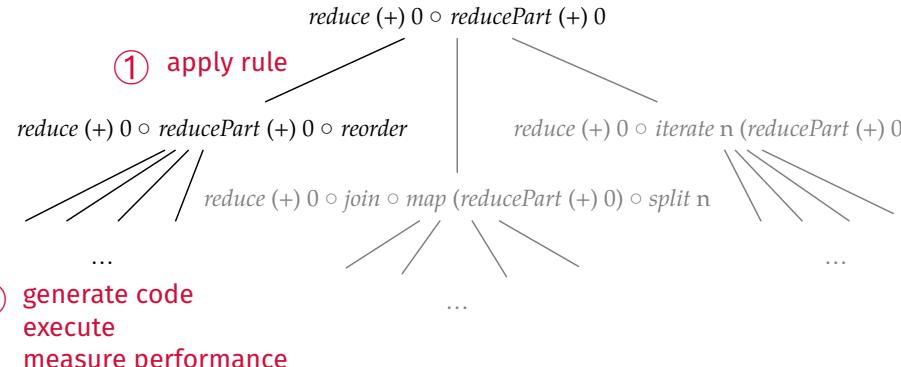
## Rewrite rules define a space of possible implementations



- Fully automated search for good implementations possible

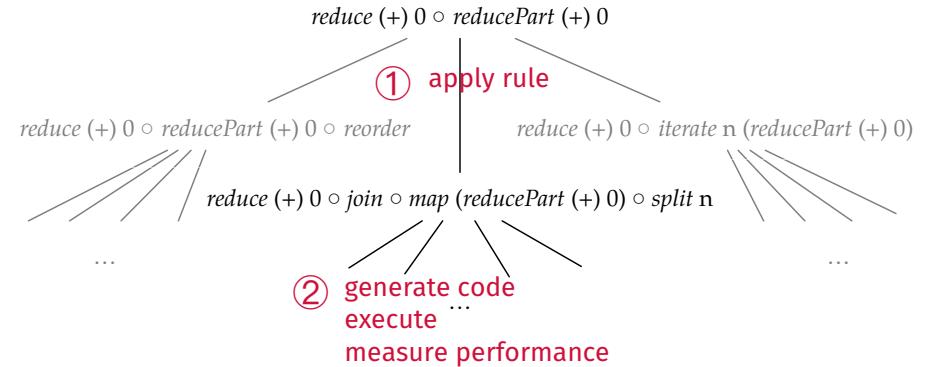
## Search Strategy

- For each node in the tree:
  - Apply one rule and randomly sample subtree
  - Repeat for node with best performing subtree



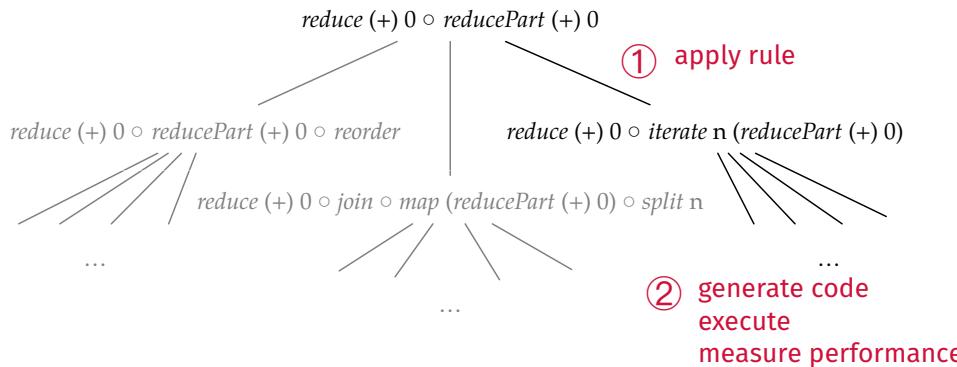
## Search Strategy

- For each node in the tree:
  - Apply one rule and randomly sample subtree
  - Repeat for node with best performing subtree



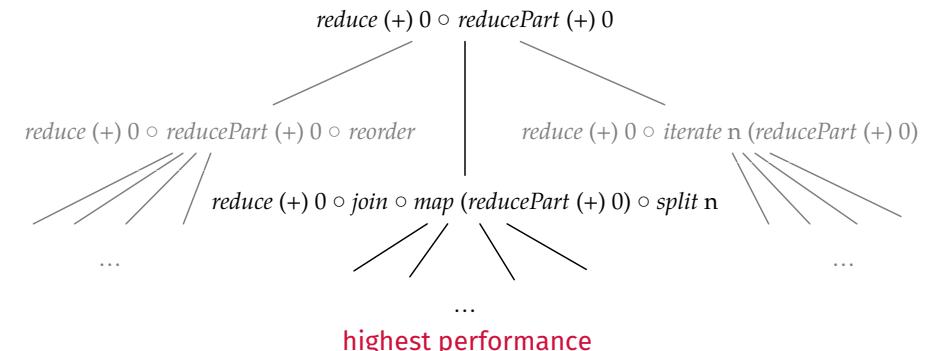
## Search Strategy

- For each node in the tree:
  - Apply one rule and randomly sample subtree
  - Repeat for node with best performing subtree



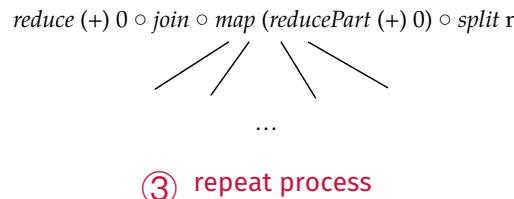
## Search Strategy

- For each node in the tree:
  - Apply one rule and randomly sample subtree
  - Repeat for node with best performing subtree



## Search Strategy

- For each node in the tree:
  - Apply one rule and randomly sample subtree
  - Repeat for node with best performing subtree



## Search Results Automatically Found Expressions

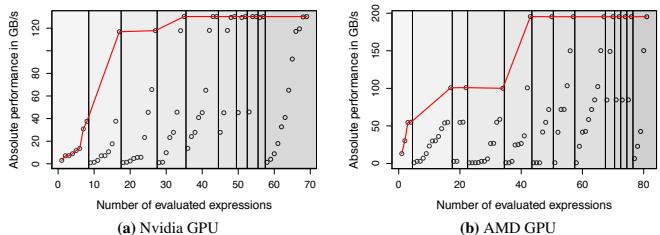
$asum = reduce (+) 0 ○ map abs$



Nvidia GPU	$\lambda x.(reduceSeq ○ join ○ mapWorkgroup (toGlobal (mapLocal (reduceSeq (\lambda(a, b). a + (abs b)) 0)) ○ reorderStride 2048) ○ split 128 ○ split 2048) x$
AMD GPU	$\lambda x.(reduceSeq ○ join ○ joinVec ○ join ○ mapWorkgroup (mapLocal (reduceSeq (mapVec 2 (\lambda(a, b). a + (abs b))) 0 ○ reorderStride 2048) ○ split 128 ○ splitVec 2 ○ split 4096) x$
Intel CPU	$\lambda x.(reduceSeq ○ join ○ mapWorkgroup (join ○ joinVec ○ mapLocal (reduceSeq (mapVec 4 (\lambda(a, b). a + (abs b))) 0 ○ splitVec 4 ○ split 32768) ○ split 32768) x$

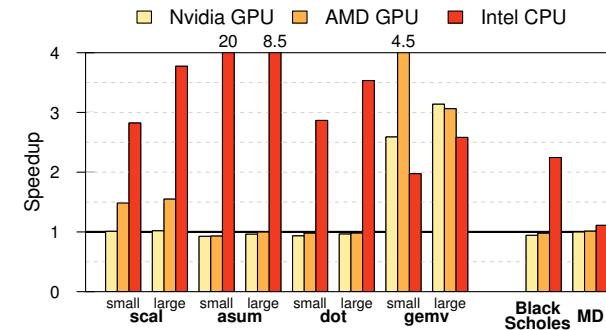
- Search on: **Nvidia GTX 480 GPU, AMD Radeon HD 7970 GPU, Intel Xeon E5530 CPU**

## Search Results Search Efficiency



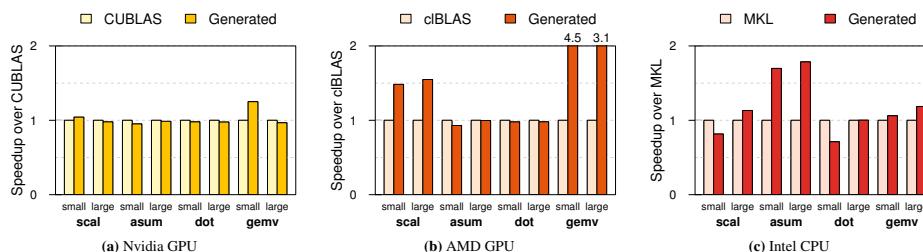
- Overall search on each platform took < 1 hour
- Average execution time per tested expression < 1/2 second

## Performance Results vs. Portable Implementation



- Up to 20x speedup on fairly simple benchmarks vs. portable cBLAS implementation

## Performance Results vs. Hardware-Specific Implementations



- Automatically generated code vs. expert written code
- Competitive performance vs. highly optimised implementations
- Up to 4.5x speedup for gemv on AMD

## Summary

- DSLs simplify programming but also enable optimisation opportunities
- Algorithmic skeletons allow for structured parallel programming
- OpenCL code is not *performance portable*
- Our code generation approach uses
  - functional high-level primitives,**
  - OpenCL-specific low-level primitives,** and
  - rewrite-rules** to generate *performance portable* code.
- Rewrite-rules define a space of possible implementations
- Performance on par with specialised, highly-tuned code