

# EXPERIMENT 3

## Analytical Method

```
In [8]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt

# Load the dataset
df = pd.read_csv(r'C:\Users\hp\OneDrive\Desktop\housing.csv') # Update the path to your dataset

# Select relevant columns (Area as the independent variable and Price as the dependent variable)
X = df['area'].values
y = df['price'].values

# Add a column of ones to include the intercept (bias) in the model
X_b = np.c_[np.ones((len(X), 1)), X]

# Analytical method:  $\theta = (X^T X)^{-1} X^T y$ 
theta_best = np.linalg.inv(X_b.T.dot(X_b)).dot(X_b.T).dot(y)

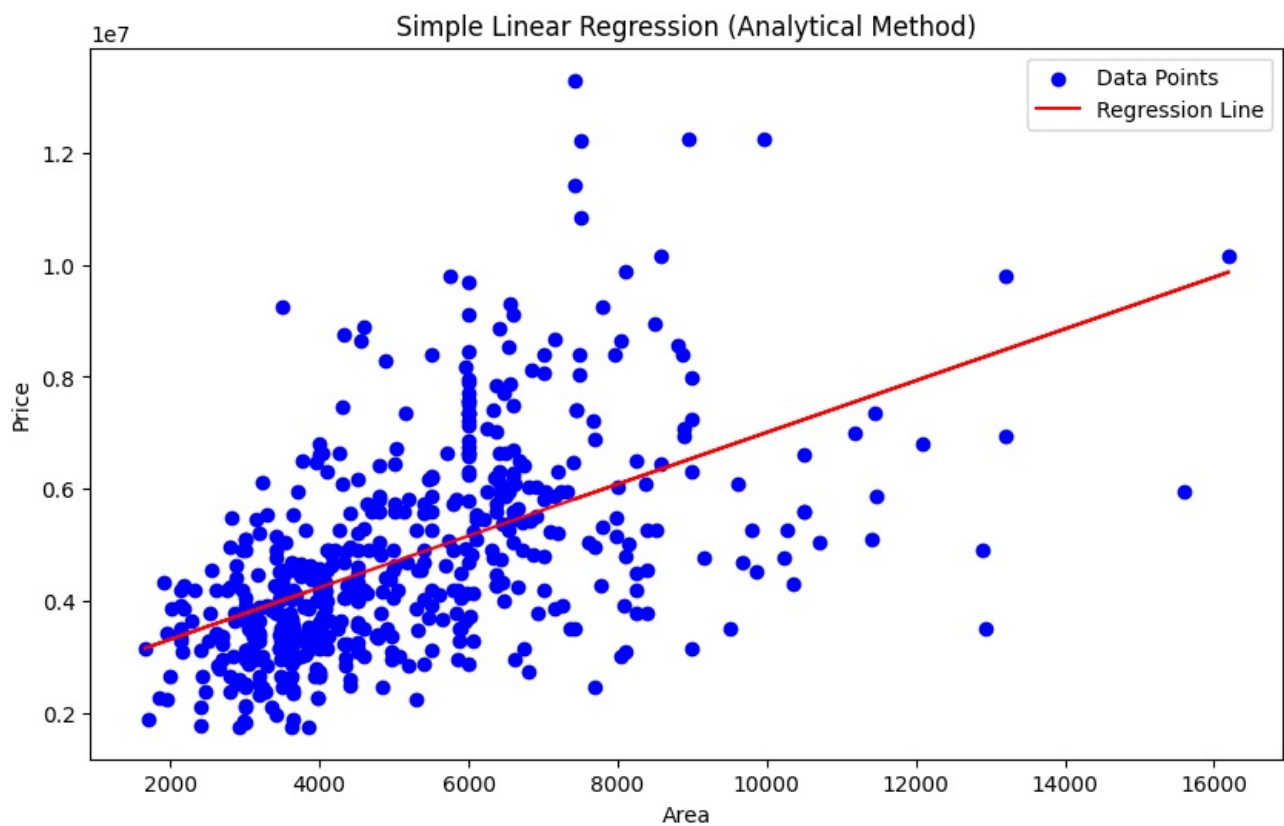
print("Optimal parameters (theta):", theta_best)

# Make predictions
y_pred = X_b.dot(theta_best)

# Plotting the data points and the regression line
plt.figure(figsize=(10, 6))
plt.scatter(X, y, color='blue', label='Data Points')
plt.plot(X, y_pred, color='red', label='Regression Line')
plt.xlabel('Area')
plt.ylabel('Price')
plt.title('Simple Linear Regression (Analytical Method)')
plt.legend()
plt.show()

# Print steps of analytical solution
print("\nSteps of Analytical Solution:")
print("1. Compute  $X^T X$ :")
X_T_X = X_b.T.dot(X_b)
print(X_T_X)
print("\n2. Compute  $(X^T X)^{-1}$ :")
X_T_X_inv = np.linalg.inv(X_T_X)
print(X_T_X_inv)
print("\n3. Compute  $X^T y$ :")
X_T_y = X_b.T.dot(y)
print(X_T_y)
print("\n4. Compute  $\theta = (X^T X)^{-1} X^T y$ :")
print(theta_best)
```

Optimal parameters (theta): [2.38730848e+06 4.61974894e+02]



Steps of Analytical Solution:

1. Compute  $X^T * X$ :

```
[[5.45000000e+02 2.80704500e+06]
 [2.80704500e+06 1.70197757e+10]]
```

2. Compute  $(X^T * X)^{-1}$ :

```
[[ 1.21894053e-02 -2.01037956e-06]
 [-2.01037956e-06  3.90323938e-10]]
```

3. Compute  $X^T * y$ :

```
[2.59786744e+09 1.45639914e+13]
```

4. Compute  $\theta = (X^T * X)^{-1} * X^T * y$ :

```
[2.38730848e+06 4.61974894e+02]
```

## Machine learning Method

```
In [9]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt

# Load the dataset
df = pd.read_csv(r'C:\Users\hp\OneDrive\Desktop\housing.csv') # Update the path to your dataset
```

```

# Select relevant columns (Area as the independent variable and Price as the dependent variable)
X = df['area'].values
y = df['price'].values

# Normalize the features for better performance
X = (X - X.mean()) / X.std()

# Add a column of ones to include the intercept (bias) in the model
X_b = np.c_[np.ones((len(X), 1)), X]

# Gradient Descent parameters
learning_rate = 0.01
n_iterations = 1000
m = len(X)

# Initialize theta (weights)
theta = np.random.randn(2)

# Gradient Descent Loop
print(f"{'Iteration':<10}{'Theta0':<15}{'Theta1':<15}{'Cost Function':<15}")
print("-" * 45)

for iteration in range(n_iterations):
    gradients = 2/m * X_b.T.dot(X_b.dot(theta) - y)
    theta = theta - learning_rate * gradients
    cost = np.sum((X_b.dot(theta) - y) ** 2) / (2 * m)

    if iteration % 100 == 0: # Print every 100 iterations
        print(f"{'iteration':<10}{'theta[0]':<15.4f}{'theta[1]':<15.4f}{'cost':<20.4f}")

print("\nOptimal parameters (theta):", theta)

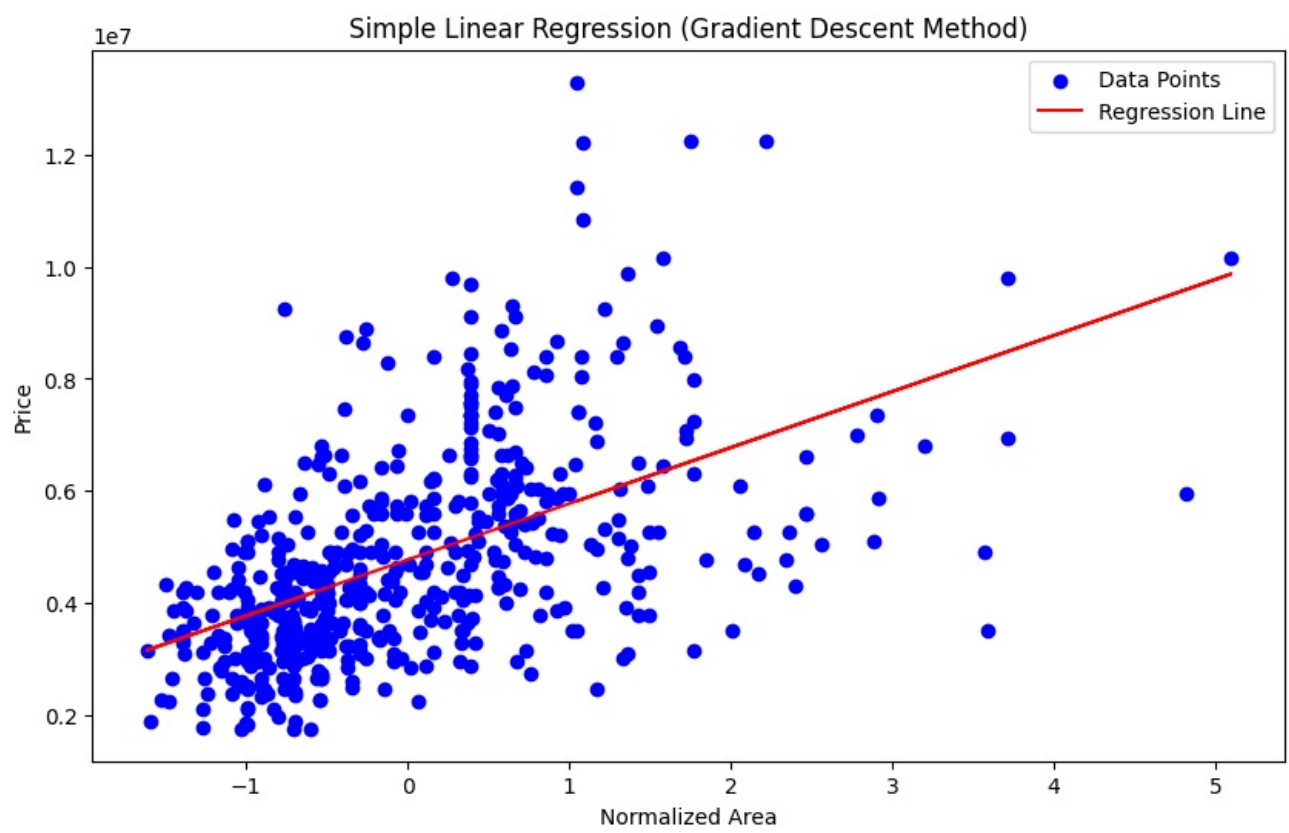
# Make predictions
y_pred = X_b.dot(theta)

# Plotting the data points and the regression line
plt.figure(figsize=(10, 6))
plt.scatter(X, y, color='blue', label='Data Points')
plt.plot(X, y_pred, color='red', label='Regression Line')
plt.xlabel('Normalized Area')
plt.ylabel('Price')
plt.title('Simple Linear Regression (Gradient Descent Method)')
plt.legend()
plt.show()

```

Iteration	Theta0	Theta1	Cost Function
0	95334.3807	20031.7703	12637163710153.3242
100	4147210.9350	871451.2915	1444805478982.1462
200	4684569.0042	984366.1703	1247954880020.1990
300	4755833.1927	999340.8913	1244492682196.3521
400	4765284.2177	1001326.8322	1244431789245.8879
500	4766537.6085	1001590.2068	1244430718263.9263
600	4766703.8326	1001625.1354	1244430699427.5530
700	4766725.8772	1001629.7676	1244430699096.2595
800	4766728.8007	1001630.3819	1244430699090.4329
900	4766729.1884	1001630.4634	1244430699090.3306

Optimal parameters (theta): [4766729.23968417 1001630.47418752]



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