

```
In [5]: import sympy as sp
import math
```

```
In [3]: x = sp.Symbol('x')
```

```
In [4]: f = sp.Function('f')
```

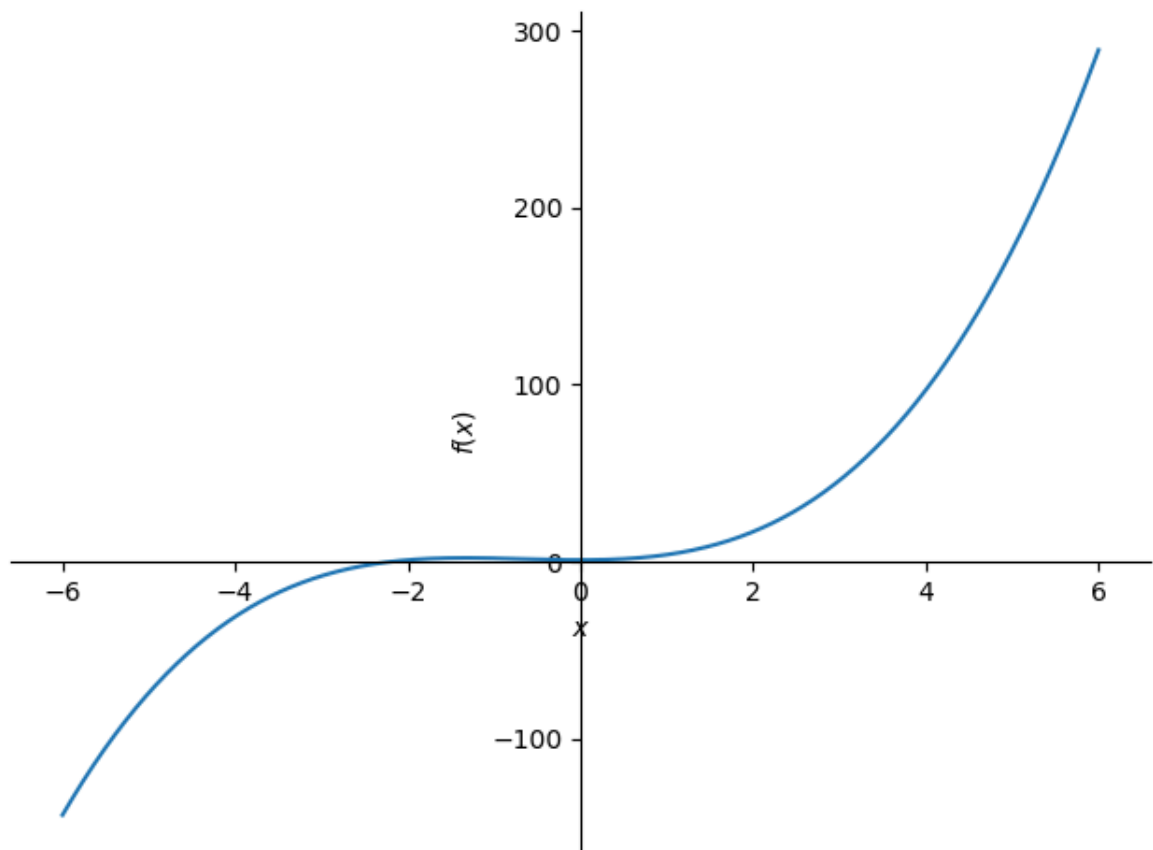
```
In [6]: f = pow(x,3) + 2*x**2 + 1
```

```
In [7]: display(f)
```

$$x^3 + 2x^2 + 1$$

```
In [9]: display(r'la courbe de f pour x = [-6,6]')
sp.plot(f,(x,-6,6))
```

'la courbe de f pour x = [-6,6]'

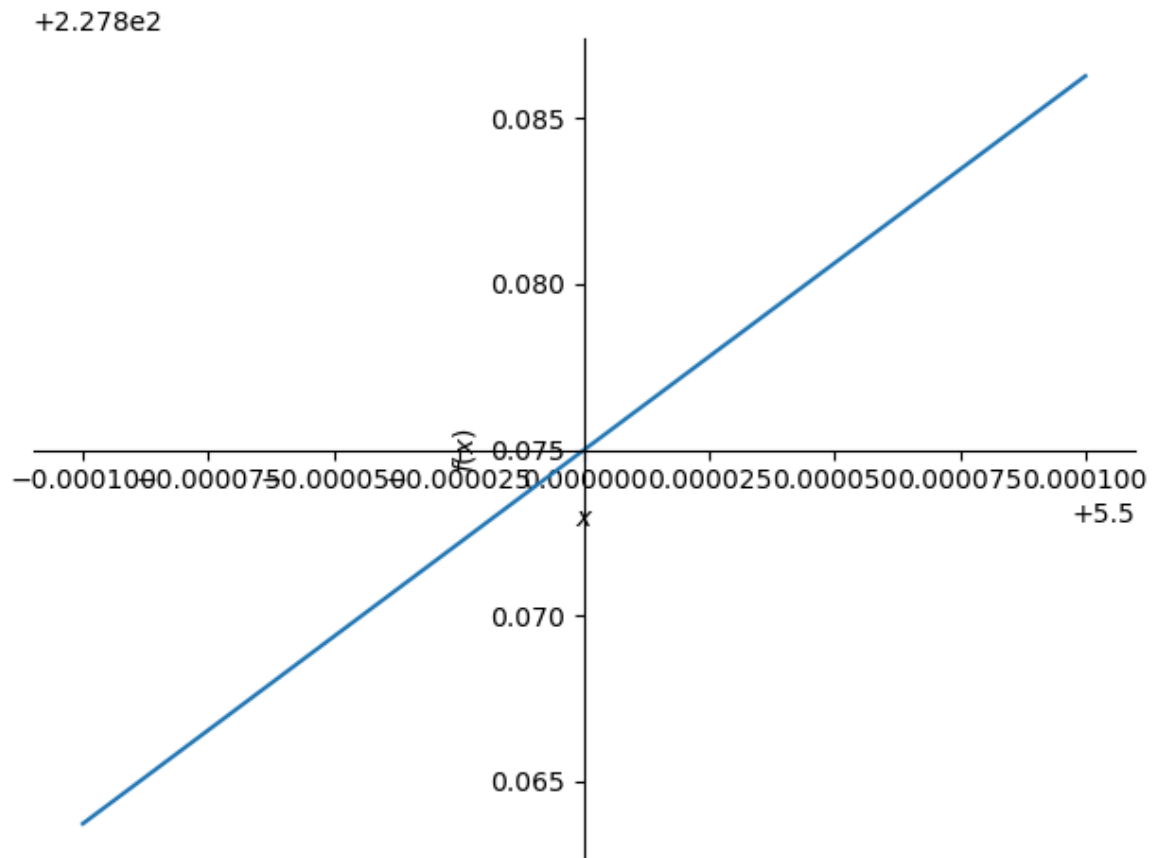


```
Out[9]: <sympy.plotting.backends.matplotlibbackend.matplotlib.MatplotlibBackend at 0x20e4c49dd00>
```

```
In [11]: display(r'la courbe de f pour x = [5.4999,5.5001]')
```

'la courbe de f pour x = [5.4999,5.5001]'

```
In [13]: sp.plot(f,(x,5.4999,5.5001))
```



Out[13]: <sympy.plotting.backends.matplotlibbackend.matplotlib.MatplotlibBackend at 0x20e4ef4b5f0>

```
In [15]: Vgauche = [5.4999, 5.49999, 5.499999]
Vdroite = [5.500001, 5.50001, 5.5001]
print('Limite à gauche')
Ugauche = [f.subs(x,i) for i in Vgauche]
print(Vgauche)
print(Ugauche)
```

Limite à gauche  
[5.4999, 5.49999, 5.499999]  
[227.863725184999, 227.873872501850, 227.874887250018]

```
In [16]: print('limite à droite')
Udroite = [f.subs(x,i) for i in Vdroite]
print(Vdroite)
print(Udroite)
```

limite à droite  
[5.500001, 5.50001, 5.5001]  
[227.875112750019, 227.876127501850, 227.886275185001]

```
In [19]: print(sp.limit(f,x,5.5,'-'))
```

227.875000000000

```
In [20]: print(sp.limit(f,x,5.5,'+'))
```

227.875000000000

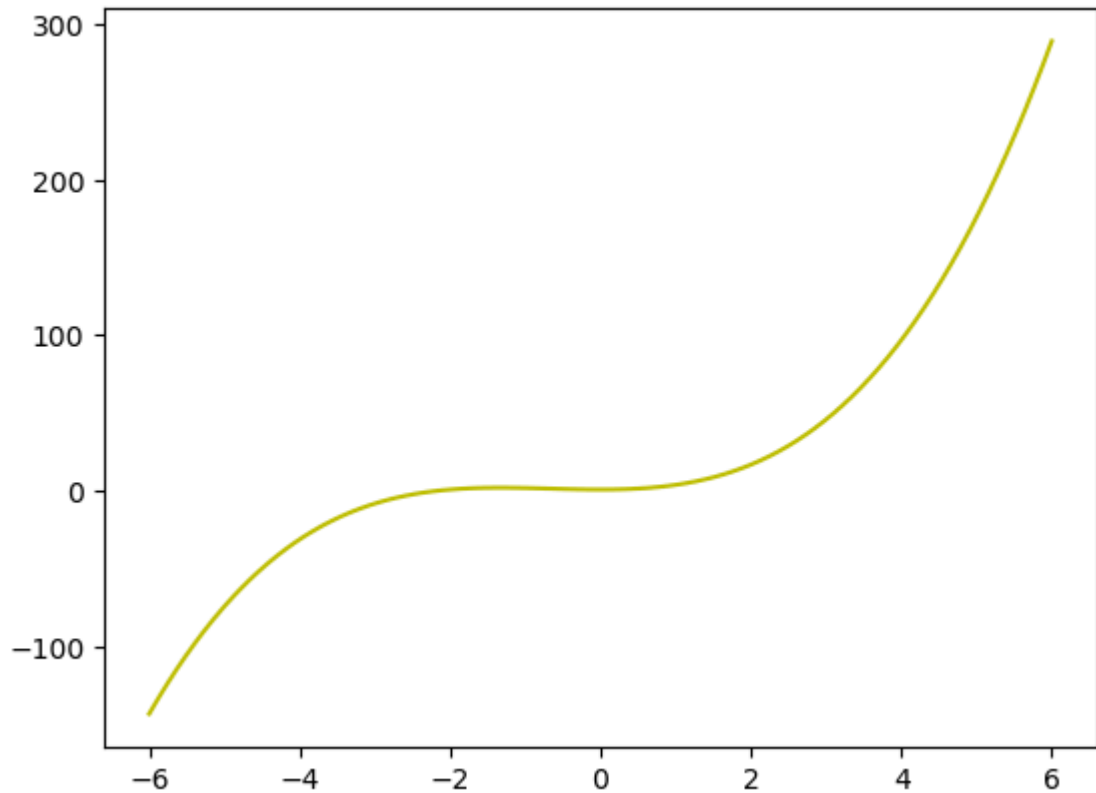
```
In [22]: import numpy as np
import matplotlib.pyplot as plt
import math
```

```
In [23]: x = np.linspace(-6,6,100)
```

```
In [24]: def f(x):  
         return pow(x,3) + 2*x**2 + 1
```

```
In [25]: print(r'la courbe de f sur [-6,6]')  
plt.plot(x,f(x),"y")  
plt.show()
```

la courbe de f sur [-6,6]



```
In [26]: x = np.linspace(5.4999,5.5001,10)  
plt.plot(x,f(x),"b")  
plt.show()
```



```
In [27]: Vgauche = np.array([5.4999,5.49999,5.499999])
print("limite à gauche")
Ugauche = f(Vgauche)
print(Vgauche)
print(Ugauche)
```

```
limite à gauche
[5.4999  5.49999  5.499999]
[227.86372518 227.8738725 227.87488725]
```

```
In [29]: Vdroite = np.array([5.500001,5.50001,5.5001])
print("limite à droite")
Udroite = f(Vdroite)
print(Vdroite)
print(Udroite)
```

```
limite à droite
[5.500001 5.50001 5.5001 ]
[227.87511275 227.8761275 227.88627519]
```

```
In [ ]:
```