

Practica 6(b)

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Newton Divided Difference Interpolating polynomial

```
In[4]:= NthDividedDiff[x0_, f0_, startindex_, endindex_] :=  
  Module[{x = x0, f = f0, i = startindex, j = endindex, answer},  
    If[i == j, Return[f[[i]]],  
      answer =  
        (NthDividedDiff[x, f, i + 1, j] - NthDividedDiff[x, f, i, j - 1]) / (x[[j]] - x[[i]]);  
      Return[answer];  
    ];  
    x = {0, 1, 3};  
    f = {1, 3, 55};  
    NthDividedDiff[x, f, 2, 3]
```

Out[7]= 26

```
In[8]:= NthDividedDiff[x, f, 1, 3]
```

Out[8]= 8

```
In[9]:= x = {-1, 0, 1, 2};  
f = {5, 1, 1, 11};  
NthDividedDiff[x, f, 1, 2]
```

Out[11]= -4

```
In[12]:= NthDividedDiff[x, f, 2, 3]
```

Out[12]= 0

```
In[13]:= NthDividedDiff[x, f, 1, 3]
```

Out[13]= 2

```
In[14]:= NthDividedDiff[x, f, 2, 4]
```

Out[14]= 5

```
In[15]:= NthDividedDiff[x, f, 1, 4]
```

```
Out[15]= 1
```

Q2

```
In[21]:= NewtonDDPoly[x0_, f0_] :=
  Module[{x1 = x0, f = f0, n, newtonPolynomial, k, j},
    n = Length[x1];
    newtonPolynomial[Y_] = 0;
    For[i = 1, i ≤ n, i++,
      prod[Y_] = 1;
      For[k = 1, k ≤ i - 1, k++,
        prod[Y_] = prod[Y] * (y - x1[[k]])];
      newtonPolynomial[Y_] = newtonPolynomial[Y] + NthDividedDiff[x1, f, 1, i] * prod[Y];
    Return[newtonPolynomial[Y]];];
nodes = {0, 1, 3};
values = {1, 3, 55};
NewtonDDPoly[nodes, values]
```

```
Out[24]= 1 + 2 y + 8 (-1 + y) y
```

```
In[25]:= Simplify[1 + 2 y + 8 (-1 + y) y]
```

```
Out[25]= 1 - 6 y + 8 y^2
```