

Natural Numbers, or the best way to enumerate anything

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Contents

'utils require import

- Required module: utils

```
'Nat_context [ { Type '.Nat } { .Nat '.zero } { .Nat 'n -> .Nat ? '.succ } ] def
'Nat Nat_context { .Nat } prods "Natural" defconstr
'zero Nat_context { .zero } funs "0" defconstr
Nat 'n -> 'succ Nat_context { .succ ( n ( .Nat .zero .succ ) ) } funs "S n" defconstr !
```

The `Nat` type is defined to *Natural* . $\lambda(n : \textit{Natural}).\mu(n)$ has type $\forall(n : \textit{Natural})(\text{Nat}^P : \textit{Natural} \rightarrow \textit{Set}_1), \text{Nat}^P 0 \rightarrow (\forall(n_0 : \textit{Natural}), \text{Nat}^P n_0 \rightarrow \text{Nat}^P (S n_0)) \rightarrow \text{Nat}^P n$.

$\lambda(n : \textit{Natural}).S n$ has type *Natural* \rightarrow *Natural* .