Московский государственный технический университет им. Н.Э. Баумана Кафедра «Системы обработки информации и управления»



Лабораторная работа №4 по дисциплине «Методы машинного обучения» на тему

«Реализация алгоритма Policy Iteration»

Выполнил: студент группы ИУ5И-23М Ли Хао

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1. Цель лабораторной работы

ознакомление с базовыми методами обучения с подкреплением.

2. Задание

На основе рассмотренного на лекции примера реализуйте алгоритм Policy Iteration для любой среды обучения с подкреплением (кроме рассмотренной на лекции).

3. Текст программы

```
from matplotlib import pyplot as plt
import numpy as np
from scipy.stats import poisson
import seaborn as sns
Hyper parameters
<int> MAX_NUM:每个停车场能停的最大数目(20)
<int> lam1_rent: 停车场 1 租车λ值(3)
<int> lam1 return: 停车场1还车λ值(3)
<int> lam2_rent: 停车场 2 租车λ值(4)
<int> lam2 return: 停车场 2 还车λ值(2)
<int> MAX_ACTION: 最大移动汽车数目(5)
<int> CAR_COST: 移动车辆的代价(2)
<int> CAR EARNING: 租车的收入(10)
<float> DISCOUNT: 收益折扣(0.9)
<np.array> actions: 动作集合(-5, -4, ..., 4, 5)
<int> POISSON UPPER BOUND: 限制泊松分布产生请求数目的上限
```

```
<dict> poisson_cache: 存储每个 (n, λ) 对应的泊松概率, key 为 n*(POISSON_UPPER_BOUND-
1)+lam
"""

MAX_NUM = 20
lam1_rent = 3
lam1_return = 3
lam2_rent = 4
lam2_return = 2

MAX_ACTION = 5

DISCOUNT = 0.9

CAR_COST = 2

CAR_EARNING = 10
actions = np.arange(-MAX_ACTION, MAX_ACTION + 1)

POISSON_UPPER_BOUND = 11
poisson_cache = dict()
```

```
def poisson_prob(n, lam):
    global poisson_cache
    key = n * (POISSON_UPPER_BOUND - 1) + lam
    if key not in poisson_cache:
        poisson_cache[key] = poisson.pmf(n, lam)
    return poisson_cache[key]
```

```
class dp:
    def __init__(self):
        self.v = np.ones((MAX_NUM + 1, MAX_NUM + 1), float)
        self.actions = np.zeros((MAX_NUM + 1, MAX_NUM + 1), int)
```

```
self.gama = DISCOUNT

self.delta = 0

self.theta = 0.01

pass
```

```
def state_value(self, state, action, state_value, constant_returned_cars):
    """
```

```
:param state: 状态定义为每个地点的车辆数
:param action: 车辆的移动数量[-5,5], 负: 2->1, 正: 1->2
:param state_value: 状态价值矩阵
:param constant_returned_cars: 将换车的数目设定为泊松均值, 替换为泊松概率分布
:return:
"""
# initial total return
returns = 0.0
```

```
# 移动车辆产生负收益
returns -= CAR_COST * abs(action)
```

```
# 移动后的车辆总数不能超过 20

NUM_OF_CARS_1 = min(state[0] - action, MAX_NUM)

NUM_OF_CARS_2 = min(state[1] + action, MAX_NUM)
```

```
# 遍历两地全部的可能概率下(截断泊松概率)租车请求数目
for rent_1 in range(POISSON_UPPER_BOUND):
```

```
for rent_2 in range(POISSON_UPPER_BOUND):
              # prob 为两地租车请求的联合概率,概率为泊松分布
              prob = poisson_prob(rent_1, lam1_rent) * poisson_prob(rent_2,
lam2_rent)
              # 两地原本汽车数量
              num_of_cars_1 = NUM_OF_CARS_1
              num of cars 2 = NUM OF CARS 2
              # 有效租车数目必须小于等于该地原有的车辆数目
              valid_rent_1 = min(num_of_cars_1, rent_1)
              valid_rent_2 = min(num_of_cars_2, rent_2)
              # 计算回报,更新两地车辆数目变动
              reward = (valid_rent_1 + valid_rent_2) * CAR_EARNING
              num_of_cars_1 -= valid_rent_1
              num of cars 2 -= valid rent 2
              # 如果还车数目为泊松分布的均值
              if constant_returned_cars:
                  # 两地的还车数目均为泊松分布均值
                  returned cars 1 = lam1 return
                  returned cars_2 = lam2_return
                  # 还车后总数不能超过车场容量
                  num_of_cars_first_loc = min(num_of_cars_1 + returned_cars_1,
MAX NUM)
                  num_of_cars_second_loc = min(num_of_cars_2 + returned_cars_2,
MAX_NUM)
                  # 策略评估: V(s) = p(s',r|s,\pi(s))[r + \gamma V(s')]
                  returns += prob * (reward + DISCOUNT *
state value[num of cars first loc, num of cars second loc])
```

```
# 否则计算所有泊松概率分布下的还车空间
               else:
                   for returned_cars_first_loc in range(POISSON_UPPER_BOUND):
                       for returned_cars_second loc in
range(POISSON_UPPER_BOUND):
                           prob_return = poisson_prob(
                               returned_cars_first_loc, lam1_return) *
poisson_prob(
                               returned_cars_second_loc, lam2_return)
                           num_of_cars_first_loc_ = min(num_of_cars_1 +
returned_cars_first_loc, MAX_NUM)
                           num_of_cars_second_loc_ = min(num_of_cars_2 +
returned_cars_second_loc, MAX_NUM)
                           # 联合概率为【还车概率】*【租车概率】
                           prob_ = prob_return * prob
                           returns += prob_ * (reward + DISCOUNT *
                                              state_value[num_of_cars_first_loc
_, num_of_cars_second_loc_])
       return returns
```

```
def policy_iteration(self, constant_returned_cars=True):
    """
```

```
:param constant_returned_cars:
:return:
"""
# 设置迭代参数
iterations = 0
```

```
# 准备画布大小,并准备多个子图
__, axes = plt.subplots(2, 3, figsize=(40, 20))
# 调整子图的问题, wspace=0.1 为水平问题, hspace=0.2 为垂直问题
plt.subplots_adjust(wspace=0.1, hspace=0.2)
# 这里将子图形成一个 1*6 的列表
axes = axes.flatten()
while True:
# 使用 seaborn 的 heatmap 作图
# flipud 为将矩阵进行垂直角度的上下翻转,第 n 行变为第一行,第一行变为第 n 行,如此。
# cmap:matplotlib 的 colormap 名称或颜色对象;
# 如果没有提供,默认为 cubehelix map (数据集为连续数据集时)或 RdBu_r (数据集为离散数据集时)
fig = sns.heatmap(np.flipud(self.actions), cmap="rainbow", ax=axes[iterations])
```

```
# 定义标签与标题

fig.set_ylabel('# cars at first location', fontsize=30)

fig.set_yticks(list(reversed(range(MAX_NUM + 1))))

fig.set_xlabel('# cars at second location', fontsize=30)

fig.set_title('policy {}'.format(iterations), fontsize=30)
```

```
# policy evaluation (in-place) 策略评估 (in-place)

# 未改进前,第一轮 policy 全为 0,即[0,0,0...]

while True:

old_value = self.v.copy()

for i in range(MAX_NUM + 1):
```

```
for j in range(MAX_NUM + 1):

# 更新 V (s)

new_state_value = self.state_value([i, j], self.actions[i
j], self.v, constant_returned_cars)

# in-place 操作

self.v[i, j] = new_state_value

# 比较 V_old(s)、V(s), 收敛后退出循环

max_value_change = abs(old_value - self.v).max()

print('max value change {}'.format(max_value_change))

if max_value_change < 1e-4:

break
```

```
action_returns.append(-np.inf)

# 找出产生最大动作价值的动作

new_action = actions[np.argmax(action_returns)]

# 更新策略

self.actions[i, j] = new_action

if policy_stable and old_action != new_action:

policy_stable = False

print('policy stable {}'.format(policy_stable))
```

```
if policy_stable:
    fig = sns.heatmap(np.flipud(self.v), cmap="rainbow", ax=axes[-1])
    fig.set_ylabel('# cars at first location', fontsize=30)
    fig.set_yticks(list(reversed(range(MAX_NUM + 1))))
    fig.set_xlabel('# cars at second location', fontsize=30)
    fig.set_title('optimal value', fontsize=30)
    break
```

```
iterations += 1

# plt.title('Policy Iteration')

plt.savefig('./policy_iteration.png')

plt.show()

plt.close()

return
```

```
def value_iteration(self, constant_returned_cars=True):
"""
```

```
:param constant_returned_cars:
:return:
"""

# 设置迭代参数
iterations = 0
```

```
# 定义标签与标题

fig.set_ylabel('# cars at first location', fontsize=30)

fig.set_yticks(list(reversed(range(MAX_NUM + 1))))

fig.set_xlabel('# cars at second location', fontsize=30)

fig.set_title('policy {}'.format(iterations), fontsize=30)
```

```
# value iteration 价值迭代
while True:
```

```
old_value = self.v.copy()
                for i in range(MAX_NUM + 1):
                    for j in range(MAX_NUM + 1):
                        action_returns = []
                        for action in actions:
                            if (0 \le action \le i) or (-j \le action \le 0):
                                action_returns.append(self.state_value([i, j],
action, self.v, constant_returned_cars))
                            else:
                                action_returns.append(-np.inf)
                        # 找出产生最大动作价值的动作
                        max_action = actions[np.argmax(action_returns)]
                        # 更新 V (s)
                        new_state_value = self.state_value([i, j], max_action,
self.v, constant_returned_cars)
                        # in-place 操作
                        self.v[i, j] = new_state_value
               max_value_change = abs(old_value - self.v).max()
               print('max value change {}'.format(max_value_change))
               if max_value_change < 1e-4:</pre>
                    print(iterations)
                    break
```

```
# policy improvement
           policy_stable = True
           for i in range(MAX NUM + 1):
               for j in range(MAX_NUM + 1):
                   old_action = self.actions[i, j]
                   action_returns = []
                   for action in actions:
                       if (0 \le action \le i) or (-j \le action \le 0):
                           action_returns.append(self.state_value([i, j], action
self.v, constant_returned_cars))
                       else:
                           action_returns.append(-np.inf)
                   # 找出产生最大动作价值的动作
                   new_action = actions[np.argmax(action_returns)]
                   # 更新策略
                   self.actions[i, j] = new_action
                   if policy_stable and old_action != new_action:
                       policy stable = False
           print('policy stable {}'.format(policy_stable))
```

```
if policy_stable:
    fig = sns.heatmap(np.flipud(self.v), cmap="rainbow", ax=axes[-1])
    fig.set_ylabel('# cars at first location', fontsize=30)
    fig.set_yticks(list(reversed(range(MAX_NUM + 1))))
```

```
fig.set_xlabel('# cars at second location', fontsize=30)
fig.set_title('optimal value', fontsize=30)
break
```

```
iterations += 1
```

```
# plt.title('Value Iteration')

plt.savefig('./value_iteration.png')

plt.show()

plt.close()

return
```

```
if __name__ == '__main__':
    model = dp()
    model.policy_iteration(constant_returned_cars=True)
```

```
model1 = dp()
model1.value_iteration(constant_returned_cars=True)
pass
```

4. Результат

