

Review: $150^\circ = \frac{5}{6}\pi$, $72^\circ = \frac{2\pi}{5}$

$$\frac{\pi}{7} = \frac{180^\circ}{7}, \quad -1 = -\frac{180^\circ}{\pi}$$

$$\sin\left(\frac{\pi}{2} - x\right) = \sin\left(\frac{\pi}{2}\right) \cos x - \cos\left(\frac{\pi}{2}\right) \sin x = \cos x$$

$$\cos\left(\frac{\pi}{2} + x\right) = -\sin x$$

$$\tan(x+y) = \frac{\sin(x+y)}{\cos(x+y)} = \frac{\sin x \cos y + \cos x \sin y}{\cos x \cos y - \sin x \sin y}$$

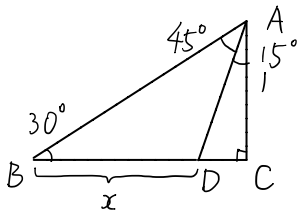
divide $\cos x \cos y$ $= \frac{\tan x + \tan y}{1 - \tan x \tan y}$

$$\tan\left(x + \frac{\pi}{2}\right) = -\frac{1}{\tan x} = -\cot x$$

$$\sin t = \frac{1}{2} \Rightarrow t = \frac{\pi}{6} + 2k\pi, \frac{5\pi}{6} + 2k\pi, k \in \mathbb{Z}$$

$$\cos t = -1 \Rightarrow t = -\pi + 2k\pi, k \in \mathbb{Z}$$

$$\cos t = 0 \Rightarrow t = k\pi, k \in \mathbb{Z}$$



$$\frac{1}{BC} = \frac{AC}{BC} = \tan 30^\circ = \frac{\sqrt{3}}{3} \Rightarrow BC = \sqrt{3}$$

$$DC = \frac{DC}{AC} = \tan 15^\circ = \tan(45^\circ - 30^\circ)$$

$$= \frac{\tan 45^\circ - \tan 30^\circ}{1 + \tan 45^\circ \tan 30^\circ} = \frac{1 - \frac{\sqrt{3}}{3}}{1 + 1 \times \frac{\sqrt{3}}{3}}$$

$$= \frac{1 - \frac{\sqrt{3}}{3}}{1 + \frac{\sqrt{3}}{3}} = \frac{\left(1 - \frac{\sqrt{3}}{3}\right)^2}{\left(1 + \frac{\sqrt{3}}{3}\right)\left(1 - \frac{\sqrt{3}}{3}\right)} = \frac{1 + \frac{1}{3} - \frac{2\sqrt{3}}{3}}{1 - \frac{1}{3}}$$

$$= \frac{\frac{4}{3} - \frac{2\sqrt{3}}{3}}{\frac{2}{3}} = \frac{4 - 2\sqrt{3}}{2} = 2 - \sqrt{3}$$

$$x = BD = BC - DC = \sqrt{3} - (2 - \sqrt{3}) = 2\sqrt{3} - 2$$

Section 8.3

$$\frac{d}{dt} \sin t = \cos t, \quad \frac{d}{dt} \cos t = -\sin t$$

$$(\sin 3t)' = 3 \cos 3t, \quad (\cos(t^3))' = -3t^2 \sin t^3$$

$$(t^2 \cos 3t)' = (t^2)' \cos 3t + t^2 (\cos 3t)'$$

$$= 2t \cos 3t - 3t^2 \sin 3t$$

$$\int \cos t \, dt = \sin t + C, \quad \int \sin t \, dt = -\cos t + C$$

$$\int \cos 3t \, dt = \frac{1}{3} \int \cos 3t \, d(3t) = \frac{1}{3} \sin 3t + C$$

$$\int_0^{\pi} \sin t \, dt = [-\cos t] \Big|_0^{\pi} = [-(-1) - (-1)] = 2$$

$$\lim_{h \rightarrow 0} \frac{\sin h}{h} = \lim_{h \rightarrow 0} \frac{\sin(0+h) - \sin(0)}{h} = \cos 0 = 1$$

$$\int \tan t \, dt = \int \frac{\sin t}{\cos t} \, dt = - \int \frac{1}{\cos t} \, d(\cos t) = -\ln |\cos t| + C$$

$$\int \cos \frac{x-2}{2} \, dx = \int \cos \frac{x-2}{2} \, d(x-2) = 2 \int \cos \frac{x-2}{2} \, d \frac{x-2}{2} =$$

$$2 \sin \frac{x-2}{2} + C$$