

3a.  $K_T = \text{maximum of } |f''(x)| \text{ on } [a, b]$ , here  $f(x) = \frac{3}{x}$ , so  $f''(x) = \frac{6}{x^3}$  ↓ decrease  
 $a=1, b=2$

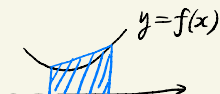
$$\text{so } K_T = |f''(1)| = \left| \frac{6}{1^3} \right| = 6$$

$$E_n^T \leq \frac{6}{12n^2} (2-1)^3 = \frac{1}{2n^2} \leq \frac{1}{100} \Rightarrow n^2 \geq \frac{100}{2} = 50 \Rightarrow n \geq \sqrt{50} = 7.07 \dots \Rightarrow n \text{ is at least } 8$$

$$\begin{aligned} 3b. \int_0^3 e^{(t^2)} dt &= \frac{3-0}{3 \times 6} \left[ e^{0^2} + 4e^{(\frac{1}{2})^2} + 2e^{1^2} + 4e^{(\frac{3}{2})^2} + 2e^{2^2} + 4e^{(\frac{5}{2})^2} + e^{3^2} \right] \\ &= \frac{1}{6} \left( 1 + 4e^{\frac{1}{4}} + 2e + 4e^{\frac{9}{4}} + 2e^4 + 4e^{\frac{25}{4}} + e^9 \right) \end{aligned}$$

3c. It is necessary that  $n$  be even for Simpson's Rule, since it uses parabolas, each of which is defined by 3 distinct points, yielding 2 intervals on the  $x$  axis

$$4a. \int_1^\infty \frac{x^{\frac{3}{2}}}{\pi + x^3} dx \stackrel{\text{comparison property}}{\leq} \int_1^\infty \frac{x^{\frac{3}{2}}}{x^3} dx = \int_1^\infty x^{-\frac{3}{2}} dx = -2x^{-\frac{1}{2}} \Big|_1^\infty = 0 - (-2) = 2, \text{ so convergent}$$

4b. Trapezoidal Rule yields a bigger number than  $\int_a^b f(x) dx$ . Graph: 

4c

| $n$          | 0        | 1         | 2               | 3               | 4               | ... | $n$             |
|--------------|----------|-----------|-----------------|-----------------|-----------------|-----|-----------------|
| $f^{(n)}(x)$ | $e^{-x}$ | $-e^{-x}$ | $(-1)^2 e^{-x}$ | $(-1)^3 e^{-x}$ | $(-1)^4 e^{-x}$ | ... | $(-1)^n e^{-x}$ |
| $f^{(n)}(0)$ | 1        | -1        | $(-1)^2$        | $(-1)^3$        | $(-1)^4$        | ... | $(-1)^n$        |

$$\text{Hence } P_n(x) = 1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \dots + \frac{(-1)^n x^n}{n!}$$