

# Assigment 1

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## Question 1

Based on the diagram, we can solve the sub parts in the following way:

### Part a

Rise time ( $t_r$ ) is defined as the time taken for the voltage to rise from  $0.1(V_{dd})$  to  $0.9(V_{dd})$ . Fall time ( $t_f$ ) is defined as the time taken for the voltage to fall from  $0.9(V_{dd})$  to  $0.1(V_{dd})$ .

Hence the rise time and fall time for the waveform  $V_{out}$  can be calculated as:

$$t_r = 383.86ps - 359.95ps = 23.91ps \quad (1)$$

$$t_f = 132.36ps - 113.35ps = 19.01ps \quad (2)$$

### Part b

The high-to-low propagation delay ( $t_{pHL}$ ) is defined as the time delay between  $0.5(V_{in})$  in the rising edge and  $0.5(V_{out})$  in the falling edge. Based on the graph provided in the question, the following can be obtained:

$$t_{pHL} = 120.88ps - 108.62ps = 12.26ps \quad (3)$$

### Part c

The low-to-high propagation delay ( $t_{pLH}$ ) is defined as the time delay between  $0.5(V_{in})$  in the falling edge and  $0.5(V_{out})$  in the rising edge. Based on the graph provided in the question, the following can be obtained:

$$t_{pLH} = 368.35ps - 355.05ps = 13.3ps \quad (4)$$

### Part d

Based on the diagram, we can assume that the clock cycle in pico-seconds can be assumed to be  $T_{in}$ .

Hence:

$$\frac{10}{100} * T_{in} = 355.05ps - 108.62ps = 246.43ps \quad (5)$$

Solving this for  $T_{in}$  would result in the following:

$$T_{in} = 246.43ps * 10 = 2464.3ps \quad (6)$$

The frequency can be calculated to be the following:

$$f_{in} = \frac{1}{2464.3 * 10^{-12}} = 406 * 10^6 Hz = 406MHz. \quad (7)$$

### Question 2

Based on the notes, we note that  $R_{on}$  is inversely proportional to  $\frac{W}{L}$ . This implies the following:

$$R_{on} \propto \frac{1}{W} \quad (8)$$

and

$$R_{on} \propto L \quad (9)$$

### Part a

We are given that  $R_{on}$  is initially  $100k\Omega$ . Based on the relationship mentioned in (8), we can determine the current value of  $R_{on}$

$$R_{on} = \frac{100}{5} k\Omega = 20k\Omega \quad (10)$$

### Part b

Similarly, based on (9):

$$R_{on} = 100k\Omega * 5 = 500k\Omega \quad (11)$$