Homework 03.11

Use the lm() function to perform a simple linear regression on the Boston data set with medv as the response and rm as the predictor. Use the summary() function to print the results. Comment on the output.

The simple linear model:

$$(medv) = \beta_0 + \beta_1(rm) + \varepsilon, E(\varepsilon) = 0, Var(\varepsilon) = \sigma^2$$

- 1. Find out $\hat{\beta}_0$, $\hat{\beta}_1$, and $\hat{\sigma}$.
- 2. Provide an interpretation of $\hat{\beta}_1$.
- 3. Based on the results, is there a relationship between the predictor and the response? Use the p-value in the printed result, and write down the null and alternative hypotheses.
- 4. Find out the 95% confidence interval of $\hat{\beta}_0$, $\hat{\beta}_1$.
- 5. According to the printed results of *summary()*, write down the equation describing the prediction for y_i based on the value of x_i .
- 6. If we have rm equal to 6, what is the predicted value of medv based on rm = 6?