# HyPrColoc

Ref: HyPrColoc: Foley CN, Staley JR, et al. A fast and efficient colocalization algorithm for identifying shared genetic risk factors across multiple traits. BioRxiv 2019. doi: https://doi.org/10.1101/592238

### Three key assumptions

- 1. GWAS results are from the same underlying population (same LD pattern)
- 2. at most one causal variant in the genomic region for each trait
- 3. Causal variant are either directly typed or well imputed

## R package: hyprcoloc 安裝

- 1. install.packages("devtools")
- 2. library(devtools)
- 3. install\_github("cnfoley/hyprcoloc", build\_opts = c("--resave-data", "--no-manual"), build\_vignettes = TRUE)
- 4. library(hyprcoloc)
- 5. browseVignettes("hyprcoloc")

#### If issue with installation (owing to c++ compiler)

Try replacing 3 above with previous package version:

3. install\_github("jrs95/hyprcoloc", build\_opts = c("--no-resave-data", "--no-manual"), build\_vignettes = TRUE)

我的 R 版本: 4.3.2

# Note there is no "prior.c" parameter in this version, instead use "prior.2 = 1 - prior.c". Default settings are matched.

Otherwise, on a Windows machine try updating Rtools: remove the previous version of Rtools (probably located C:\Rtools) and download Rtools40 from CRAN [https://cran.r-project.org/bin/windows/Rtools/]

## Example

執行以下指令

browseVignettes("hyprcoloc")

### **HyPrColoc**

Christopher N Foley & James R Staley 2024-09-01

- 1 Introduction
  - o 1.1 Installation
- 2 Getting started
  - o 2.1 Basic set-up: assuming independence between studies
  - 2.2 Computing a credible set of snps for each cluster of colocalized traits
- 3 An analysis protocol: assessing stability of clusters via a sensitivity analysis
  - 3.1 Assessing sensitivity to changes in the prior configuration parameters
  - o 3.2 The Bayesian divisive clustering algorithm
- 4 Mapping pleiotropy: an alternative to PheWAS
- 5 Analysing large numbers of traits
- 6 Analysing correlated traits

https://github.com/lihsinchien/MWAS-HyPrColoc/blob/main/hyprcoloc.md#6-analysing-correlated-traits

### Continuous traits, ind. SNPs & traits

- i. a cluster of putatively colocalized traits
- ii. the posterior probability that these traits are colocalized
- iii. the 'regional association' probability\* (which is always > the posterior probability)
- iv. a candidate causal variant explaining the shared association
- v. the proportion of the posterior probability explained by this variant (which represents the HyPrColoc multi-trait fine-mapping probability).

```
> res:
                                                       iii.
                                        ii.
                                                                     iv.
                                                                                    V.
$results
                         traits posterior_prob regional_prob candidate_snp posterior_explained_by_snp dropped_trait
  iteration
            т1, т2, т3, т4, т5
                                         1.0000
                                                                   rs11591147
                                                                                                   1.0000
                                                                                                                       NA
                                                                                                    0.4197
                     T6, T7, T8
                                         0.9164
                                                                   rs12117612
                                                                                                                       NA
                                                                                                   0.0763
                        T9, T10
                                         0.9018
                                                                    rs7524677
                                                                                                                       NA
attr(,"class")
```

- [1] "hyprcoloc"
  - ii. 越大代表, i. 中的 traits 受同一個 SNP 影響的可能性越高 (colocalization)
  - v. 越大,代表 iv. 中的 SNPs 為 causal 的可能性越大

Ex: T1~5 等五個 traits 為 colocalized traits可能性高(1.00), 其 causal variant 為 rs11591147可能性高(1.00)

Ex: T9, T10 為 colocalized traits 可能性高(0.90),其 causal variant 為 rs7524677 的可能性低(0.08)

### Binary traits, ind. SNPs & traits

```
binary.traits = c(1,1,1,rep(0,dim(betas)[2]-3));
res <- hyprcoloc(betas, ses, trait.names=traits, snp.id=rsid, binary.outcomes = binary.traits);
res
#> $results
                          traits posterior_prob regional_prob candidate snp
#> iteration
            1 T1, T2, T3, T4, T5
#> 1
                                         1.0000
                                                                rs11591147
                      T6, T7, T8
#> 2
                                         0.9164
                                                                rs12117612
                       T9, T10
#> 3
                                         0.9018
                                                           1 rs7524677
#> posterior explained by snp dropped trait
#> 1
                        1.0000
#> 2
                        0.4197
                                          NA
#> 3
                        0.0763
                                          NΑ
#> attr(,"class")
#> [1] "hyprcoloc"
```

- Binary.outcomes=c(1,1,1,0,0,0,0,0,0,0)
- T1~T3 continuous, T4~T10 binary

## 測試某些traits (T1, T2) 是否有 colocalization

• Trait.subset = c("T1","T2")

### Computing a credible set of snps

```
res <- hyprcoloc(betas, ses, trait.names=traits, snp.id=rsid, snpscores = TRUE);
res[[1]];
     iteration
                           traits posterior prob regional prob candidate snp
             1 T1, T2, T3, T4, T5
                                           1.0000
                                                                    rs11591147
                       T6, T7, T8
                                           0.9164
                                                                    rs12117612
                          T9, T10
                                           0.9018
                                                                     rs7524677
     posterior explained by snp dropped trait
                         1.0000
#> 1
                                            NΑ
#> 2
                         0.4197
                                            NA
#> 3
                         0.0763
                                            NΑ
head(res[[2]][[1]]);
      rs6694014
                  rs11206477
                                  rs978479
                                              rs6684892
                                                         rs149881092
                                                                         rs2081705
#> 4.109458e-67 3.004278e-68 5.637121e-67 6.486572e-68 6.063410e-66 5.765875e-67
```

fine-mapping score(snpscore): the probability that a snp is likely to be causal

identifies a credible set of snps which explains 95% of the posterior probability of colocalization for each cluster of colocalized traits

```
cred.sets(res, value = 0.95);
#> [[1]]
  rs11591147
#>
#> [[2]]
    rs12117612
                 rs7532349
                           rs11206481 rs12145624
   0.419677651 0.419677651 0.025324539 0.022969148 0.022969148 0.022332481
   rs13375783
                 rs1544909
  0.014513746 0.009991906
#>
#> [[3]]
   rs7524677 rs7547776 rs7524783 rs6701789 rs1035817 rs7530321
   0.07626197 0.07626197 0.07626197 0.07626197 0.07626197 0.05349125 0.05349125
   rs7553410 rs11206486 rs7524899
                                    rs6681189
                                               rs7537797 rs11206485 rs10888890
   0.05349125 0.02231383 0.02231383 0.02231383 0.02231383 0.02231383 0.02098626
   rs2114574 rs6664660 rs6588539 rs11206489
                                               rs6668051 rs10218512 rs11206492
   0.02098626 0.02098626 0.02098626 0.02098626 0.02098626 0.02098626 0.02098626
              rs7539163 rs7529244 rs6687414
                                               rs7538808 rs11206487 rs12745865
   0.02098626 0.02098626 0.02098626 0.02098626 0.02098626 0.01203687 0.01203687
#> rs12725873
#> 0.01203687
```

```
ld.matrix["rs12117612","rs7532349"];
#> [1] 1
```

### 3 Assessing stability of clusters (sensitivity analysis)

3.1 Change prior

3.2 The Bayesian divisive clustering algorithm

## 6 Analysing correlated traits

- (i) a matrix containing the putative correlation between the traits;
- (ii) a matrix containing the LD between the snps in the region
- (iii) a matrix containing the proportion of shared participants between each pair of studies.

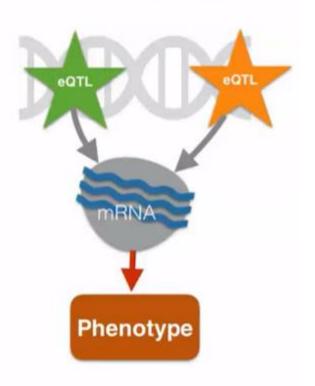
- Note the matrix of overlapping sample proportions has diagonal elements set to 1 and off diagonal elements (i,j) denote the proportion of overlap between the i'th and j'th studies
  - ex:if N denotes the total number of overlapping participants and Ni,Nj denote the numbers of participants in the i'th and j'th studies respectively, then N/(NiNj) is the (i,j)=(j,i) element.

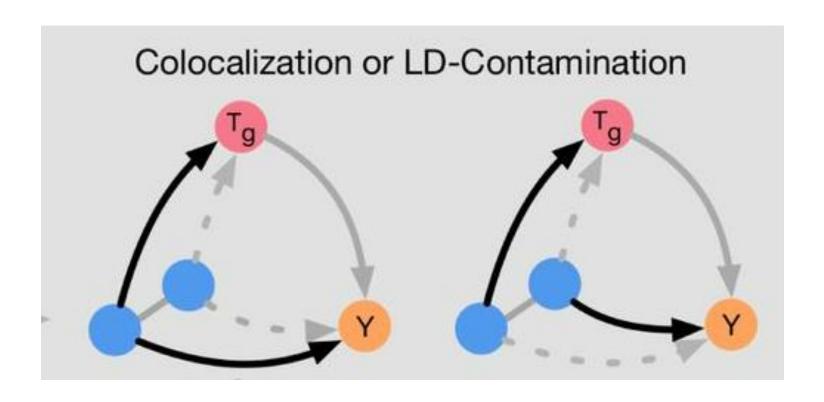
```
sample.overlap = matrix(1, dim(betas)[2], dim(betas)[2]);
traits <- paste0("T", 1:dim(betas)[2]);</pre>
ptm = proc.time();
res <- hyprcoloc(betas, ses, trait.names=traits, snp.id=rsid, trait.cor = trait.cor,
                ld.matrix = ld.matrix, sample.overlap = sample.overlap, uniform.priors = FALSE);
time.corr = proc.time() - ptm;
res
#> $results
                          traits posterior prob regional prob candidate snp
#> iteration
#> 1
             1 T1, T2, T3, T4, T5
                                         1.0000
                                                                rs11591147
#> 2
                       T6, T7, T8
                                         0.8257
                                                                rs12117612
#> 3
             3
                         T9, T10
                                         0.8944
                                                           1
                                                                 rs7524677
#> posterior explained by snp dropped trait
#> 1
                        1.0000
                                          NA
                        0.3535
#> 2
                                          NΑ
#> 3
                        0.0696
                                          NΑ
#>
#> attr(,"class")
#> [1] "hyprcoloc"
res <- hyprcoloc(betas, ses, trait.names=traits, snp.id=rsid, trait.cor = trait.cor,
                 ld.matrix = ld.matrix, sample.overlap = sample.overlap, uniform.priors = TRUE);
res
#> $results
#> iteration
                           traits posterior prob regional prob candidate snp
#> 1
             1 T1, T2, T3, T4, T5
                                           1.0000
                                                                   rs11591147
                                                                   rs12117612
#> 2
             2
                       T6, T7, T8
                                           0.9744
#> 3
             3
                          T9, T10
                                           0.9782
                                                                     rs7524677
#> posterior_explained_by_snp dropped_trait
#> 1
                         1.0000
                                            NΑ
#> 2
                         0.3535
                                            NΑ
#> 3
                         0.0696
                                            NA
#>
#> attr(,"class")
#> [1] "hyprcoloc"
```

# default assumption, presented for clarity:

```
res <- hyprcoloc(betas, ses, trait.names=traits, snp.id=rsid);</pre>
res;
#> $results
#> iteration
                          traits posterior prob regional prob candidate snp
#> 1
                                         1.0000
                                                                rs11591147
            1 T1, T2, T3, T4, T5
#> 2
                      T6, T7, T8
                                         0.9164
                                                                rs12117612
                         T9, T10
#> 3
                                         0.9018
                                                                 rs7524677
    posterior explained by snp dropped trait
#> 1
                        1.0000
                                          NΑ
#> 2
                        0.4197
                                          NA
#> 3
                        0.0763
                                          NA
#> attr(,"class")
#> [1] "hyprcoloc"
ptm = proc.time();
res <- hyprcoloc(betas, ses, trait.names=traits, snp.id=rsid);</pre>
time.ind = proc.time() - ptm;
time.ind:
#> 使用者 系統
                 流逝
    0.00 0.01 0.01
time.corr;
#> 使用者
           系統
                 流逝
#> 33.02 0.37 33.40
```

### Association





PrediXcan, SMR, FUSION (formerly TWAS)

https://www.biorxiv.org/content/10.1101/045260v7.full

## Lung cancer, methylation, gene expression

M個 SNPs

3個 trait: T1, T2, T3

資料來源	所需資料1
Disease (T1) ~ SNPs	1. $\hat{\beta}_{T1}$ 2. $se(\hat{\beta}_{T1})$
Expression (T2)~ SNPs	1. $\hat{\beta}_{T2}$ 2. $se(\hat{\beta}_{T2})$
Methylation (T3)~ SNPs	1. $\hat{\beta}_{T3}$ 2. $se(\hat{\beta}_{T3})$

#### 所需資料 2 (預設為單位矩陣)

- 1. LD matrix (MxM 矩陣)
- 2. Trait correlation matrix (3x3 矩陣)
- 3. Proportion of shared participants (3x3 矩陣)

### Comparison of Colocalization Methods

	COLOC	ENLOC	eCAVIAR
User friendly		<b>/</b>	~
eQTL: multiple causal variants	X		
GWAS: multiple causal variants	X	X	
Prior sensitivity	X		X

The posterior odds:

$$\frac{P(H_m|D)}{P(H_0|D)} = \sum_{S \in S_m} \frac{P(D|S)}{P(D|S_0)} \times \frac{p(S)}{p(S_0)}$$
Bayes factor Prior odds

$$S^* = \max_{S \in S_m} P(S|D)$$

$$P(H|D) = \frac{\sum_{S \in \mathcal{S}_H} BF(S) \frac{p(S)}{p(S_0)}}{\sum_{H_i \in \Omega} \sum_{S \in \mathcal{S}_{H_i}} BF(S) \frac{p(S)}{p(S_0)}},$$
(5)

BF(S): Bayes factor which is the likelihood of the data being generated under  $S \in S_H$  relative to the likelihood of the data being generated  $S_0$ 

### prior

#### 1. variant-level priors

$$p_0 + \sum_{k=1}^m \left( \sum_{j_1=1}^m \sum_{j_2 > j_1} \dots \sum_{j_k > j_{k-1}} p_{j_1 j_2 \dots j_k} \right) = 1. \qquad p_{12 \dots k} = p \prod_{i=2}^k \left( 1 - \gamma^{i-1} \right), k = 2, \dots m,$$

A genetic variant is associated with *k* traits

$$p_{12...k} = p \prod_{i=2}^{k} (1 - \gamma^{i-1}), k = 2, ... m,$$
 (10)

p: the probability of the genetic variant being associated with one trait  $\gamma$ : controls the probability that a genetic variant is associated with an additional trait  $p_c = 1 - \gamma$ : the probability of a variant being causal for a second trait given it is causal for one trait (the conditional colocalization prior),  $p_c = p_{12}/p_1$ 

$$\frac{p(S)}{p(S_0)} = \frac{p_{12...k}}{p_0} = \frac{p}{p_0} \prod_{i=2}^k (1 - \gamma^{i-1}), k = 2, ..., m,$$

 $\frac{p(S)}{p(S_0)} = \frac{p_{12...k}}{p_0} = \frac{p}{p_0} \prod_{i=2}^k (1 - \gamma^{i-1}), k = 2, ..., m,$  for configurations  $S \in S_{\mathcal{H}_k}$ , where k traits share a causal variant and the remaining m - k traits do not have a casual variant, and

## prior

### 2. Conditionally uniform prior probabilities

- (i) not setting variant-level information
- (ii) implicitly accounting for large differences in the causal configuration space between hypotheses

$$\frac{P(S|H)}{P(S_0|H_0)} = \frac{1/|\mathcal{S}_H|}{1/|S_0|} = 1/|\mathcal{S}_H|,\tag{13}$$

where 
$$\left|\mathcal{S}_{\mathcal{H}_k}\right| = Q$$
 and

$$\left| \mathcal{S}_{\mathcal{H}_{(m-1,1)}} \right| = \begin{cases} Q(Q-1) : m=2, \\ mQ(Q-1) : m>2. \end{cases}$$
 (14)