STATS 415 Final Project

Group 15

```
library(tidyverse)
## - Attaching packages
                                                    – tidyverse 1.2.1 –
## ✓ ggplot2 3.2.1
                        ✓ purrr
                                    0.3.3
## ✓ tibble 2.1.3
                        ✓ dplyr
                                    0.8.3
## ✔ tidyr
              1.0.0

✓ stringr 1.4.0

## ✔ readr

✓ forcats 0.4.0

              1.3.1
## - Conflicts -
                                           — tidyverse conflicts() -
## X dplyr::filter() masks stats::filter()
## X dplyr::lag()
                    masks stats::lag()
library(FNN)
library(parallel)
library(glmnet)
## Loading required package: Matrix
##
## Attaching package: 'Matrix'
## The following objects are masked from 'package:tidyr':
##
##
      expand, pack, unpack
## Loaded glmnet 3.0-2
library(pls)
##
## Attaching package: 'pls'
## The following object is masked from 'package:stats':
##
##
      loadings
#Load dataset
dat = read.csv("/Users/1604091407/Downloads/final_project.csv")
2.1
# use blank dataframe to b joined
dat_blank = data.frame(rep(1:nrow(dat),1))
```

```
# use blank dataframe to b joined
dat_blank = data.frame(rep(1:nrow(dat),1))

# h index
h = c(3,10,30)
```

```
#use for loop to create and join 9 columns to dat_blank
for(i in 1:3){
  for(j in 1:3){
  dat_col = dat[,i+1]
  dat temp = dat %>% mutate(shift = lag(dat col,h[i])) %>% mutate(temp =
ifelse(is.na(shift),dat[1,i+1],shift) , last = (dat[,i+1] - temp) / temp)
  dat blank = cbind(dat blank, dat temp$last)
}
#drop the first column
dat blank = dat blank[,-1]
#rename the column
name first = rep(NA, 9)
for(i in 1:3){
  for(j in 1:3){
    name_first[j +(i-1)*3] = paste0("Asset_",i,"_BRet_",h[j])
  }
}
colnames(dat_blank) = name_first
```

```
#export csv
dat_blank = dat_blank %>% round(4)
dat_2.1 = write.csv(dat_blank,"/Users/1604091407/Desktop/stats 415
hw/final_project/bret.csv",row.names=FALSE)
```

#2.2

```
dat_cor = dat_blank[,c(1,4,7)]
left = nrow(dat_cor) - 21*24*60
first_index = c(rep(1,21*24*60),(1:left))
second_index = 1:nrow(dat_blank)

Rho_1_2 = rep(NA, 524160)
Rho_2_3 = rep(NA, 524160)
Rho_1_3 = rep(NA, 524160)

for(i in 1:nrow(dat_cor)){
   temp_dat_1 = dat_cor$Asset_1_BRet_3[first_index[i]:second_index[i]]
   temp_dat_2 = dat_cor$Asset_2_BRet_3[first_index[i]:second_index[i]]
   temp_dat_3 = dat_cor$Asset_3_BRet_3[first_index[i]:second_index[i]]

   Rho_1_2[i] = cor(temp_dat_1,temp_dat_2)
   Rho_1_3[i] = cor(temp_dat_1,temp_dat_3)
```

```
Rho_2_3[i] = cor(temp_dat_2,temp_dat_3)
}
```

```
corr_dat = corr_dat %>% round(4)
corr_dat[is.na(corr_dat)] = 0
corr_dat
write_csv(corr_dat,"/Users/1604091407/Desktop/stats 415
hw/final_project/corr.csv")
#fill NA with value of 0
corr_dat[is.na(corr_dat)] = 0
```

2.3

Remark: As we can see from the summary of linear regression below, all the backward returns of Asset 2 and Asset 3 are significant in predicting the forward return of Asset 1 except the 30-min backward return of asset 3.

The in-sample correlation between $\hat{r}_f(t, 10)$ and $r_f(t, 10)$ is 0.0678748, and the out-of-sample correlation between $\hat{r}_f(t, 10)$ and $r_f(t, 10)$ is 0.04067645.

#It seems that the correlation structure is stable over the year. However, there is some fluctuations in the beginning of the year

```
#dataset of forward return with asset_1 and h = 10
index_forward = c(11:524160,rep(524160,10))

dat_lead = dat %>% mutate(rf_10 = (Asset_1[index_forward] - Asset_1)/Asset_1)

#combine the rf_10 and the backward returns in 2.1
dat_forward = cbind(rf_10 = dat_lead$rf_10 ,dat_blank)

train_set = dat_forward[1:366912,]
test_set = dat_forward[366913:524160,]
```

```
#fit the training dataset with linear regression
lm_mod = lm(rf_10~.,data = train_set)
summary(lm_mod)
##
## Call:
## lm(formula = rf_10 ~ ., data = train_set)
```

```
##
## Residuals:
        Min
                   10
                         Median
                                       3Q
                                                Max
##
## -0.147289 -0.000919
                       0.000010 0.000928 0.085484
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
                  -1.036e-05 4.758e-06 -2.178 0.029391 *
## (Intercept)
## Asset_1_BRet_3   4.078e-02   4.077e-03   10.002   < 2e-16 ***
## Asset 1 BRet 10 1.708e-02 2.538e-03 6.730 1.70e-11 ***
## Asset_1_BRet_30 6.252e-03 1.261e-03 4.958 7.11e-07 ***
## Asset_2_BRet_3
                   2.591e-02 2.228e-03 11.626 < 2e-16 ***
## Asset 2 BRet 10 -5.405e-03 1.435e-03 -3.766 0.000166 ***
## Asset_2_BRet_30 8.884e-03 7.609e-04 11.677 < 2e-16 ***
                   1.834e-02 2.247e-03 8.164 3.26e-16 ***
## Asset_3_BRet_3
## Asset 3 BRet 10 3.418e-03 1.441e-03 2.372 0.017716 *
## Asset_3_BRet_30 -9.622e-04 7.295e-04 -1.319 0.187194
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.002882 on 366902 degrees of freedom
## Multiple R-squared: 0.004607,
                                  Adjusted R-squared: 0.004583
## F-statistic: 188.7 on 9 and 366902 DF, p-value: < 2.2e-16
#the prediciton with linear regression wrt to training set
lm_predict_train = predict(lm_mod,newdata = train_set)
#the prediciton with linear regression wrt to testing set
lm_predict_test = predict(lm_mod, newdata = test_set)
#in-sample correlation
cor(lm_predict_train,train_set$rf_10)
## [1] 0.0678748
#out-of-sample correlation
cor(lm_predict_test, test_set$rf_10)
## [1] 0.04067645
```

```
lm_cor = rep(NA,524160)

#calculate the three week backward returns
left = length(lm_cor) - 21*24*60
first_index = c(rep(1,21*24*60),(1:left))
second_index = 1:length(lm_cor)

#using the train model to predict the whole year rf(t,10)
```

```
lm_year_pred = predict(lm_mod,newdata = dat_forward)

for(i in 1:524160){
   temp_year_pred = lm_year_pred[first_index[i]:second_index[i]]
   temp_rf_10 = dat_forward$rf_10[first_index[i]:second_index[i]]
   lm_cor[i] = cor(temp_year_pred,temp_rf_10)
}
lm_cor[1] = 0
# plot the three week backward correlation between rf(t,10)_head and rf(t,10)
plot(lm_cor,cex = 0.5,ylab = "correlation coefficient")
```

2.4

```
# run KNN with the rest of the K candidates
k_reg_c = c(5,25,50,125,625)
train_mse_knn_c = rep(NA,length(k_reg_c))
test_mse_knn_c = rep(NA,length(k_reg_c))

#run KNN regression
for(i in 1:length(k_reg_c)){
    train_temp = knn.reg(train = train_set[,-1],test = train_set[,-1],y =
    train_set$rf_10,k = k_reg_c[i])
    train_mse_knn_c[i] = mean((train_temp$pred - train_set$rf_10)^2)

    test_temp = knn.reg(train = train_set[,-1],test = test_set[,-1],y =
    train_set$rf_10,k = k_reg_c[i])
    test_mse_knn_c[i] = mean((test_temp$pred - test_set$rf_10)^2)
}
```

```
# run KNN with the rest of the K candidates
k_reg_w = c(1000)
train_mse_knn_w = rep(NA,length(k_reg_w))
test_mse_knn_w = rep(NA,length(k_reg_w))

#run KNN regression
for(i in 1:length(k_reg_w)){
    train_temp = knn.reg(train = train_set[,-1],test = train_set[,-1],y =
    train_set$rf_10,k = k_reg_w[i])
    train_mse_knn_w[i] = mean((train_temp$pred - train_set$rf_10)^2)

    test_temp = knn.reg(train = train_set[,-1],test = test_set[,-1],y =
    train_set$rf_10,k = k_reg_w[i])
    test_mse_knn_w[i] = mean((test_temp$pred - test_set$rf_10)^2)
}
```

```
k_reg_all = c(k_reg_c,k_reg_w) %>% print()
## [1] 5 25 50 125 625 1000

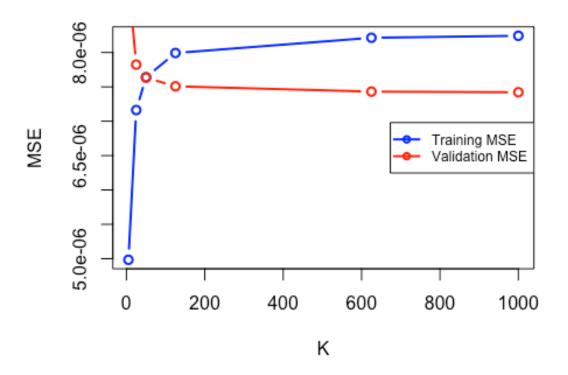
train_mse_all = c(train_mse_knn_c,train_mse_knn_w) %>% print()
## [1] 4.983888e-06 7.162388e-06 7.640673e-06 7.992362e-06 8.214067e-06
## [6] 8.242839e-06

test_mse_all = c(test_mse_knn_c,test_mse_knn_w) %>% print()
## [1] 9.056682e-06 7.823743e-06 7.633455e-06 7.507690e-06 7.430419e-06
## [6] 7.421158e-06

plot(x = k_reg_all,y = train_mse_all,type = "b",col = "blue",main = "Training and Testing MSE v.s. different K",xlab = "K",ylab = "MSE",lwd = 2)
lines(x = k_reg_all,y = test_mse_all, type = "b", lwd = 2, col = "red")

legend("right", legend = c("Training MSE", "Validation MSE"),
col = c("blue", "red"), cex = .75, lwd = c(2, 2), pch = c(1, 1), lty = c(1, 1))
```

Training and Testing MSE v.s. different K



```
#optimal K based on the validation MSE
best_k = k_reg_all[which.min(test_mse_all)] %>% print()
## [1] 1000
#in-sample correlation between prediction and response
train_knn_best = knn.reg(train = train_set[,-1],test = train_set[,-1],y =
train_set$rf_10,k = best_k)
cor(train_knn_best$pred,train_set$rf_10) %>% print()
## [1] 0.1181981
#out-of-sample correlation between prediction and response
test_knn_best = knn.reg(train = train_set[,-1],test = test_set[,-1],y =
train_set$rf_10,k = best_k)
cor(test_knn_best$pred,test_set$rf_10) %>% print()
## [1] 0.0432636
#prediction of whole year using the optimal K
knn_best_all = knn.reg(train = train_set[,-1],test = dat_forward[,-1],y =
train_set$rf_10,k = best_k)
knn_best_all$pred %>% head(10)
```

```
## [1] -1.195285e-04 1.911873e-04 1.527146e-04 3.135965e-05 -5.334502e-05 ## [6] -3.334279e-04 -1.269600e-04 -2.894834e-05 -4.473460e-04 -5.403406e-04
```

2.5 Ridge and Lasso

Hello

```
h_{ridge} = c(3,10,30,60,120,180,240,360,480,600,720,960,1200,1440)
dat rl blank = data.frame(rep(1:nrow(dat),1))
#use for loop to create and join 9 columns to dat blank
for(i in 1:3){
  for(j in 1:length(h_ridge)){
  dat_rl_col = dat[,i+1]
  dat_rl_temp = dat %>% mutate(shift_rl = lag(dat_rl_col,h_ridge[j])) %>%
mutate(temp = ifelse(is.na(shift_rl),dat[1,i+1],shift_rl) , last = (dat[,i+1]
- temp) / temp)
  dat_rl_blank = cbind(dat_rl_blank, dat_rl_temp$last)
  }
}
#drop the first column
data_rl = dat_rl_blank[,-1]
#rename the column
name rl = rep(NA, 42)
for(i in 1:3){
  for(j in 1:14){
    name_rl[j + (i-1)*14] = paste0("Asset_",i,"_BRet_",h_ridge[j])
  }
colnames(data rl) = name rl
data_rl_full = cbind(rf_10 = dat_forward$rf_10,data_rl)
```

Hello

```
# use prediction matix
X_rl = model.matrix(rf_10 ~ .,data = data_rl_full)[, -1]

# y value
Y_rl = data_rl_full$rf_10

train_index = 1:(nrow(data_rl_full)*0.7)

#set up the training/testing X and Y
train_set_x = X_rl[train_index,]
train_set_y = Y_rl[train_index]
```

```
test_set_x = X_rl[-train_index,]
test_set_y = Y_rl[-train_index]
#check if the rows match the original dataset
nrow(train_set_x) + nrow(test_set_x)
## [1] 524160
length(train_set_y) + length(test_set_y)
## [1] 524160
###ridge regression hello
#ridge regression
ridge.mod = glmnet(x = train_set_x,train_set_y,alpha = 0)
ridge.pred.test = predict(ridge.mod, newx = test_set_x)
#test MSE
ridge.test.mse = colMeans((ridge.pred.test - matrix(test_set_y ,
length(test_set_y),ncol(ridge.pred.test)))^2)
ind.min = which.min(ridge.test.mse)
ridge.lambda = ridge.mod$lambda[ind.min]
#prediction for whole year
ridge.pred = predict(ridge.mod, s=ridge.lambda, newx=X_rl)
ridge.pred %>% head(10)
##
                  1
## 1 -1.105216e-05
## 2 2.809314e-04
## 3 2.606674e-04
## 4 1.401545e-04
## 5 -1.482366e-04
## 6 -2.238085e-04
## 7 -1.253763e-04
     1.151948e-05
## 8
## 9 -6.792211e-05
## 10 -3.365496e-04
#in-sample correlation
cor(ridge.pred[train_index],train_set_y)
## [1] 0.07374825
#out-of-sample correlation
cor(ridge.pred[-train_index],test_set_y)
```

#lasso regression

```
#lasso regression
lasso.mod = glmnet(x = train_set_x,train_set_y,alpha =1)
lasso.pred.test = predict(lasso.mod, newx = test_set_x)
#test MSE
lasso.test.mse = colMeans((lasso.pred.test - matrix(test_set_y ,
length(test_set_y),ncol(lasso.pred.test)))^2)
ind.min.lasso = which.min(lasso.test.mse)
lasso.lambda = lasso.mod$lambda[ind.min.lasso]
#prediction for whole year
lasso.pred = predict(lasso.mod, s=lasso.lambda, newx=X_rl)
lasso.pred %>% head(10)
##
                  1
## 1 -1.079673e-05
## 2 3.223592e-04
## 3 3.038444e-04
     1.683735e-04
## 4
## 5 -1.694856e-04
## 6 -2.436007e-04
## 7 -1.292494e-04
## 8 2.994541e-05
## 9 -4.449895e-05
## 10 -3.208587e-04
#in-sample correlation
cor(lasso.pred[train_index],train_set_y)
## [1] 0.06743857
#out-of-sample correlation
cor(lasso.pred[-train_index],test_set_y)
## [1] 0.03913352
#2.6
pcr mse = rep(NA, 42)
   asset_pcr = pcr(rf_10~.,data =data_rl_full[train_index,],scale =
TRUE, center = TRUE)
for (i in 1:42){
    pcr_pred = predict(asset_pcr,newdata =data_rl_full[-train_index,],ncomp =
```

```
i)
    pcr_mse[i] = mean((pcr_pred -data_rl_full[-train_index,]$rf_10)^2)
}
best_ncp = which.min(pcr_mse)
```

```
#prediction of the whole year
pcr_pred = predict(asset_pcr,data_rl_full
[,names(data_rl_full)!='rf_10'],ncomp=best_ncp)
pcr_pred %>% head(10)

## [1] -9.850549e-06  3.199368e-04  2.878643e-04  1.372336e-04 -1.713111e-04

## [6] -2.573936e-04 -1.516407e-04  6.943068e-06 -8.316171e-05 -3.824973e-04

train_size = nrow(data_rl_full) *0.7

#in-sample correlation
cor(data_rl_full[train_index,]$rf_10, pcr_pred[1:train_size]) %>% print()

## [1] 0.06698264

#out-of-sample correlation
cor(data_rl_full[-train_index,]$rf_10, pcr_pred[-(1:train_size)]) %>% print()

## [1] 0.04155347
```