

# Introduction to Database Systems CSE 414

## Lecture 20: Design Theory

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## Class Overview

- Unit 1: Intro
- Unit 2: Relational Data Models and Query Languages
- Unit 3: Non-relational data
- Unit 4: RDBMS internals and query optimization
- Unit 5: Parallel query processing
- Unit 6: DBMS usability, conceptual design
  - E/R diagrams
  - Schema normalization
- Unit 7: Transactions

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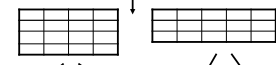
## Database Design Process

Conceptual Model:



Relational Model:

Tables + constraints  
And also functional dep.



Normalization:

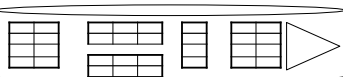
Eliminates anomalies

Conceptual Schema



Physical storage details

Physical Schema



## Entity / Relationship Diagrams

- Entity set = a class
  - An entity = an object
- Attribute
- Relationship

Product

city

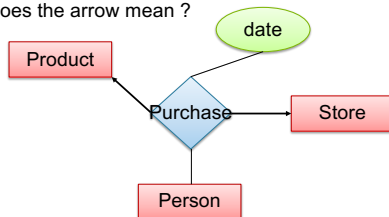
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## Arrows in Multiway Relationships

Q: What does the arrow mean ?

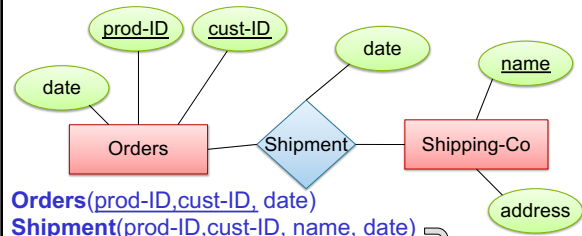


A: Any person buys a given product from at most one store  
AND every store sells to every person at most one product

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## N-N Relationships to Relations

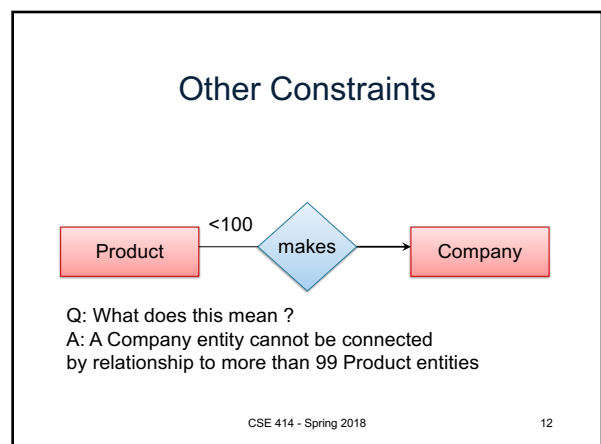
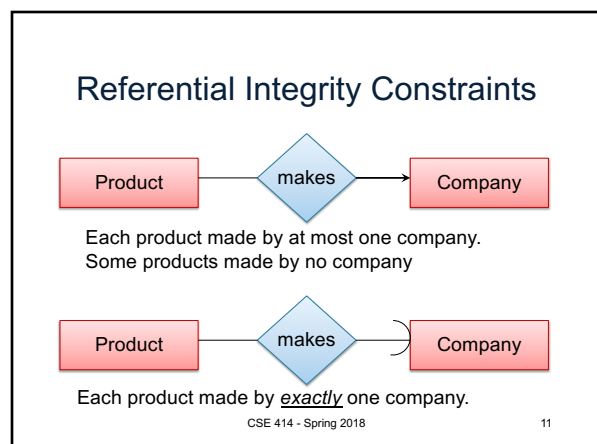
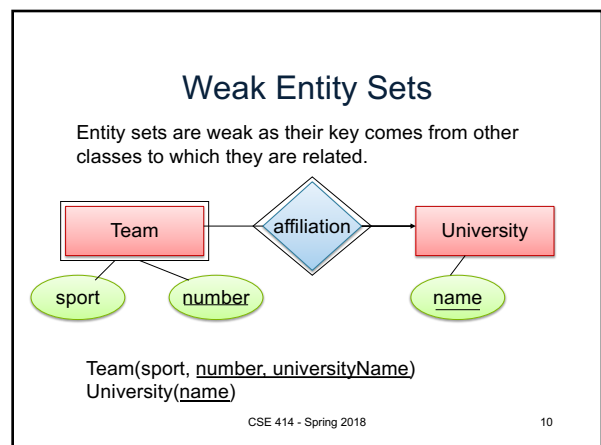
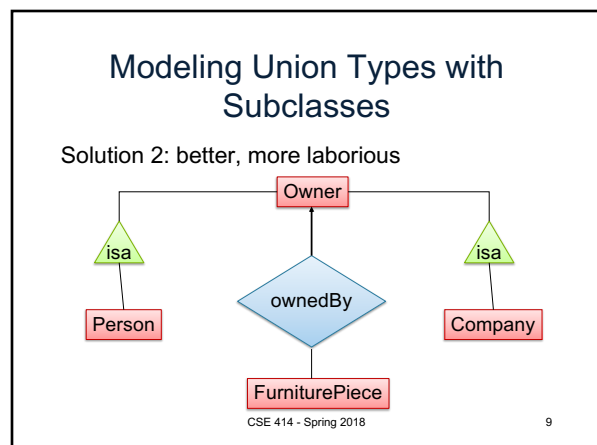
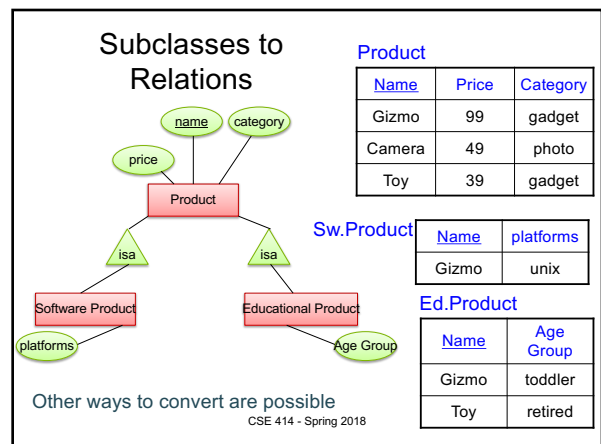
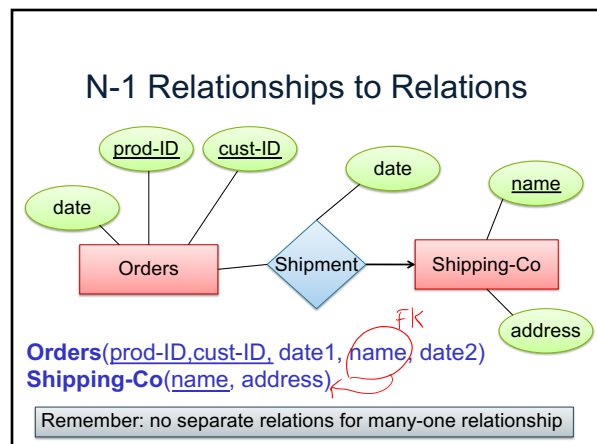


**Orders**(prod-ID, cust-ID, date)

**Shipment**(prod-ID, cust-ID, name, date)

**Shipping-Co**(name, address)

prod-ID	cust-ID	name	date
Gizmo55	Joe12	UPS	4/10/2011
Gizmo55	Joe12	FEDEX	4/9/2011



## Constraints in SQL

Constraints in SQL:

- **Keys, foreign keys**
- **Attribute-level** constraints
- **Tuple-level** constraints
- **Global** constraints: assertions

simplest

Most complex

- The more complex the constraint, the harder it is to check and to enforce

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## What happens when data changes?

- SQL has three policies for maintaining referential integrity:
- **NO ACTION** reject violating modifications (default)
- **CASCADE** after delete/update do delete/update
- **SET NULL** set foreign-key field to NULL
- **SET DEFAULT** set foreign-key field to default value
  - need to be declared with column, e.g.,  
CREATE TABLE Product (pid INT DEFAULT 42)

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## What makes good schemas?



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## Relational Schema Design

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

One person may have multiple phones, but lives in only one city

Primary key is thus (SSN, PhoneNumber)

What is the problem with this schema?

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## Relational Schema Design

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

### Anomalies:

- **Redundancy** = repeat data
- **Update anomalies** = what if Fred moves to "Bellevue"?
- **Deletion anomalies** = what if Joe deletes his phone number?

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## Relation Decomposition

Break the relation into two:

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

Name	SSN	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

SSN	PhoneNumber
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121

### Anomalies have gone:

- No more repeated data
- Easy to move Fred to "Bellevue" (how ?)
- Easy to delete all Joe's phone numbers (how ?)

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## Relational Schema Design (or Logical Design)

How do we do this systematically?

- Start with some relational schema
- Find out its **functional dependencies** (FDs)
- Use FDs to **normalize** the relational schema

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## Functional Dependencies (FDs)

### Definition

If two tuples agree on the attributes

$A_1, A_2, \dots, A_n$

then they must also agree on the attributes

$B_1, B_2, \dots, B_m$

Formally:

$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$

$A_1 \dots A_n$  determines  $B_1 \dots B_m$

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## Functional Dependencies (FDs)

**Definition**  $A_1, \dots, A_m \rightarrow B_1, \dots, B_n$  holds in R if:

for all  $t, t' \in R$ ,  
 $(t.A_1 = t'.A_1 \wedge \dots \wedge t.A_m = t'.A_m) \rightarrow t.B_1 = t'.B_1 \wedge \dots \wedge t.B_n = t'.B_n$

R	$A_1$	...	$A_m$	$B_1$	...	$B_n$
t						
t'						

if  $t, t'$  agree here then  $t, t'$  agree here

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## Example

An FD holds, or does not hold on an instance:

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234	Lawyer

$EmpID \rightarrow Name, Phone, Position$

$Position \rightarrow Phone$

but not  $Phone \rightarrow Position$

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## Example

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234	Lawyer

$Position \rightarrow Phone$

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## Example

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234	Lawyer

But not  $Phone \rightarrow Position$

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## Example

$\text{name} \rightarrow \text{color}$   
 $\text{category} \rightarrow \text{department}$   
 $\text{color, category} \rightarrow \text{price}$

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Green	Toys	99

Do all the FDs hold on this instance?

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## Example

$\text{name} \rightarrow \text{color}$   
 $\text{category} \rightarrow \text{department}$   
 $\text{color, category} \rightarrow \text{price}$

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Green	Toys	49
Gizmo	Stationary	Green	Office-supply	59

What about this one ?

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## Buzzwords

- FD **holds** or **does not hold** on an instance
- If we can be sure that *every instance of R* will be one in which a given FD is true, then we say that **R satisfies the FD**
- If we say that R satisfies an FD, we are **stating a constraint on R**

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## Why bother with FDs?

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

### Anomalies:

- Redundancy** = repeat data
- Update anomalies** = what if Fred moves to "Bellevue"?
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## An Interesting Observation

If all these FDs are true:

$\text{name} \rightarrow \text{color}$   
 $\text{category} \rightarrow \text{department}$   
 $\text{color, category} \rightarrow \text{price}$

Then this FD also holds:

$\text{name, category} \rightarrow \text{price}$

If we find out from application domain that a relation satisfies some FDs, it doesn't mean that we found all the FDs that it satisfies! There could be more FDs implied by the ones we have.

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## Closure of a set of Attributes

Given a set of attributes  $A_1, \dots, A_n$

The **closure** is the set of attributes B, notated  $\{A_1, \dots, A_n\}^+$ , s.t.  $A_1, \dots, A_n \rightarrow B$

Example:

1.  $\text{name} \rightarrow \text{color}$   
 2.  $\text{category} \rightarrow \text{department}$   
 3.  $\text{color, category} \rightarrow \text{price}$

Closures:

$\text{name}^+ = \{\text{name, color}\}$

$\{\text{name, category}\}^+ = \{\text{name, category, color, department, price}\}$

$\text{color}^+ = \{\text{color}\}$

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## Closure Algorithm

$X = \{A_1, \dots, A_n\}$ .

**Repeat** until  $X$  doesn't change **do**:  
**if**  $B_1, \dots, B_n \rightarrow C$  is a FD **and**  
 $B_1, \dots, B_n$  are all in  $X$   
**then** add  $C$  to  $X$ .

Example:

1.  $\text{name} \rightarrow \text{color}$
2.  $\text{category} \rightarrow \text{department}$
3.  $\text{color, category} \rightarrow \text{price}$

$\{\text{name, category}\}^+ =$   
 $\{\text{name, category, color, department, price}\}$

Hence:  $\text{name, category} \rightarrow \text{color, department, price}$

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## Example

In class:

$R(A, B, C, D, E, F)$

$A, B \rightarrow C$
$A, D \rightarrow E$
$B \rightarrow D$
$A, F \rightarrow B$

Compute  $\{A, B\}^+ \quad X = \{A, B, \quad \quad \quad \}$

Compute  $\{A, F\}^+ \quad X = \{A, F, \quad \quad \quad \}$

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## Example

In class:

$R(A, B, C, D, E, F)$

$A, B \rightarrow C$
$A, D \rightarrow E$
$B \rightarrow D$
$A, F \rightarrow B$

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Compute  $\{A, F\}^+ \quad X = \{A, F, \quad \quad \quad \}$

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Compute  $\{A, F\}^+ \quad X = \{A, F, B, C, D, E\}$

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## Example

In class:

$R(A, B, C, D, E, F)$

$A, B \rightarrow C$
$A, D \rightarrow E$
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Compute  $\{A, B\}^+ \quad X = \{A, B, C, D, E\}$

Compute  $\{A, F\}^+ \quad X = \{A, F, B, C, D, E\}$

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What is the key of  $R$ ?

## Practice at Home

Find all FD's implied by:

$A, B \rightarrow C$
$A, D \rightarrow B$
$B \rightarrow D$

Step 1: Compute  $X^+$ , for every  $X$ :

$A^+ = A, \quad B^+ = BD, \quad C^+ = C, \quad D^+ = D$

$AB^+ = ABCD, \quad AC^+ = AC, \quad AD^+ = ABCD,$

$BC^+ = BCD, \quad BD^+ = BD, \quad CD^+ = CD$

$ABC^+ = ABD^+ = ACD^+ = ABCD$  (no need to compute— why ?)

$BCD^+ = BCD, \quad ABCD^+ = ABCD$

Step 2: Enumerate all FD's  $X \rightarrow Y$ , s.t.  $Y \subseteq X^+$  and  $X \cap Y = \emptyset$  :

$AB \rightarrow CD, \quad AD \rightarrow BC, \quad ABC \rightarrow D, \quad ABD \rightarrow C, \quad ACD \rightarrow B$

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## Keys

$R(A_1, \dots, A_n, B)$

- A **superkey** is a set of attributes  $A_1, \dots, A_n$  s.t. for any other attribute  $B$ , we have  $A_1, \dots, A_n \rightarrow B$
- A **key** is a minimal superkey
  - A superkey and for which no subset is a superkey

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## Computing (Super)Keys

- For all sets  $X$ , compute  $X^+$
- If  $X^+ = [\text{all attributes}]$ , then  $X$  is a superkey
- Try reducing to the minimal  $X$ 's to get the key

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## Example

Product(name, price, category, color)

name, category  $\rightarrow$  price  
category  $\rightarrow$  color

What is the key ?

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## Example

Product(name, price, category, color)

name, category  $\rightarrow$  price  
category  $\rightarrow$  color

What is the key ?

$(\text{name, category})^+ = \{ \text{name, category, price, color} \}$

Hence (name, category) is a key

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## Key or Keys ?

Can we have more than one key ?

Given  $R(A,B,C)$  define FD's s.t. there are two or more distinct keys

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## Key or Keys ?

Can we have more than one key ?

Given  $R(A,B,C)$  define FD's s.t. there are two or more distinct keys

$A \rightarrow B$   
 $B \rightarrow C$   
 $C \rightarrow A$

or

$AB \rightarrow C$   
 $BC \rightarrow A$

or

$A \rightarrow BC$   
 $B \rightarrow AC$

what are the keys here ?

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## Eliminating Anomalies

Main idea:

- $X \rightarrow A$  is OK if X is a (super)key
- $X \rightarrow A$  is not OK otherwise
  - Need to decompose the table, but how?

## Boyce-Codd Normal Form

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## Boyce-Codd Normal Form

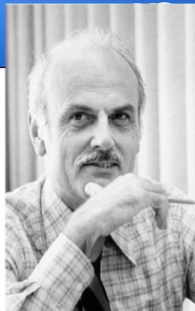
Dr. Raymond F. Boyce

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Edgar Frank "Ted" Codd

"A Relational Model of Data for Large Shared Data Banks"



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## Boyce-Codd Normal Form

There are no "bad" FDs:

**Definition.** A relation R is in BCNF if:

Whenever  $X \rightarrow B$  is a non-trivial dependency, then X is a superkey.

Equivalently:

**Definition.** A relation R is in BCNF if:

$\forall X$ , either  $X^+ = X$  or  $X^+ = [\text{all attributes}]$

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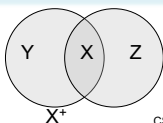
## BCNF Decomposition Algorithm

Normalize(R)

find X s.t.:  $X \neq X^+$  and  $X^+ \neq [\text{all attributes}]$

**if** (not found) **then** "R is in BCNF"

**let**  $Y = X^+ - X$ ;  $Z = [\text{all attributes}] - X^+$   
 decompose R into  $R_1(X \cup Y)$  and  $R_2(X \cup Z)$   
 Normalize( $R_1$ ); Normalize( $R_2$ );



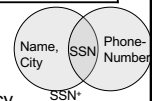
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## Example

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

$SSN \rightarrow \text{Name, City}$



The only key is:  $\{SSN, \text{PhoneNumber}\}$

Hence  $SSN \rightarrow \text{Name, City}$  is a "bad" dependency

In other words:

$SSN^+ = SSN, \text{Name, City}$  and is neither SSN nor All Attributes

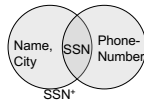


## Example BCNF Decomposition

Name	SSN	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

SSN  $\rightarrow$  Name, City

SSN	PhoneNumber
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121
987-65-4321	908-555-1234



Let's check anomalies:

- Redundancy ?
- Update ?
- Delete ?