



UNIVERSITY OF
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Bag A or Bag B?

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Bag A or Bag B?

BAG A

Face Value	Frequency
- 1,000	1
10	7
20	6
30	2
40	2
50	1
60	1

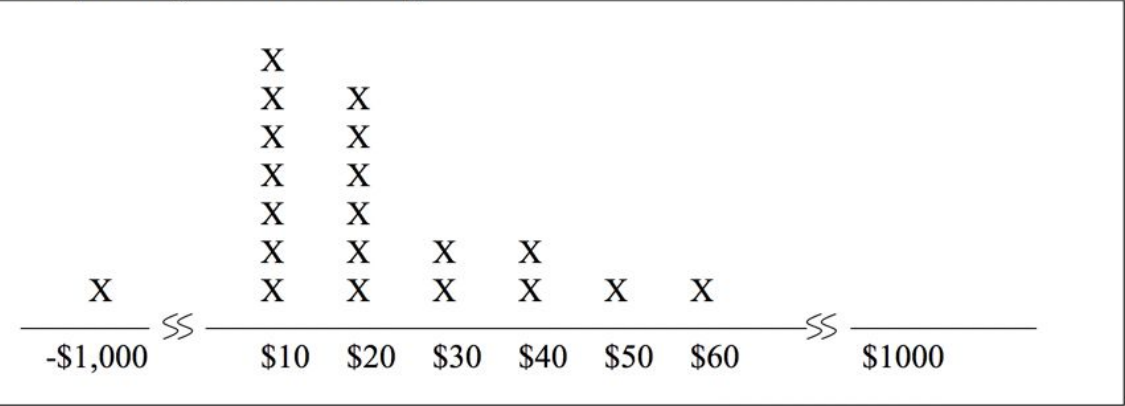
Total Value: -\$560

BAG B

Face Value	Frequency
10	1
20	1
30	2
40	2
50	6
60	7
1,000	1

Total Value: -\$1890

Frequency Plot for Bag A:

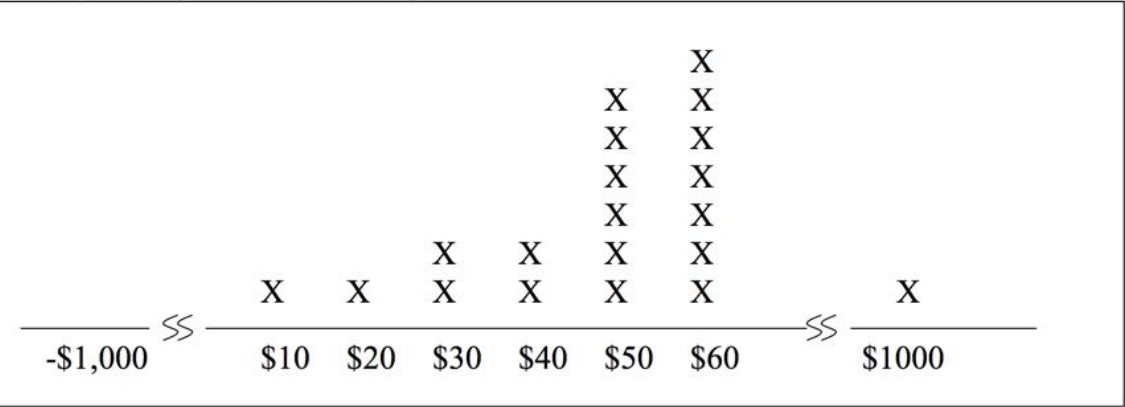


Select one voucher at random from shown bag and decide between two competing theories

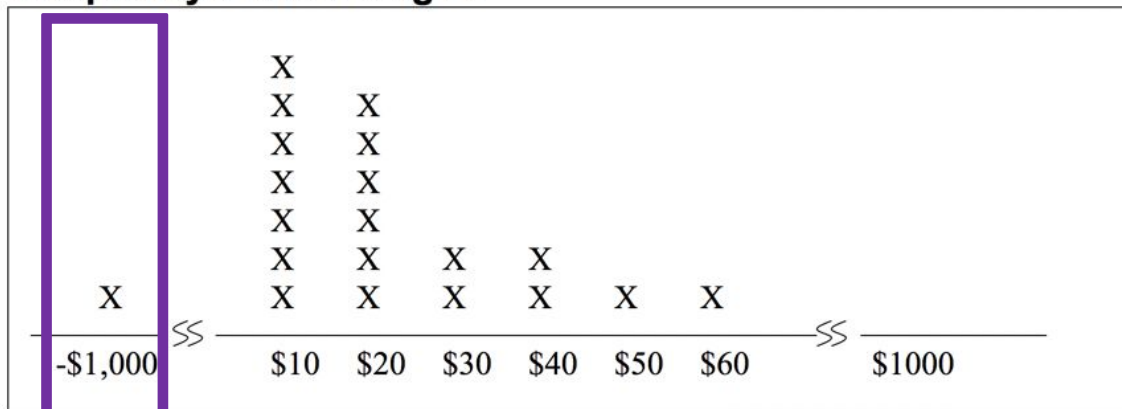
Null:
Shown bag is **Bag A**

Alternative:
Shown bag is **Bag B**

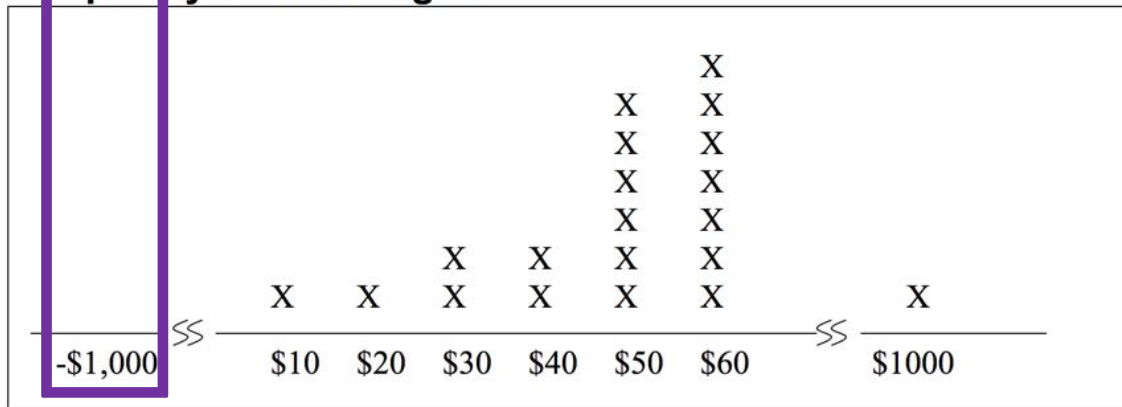
Frequency Plot for Bag B:



Frequency Plot for Bag A:



Frequency Plot for Bag B:



Null:

Shown bag is **Bag A**

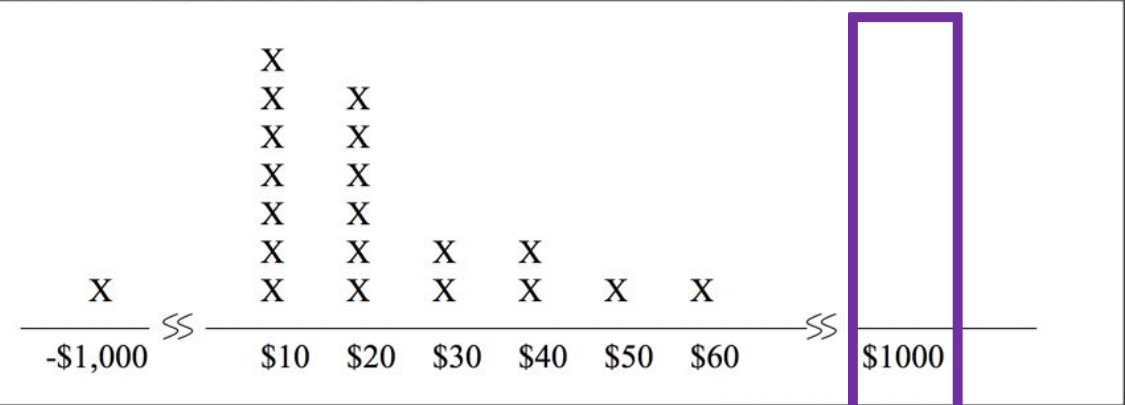
Alternative:

Shown bag is **Bag B**

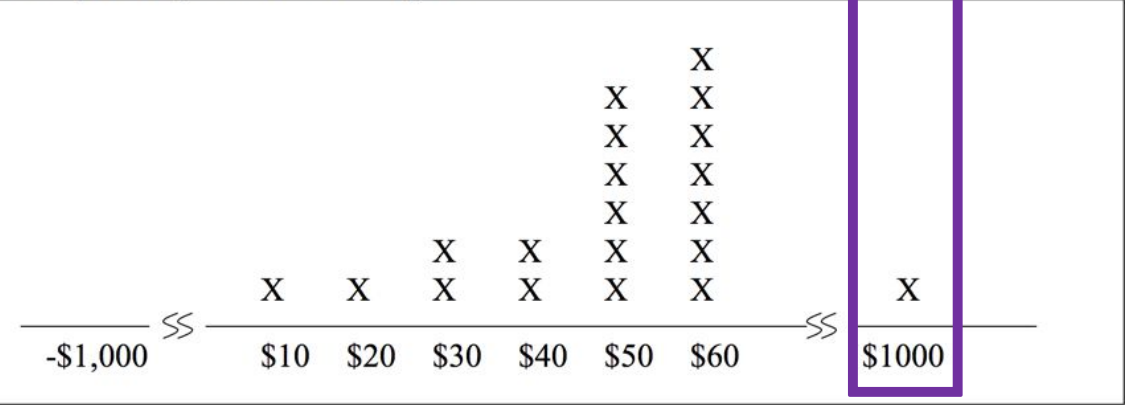
What if select -\$1,000?

=> Bag A

Frequency Plot for Bag A:



Frequency Plot for Bag B:



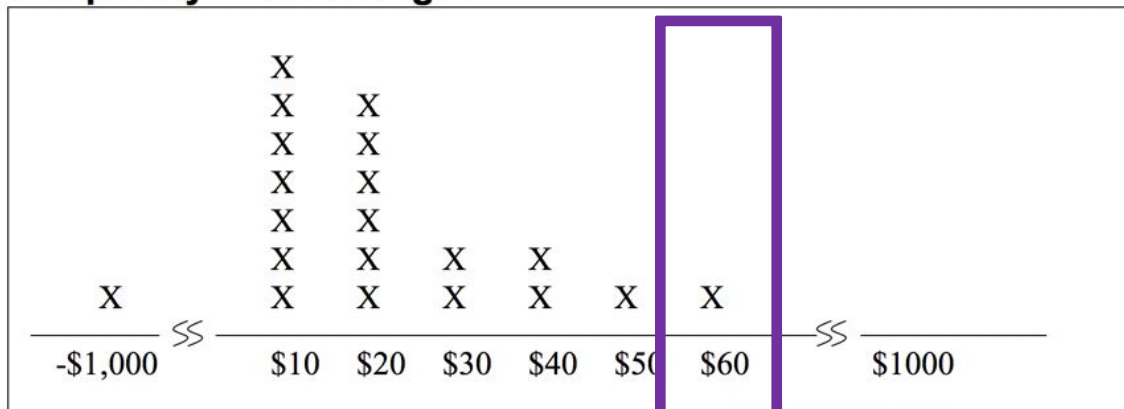
Null:
Shown bag is **Bag A**

Alternative:
Shown bag is **Bag B**

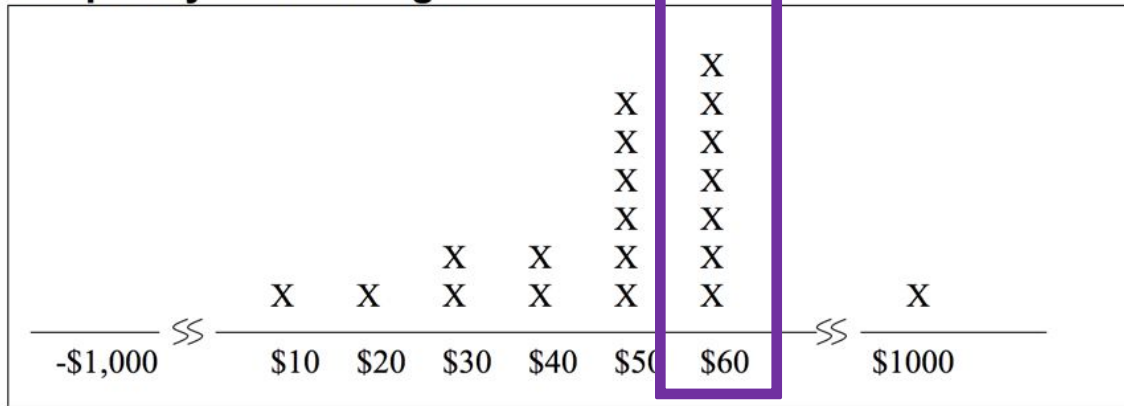
What if select \$1000?

⇒ Bag B

Frequency Plot for Bag A:



Frequency Plot for Bag B:



Null:

Shown bag is **Bag A**

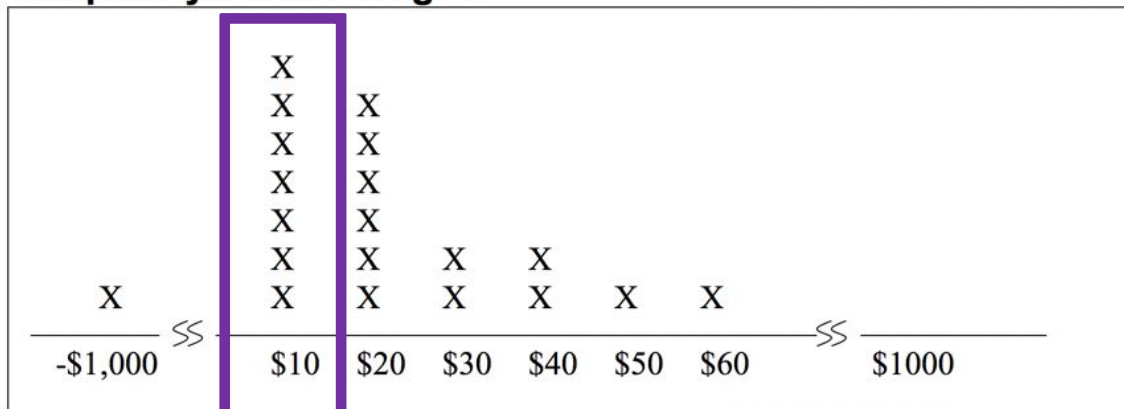
Alternative:

Shown bag is **Bag B**

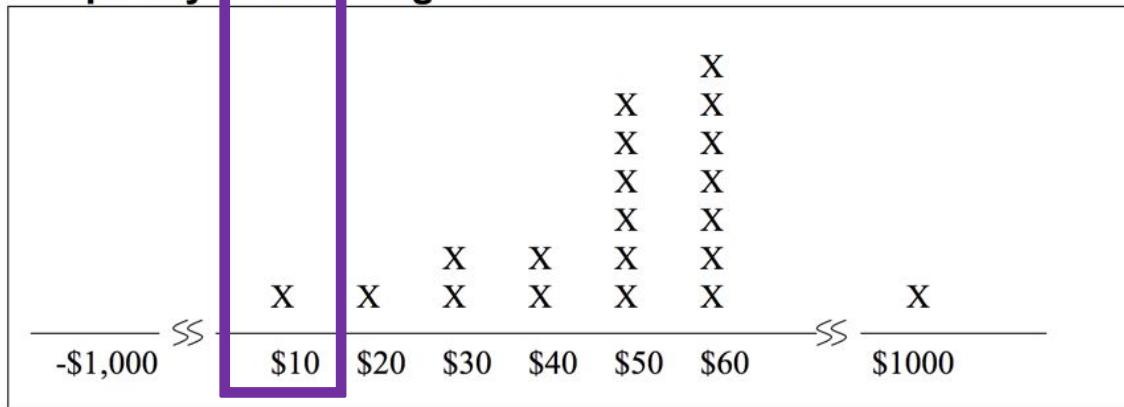
What if select \$60?

⇒ *Bag B*

Frequency Plot for Bag A:



Frequency Plot for Bag B:



Null:

Shown bag is **Bag A**

Alternative:

Shown bag is **Bag B**

What if select \$10?

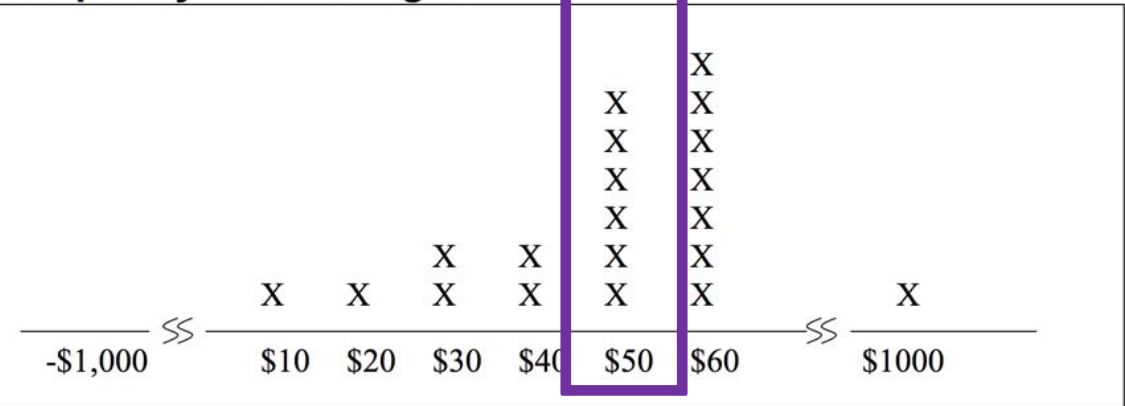
⇒ Bag A

Starting for form
a **decision rule**

Frequency Plot for Bag A:



Frequency Plot for Bag B:



Null:
Shown bag is **Bag A**

Alternative:
Shown bag is **Bag B**

What if select \$50?
⇒ Bag B

Frequency Plot for Bag A:



Frequency Plot for Bag B:

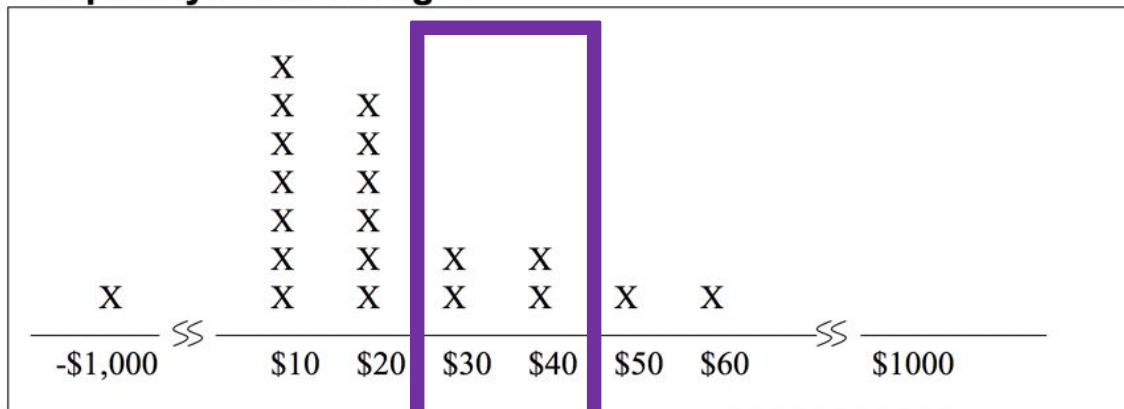


Null:
Shown bag is **Bag A**

Alternative:
Shown bag is **Bag B**

What if select \$20?
⇒ Bag A

Frequency Plot for Bag A:



Frequency Plot for Bag B:



Null:

Shown bag is **Bag A**

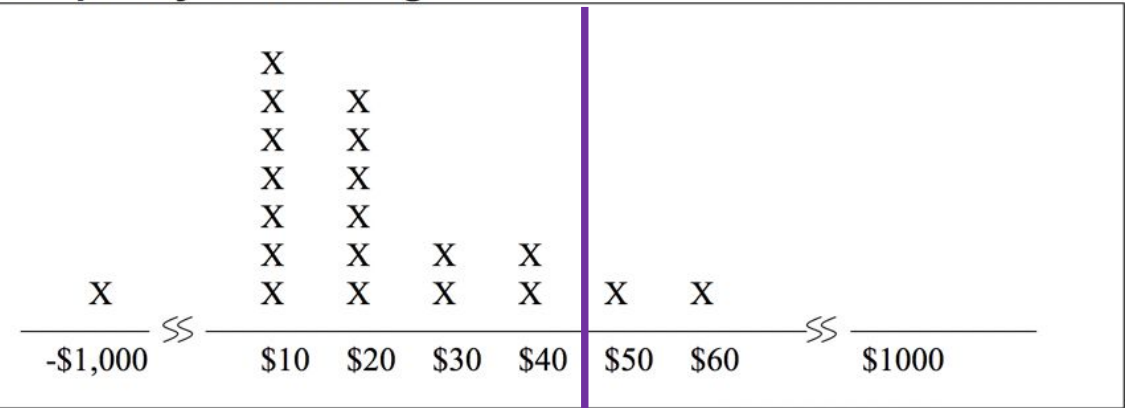
Alternative:

Shown bag is **Bag B**

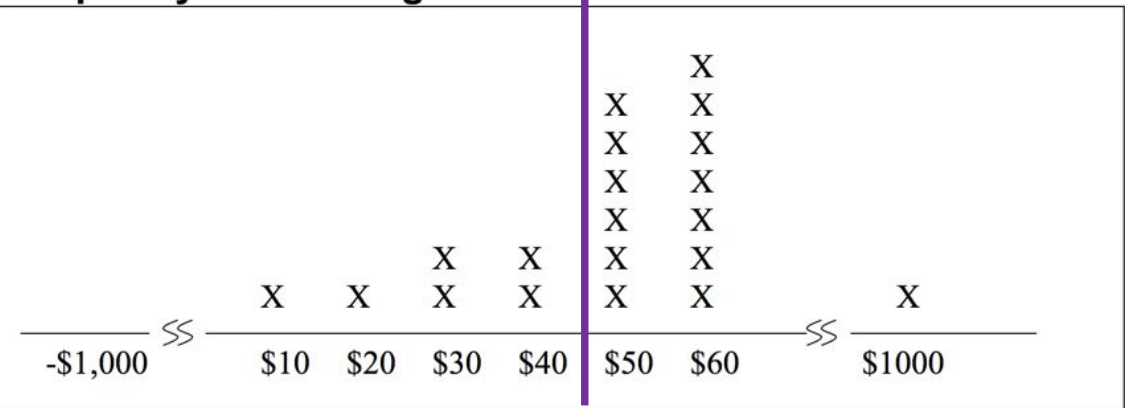
What if select \$40 or \$30?

equally likely

Frequency Plot for Bag A:



Frequency Plot for Bag B:



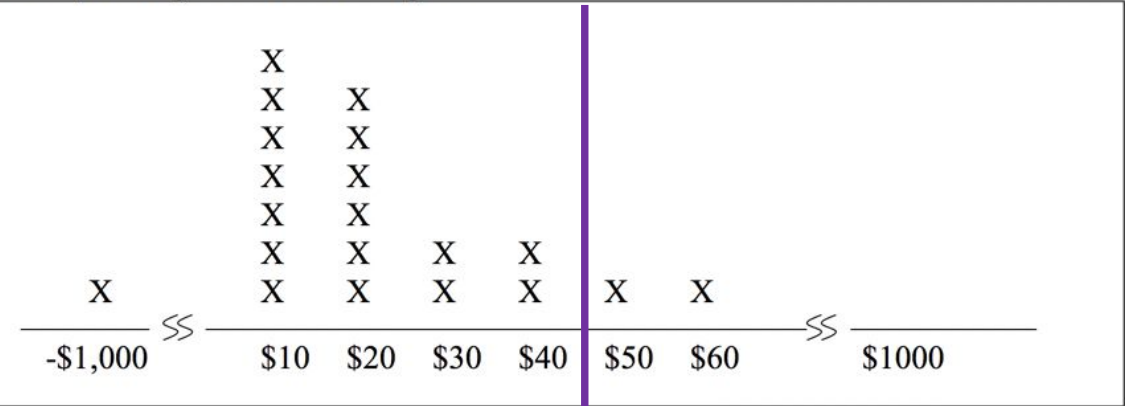
Reject the Null

Null:
Shown bag is **Bag A**

Alternative:
Shown bag is **Bag B**

Decision Rule:
Reject the Null if
voucher is
\$50 or higher

Frequency Plot for Bag A:



Frequency Plot for Bag B:



Reject the Null

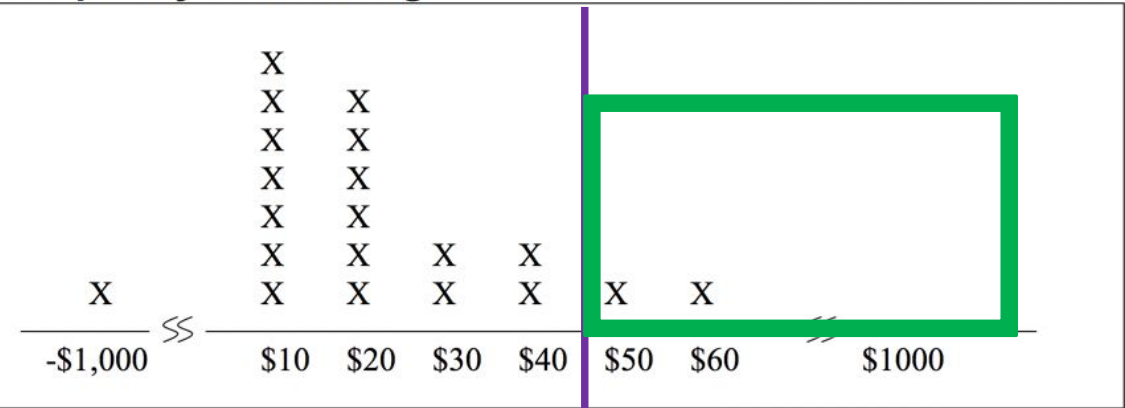
Null:
Shown bag is **Bag A**

Alternative:
Shown bag is **Bag B**

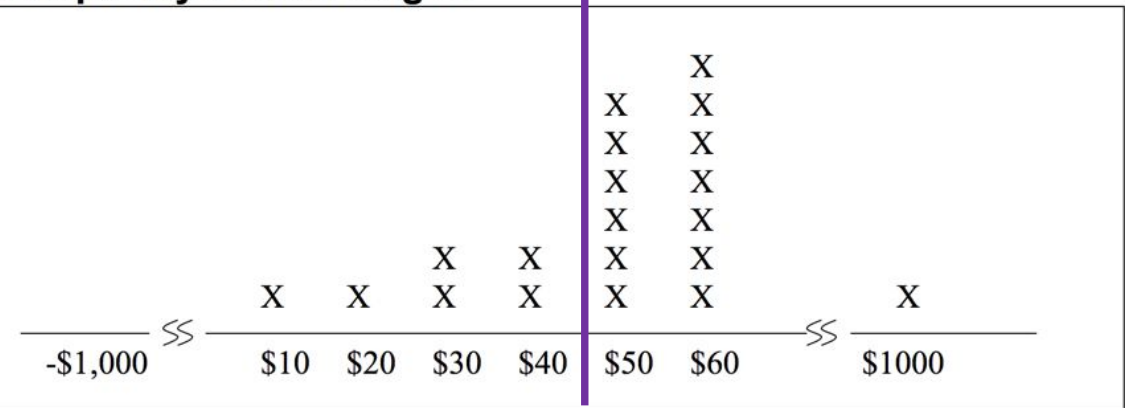
Decision Rule:
Reject the Null if
voucher is
\$50 or higher

Error: Reject Null when Null True

Frequency Plot for Bag A:



Frequency Plot for Bag B:



Reject the Null

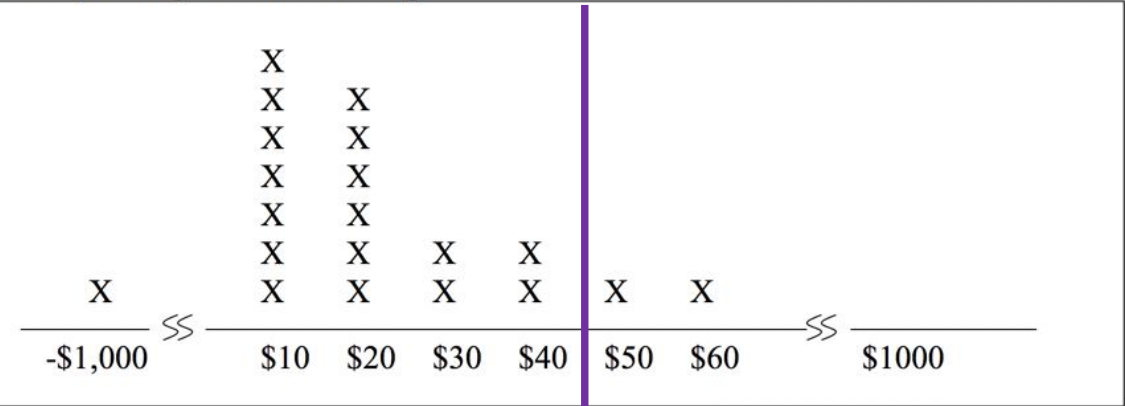
Null:
Shown bag is **Bag A**

Alternative:
Shown bag is **Bag B**

Decision Rule:
Reject the Null if
voucher is
\$50 or higher

Error: Reject Null when Null True

Frequency Plot for Bag A:



Frequency Plot for Bag B:



Reject the Null

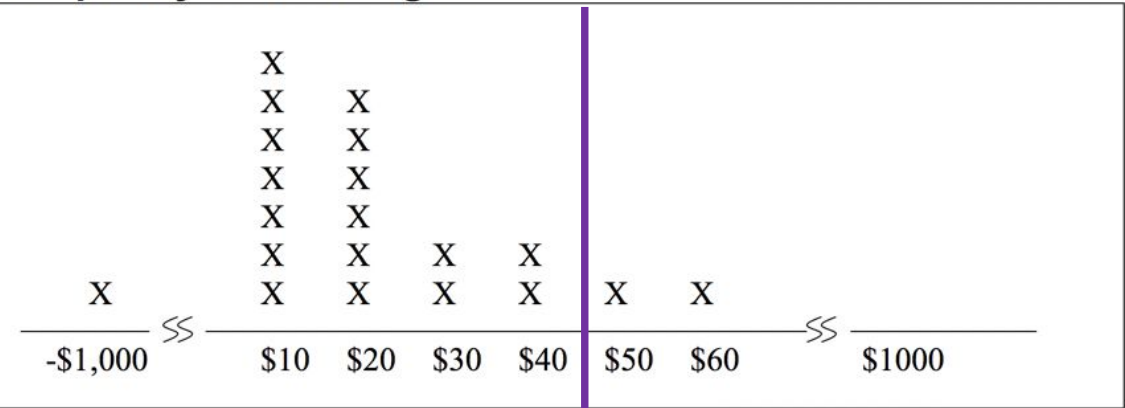
Null:
Shown bag is **Bag A**

Alternative:
Shown bag is **Bag B**

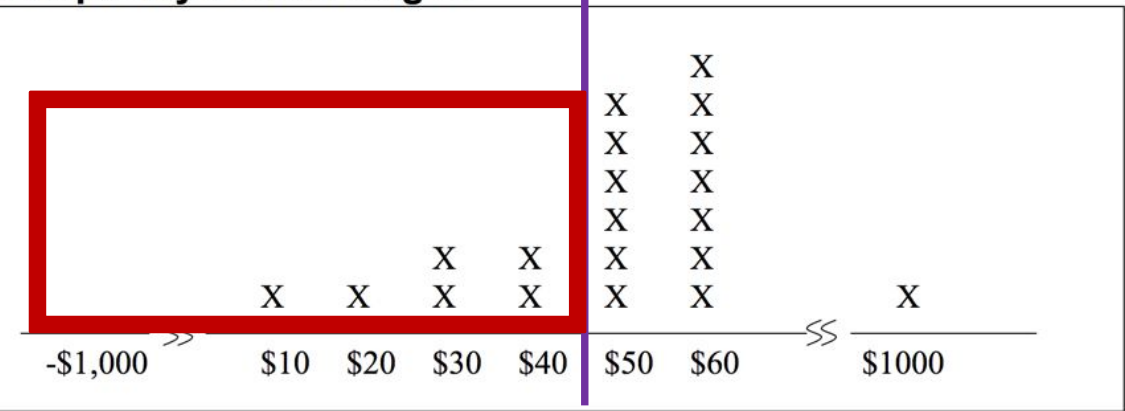
Decision Rule:
Reject the Null if
voucher is
\$50 or higher

**Other Error: Do not Reject Null
when Alternative True**

Frequency Plot for Bag A:



Frequency Plot for Bag B:



Reject the Null

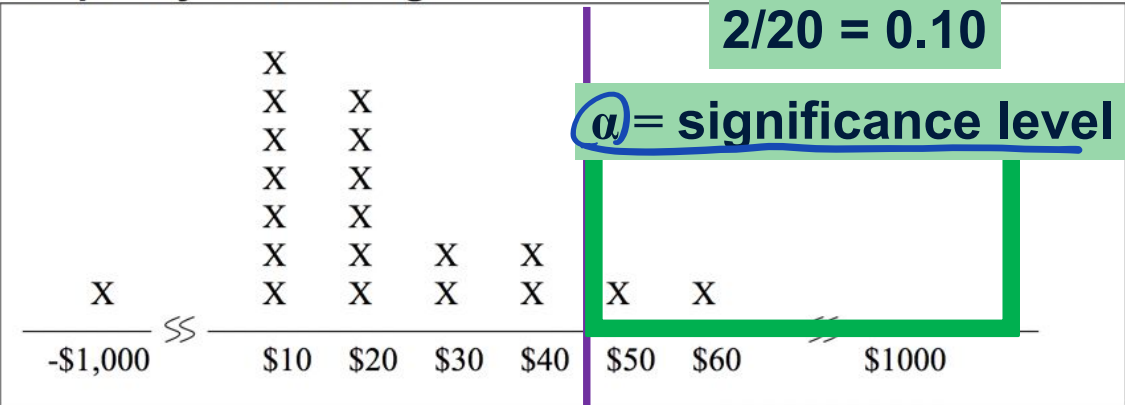
Null:
Shown bag is **Bag A**

Alternative:
Shown bag is **Bag B**

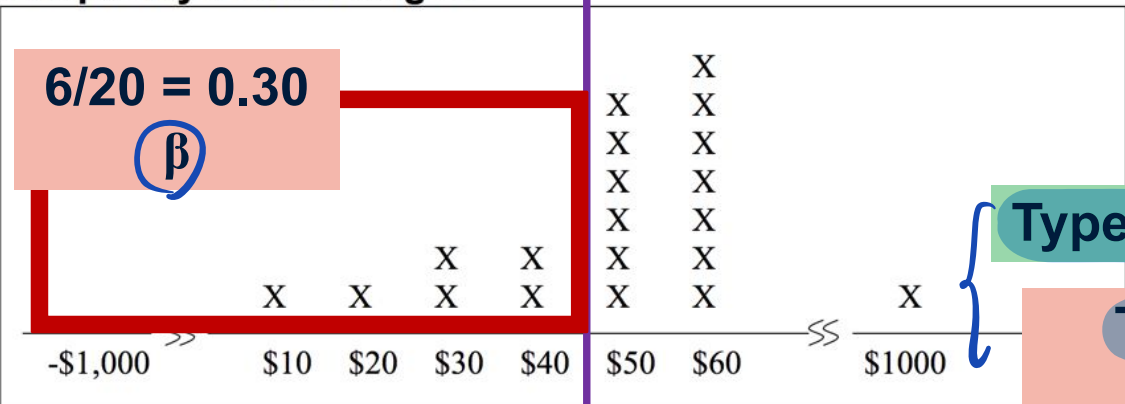
Decision Rule:
Reject the Null if
voucher is
\$50 or higher

**Other Error: Do not Reject Null
when Alternative True**

Frequency Plot for Bag A:



Frequency Plot for Bag B:



Reject the Null

Null:
Shown bag is **Bag A**

Alternative:
Shown bag is **Bag B**

Decision Rule:
Reject the Null if
voucher is
\$50 or higher

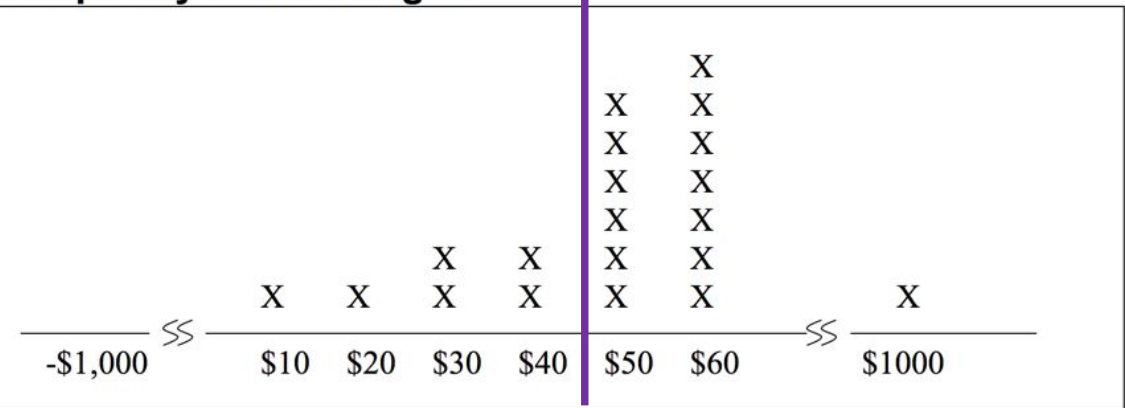
Type 1 Error: Reject Null when Null True

Type 2 Error: Do not Reject Null
when Alternative True

Frequency Plot for Bag A:



Frequency Plot for Bag B:



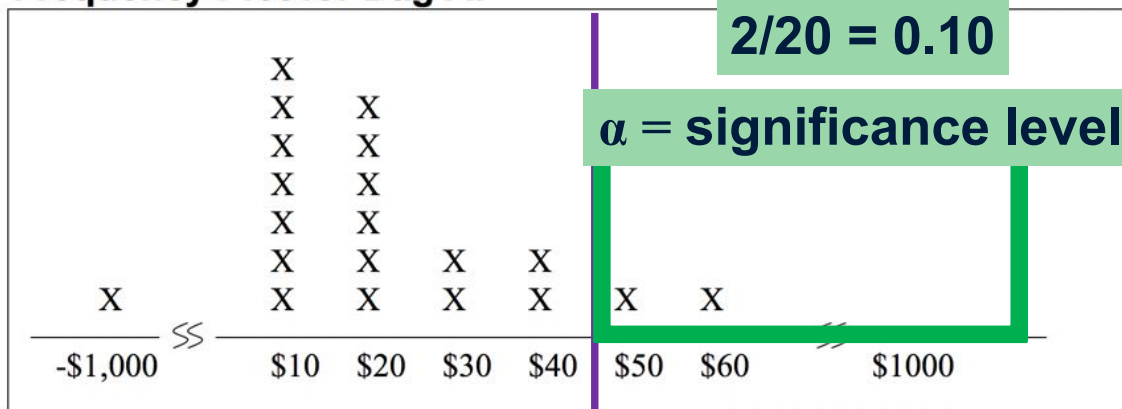
Reject the Null

Null:
Shown bag is **Bag A**

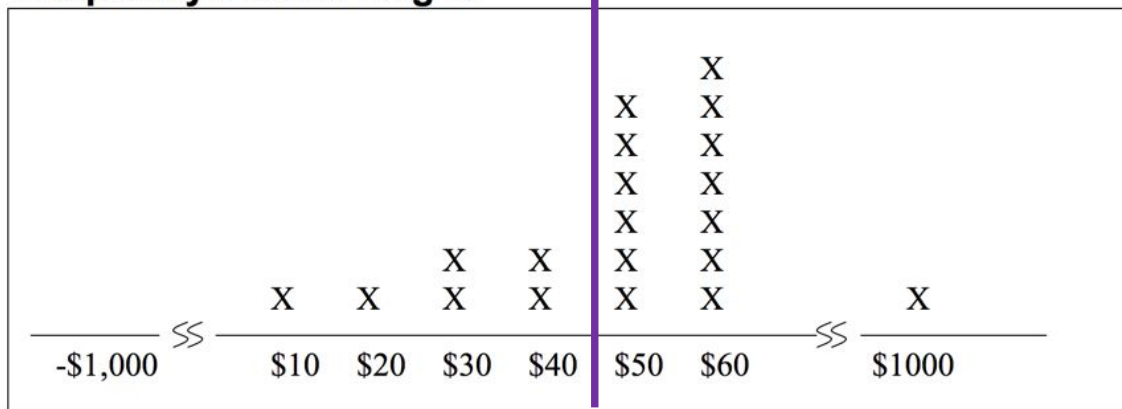
Alternative:
Shown bag is **Bag B**

Decision Rule:
Reject the Null if
voucher is
\$50 or higher

Frequency Plot for Bag A:



Frequency Plot for Bag B:



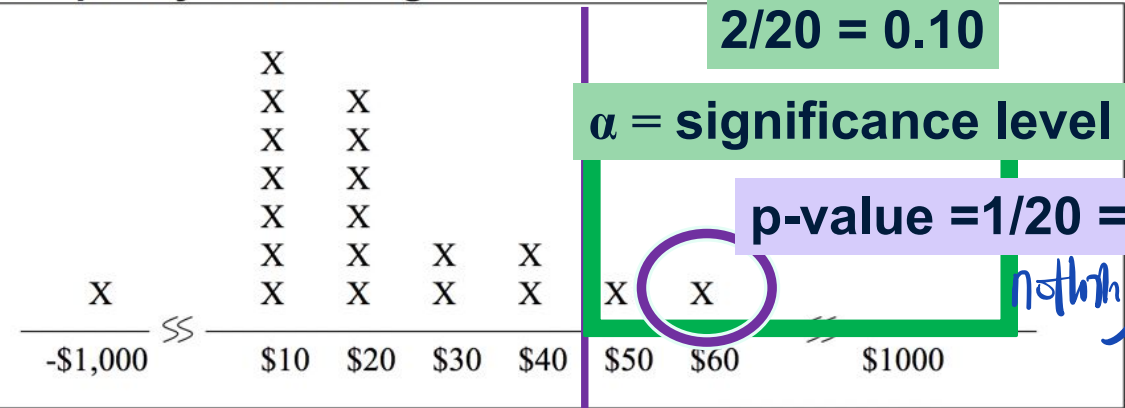
Null:
Shown bag is **Bag A**

Alternative:
Shown bag is **Bag B**

Decision Rule:
Reject the Null if
p-value is $\leq \alpha$

probability

Frequency Plot for Bag A:



Null:
Shown bag is **Bag A**

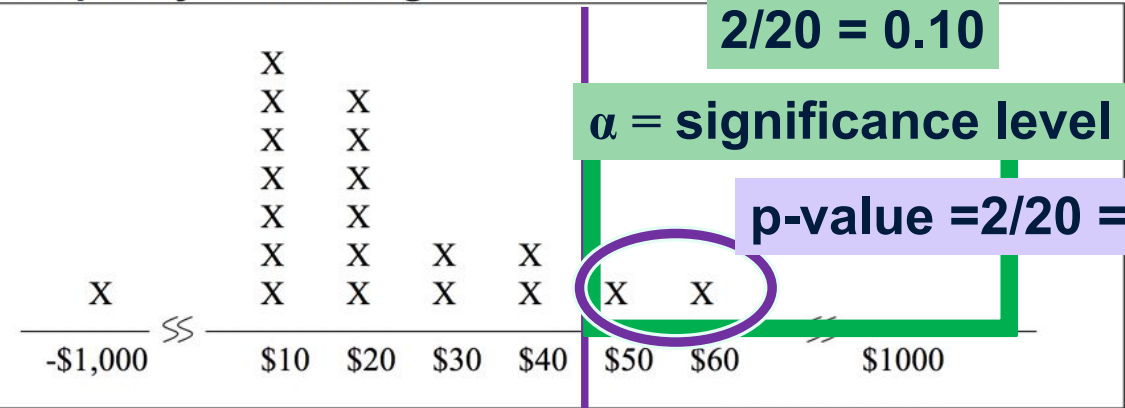
Alternative:
Shown bag is **Bag B**

Frequency Plot for Bag B:

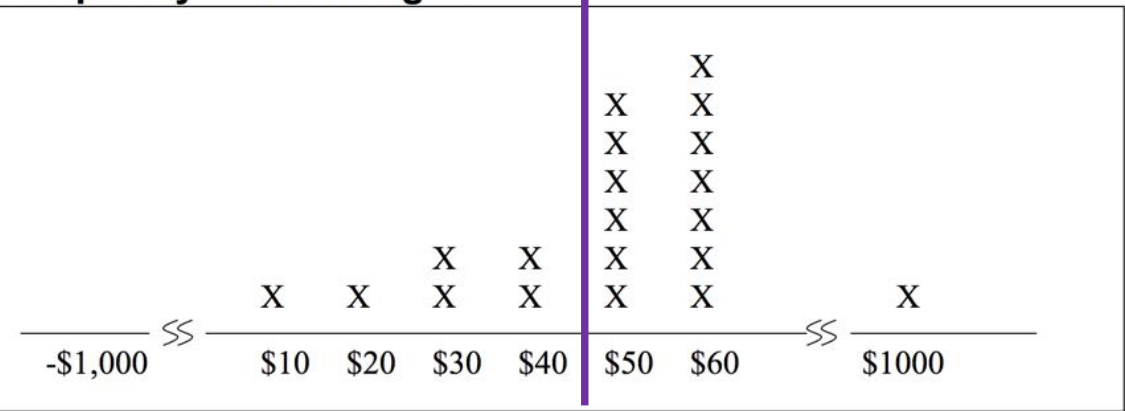


Decision Rule:
Reject the Null if
p-value is $\leq \alpha$

Frequency Plot for Bag A:



Frequency Plot for Bag B:

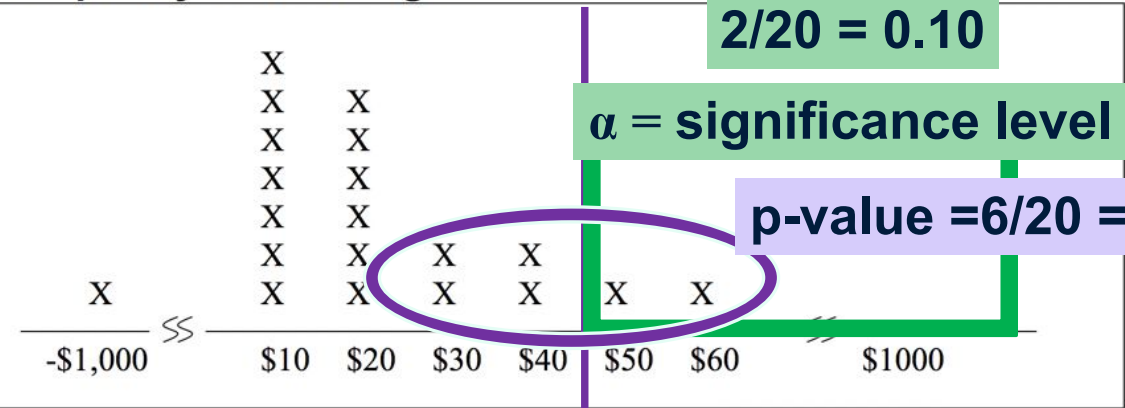


Null:
Shown bag is **Bag A**

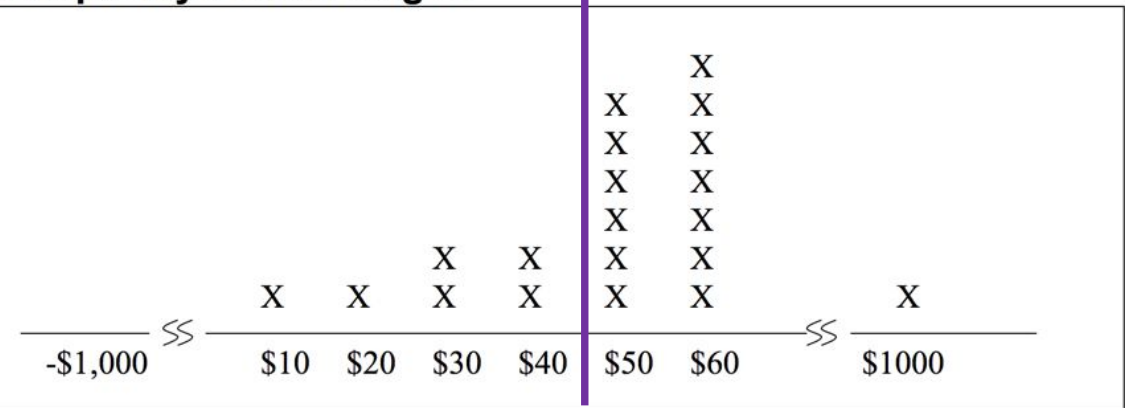
Alternative:
Shown bag is **Bag B**

Decision Rule:
Reject the Null if
 $p\text{-value} \leq \alpha$

Frequency Plot for Bag A:



Frequency Plot for Bag B:



Reject the Null

Null:
Shown bag is **Bag A**

Alternative:
Shown bag is **Bag B**

Decision Rule:
Reject the Null if
 $p\text{-value} \leq \alpha$

Hypothesis Testing

- Stating Hypotheses
- Selecting a Significance Level α
- Using data to make our decision (via p-value)

probability of at least extreme
when Null is true

More details about making inferences ahead!

happen frequentist
 or not happen

vs.

Bayesian

① probability is in your mind rather than in the world

② based on new information, you can update your probability