



### Bag A or Bag B?

### Brenda Gunderson





## Bag A or Bag B?

BAG A		BAG	В
Face Value	Frequency	Face Value	Frequency
- 1,000	1		
10	7	10	1
20	6	20	1
30	2	30	2
40	2	40	2
50	1	50	6
60	1	60	7
		1,000	1
	<b>+ - .</b> •		<b>+100</b>

Total Value: -\$560

Total Value: -\$1890





$$\frac{X}{X} = \frac{X}{X} = \frac{X}$$

Frequency Plot for Bag B:

						X	
					$\mathbf{X}$	X	
					$\mathbf{X}$	X	
					$\mathbf{X}$	X	
					X	X	
			X	X	X	X	
	X	X	X	$\mathbf{X}$	$\mathbf{X}$	X	X
	6	<u> </u>	8	- 13	100	860	—SS ———
-\$1,000	\$10	\$20	\$30	\$40	\$50	\$60	\$1000

Select one voucher at random from shown bag and decide between two competing theories

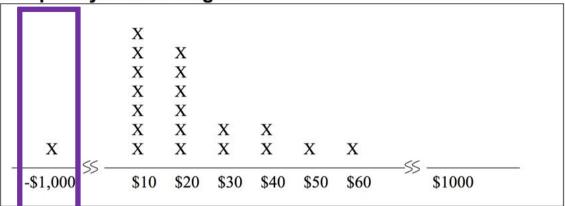
Null:

Shown bag is Bag A

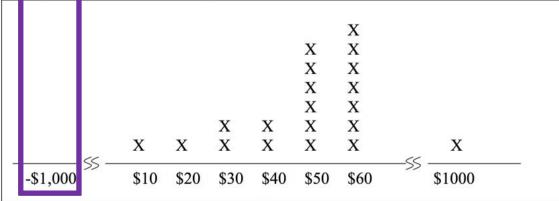
**Alternative**:

Shown bag is Bag B





Frequency Plot for Bag B:



Null:

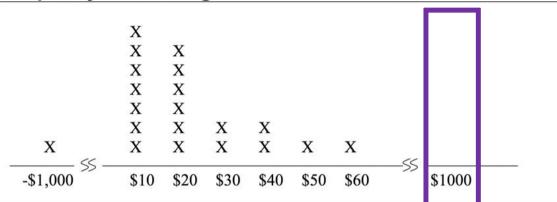
Shown bag is Bag A

**Alternative:** 

Shown bag is Bag B

What if select -\$1000?





Frequency Plot for Bag B:

						X			
					X	X			
					$\mathbf{X}$	X			
					$\mathbf{X}$	$\mathbf{X}$			
					X	X			
			X	X	X	$\mathbf{X}$			
	$\mathbf{X}$	X	X	X	X	X		X	
<del>-\$1,000</del> \$\$	\$10	\$20	\$30	\$40	\$50	\$60	——SS	\$1000	

Null:

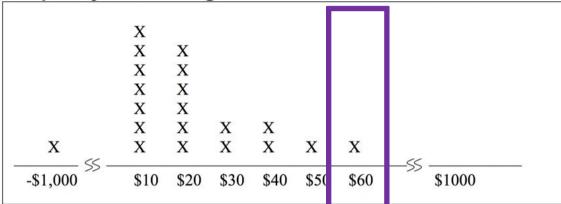
Shown bag is Bag A

**Alternative**:

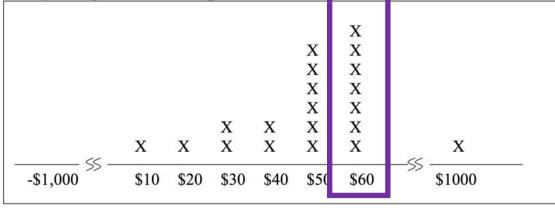
Shown bag is Bag B

What if select \$1000?





Frequency Plot for Bag B:



Null:

Shown bag is Bag A

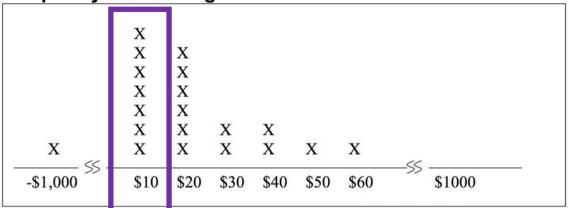
**Alternative:** 

Shown bag is Bag B

What if select \$60?







Frequency Plot for Bag B:

The second secon							
						X	
					X	X	
					X	X	
					X	$\mathbf{X}$	
					X	X	
	04000	0.1252	X X	X X	X X	$\mathbf{X}$	
	X	X	X	X	X	X	X
-\$1,000 SS ·	\$10	\$20	\$30	\$40	\$50	\$60	\$1000

Null:

Shown bag is Bag A

**Alternative:** 

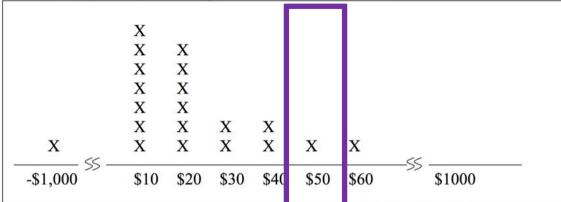
Shown bag is Bag B

What if select \$10?



Starting for form a **decision rule** 





Frequency Plot for Bag B:

						Y		
					X	X X X X X X		
					X X X X X	X		
					X	X		
					X	X		
			X X	X	X	X		
	X	X	X	X	X	X	X	
<del>-\$1,000</del> \$\$	\$10	\$20	\$30	\$40	\$50	\$60	\$1000	

Null:

Shown bag is Bag A

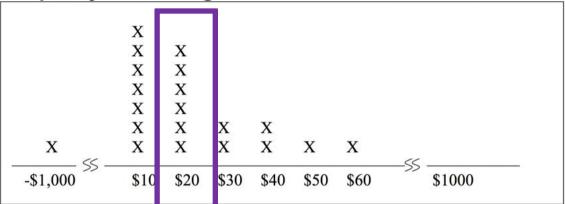
**Alternative:** 

Shown bag is Bag B

What if select \$50?







Frequency Plot for Bag B:

						X	
					$\mathbf{X}$	X	
					X	X	
					X	X	
					X	X	
			X	X	X	$\mathbf{X}$	
	X	X	X	X	X	X	X
<u> </u>							—SS ———
-\$1,000	\$10	\$20	\$30	\$40	\$50	\$60	\$1000
Ψ1,000	ΨΙΟ	Ψ20	Ψυσ	Ψισ	ΨΣΟ	ΨΟΟ	\$1000

Null:

Shown bag is Bag A

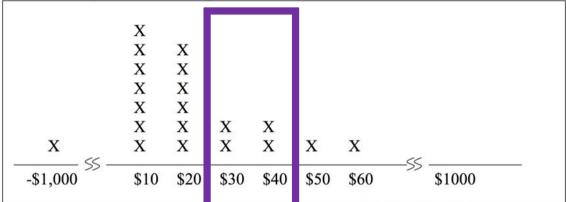
**Alternative:** 

Shown bag is Bag B

What if select \$20?







Frequency Plot for Ba B:

						X	
					X	X	
					X	X	
					X	$\mathbf{X}$	
					X X	X	
			X	X	X	$\mathbf{X}$	
	X	X	X	X	X	X	X
							<<
-\$1,000	\$10	\$20	\$30	\$40	\$50	\$60	\$1000

Null:

Shown bag is Bag A

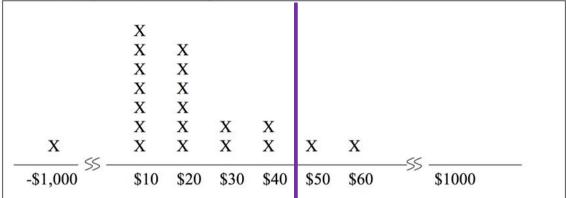
**Alternative:** 

Shown bag is Bag B

What if select \$40 or \$30?

equally likely





**Reject the Null** 

Frequency Plot for Bag B:

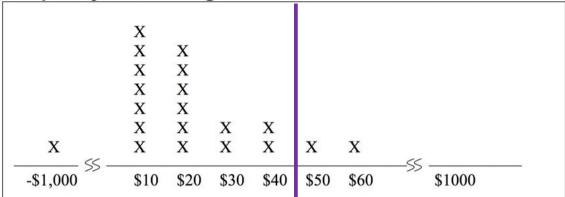
		;	,				
			·				
						X	
					X	X	
					X X X X	X	
					X	X	
					X	X	
			X	X X	X	$\mathbf{X}$	
	X	X	X	X	X	X	X
<del></del> \$\$ -						+	—SS ———
-\$1,000	\$10	\$20	\$30	\$40	\$50	\$60	\$1000

Null: Shown bag is **Bag A** 

Alternative: Shown bag is **Bag B** 

Decision Rule: Reject the Null if voucher is \$50 or higher





Reject the Null

Frequency Plot for Bag B:

					950000	X	
					X	$\mathbf{X}$	
					X	$\mathbf{X}$	
					X	X	
					X X X X	X	
			X X	X X	X	X	
	X	X	X	X	X	X	X
<del>-\$1,000</del> \$\$	\$10	\$20	\$30	\$40	\$50	\$60	<del></del>

Null:

Shown bag is Bag A

**Alternative:** 

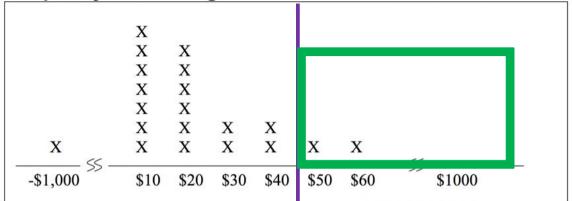
Shown bag is Bag B

Decision Rule: Reject the Null if voucher is \$50 or higher

**Error: Reject Null when Null True** 







**Reject the Null** 

#### Frequency Plot for Bag B:

						v			
					X	X X			
					X	X			
					X X X	X X			
					X	X			
			X X	X	X	X			
	X	X	X	X	X	X		X	
<del>-\$1,000</del> \$\$ -	\$10	\$20	\$30	\$40	\$50	\$60	—-SS	\$1000	

#### Null:

Shown bag is Bag A

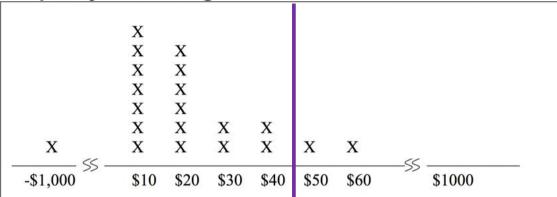
#### **Alternative:**

Shown bag is Bag B

Decision Rule: Reject the Null if voucher is \$50 or higher

**Error: Reject Null when Null True** 





Reject the Null

Frequency Plot for Bag B:

						$\mathbf{X}$	
					X	X	
					X	$\mathbf{X}$	
					X	$\mathbf{X}$	
					X	X	
			X	X	X	X X X X	
	X	X	X X	X X	X X X X	X	X
		8	8	136	100	1920	—SS ———
-\$1,000	\$10	\$20	\$30	\$40	\$50	\$60	\$1000
				•			

Null:

Shown bag is Bag A

**Alternative:** 

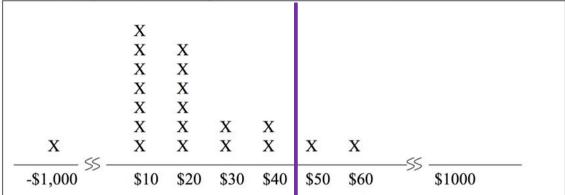
Shown bag is Bag B

Decision Rule: Reject the Null if voucher is \$50 or higher

Other Error: Do not Reject Null when Alternative True

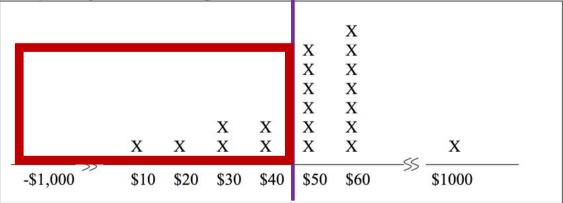






#### Reject the Null

#### Frequency Plot for Bag B:



#### Null:

Shown bag is Bag A

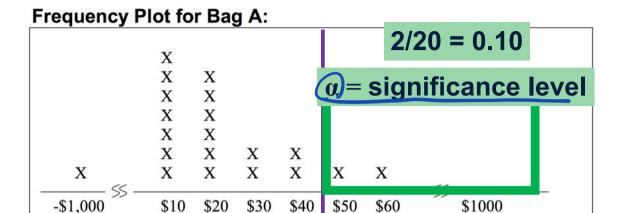
#### **Alternative:**

Shown bag is Bag B

Decision Rule: Reject the Null if voucher is \$50 or higher

Other Error: Do not Reject Null when Alternative True





Null:

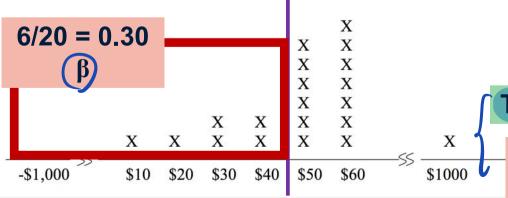
Shown bag is Bag A

**Alternative:** 

Shown bag is Bag B

#### Reject the Null





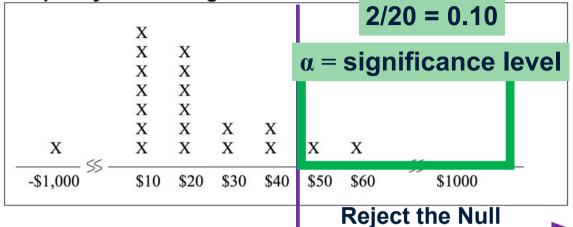
Decision Rule:
Reject the Null if
voucher is
\$50 or higher

Type 1 Error: Reject Null when Null True

Type 2 Error: Do not Reject Null when Alternative True







						X	
					X	X	
					X	X	
					X X	$\mathbf{X}$	
					X	X	
			X	X X	X	X	
	X	X	X	X	X	X	X
<del></del> \$\$ -	¢10	620	620	040	050	0.00	—SS —
-\$1,000	\$10	\$20	\$30	\$40	\$50	\$60	\$1000

#### Null:

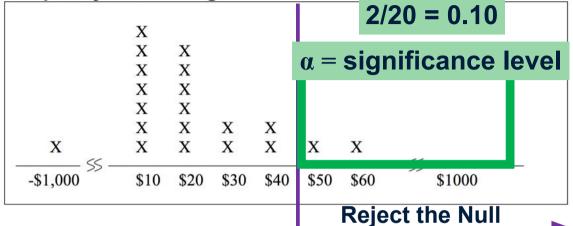
Shown bag is Bag A

#### **Alternative:**

Shown bag is Bag B

Decision Rule: Reject the Null if voucher is \$50 or higher





Frequency Plot for Bag B:

			-				
						X	
					X	X	
					X	$\mathbf{X}$	
						$\mathbf{X}$	
					X X	X	
			X	X	X X	$\mathbf{X}$	
	$\mathbf{X}$	X	X	X	X	X	X
——— SS —	9		2	1	14	723	—SS ———
-\$1,000	\$10	\$20	\$30	\$40	\$50	\$60	\$1000

Null:

Shown bag is Bag A

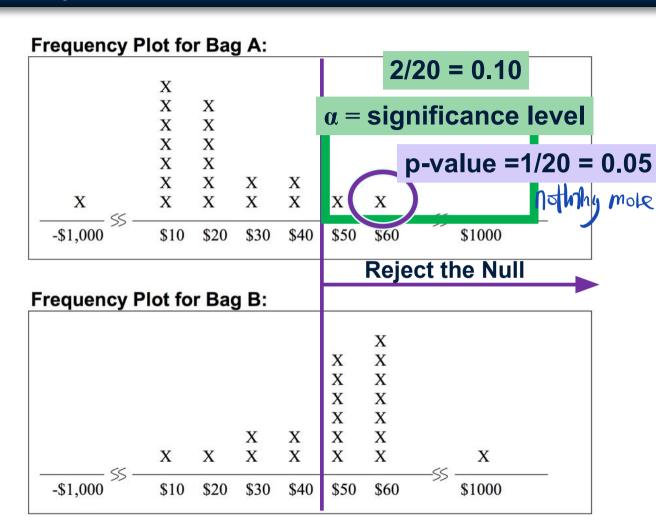
**Alternative:** 

Shown bag is Bag B

Decision Rule: Reject the Null if p-value is  $\leq \alpha$ 

Phobability



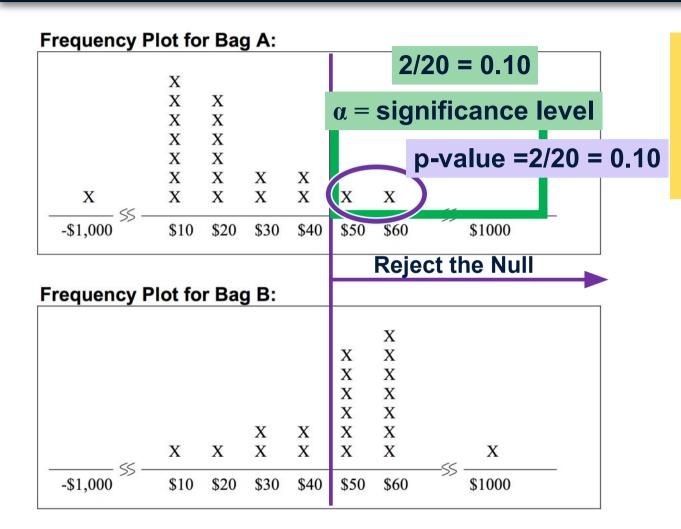


Null: Shown bag is **Bag A** 

Alternative:
Shown bag is Bag B

Decision Rule: Reject the Null if p-value is  $\leq \alpha$ 



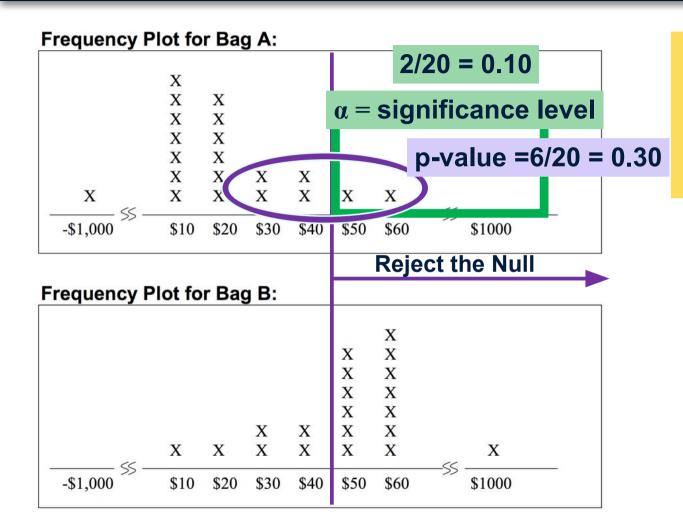


Null: Shown bag is **Bag A** 

Alternative:
Shown bag is Bag B

Decision Rule: Reject the Null if p-value is  $\leq \alpha$ 





Null: Shown bag is **Bag A** 

Alternative: Shown bag is Bag B

Decision Rule: Reject the Null if p-value is  $\leq \alpha$ 



# Hypothesis Testing

- Stating Hypotheses
- Selecting a Significance Level
- Using data to make our decision (via p-value)

Probability of at least extreme when Null is true

More details about making inferences ahead!

happen or not happen

O Phobability 1's The your mind rather than

The world

S based on new Information, you can

update your probability