

習題

張軍力

A105270002.

9. 解：

$$\begin{aligned}
 (1) \quad S &= \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}} = \sqrt{\frac{\sum x_i^2 - n\bar{x}^2}{n-1}} \\
 &= \sqrt{\frac{1.284 - 6 \times 14.33^2}{5}} = \sqrt{10.38} = 3.22.
 \end{aligned}$$

∴ σ 之點估計為 3.22.

$$(2) \quad 1 - \alpha = 0.90, \quad \frac{\alpha}{2} = 0.05, \quad n-1 = 5.$$

$$\chi^2_{\frac{\alpha}{2}}(n-1) = \chi^2_{0.05}(5) = 11.07.$$

$$\chi^2_{1-\frac{\alpha}{2}}(n-1) = \chi^2_{0.95}(5) = 1.15.$$

$$\therefore \sigma \text{ 之 } 90\% \text{ 信賴區間為 } \left(\sqrt{\frac{5 \times 10.38}{\chi^2_{0.05}(5)}}, \sqrt{\frac{5 \times 10.38}{\chi^2_{0.95}(5)}} \right)$$

$$= \left(\sqrt{\frac{51.9}{11.07}}, \sqrt{\frac{51.9}{1.15}} \right)$$

$$= (2.17, 6.72).$$