

習題 21.

$$(1) \hat{p} = \frac{105}{250} = 0.42, 1-\alpha = 0.90, Z_{\frac{\alpha}{2}} = Z_{0.05} = 1.645$$

$$\therefore p \pm 90\% \text{ 信賴區間為 } 0.42 \pm Z_{0.05} \sqrt{\frac{0.42 \times 0.58}{250}}$$

$$= 0.42 \pm 1.645 \times 0.03$$

$$= 0.42 \pm 0.05$$

$$\text{即 } (0.37, 0.47)$$

$$(2) \alpha = 0.03, 1-\alpha = 0.95, Z_{\frac{\alpha}{2}} = Z_{0.025} = 1.96$$

$$a. p = 0.3$$

$$\therefore n = \left(\frac{1.96}{0.03} \right)^2 (0.3)(0.7) = 896.37 \div 897 \Rightarrow n = 897$$

$$b. \hat{p} = \frac{105}{250} = 0.42$$

$$\therefore n = \left(\frac{1.96}{0.03} \right)^2 (0.42)(0.58) = 1,039.79 \div 1,040 \Rightarrow n = 1,040$$

$$c. p = 0.5$$

$$\therefore n = \left(\frac{1.96}{0.03} \right)^2 (0.5)(0.5) = 1,067.11 \div 1,068 \Rightarrow n = 1,068$$