



ELTE

FACULTY OF  
INFORMATICS

# ANALOGY AND SIGNALS

Embodied Intelligence – Balázs Nagy, PhD



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DEPARTMENT OF  
ARTIFICIAL  
INTELLIGENCE

# What is embodied intelligence?

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Cangelosi, A., Bongard, J., Fischer, M.H., Nolfi, S. (2015). Embodied Intelligence. In: Kacprzyk, J., Pedrycz, W. (eds) Springer Handbook of Computational Intelligence. Springer Handbooks. Springer, Berlin, Heidelberg. [https://doi.org/10.1007/978-3-662-43505-2\\_37](https://doi.org/10.1007/978-3-662-43505-2_37)



# What is embodied intelligence?

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Embodied intelligence is the computational approach to the design and understanding of intelligent behavior in embodied and situated agents through the consideration of the strict coupling between the agent and its environment (situatedness), mediated by the constraints of the agent's own body, perceptual and motor system, and brain (embodiment).

Cangelosi, A., Bongard, J., Fischer, M.H., Nolfi, S. (2015). Embodied Intelligence. In: Kacprzyk, J., Pedrycz, W. (eds) Springer Handbook of Computational Intelligence. Springer Handbooks. Springer, Berlin, Heidelberg. [https://doi.org/10.1007/978-3-662-43505-2\\_37](https://doi.org/10.1007/978-3-662-43505-2_37)



# Analogy

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human



robot

# Analogy



human

Brain

Central processing  
unit

CPU



robot

# Analogy



human

Brain

Eyes  
Nose  
Tongue  
Ears  
Skin  
Spidey Sense

Central processing  
unit

Sensors

Optical sensor (cameras)  
Olfactory sensors

Audio sensor  
Equilibrium sensor

CPU



robot



# Analogy



human

Brain

Eyes  
Nose  
Tongue  
Ears  
Skin  
Spidey Sense

Muscles  
Web shooter

Central processing  
unit

Sensors

Optical sensor (cameras)  
Olfactory sensors

Audio sensor  
Equilibrium sensor

Actuators

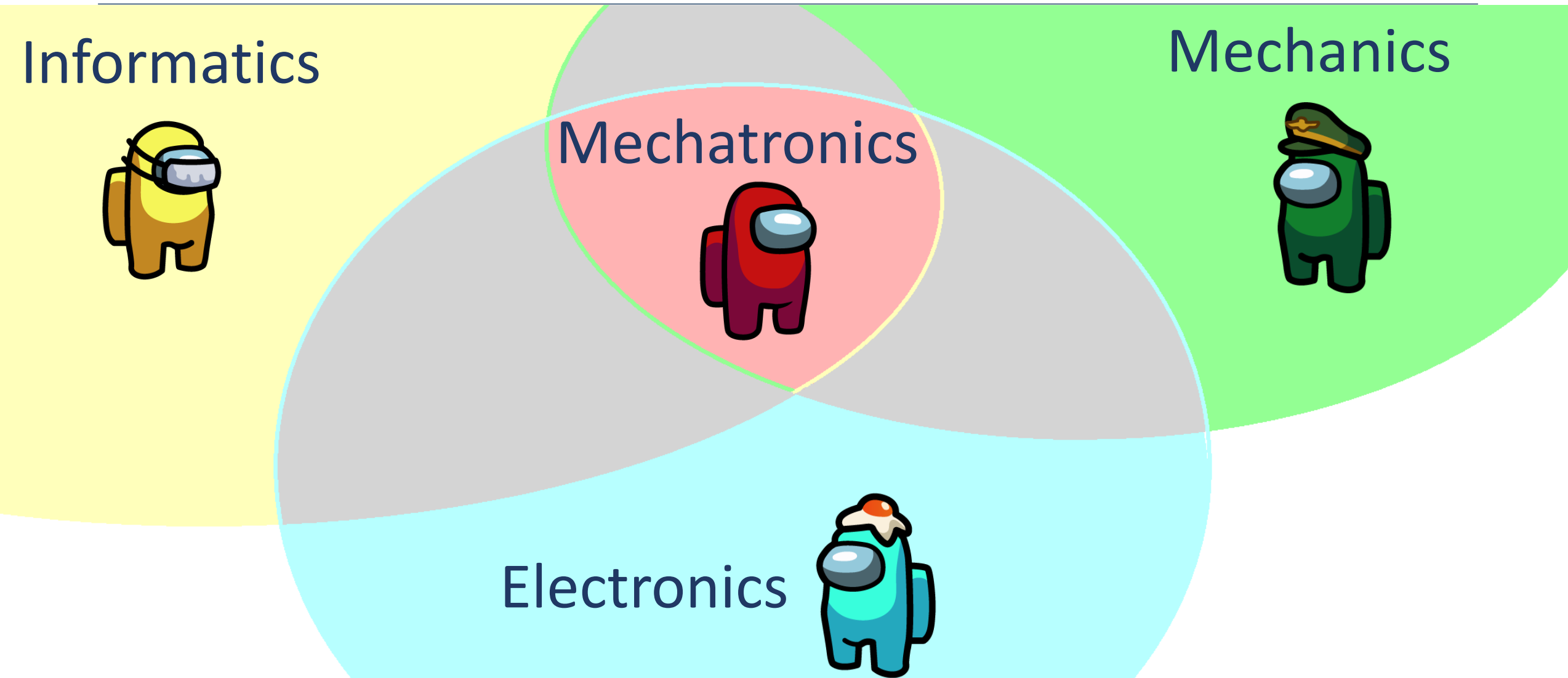
Motors  
Blasters

CPU



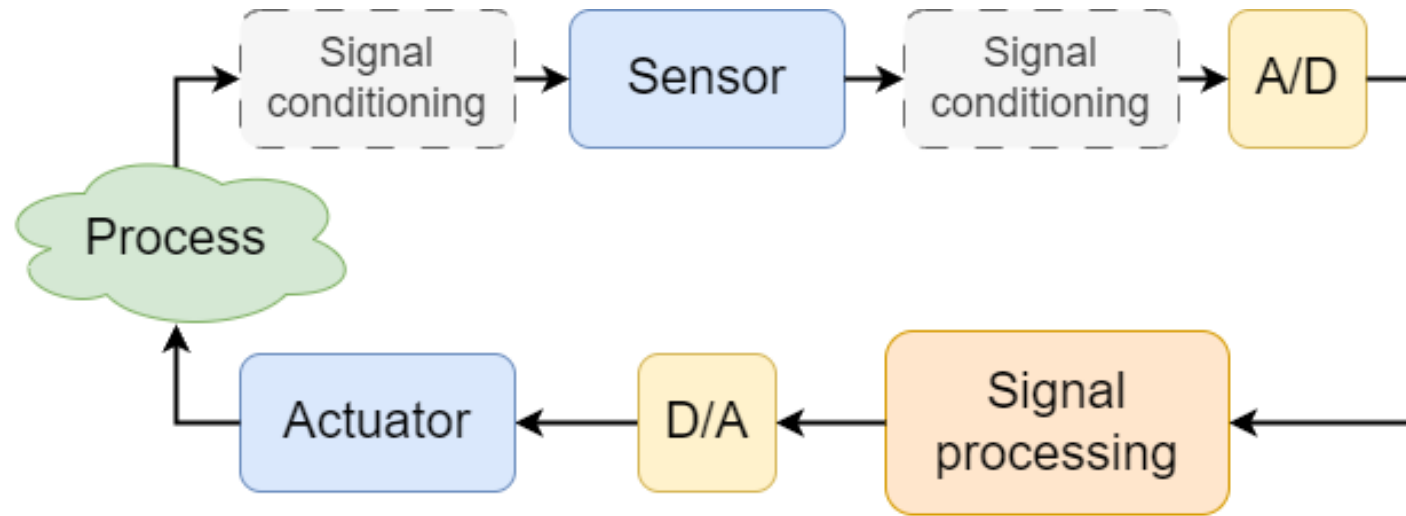
robot

# Skills needed

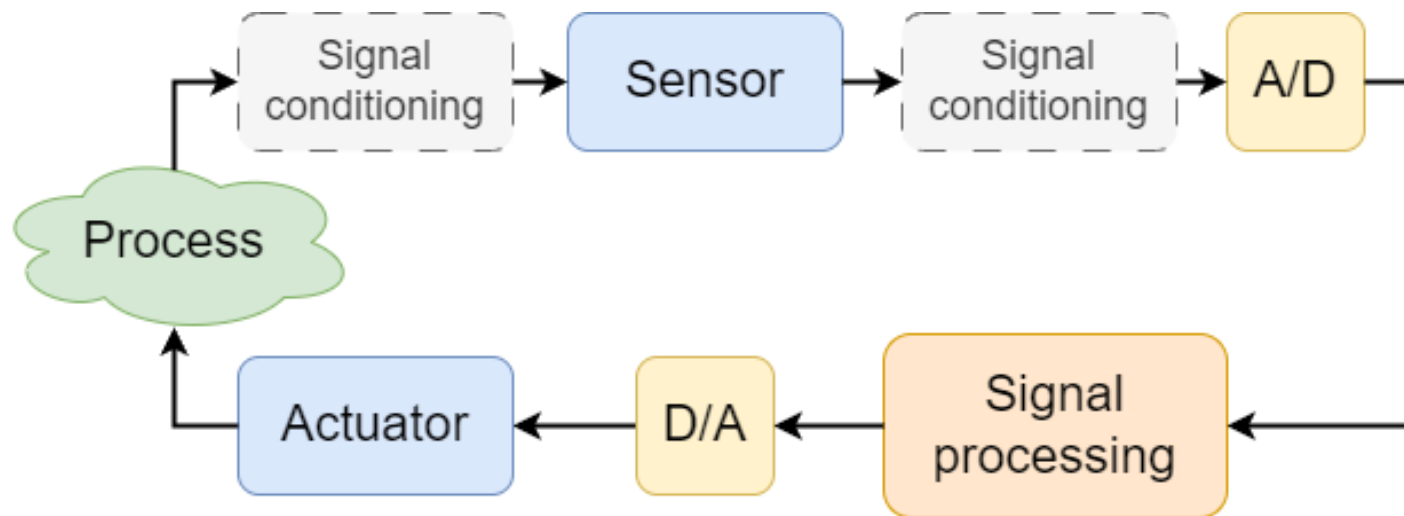




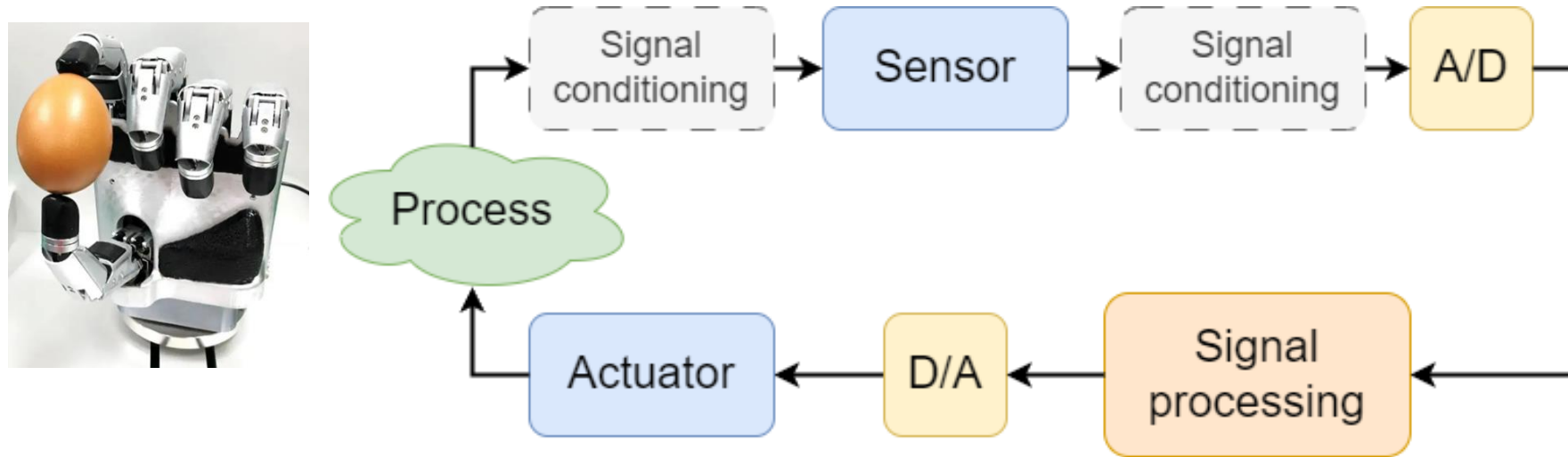
# Generalized control loop



# Generalized control loop

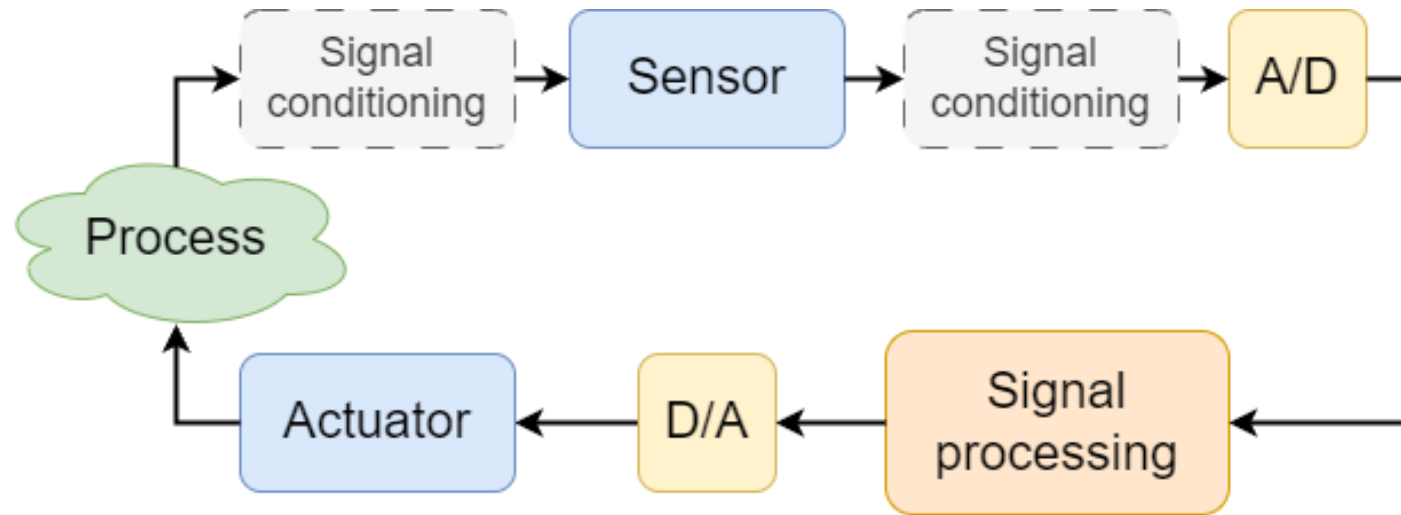


# Generalized control loop



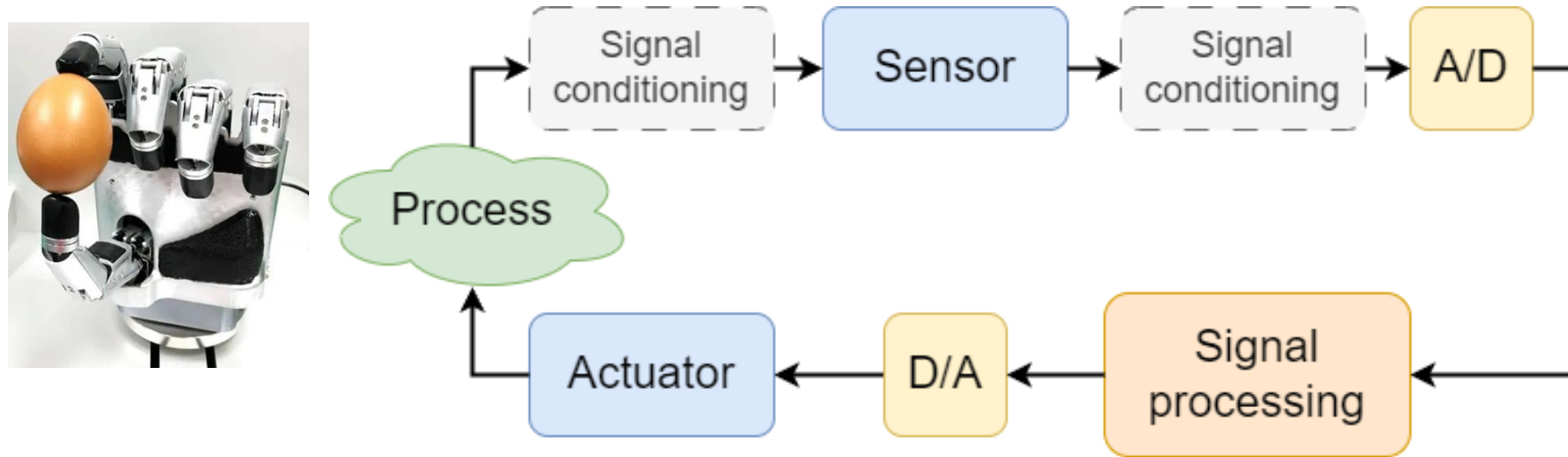
- **Signal conditioning:**  
the manipulation of an analog signal in such a way that it meets the requirements of the next stage for further processing.  
  
amplification, filtering, converting, range matching, isolation

# Generalized control loop



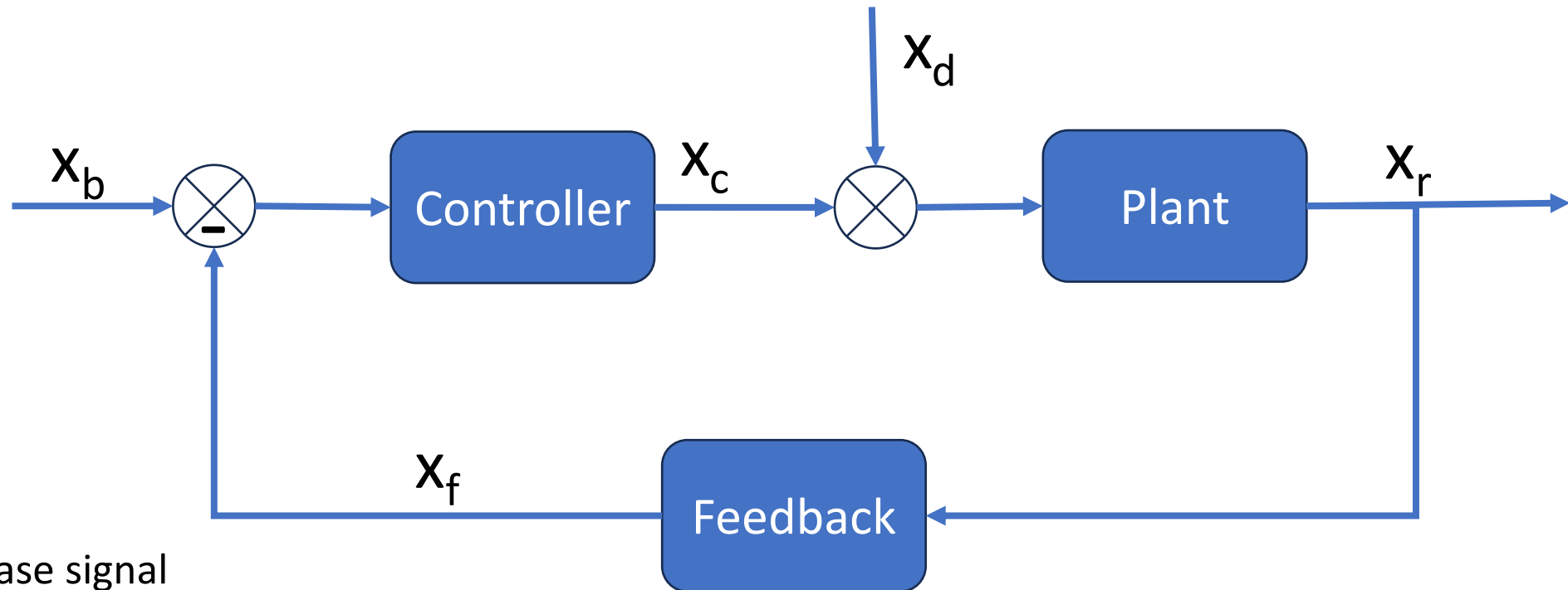
- **A/D:** Analog to digital conversion
- **D/A:** Digital to analog conversion

# Generalized control loop



- **Signal processing:** the „brain“, this is where the intelligent part is implemented

# Canonical control loop



$x_b$ : Base signal

$x_c$ : Control signal

$x_r$ : Regulated/controlled signal

$x_f$ : Feedback signal

$x_d$ : Disturbance signal

Transfer function  
= mathematical model of  
the plant



# Garbage in garbage out (GIGO)

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In computer science, garbage in, garbage out (GIGO) is the concept that flawed, or nonsense (garbage) input data produces nonsense output.

Rubbish in, rubbish out (RIRO) is an alternate wording.



# What is a signal?

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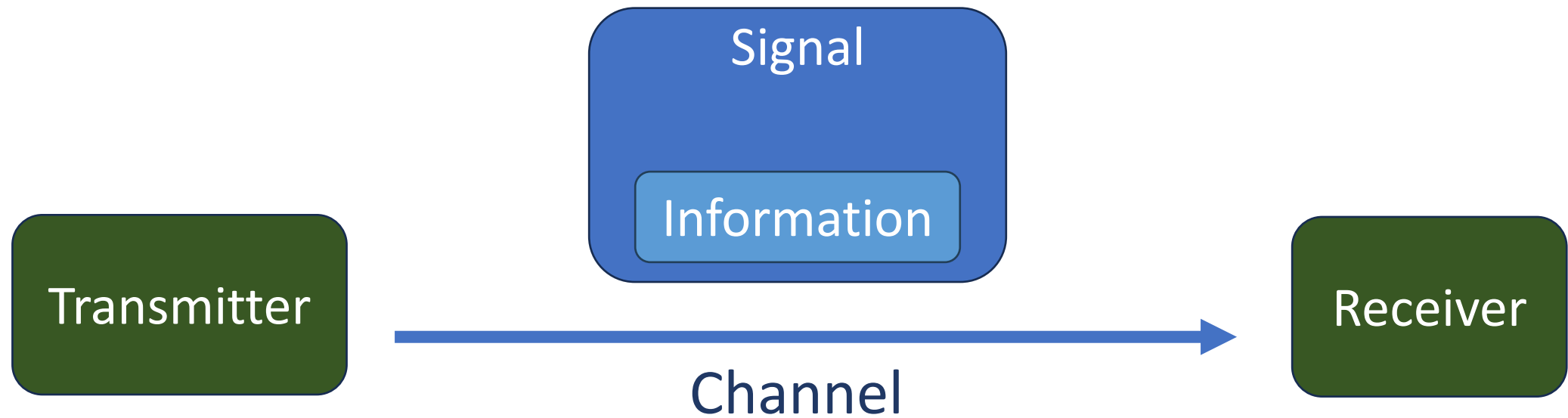
- Signal can be anything
- Physical state changes during time

$$\text{Signal} = \text{Information} + \text{Noise}$$

- **Information:** useful part of the signal
- **Noise:** unwanted disturbance

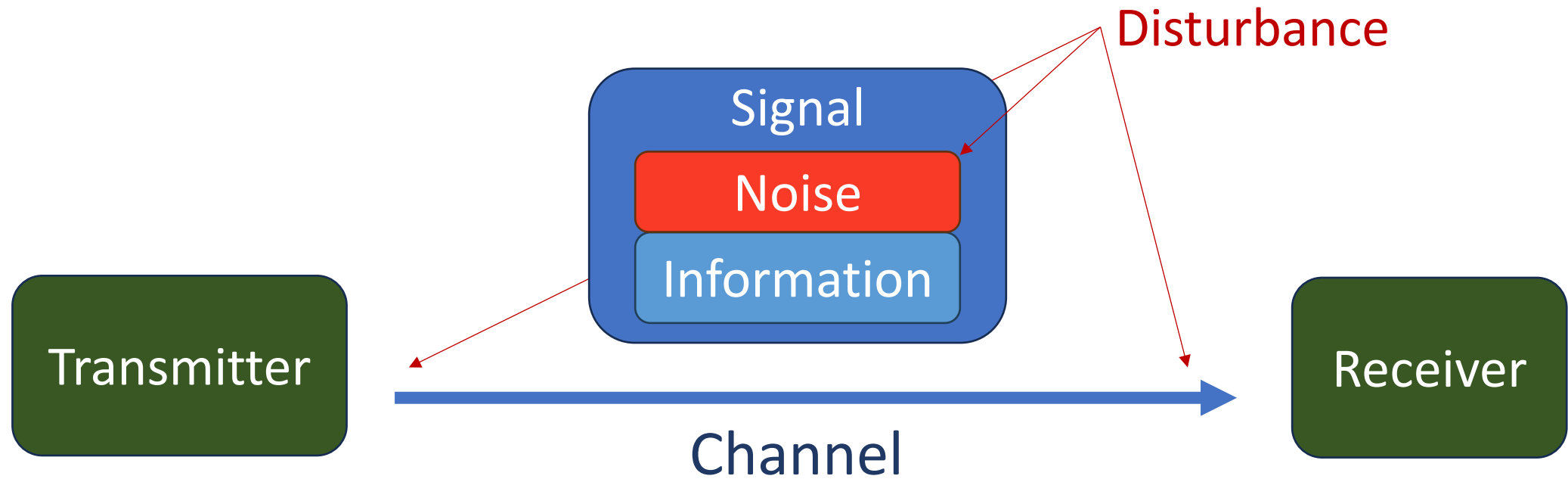
# Communication model

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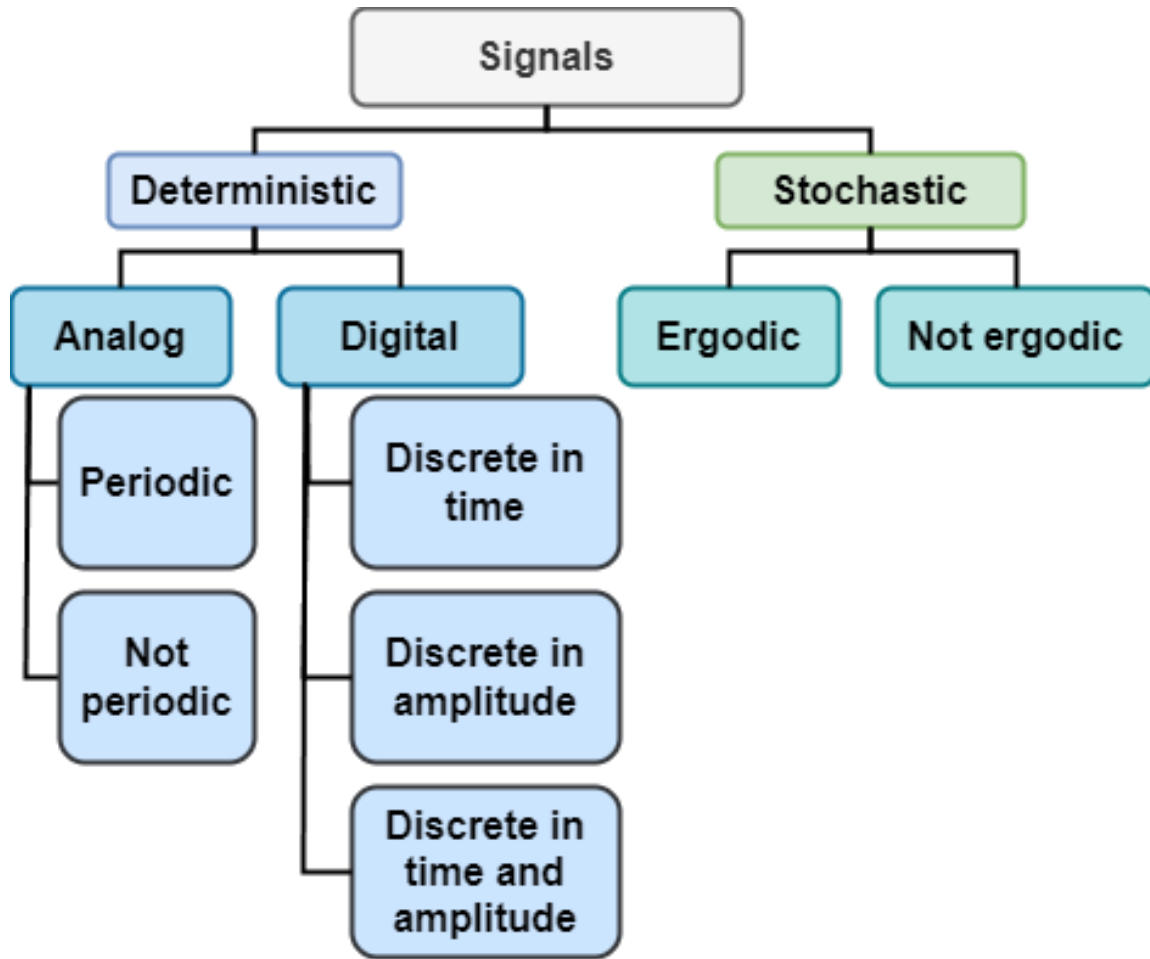


# Communication model

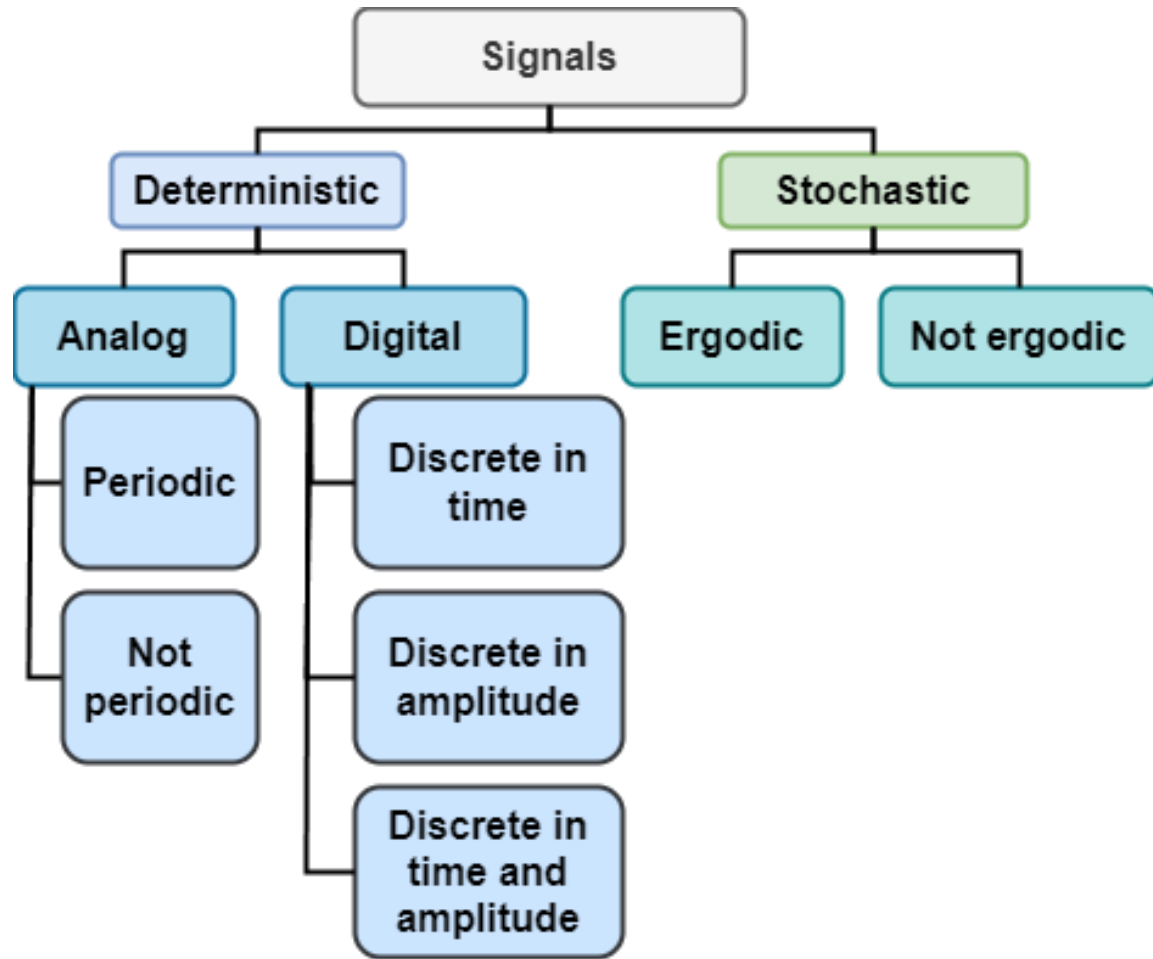
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# Signal types



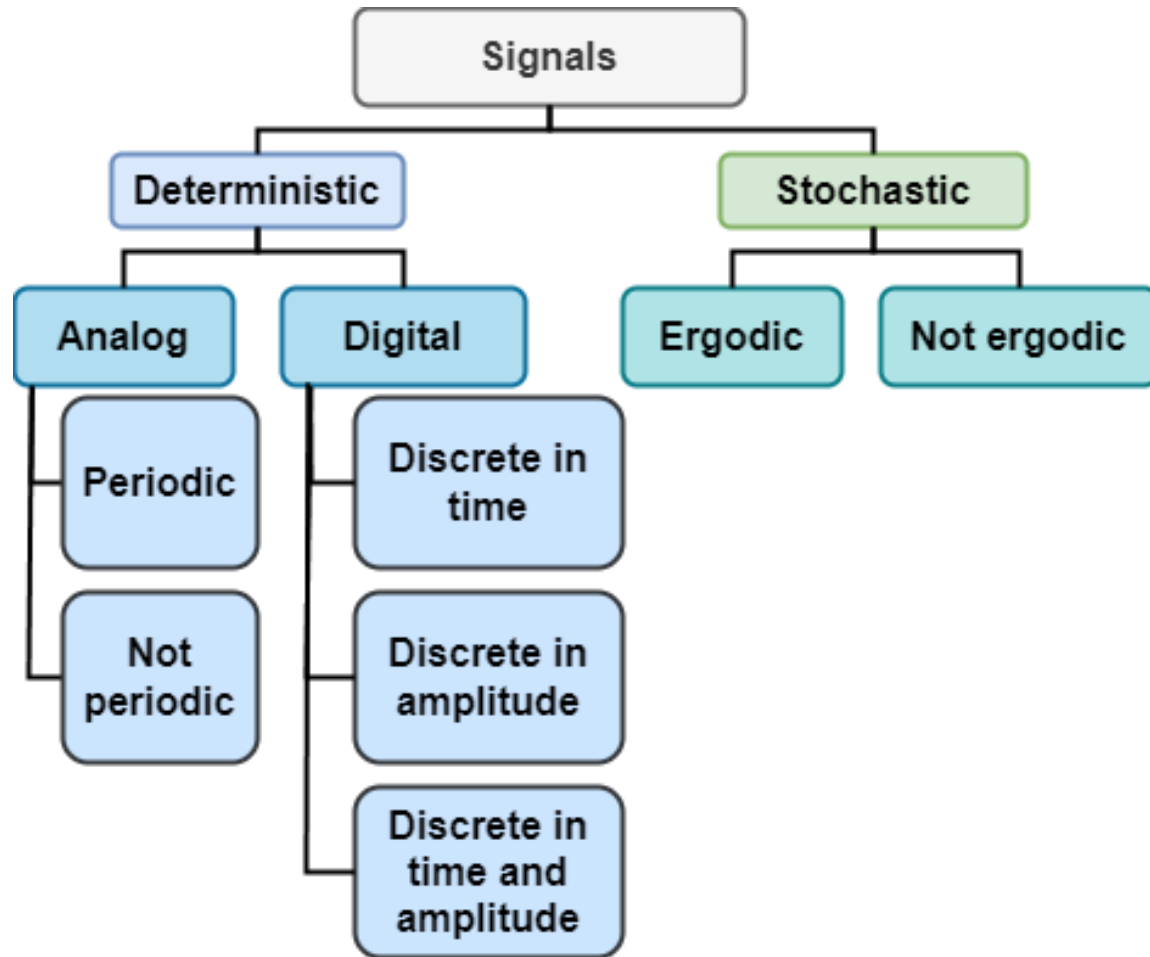
# Signal types



- **Deterministic:**  
If a signal value at any point in time can be defined precisely by a mathematical equation.
- **Stochastic (non-deterministic):**  
A signal is said to be non-deterministic if there is uncertainty with respect to its value at some instant of time

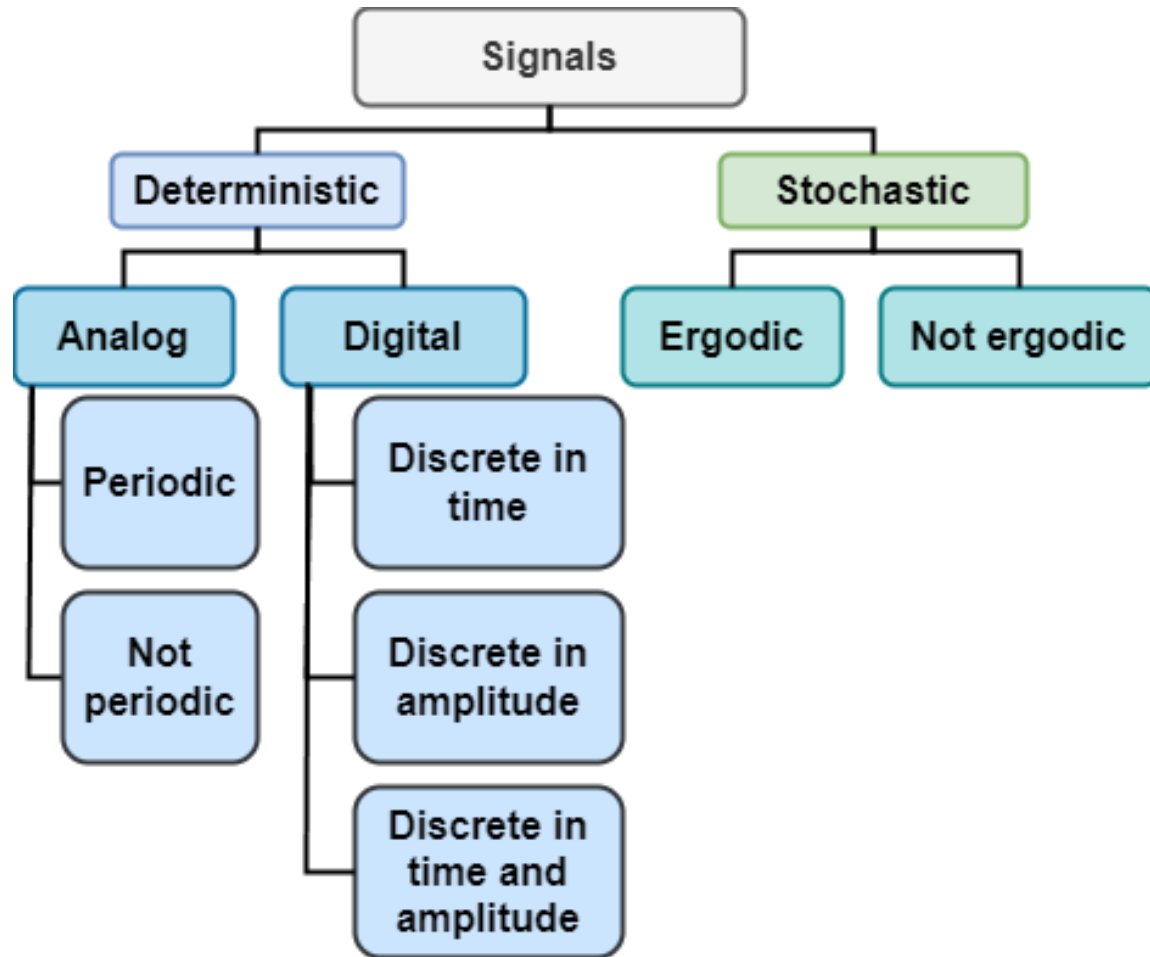


# Signal types



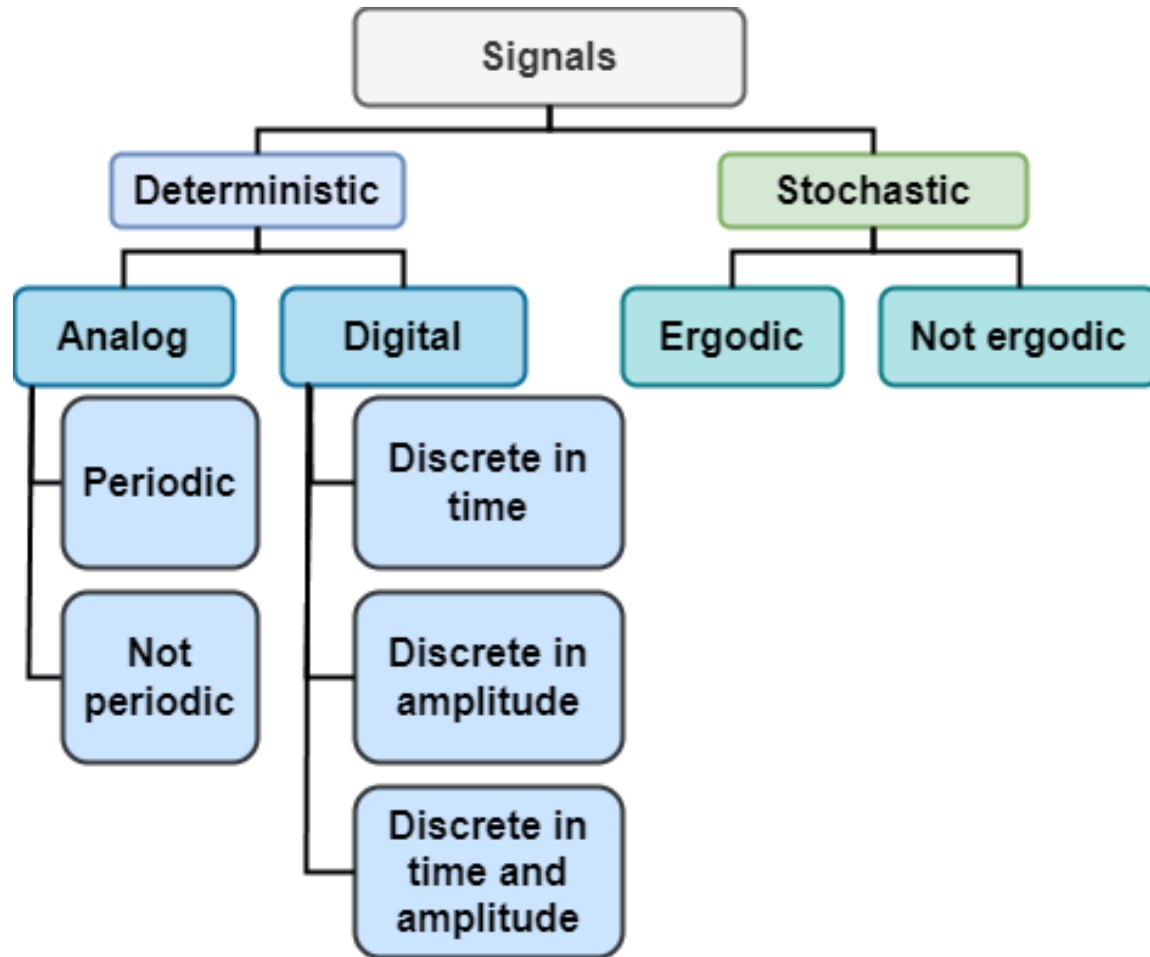
- **Ergodic:**  
A random signal where time averages equal ensemble averages for fixed time.  
=> Can be predicted with a finite statistics.  
(noise with normal distribution)
- **Not ergodic:**  
Can not be predicted.

# Signal types



- **Analog:**  
A signal that continuously and infinitely varies in accordance with some time-varying parameter
- **Digital:**  
A signal that represents data as a sequence of discrete values

# Signal types



- **Periodic**

A signal that has a definite pattern and repeats itself at a regular interval of time.

- Sinusoid
- General periodic

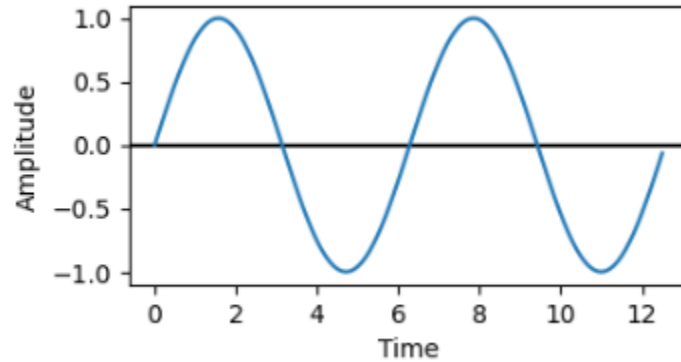
- **Not periodic (aperiodic):**

- Quasiperiodic
- Transient

# Signal types examples

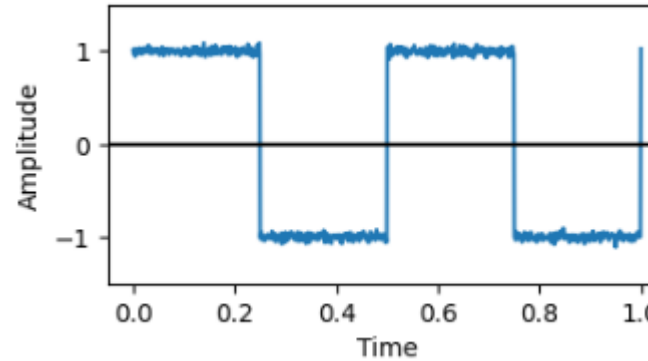
Periodic

Sinusoid



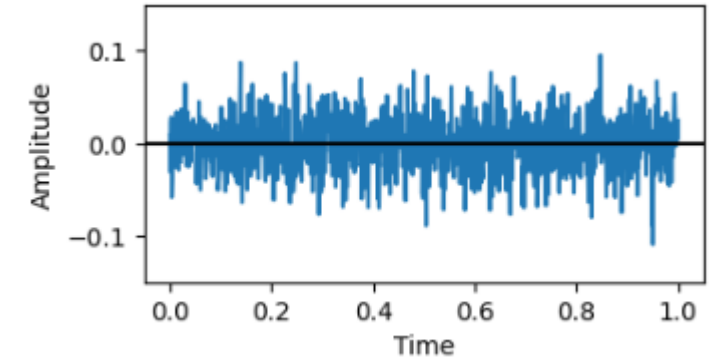
Not periodic

Quasiperiodic

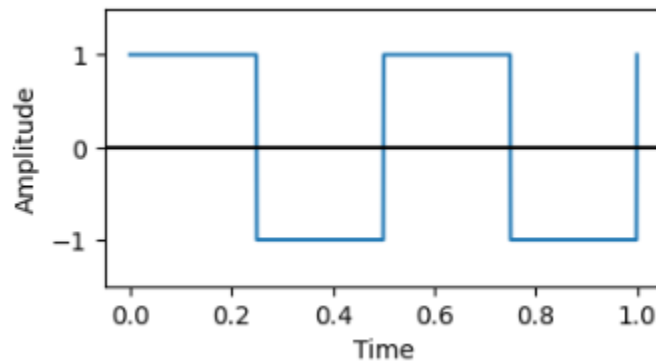


Ergodic

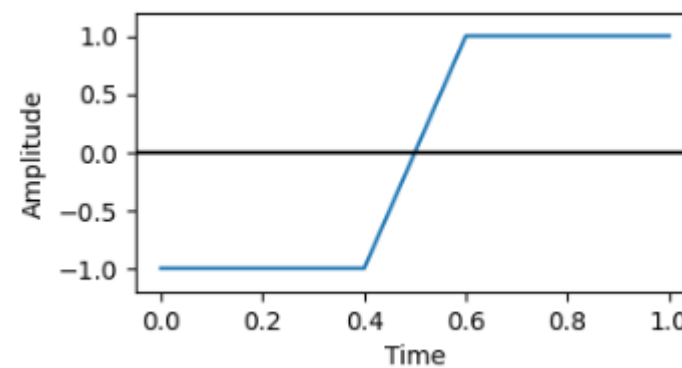
Noise



General periodic

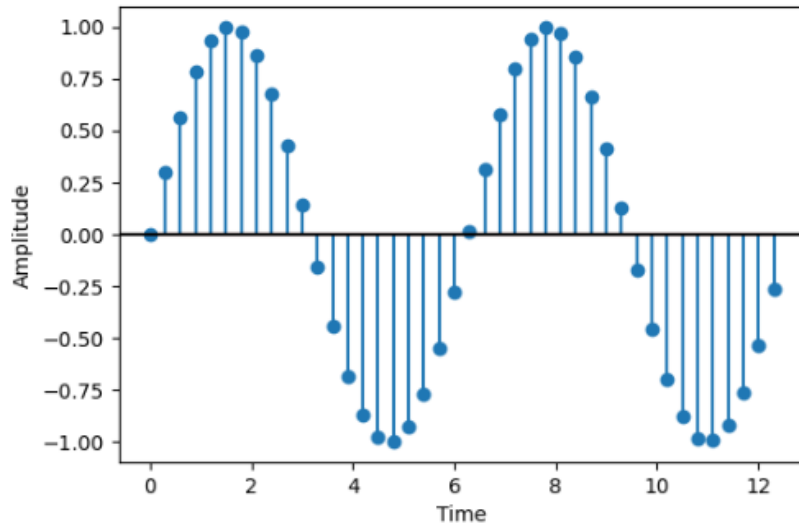


Transient

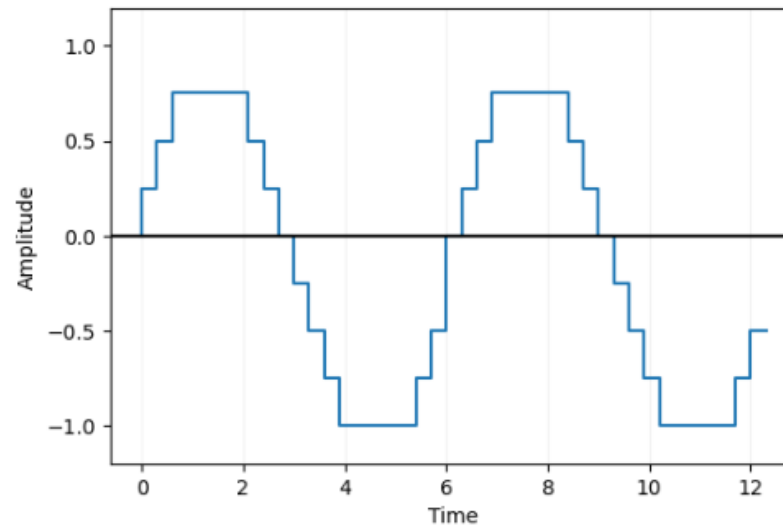


# Signal types examples

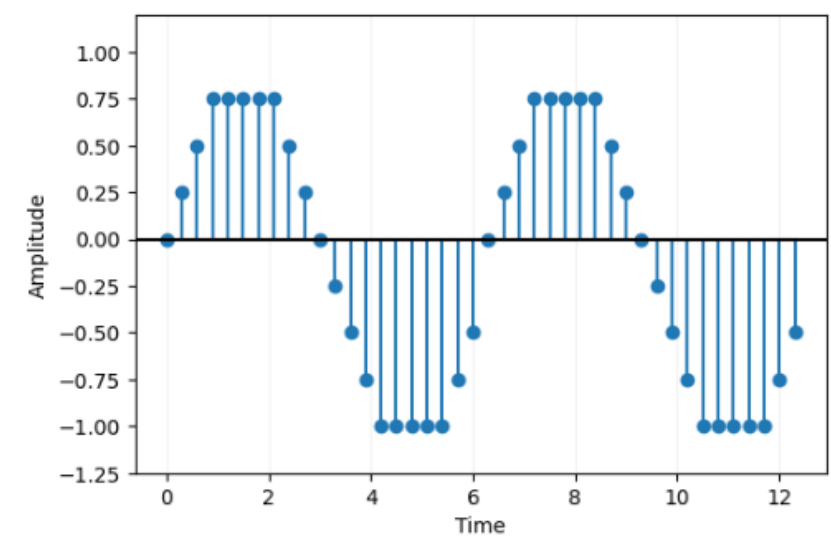
Discrete in time



Discrete in amplitude



Discrete in time and amplitude

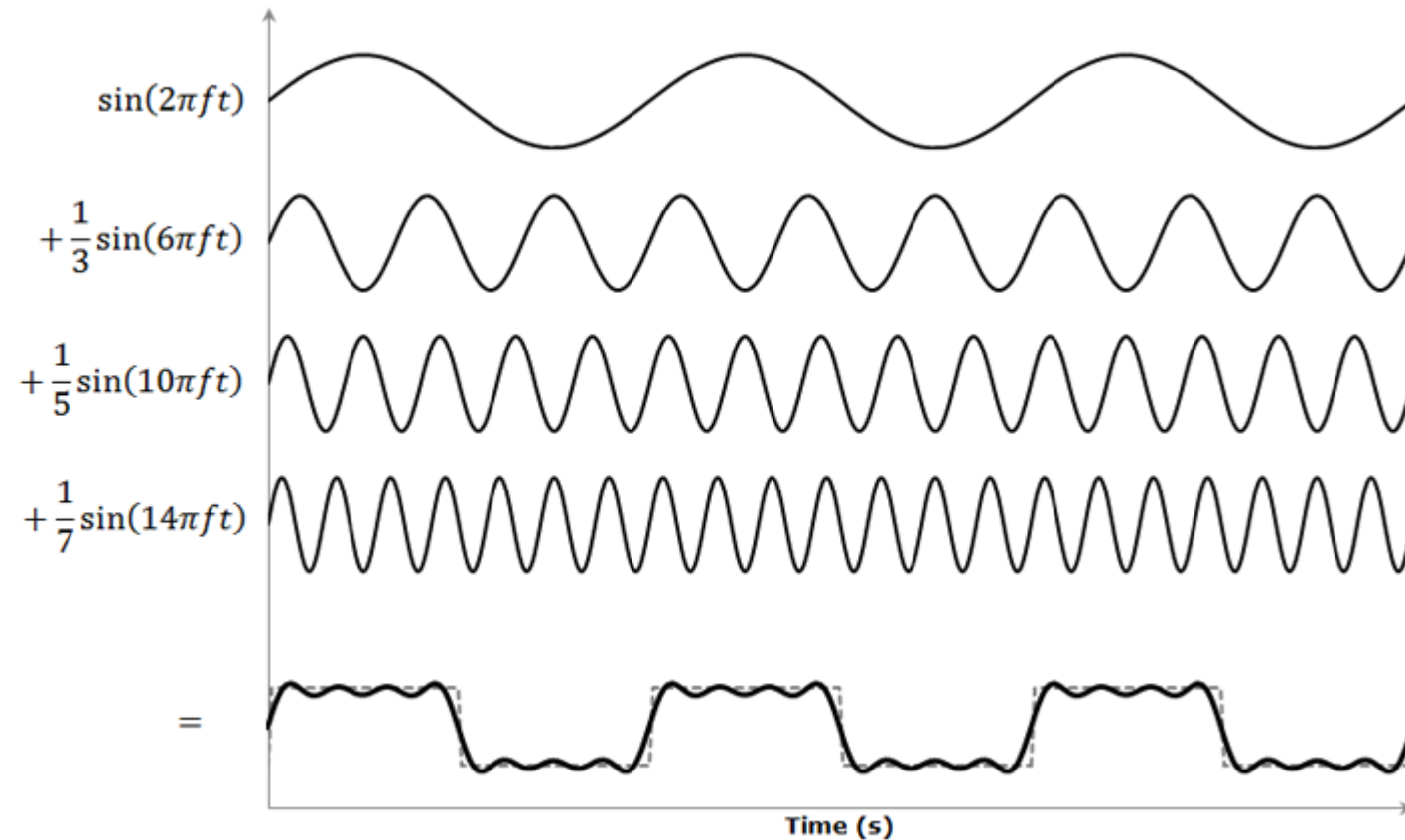


# Comparison

	Analog	Digital
<b>Signal</b>	Continuous signal	Discrete time signals
<b>Waves</b>	Denoted by sine waves	Denoted by square waves
<b>Representation</b>	Continuous range of values	Discrete or discontinuous values
<b>Noise</b>	More likely to get affected, subjected to deterioration by noise during transmission	Less affected since noise response, can be noise-immune without deterioration during transmission
<b>Flexibility</b>	Analog hardware is not flexible.	Digital hardware is flexible in implementation.
<b>Bandwidth</b>	Analog signal processing can be done in real time and consumes less bandwidth	There is no guarantee that digital signal processing can be done in real time and consumes more bandwidth to carry out the same information
<b>Power</b>	Analog instrument draws large power	Digital instrument draws only negligible power

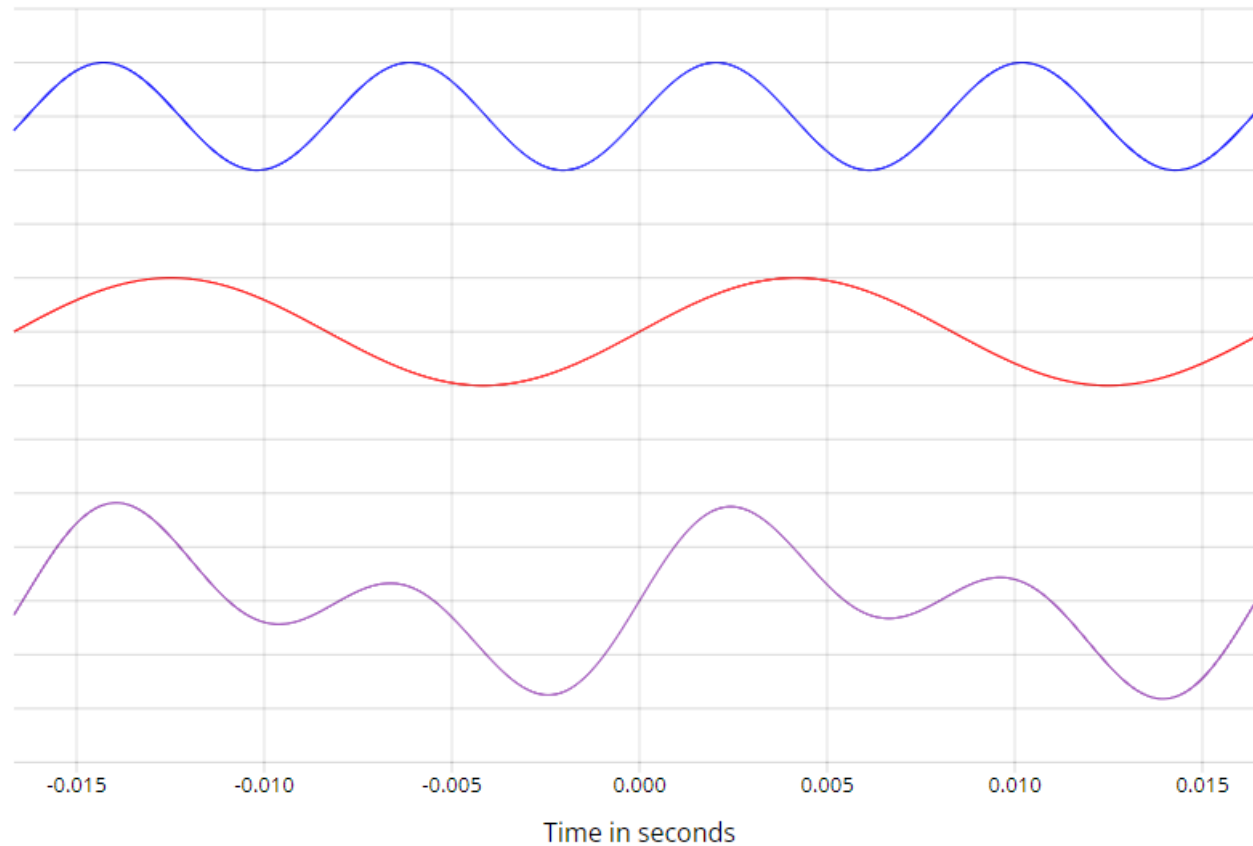


# Nature of signals



Every signal is a superposition of many sinusoid signal

# Nature of signals



$f_1$   
122.5 Hz

$f_2$   
60.0 Hz

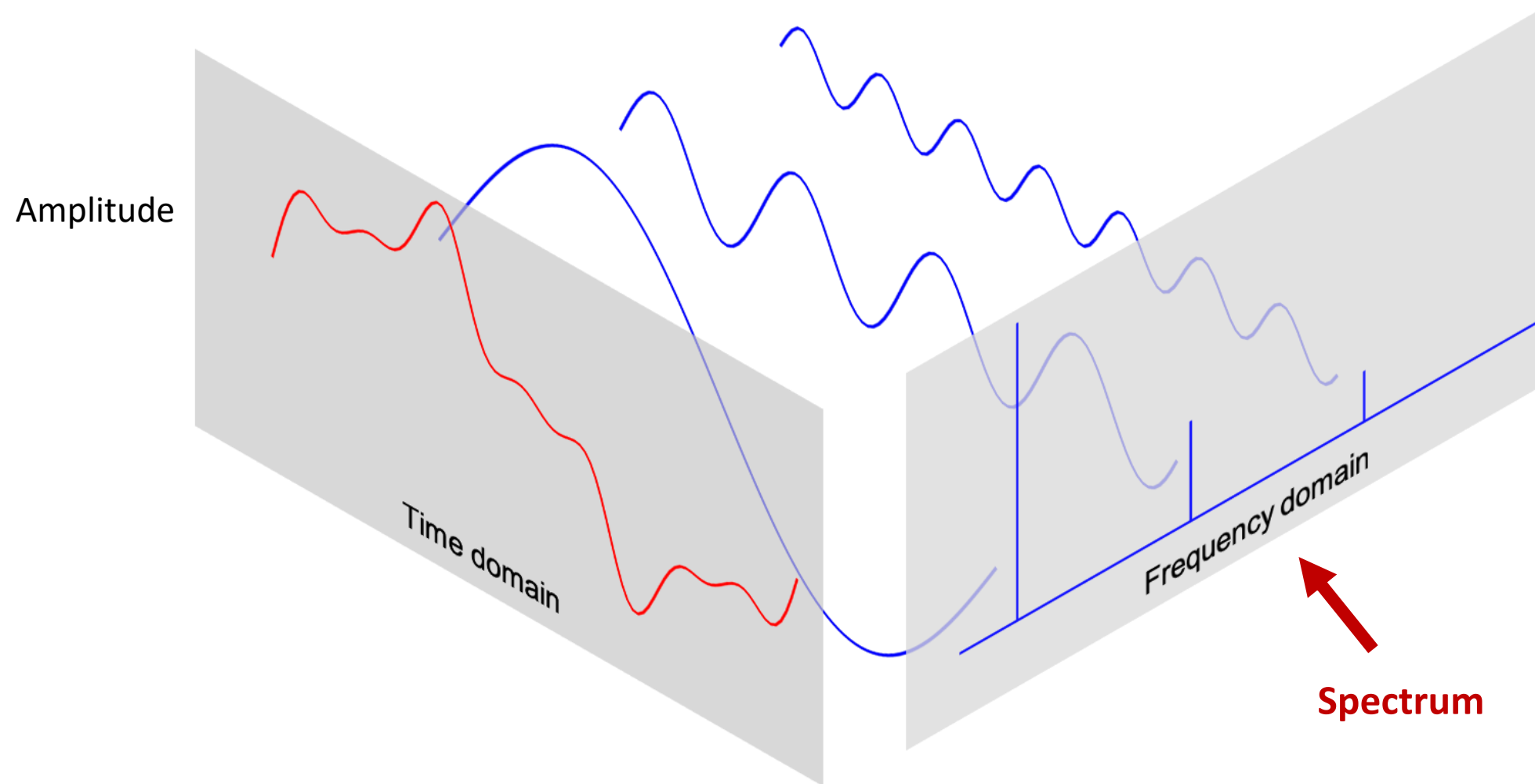
Zoom

Overlay waves  
☐

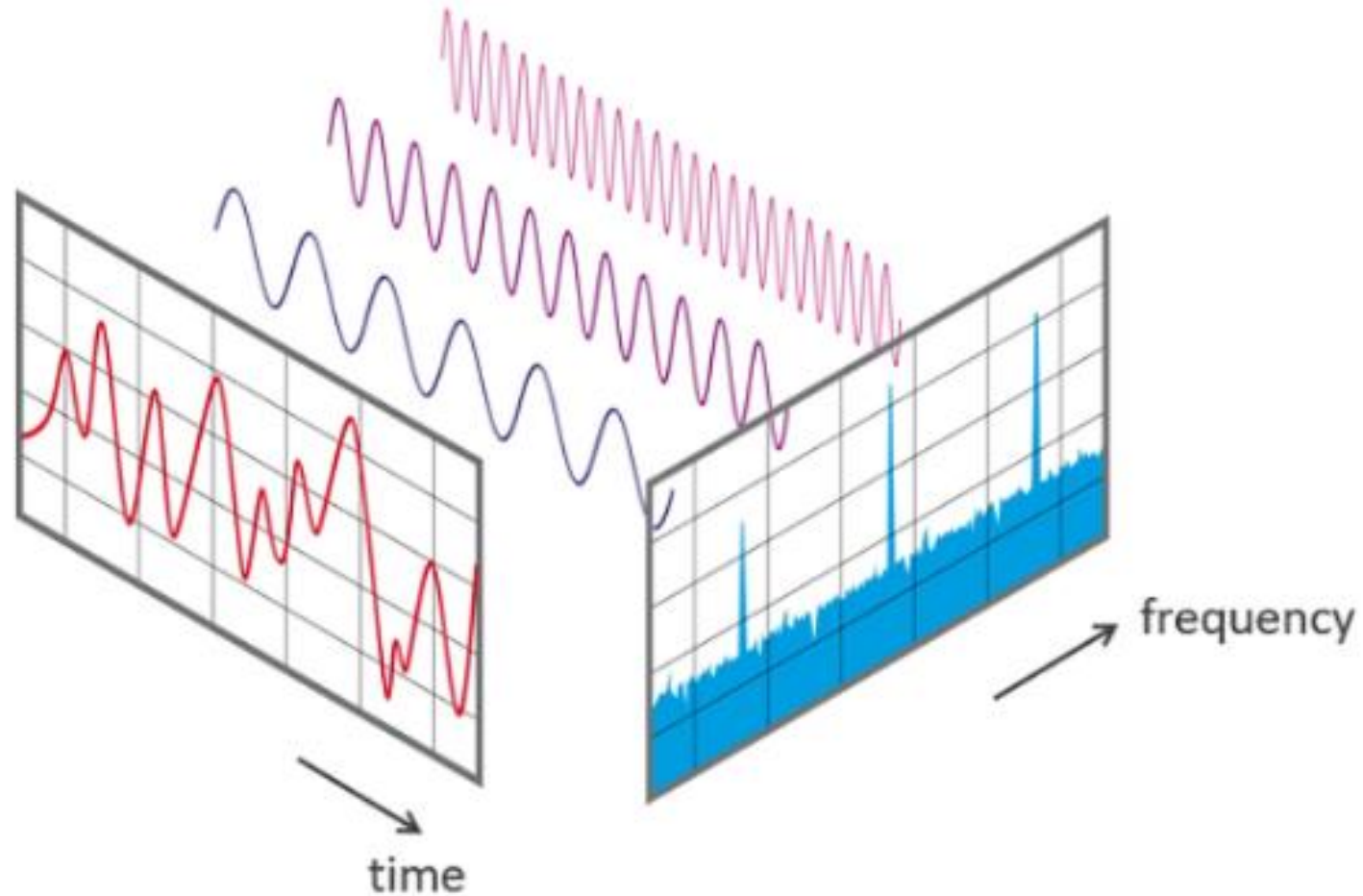
Sound on/off  
☐

<https://academo.org/demos/wave-interference-beat-frequency/>

# Nature of signals



# Nature of signals

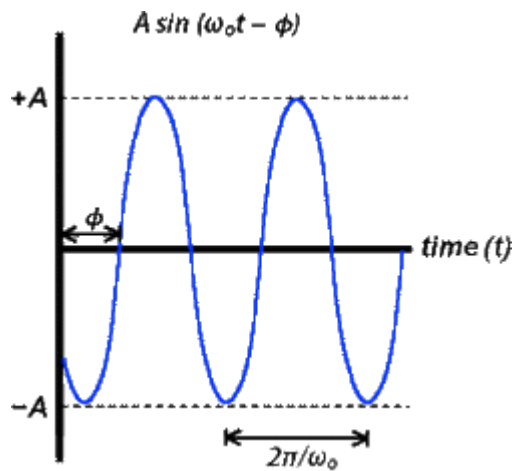
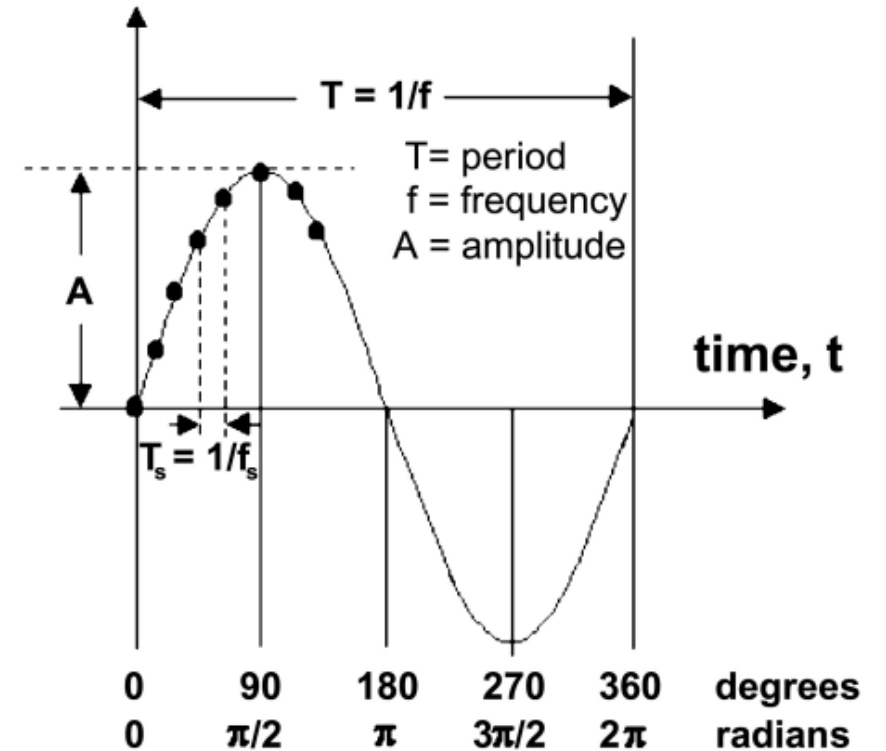
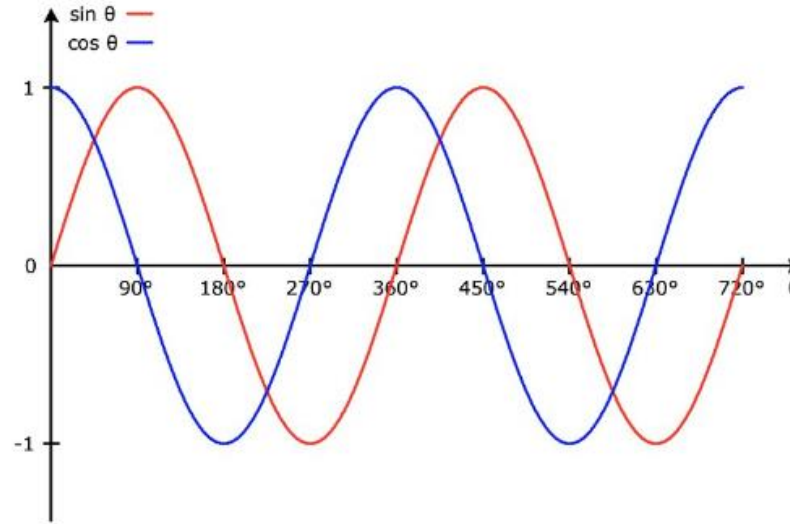
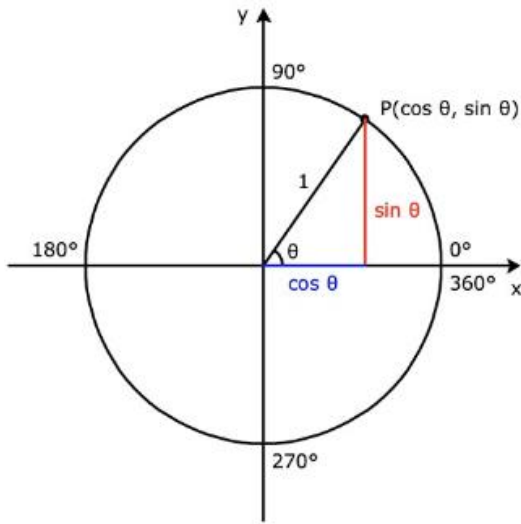


# Spectrum

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- A signal is a function of time which can be represented by a series of sinusoidal functions or sinusoidal components.
- These sinusoidal components have different frequencies, different amplitudes, and different phases.
- Therefore, the plots of frequency versus amplitude and phase for the sinusoidal components which comprise the signal are called the **Frequency Spectrum** or **Spectrum** of the signal.

# Sinusoid wave composition



$$\omega = 2\pi f$$

$$f = \frac{1}{T}$$

$$A \sin(\omega t) = A \sin(2\pi f t) = A \sin\left(\frac{2\pi}{T} t\right)$$



# Decomposition of a Signal

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- We can express the following representation of a function:

$$\begin{aligned}x(t) &= A_o + \sum_{k=1}^N A_k \cos(2\pi f_k t + \theta_k) \\&= X_o + \Re\left\{\sum_{k=1}^N X_k e^{j2\pi f_k t}\right\}\end{aligned}$$

Where  $X_o = A_o$  is a real constant (DC component) and

$X_k = A_k e^{j\theta_k}$  is the phasor for frequency  $f_k$

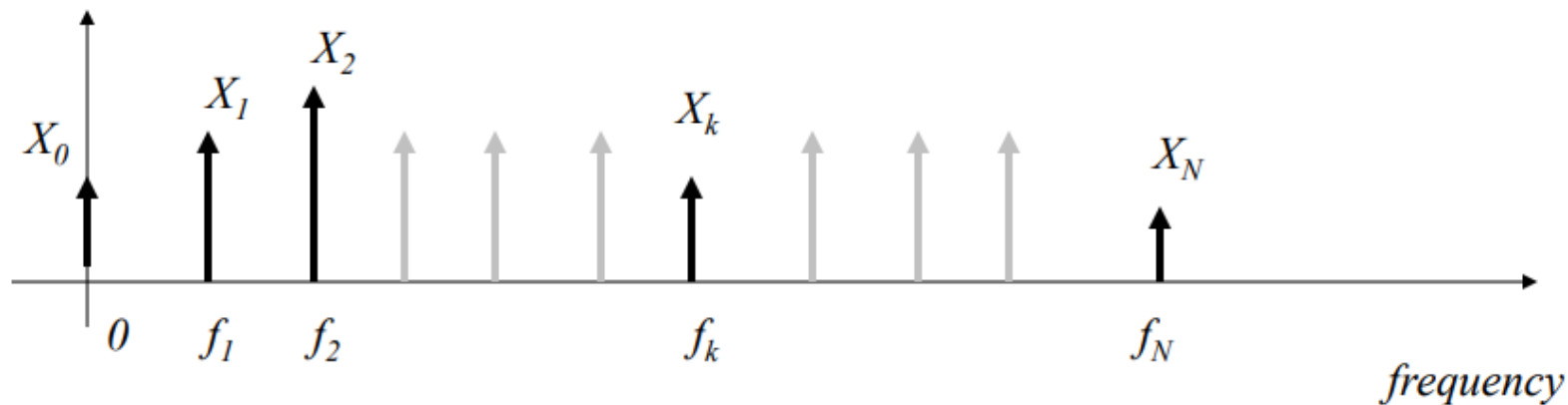
- Here we see that there are  $N+1$  frequency components for  $x(t)$ ,  $0 \leq k \leq N$  and with each frequency there is a phasor.

# Decomposition of a Signal

- For example, the  $k^{\text{th}}$  frequency has a phasor  $X_k$  with amplitude,  $A_k$ , and phase  $\theta_k$

$$x(t) = A_o + \sum_{k=1}^N A_k \cos(2\pi f_k t + \theta_k) = X_o + \Re\left\{\sum_{k=1}^N X_k e^{j2\pi f_k t}\right\}$$

Where  $X_o$  = DC component and  $X_k = A_k e^{j\theta_k}$  is the phasor for frequency  $f_k$



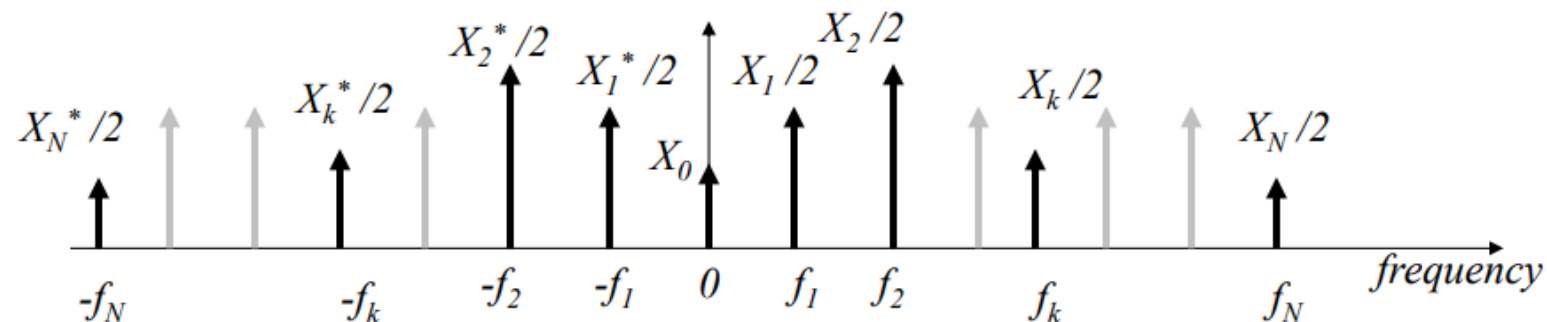
- This is really only half of the spectrum.

# Decomposition of a Signal

- Using Euler's formula, rewrite  $x(t)$ :

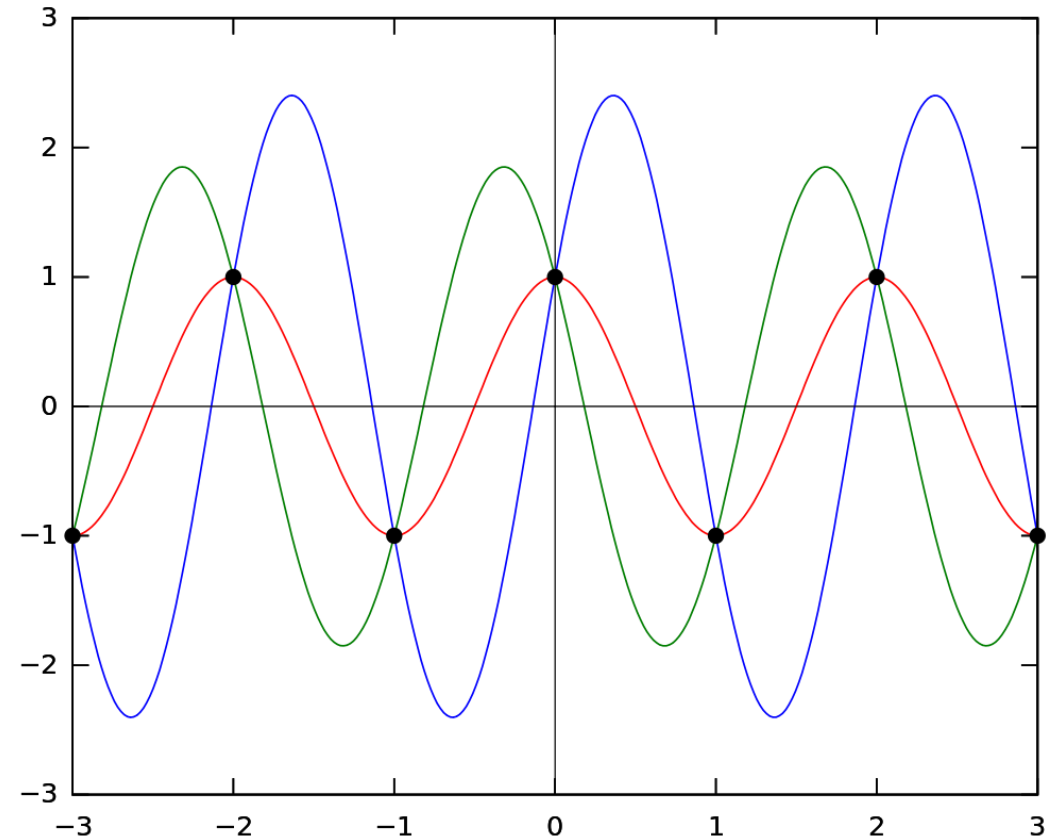
$$\begin{aligned} x(t) &= A_o + \sum_{k=1}^N A_k \cos(2\pi f_k t + \theta_k) = X_o + \sum_{k=1}^N \left\{ \frac{A_k}{2} e^{j\theta_k} e^{j2\pi f_k t} + \frac{A_k}{2} e^{-j\theta_k} e^{-j2\pi f_k t} \right\} \\ &= X_o + \sum_{k=1}^N \left\{ \frac{X_k}{2} e^{j2\pi f_k t} + \frac{X_k^*}{2} e^{-j2\pi f_k t} \right\} \end{aligned}$$

- Using this approach, we see that there are  $2N+1$  frequency component
- Or we can say that for each  $k$  where  $1 \leq k \leq N$ , there is a positive frequency  $f_k$  with phasor  $X_k/2$  and a negative frequency  $-f_k$  with phasor  $X_k^*/2$
- Therefore, we say that the spectrum is two-sided



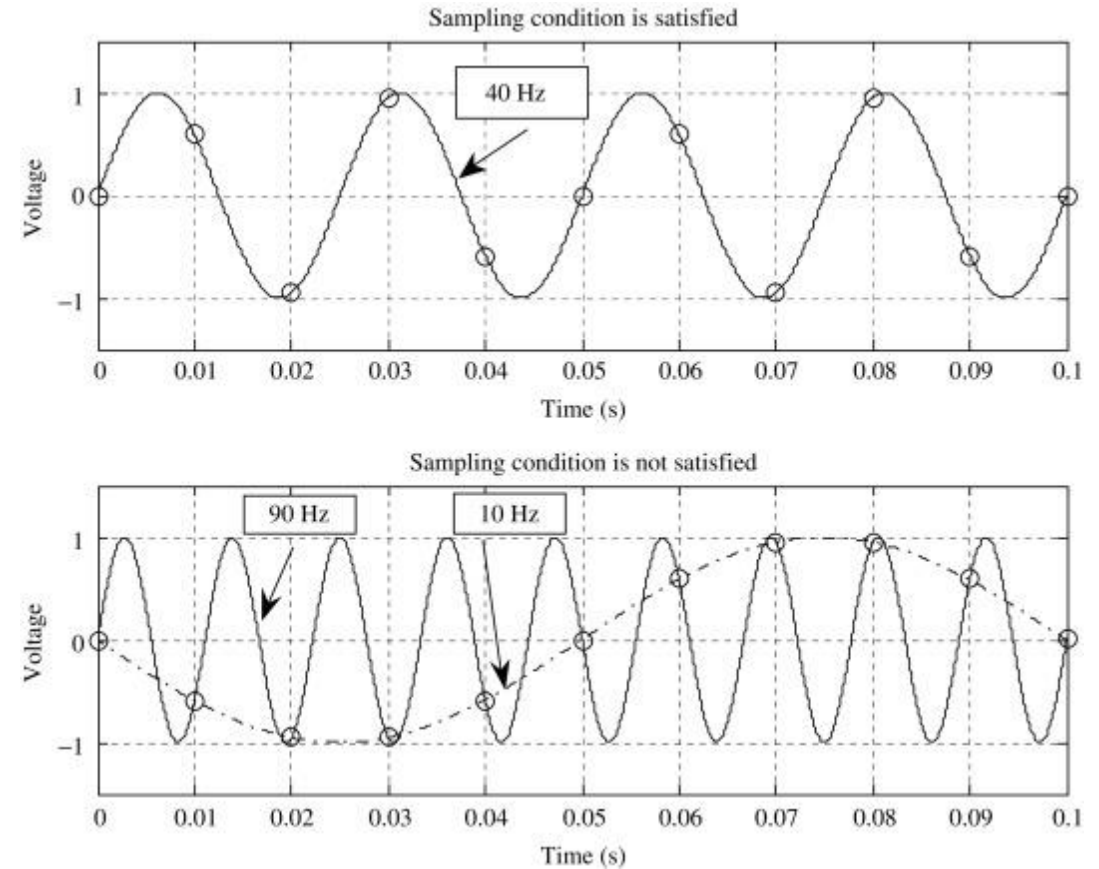
# Aliasing

- A family of sinusoids at the critical frequency, all having the same sample sequences of alternating +1 and -1. That is, they all are aliases of each other



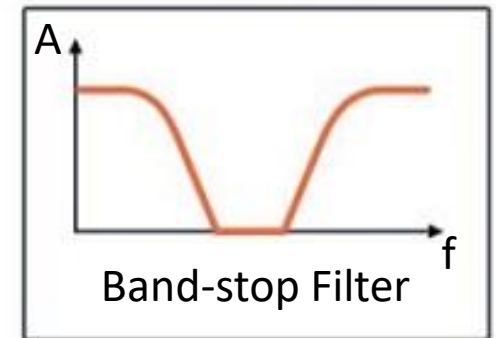
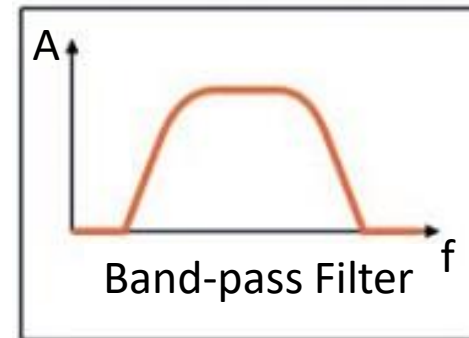
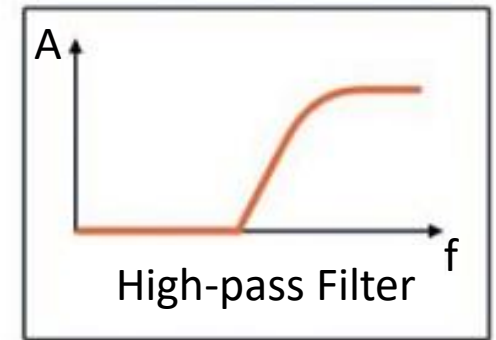
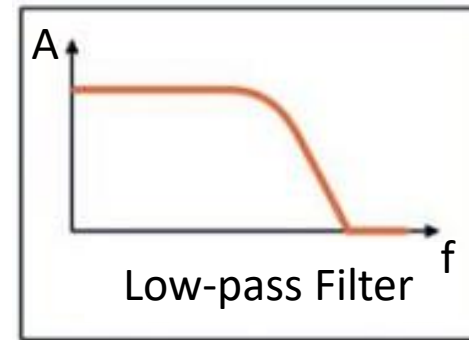
# Shannon theorem

- According to the sampling theorem (Shannon, 1949), to reconstruct a one-dimensional signal from a set of samples, the sampling rate must be equal to or greater than twice the highest frequency in the signal.



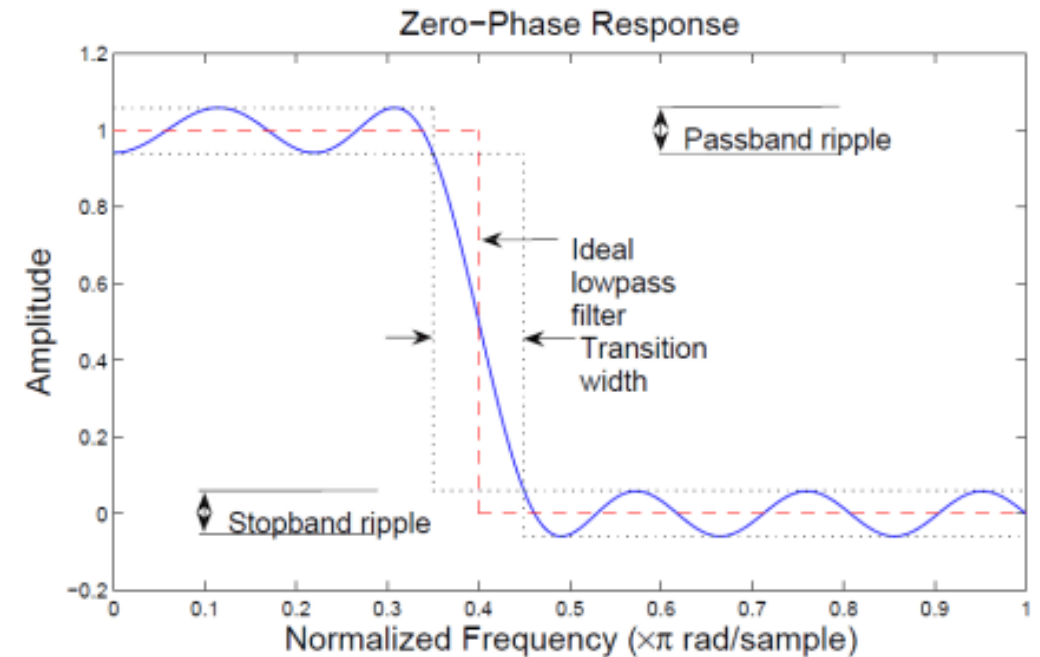
# Filter types

- **Low-pass filter:**  
low frequencies are passed, high frequencies are attenuated.
- **High-pass filter:**  
high frequencies are passed, low frequencies are attenuated.
- **Band-pass filter:**  
only frequencies in a frequency band are passed.
- **Band-stop filter** (or band-reject filter):  
only frequencies in a frequency band are attenuated.



# Parts of a filter

- **Ripples:**  
the fluctuations in the pass band, or stop band, of a filter's frequency magnitude response curve.
- **Transition region:**  
The region which is in between the passband and stopband



# No free lunch theory (NFL)

No free lunch theory states that any two optimization algorithms are equivalent when their performance is averaged across all possible problems.



Wolpert, D.H., and Macready, W.G. (2005) "Coevolutionary free lunches", *IEEE Transactions on Evolutionary Computation*, 9(6): 721–735



# No free lunch theory (NFL)

No free lunch theory states that any two optimization algorithms are equivalent when their performance is averaged across all possible problems.

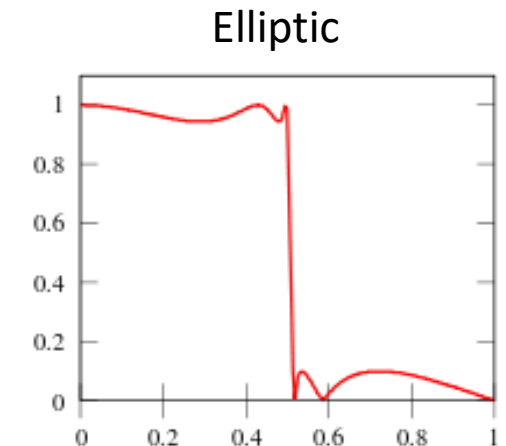
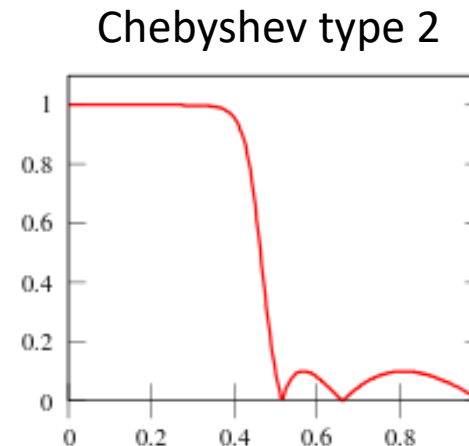
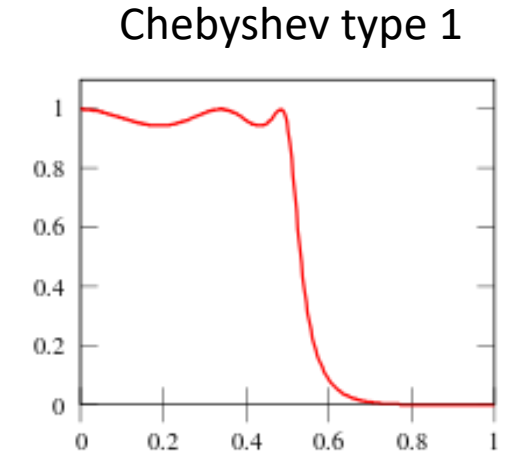
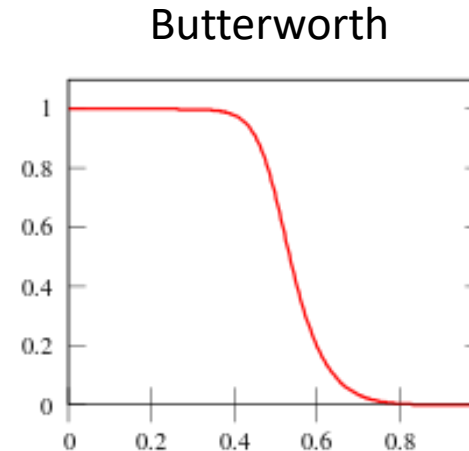
If you gain something, you will lose something. There is always an exchange.



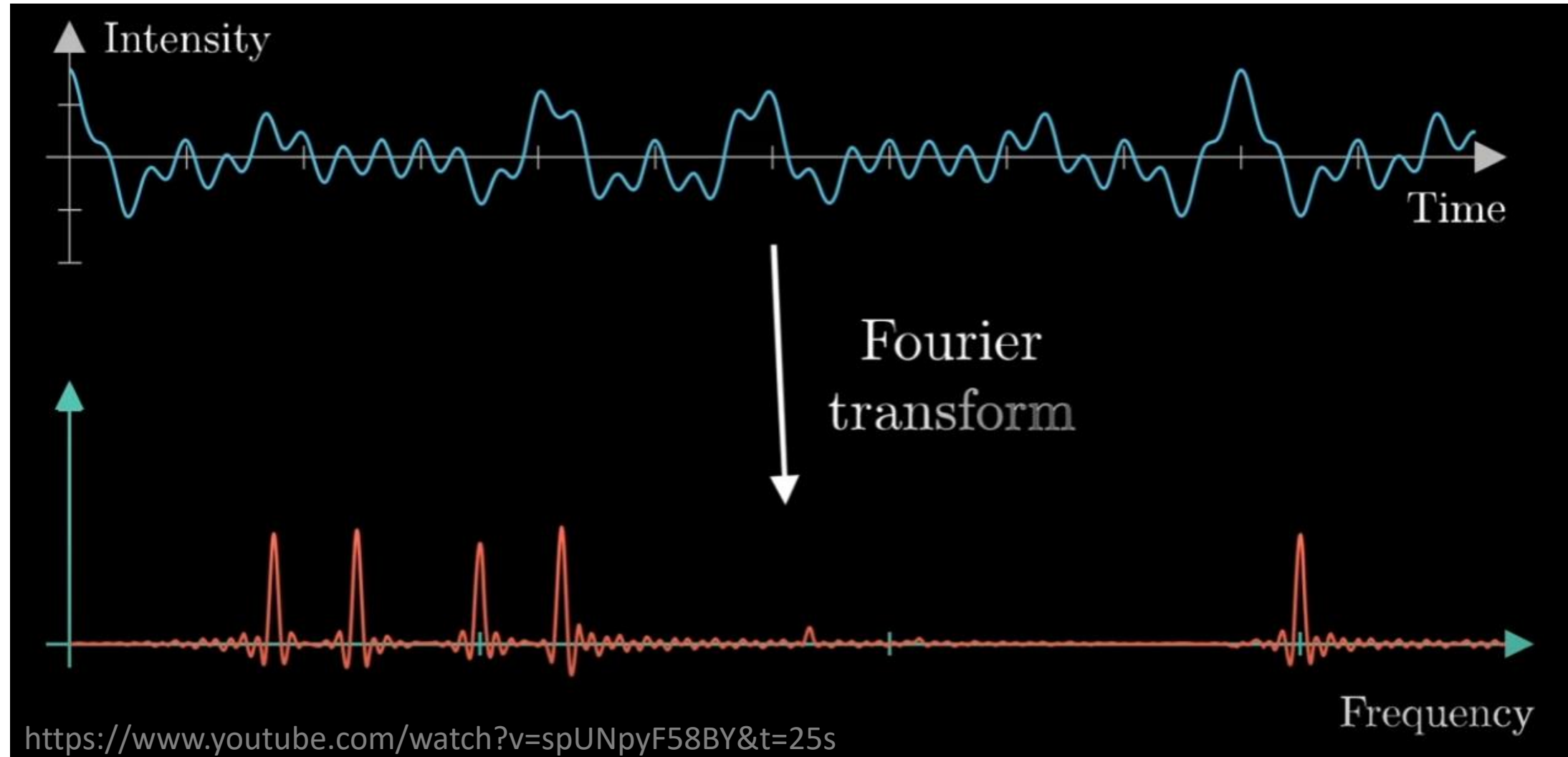
Wolpert, D.H., and Macready, W.G. (2005) "Coevolutionary free lunches", *IEEE Transactions on Evolutionary Computation*, 9(6): 721–735

# Filters

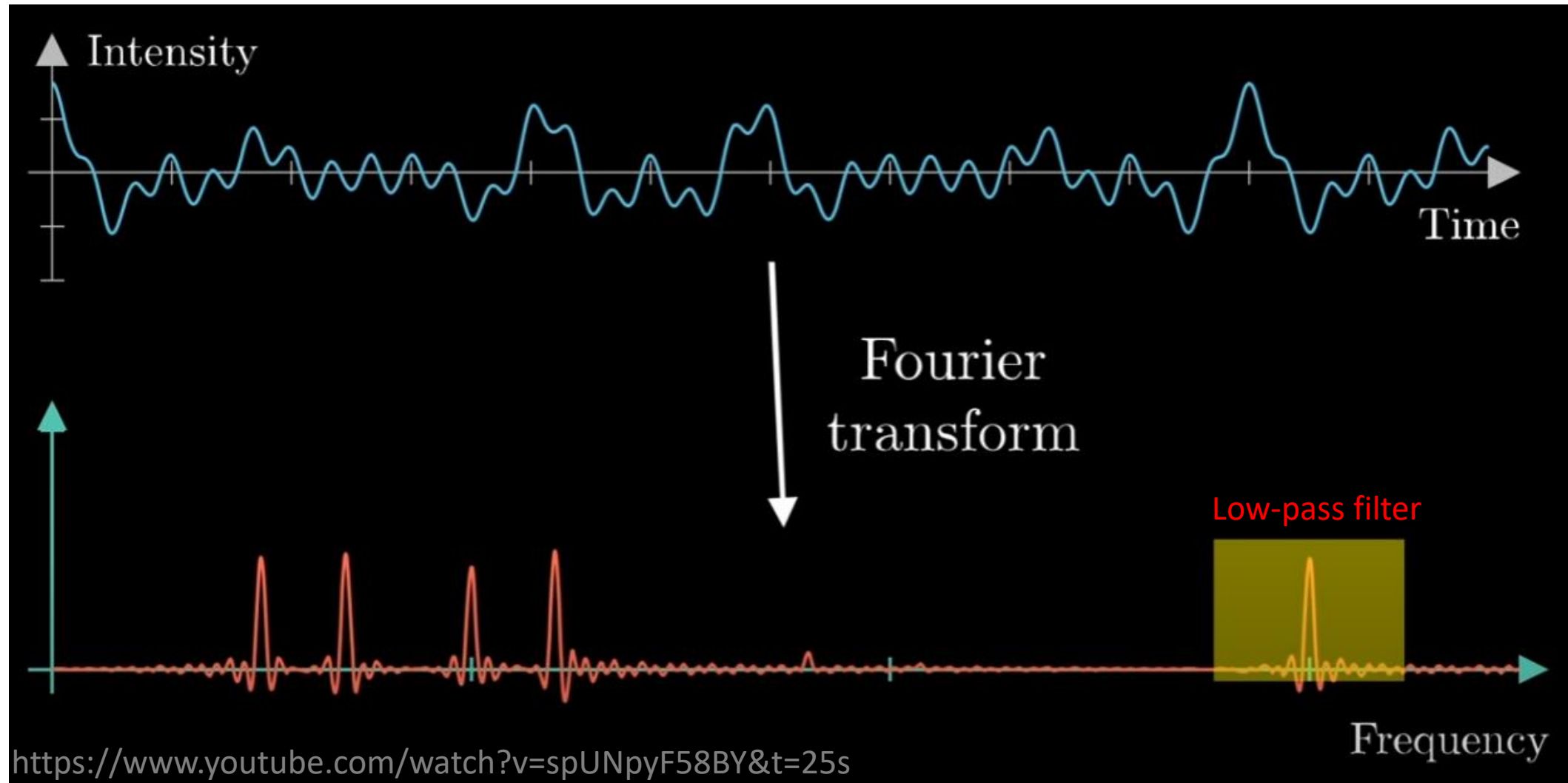
- **Butterworth**  
no gain ripple in pass band and stop band, slow cutoff
- **Chebyshev type 1:**  
no gain ripple in stop band, moderate cutoff
- **Chebyshev type 2:**  
No gain ripple in pass band, moderate cutoff
- **Elliptic:**  
gain ripple in pass and stop band, fast cutoff



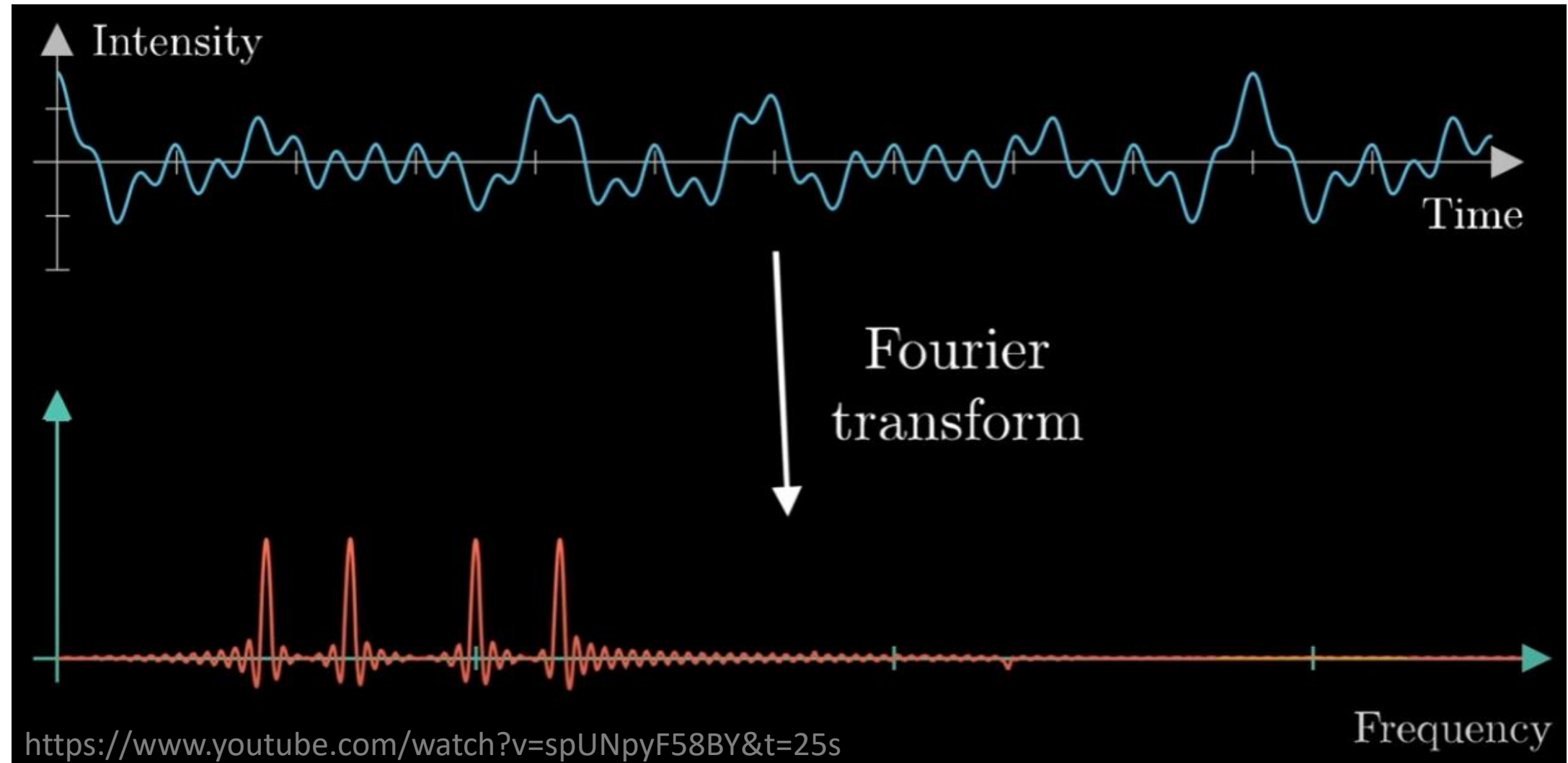
# Example



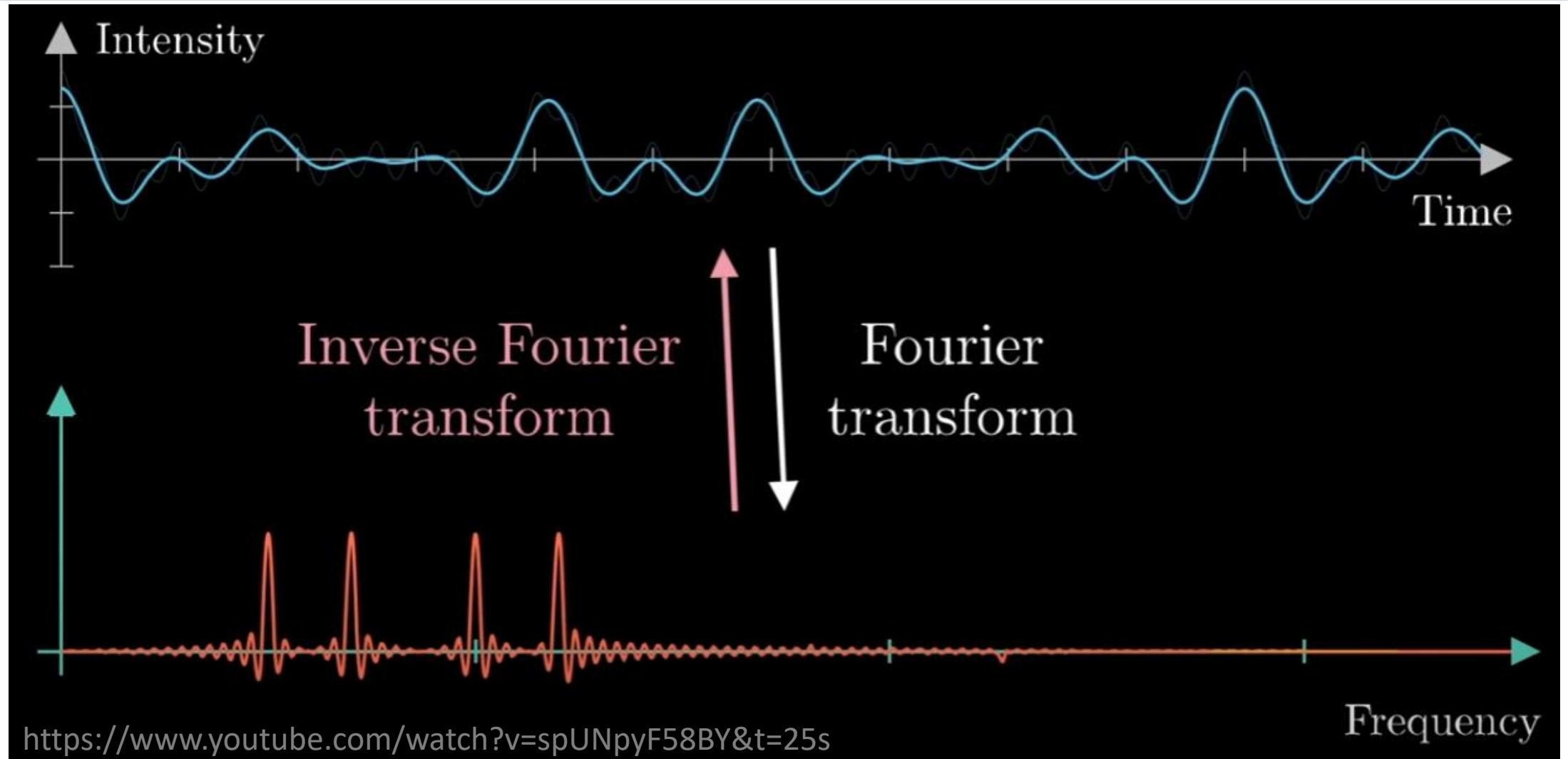
# Example



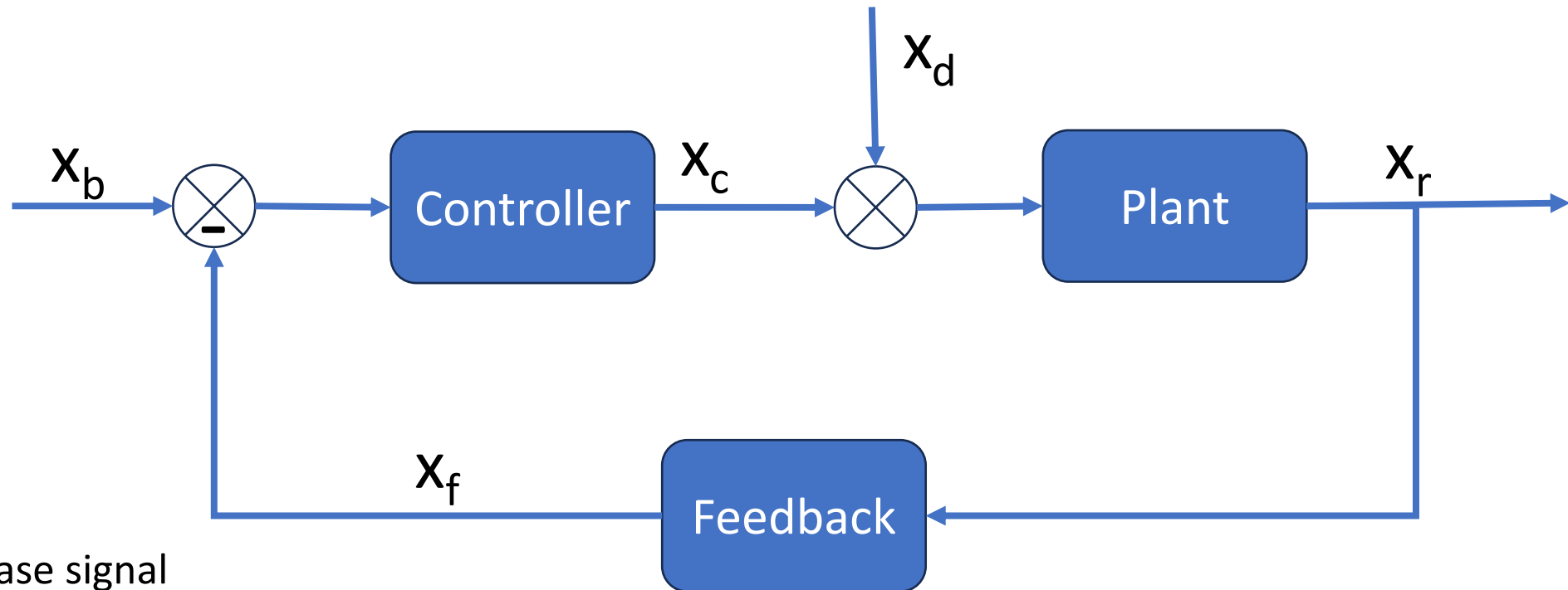
# Example



# Example



# Canonical control loop



$x_b$ : Base signal

$x_c$ : Control signal

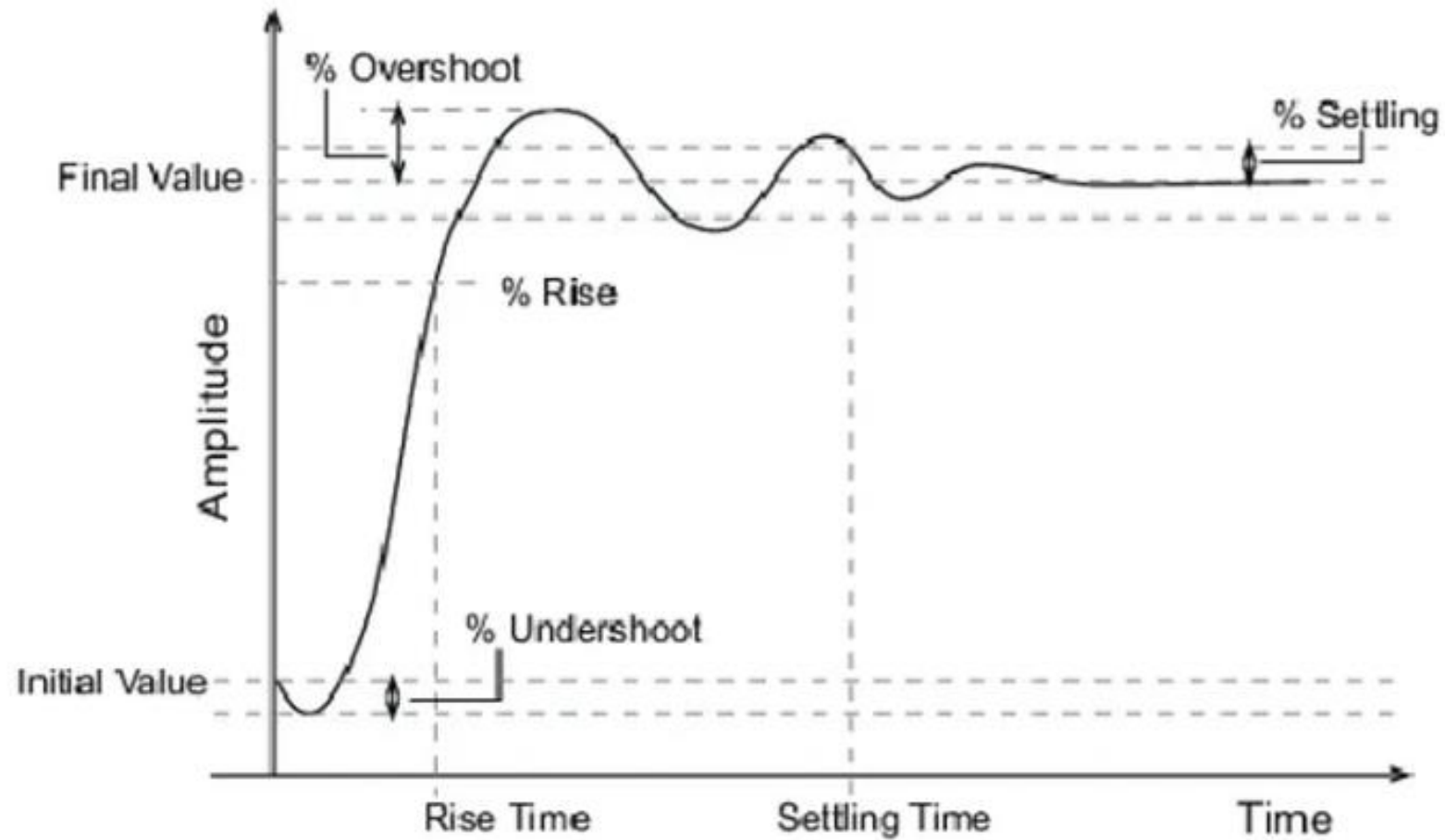
$x_r$ : Regulated/controlled signal

$x_f$ : Feedback signal

$x_d$ : Disturbance signal

Transfer function  
= mathematical model of  
the plant

# Controlled signal

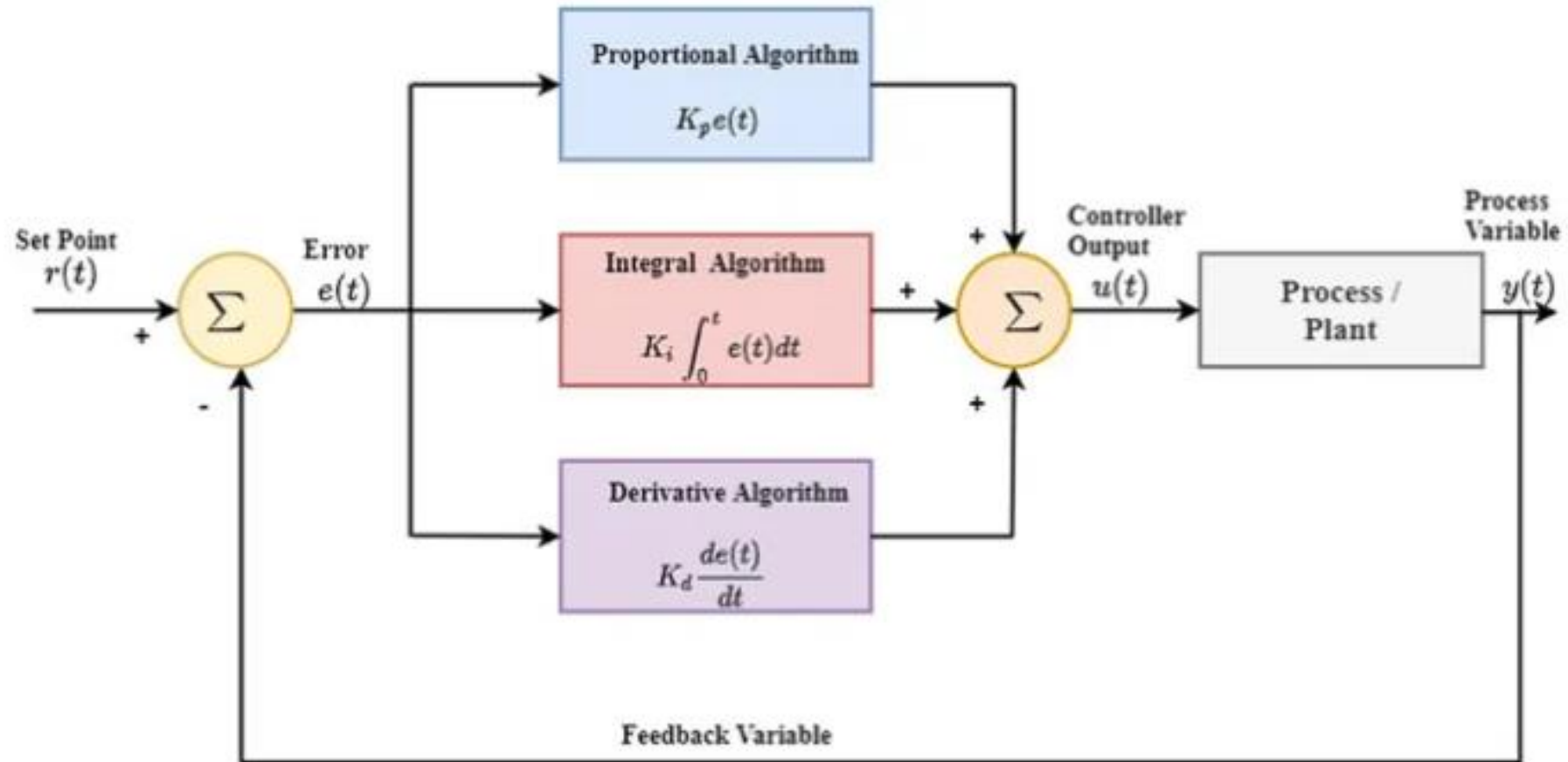




# Bike turn example



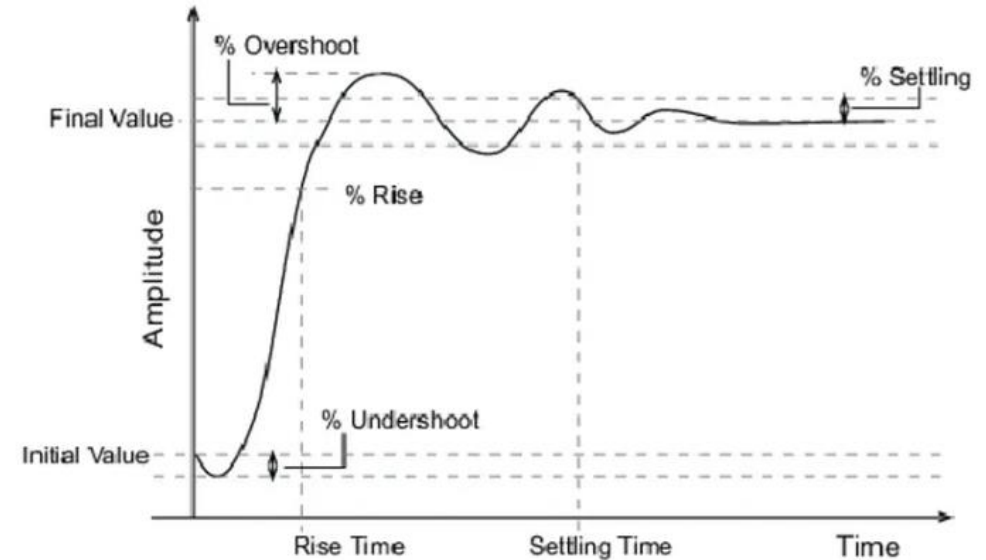
# PID controller



<https://vis-ro.web.app/robotics/pid>

# Controller types

- A **Proportional (P)** controller is used to reduce the rise time and speed up the response. This controller makes no changes in the phase response of the plant.
- A **Derivative (D)** controller is required to minimise the transient errors like overshoot and oscillations in the output of the plant. But this can create heavy instability in noisy environments. Be careful to use smaller gain with this controller. It provides a phase lead to the output when compared with the input, usually with no change in magnitude.
- An **Integral (I)** controller corrects the time invariant errors. This provides a phase lag and no change in magnitude in the output.



# Controller in action -> Behaviour





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Thank you for your attention!