

Name: \_\_\_\_\_

**Methods and Tools  
Homework**

Neptun: \_\_\_\_\_

1. Calculate the derivative of the following function.

$$f = \frac{e^{3x}}{1 + e^x}$$

2. Consider the *Laplace* distribution with parameter  $\lambda > 0$ , centered at  $\mu$ :

$$\mathcal{L}(x|\mu, \lambda) = \frac{1}{\lambda\sqrt{2}} e^{(-\frac{\sqrt{2}|x-\mu|}{\lambda})}.$$

Show that this distribution is normalized.

3. Calculate the Eigen values of the **A** matrix. If  $\lambda = 2$  is an Eigen value give a concrete example of the corresponding Eigen vectors.

$$\mathbf{A} = \begin{bmatrix} 1 & 2 & 1 \\ -1 & 4 & 1 \\ 2 & -4 & 0 \end{bmatrix}$$

4. Compute the covariance of the joint variables  $X, Y$  based on the following observations:

$$X = [98, 87, 90, 85, 95, 75]$$

$$Y = [15, 12, 10, 10, 16, 7]$$