



ELTE

FACULTY OF  
INFORMATICS

# Embodied Intelligence – L03

## *Sensors*

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DEPARTMENT OF  
ARTIFICIAL  
INTELLIGENCE

# Outline

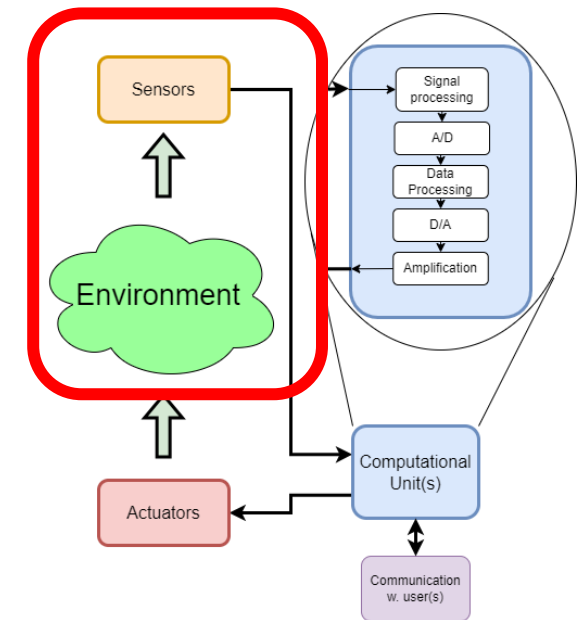
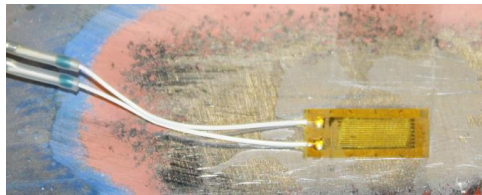
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- Basic definitions
- Signals and their properties
- Measuring mechanical quantities
  - Force, torque, position, pressure

# Definitions

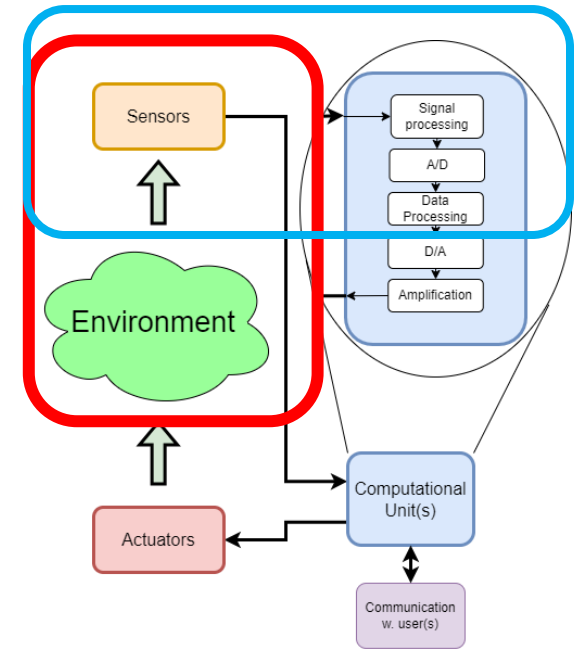
# What I said on the first lecture?

- In its broader definition, the purpose of a sensor is to ***detect a certain event, process or change in the environment and produce a corresponding output signal.***
- Human sensory inputs:
  - Vision
  - Audio
  - Smelling
  - Taste
  - Tactile
  - Temperature
  - ... etc.
  - FUN FACT: We can't sense whether something is wet or not (no humidity sensors in our skin)



# I was not completely honest

- You will see during this lecture that the encirclement was not completely correct.
- Some sensors also do:
  - Signal pre processing
  - Analog/Digital conversion
  - Communication protocols



# Communication with the environment

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- A subcategory of transducers
- In its broader definition, the purpose of a sensor is to ***detect a certain event, process or change in the environment and produce a corresponding output signal.***



Source: LoTR

# Signals - Information

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- Information means the quantifiable knowledge content of a communication that is understood to mean.
- It is transmitted by the signal, which is an abstract concept.  
(Info + Noise = Signal)



Source: LoTR

# Signals - Definition

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- A signal is a value or change in value of a physical quantity that is capable of acquiring, transmitting or storing information.

This means that, it also  
needs to be interpretable!



Source: LoTR



# Processing unit need to understand the signal

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- But this is the topic of the 5th lecture ;)



Source: LoTR

# Signals – definition (cont.)

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- A signal can be given by a  $x = x(t)$  function
- that is interpreted on the  $t_0 \leq t \leq t_1$  interpretation domain which can be:
  - Finite
  - Infinite

# Signals - categorization

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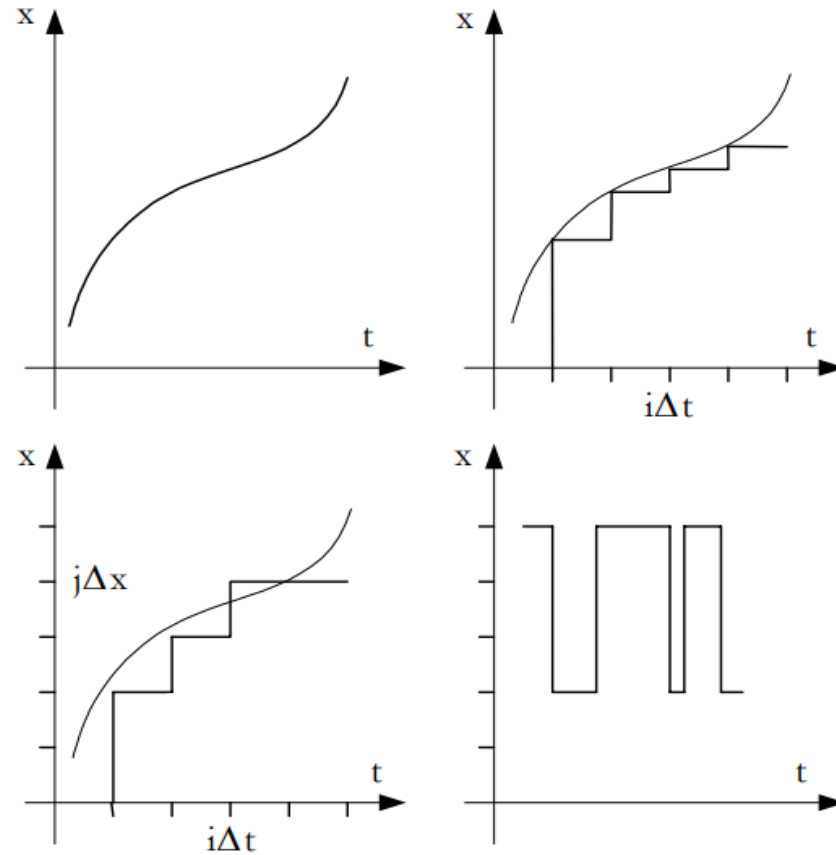
- According to the value:
  - **Continuous** [i.e.: Any kind of value can appear within a range]
  - **Discrete (Quantified in amplitude)** [i.e.: Only certain values can appear; basically this is the digitalisation]
- According to the course of time:
  - **Continuous** [i.e.: At any given time it can change value]
  - **Discrete (Quantified in time)** [i.e.: It can only change in certain times (like sampling)]

# Signals – categorization (cont.)

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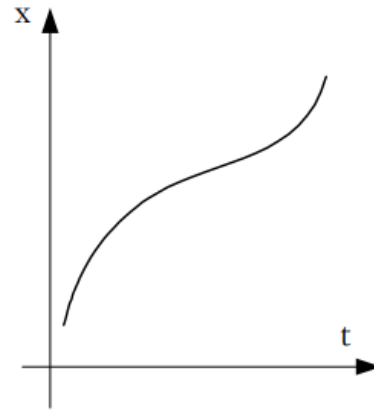
- Appearance of the information:
  - **Analogue** [i.e.: The information is represented directly in the signal]
  - **Digital** [i.e.: The information is represented in a discrete value (number)]
- Determination of value:
  - **Deterministic** [i.e.: It can be described with a function]
    - Periodic [e.g.: in cyclic processes]
    - Transient [e.g.: in transient processes]
  - **Stochastic** [i.e.: It can't be described with a concrete function but with statistical methods]

# Let's categorize these signals

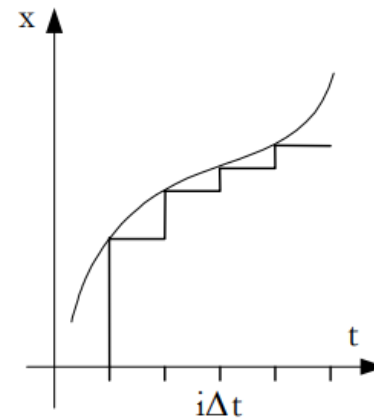


# Solutions

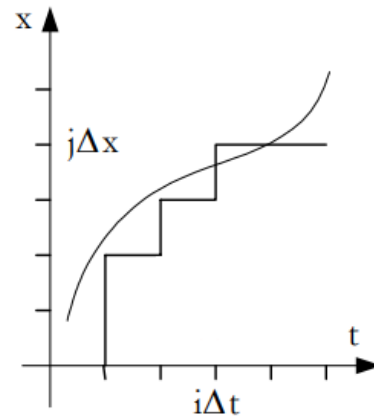
Continuous (analogue) valued  
Continuous in time



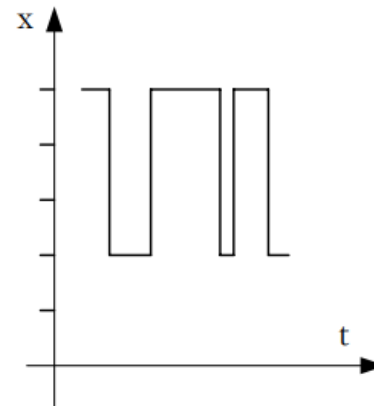
Continuous (analogue) valued  
Discrete in time



Discrete (digital) valued  
Discrete in time



Discrete (digital) valued  
Continuous in time



# Some important properties of signals

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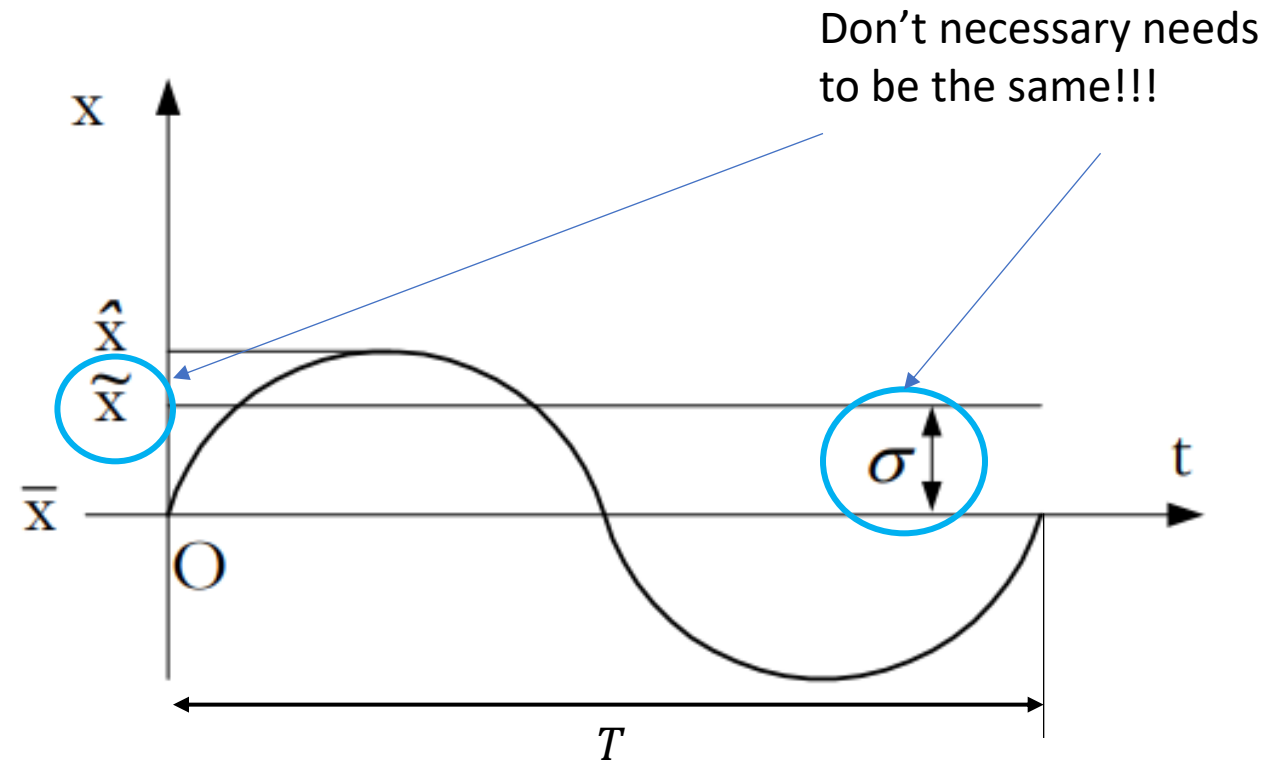
- **Maximum:**  $\hat{x} = \max(x(t))$
- **Mean:**  $\bar{x} = \frac{1}{T} \int_0^T x(t) dt$
- **RootMeanSquar (effective value):**

$$\tilde{x} = \left[ \frac{1}{T} \int_0^T x^2(t) dt \right]^{\frac{1}{2}}$$

- **Deviation:**  $\sigma_x = \left[ \frac{1}{T} \int_0^T x^2(t) dt \right]^{\frac{1}{2}}$

Example:  $x(t) = A \sin(\omega t)$ ,  $\omega = \frac{2\pi}{T}$

- $\hat{x} = \max(x(t)) = A$
- $\bar{x} = \frac{1}{T} \int_0^T x(t) dt = 0$
- $\tilde{x} = \left[ \frac{1}{T} \int_0^T x^2(t) dt \right]^{\frac{1}{2}} = \frac{A}{\sqrt{2}}$
- $\sigma_x = \left[ \frac{1}{T} \int_0^T x^2(t) dt \right]^{\frac{1}{2}} = \frac{A}{\sqrt{2}}$





# Sensors

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- According to whether they emit energy during the measurement:
  - Active (yes) [CCD, thermocouple, photodiode]
  - Passive (no) [thermistors, photoresistors, resistance strain gauges]

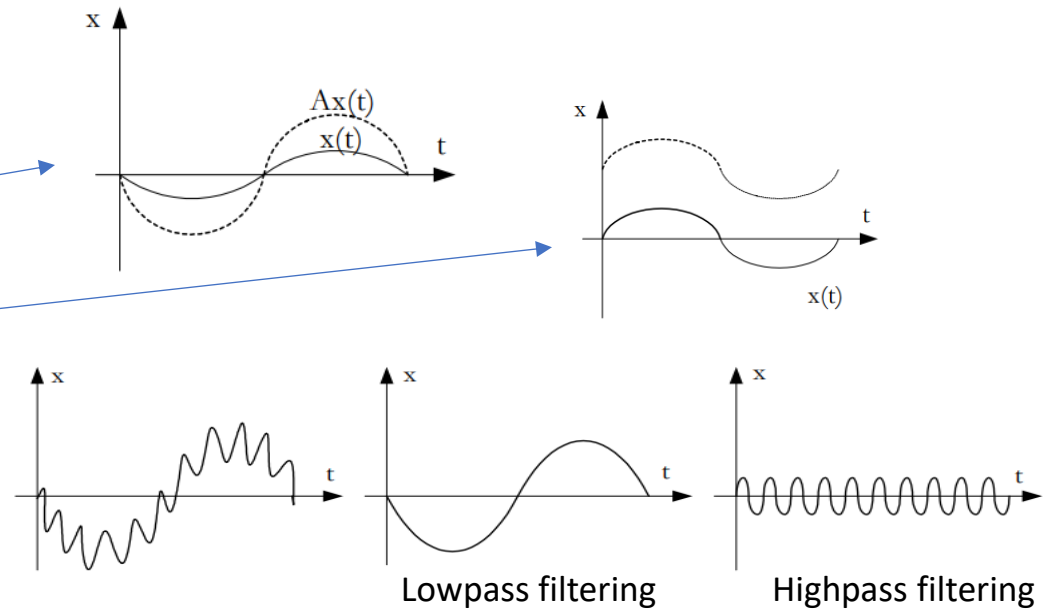
# Mostly measured physical quantities

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- **Mechanical:** position (absolute/relative), velocity, acceleration, angular position/velocity/acceleration, force, torque, pressure ...
- **Thermal:** temperature, heat flux, radiation ...
- **Electrical (magnetic):** charge, voltage, current, magnetic induction, flux ...
- **Optical:** light intensity, wavelength ...

# Most of the times the signal from the sensor is not sufficient for processing

- We need signal conditioning (not exhaustive list):
  - Amplification
  - Input coupling
  - Filtering
  - Electrical isolation
  - Linearization
  - Attenuation
  - ...



# Sensors - MUSTs

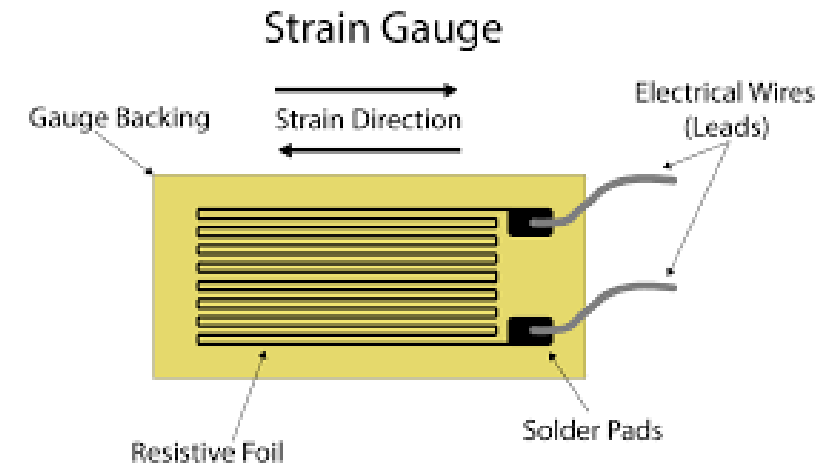
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- Unambiguous and reproducible signal
- Output is only influenced by the input
- A linear relationship between input and output. (weak requirement)
- Do not affect the measured system. (theoretically)
- Immunity to external disturbances. (mostly theoretically)
- The output signal can be normalized.

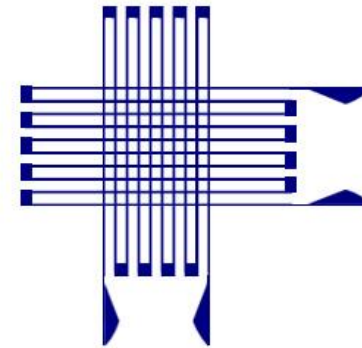
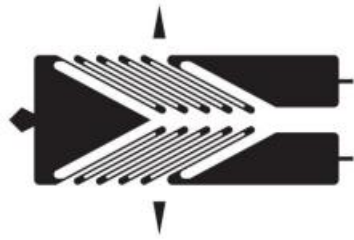
# Measuring mechanical quantities

# Measurement of deformation

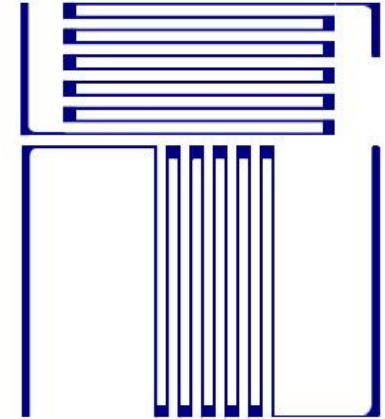
- Why measure?
  - Deformation of solid bodies on mechanical stress
    - Force measurement
    - Torque measurement
- Applications:
  - Material testing
  - Assessment/surveillance of constuctional elements of devices during load
  - Measurement of force
  - Measurement of weight



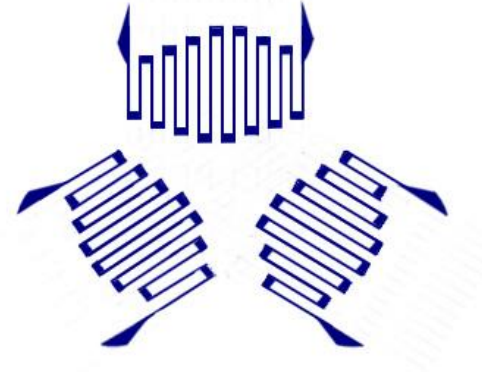
# Some usual types



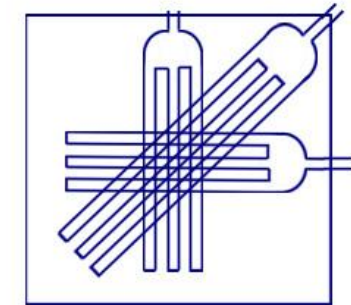
Two-Element, 90 Degree Planar (Shear)  
Rosette Strain Gauge



Two-Element 90 Degree Planar  
Rosette Strain Gauge



Three Element, 60 Degree Delta  
Rosette strain Gauge

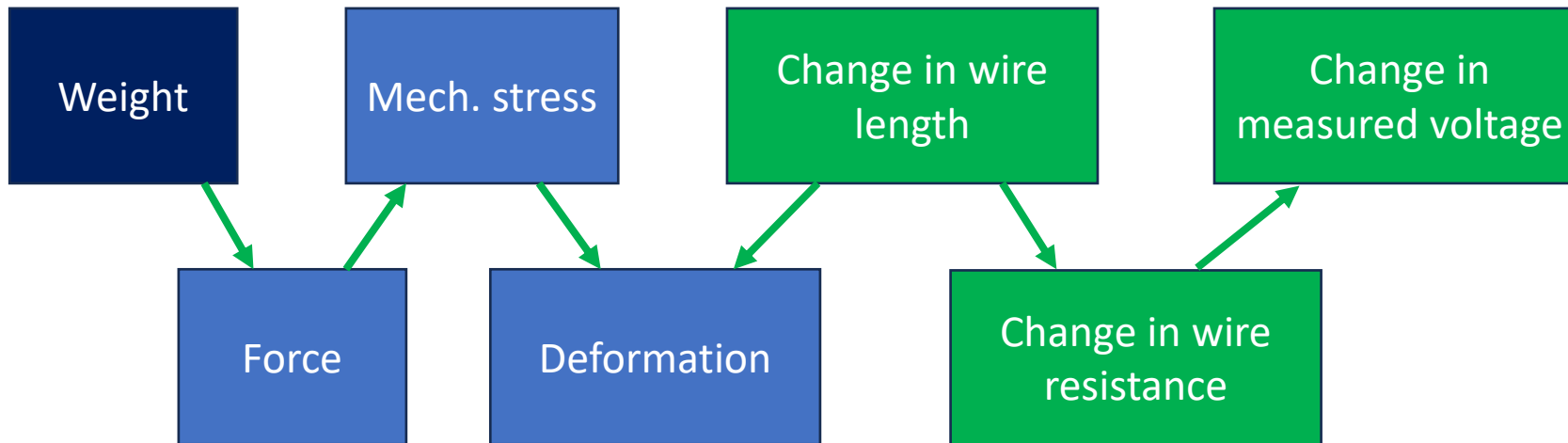


Three Element, 45 Degree Planar  
Rectangular Rosette Strain Gauge

[www.InstrumentationToday.com](http://www.InstrumentationToday.com)

# Roadmap

- Let's say we want to measure weight.
- We need to measure it indirectly





# Physical background of the measurement

- Weight → Force (simplified):

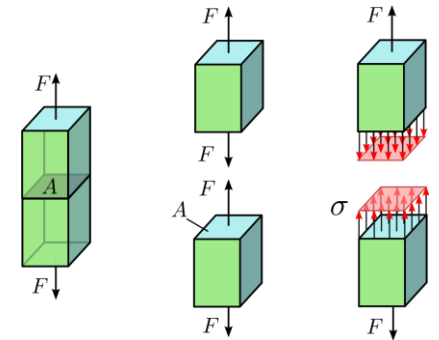
$$F_N = m \cdot g_e$$

where:  $F_N$  – normal force;  $m$  – mass;  
 $g_e$  – gravitational coefficient (Earth; 9.817 m/s<sup>2</sup>)

- Force → Mech. stress (Uniaxial normal case)

$$\sigma = \frac{F}{A}$$

where:  $\sigma$  – mechanical stress;  $F$  – force applied;  
 $A$  – normal scrossection's area of the body



- Mech. Stress → Length difference (Hook's law):

$$\sigma = E \cdot \varepsilon = E \cdot \frac{\Delta L}{L}$$

# Physical background of the measurement (cont.)

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- Resistance of a wire:

$$R = \rho \frac{l}{A} = \rho \frac{l}{r^2 \pi} \quad \text{where:} \quad R - \text{resistance; } \rho - \text{resistance coefficient; } L - \text{length of the wire; } A - \text{Area of the wire}$$

- ... (On the next slide for extra)
- Gauge – factor (ratio between the length change and resistance change):

$$g = \frac{dR/R}{dl/l} \approx 1 + 2\nu \approx 2$$

## Gauge factor (extra)

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$$dR \cong \frac{\partial R}{\partial \rho} d\rho + \frac{\partial R}{\partial l} dl + \frac{\partial R}{\partial r} dr \rightarrow dR \cong \frac{l}{r^2 \pi} d\rho + \frac{\rho}{r^2 \pi} dl + 2 \frac{\rho l}{r^3 \pi} dr$$

$$dR \cong \frac{R}{\rho} d\rho + \frac{R}{l} dl + 2 \frac{R}{r} dr \rightarrow \frac{dR}{R} \cong \frac{d\rho}{\rho} + \frac{dl}{l} + 2 \frac{dr}{r}$$

Poisson factor:  $\frac{dr}{r} = -\nu \frac{dl}{l}$

$$\frac{dR}{R} \cong \frac{d\rho}{\rho} + \frac{dl}{l} (1 + 2\nu) \rightarrow g = \frac{dR/R}{dl/l} \approx 1 + 2\nu \approx 2 \quad (\nu = 0.5)$$

# Problem with the measurement of the resistance change

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- Let's consider the following (~typical case):
- Measure maximum weight: 100kg [let be a steel measuring body with  $A = 5 \text{ mm}^2$ , ( $E = 2 \cdot 10^5 \frac{\text{N}}{\text{mm}^2}$ , elastic modulus), typical resistance strain gauge:  $R = 120 \Omega$ ]
- $F_N = 1000 \text{ N} \rightarrow \sigma = \frac{1000 \text{ N}}{5 \text{ mm}^2} = 200 \frac{\text{N}}{\text{mm}^2} \rightarrow \varepsilon_{max} = 0.001$
- $\frac{dR}{R} = g \cdot \varepsilon_{max} = 0.002 \rightarrow dR = g\varepsilon R = 0.002 \cdot 120 \Omega = \mathbf{0.24 \Omega}$

# Problem with the measurement of the resistance change

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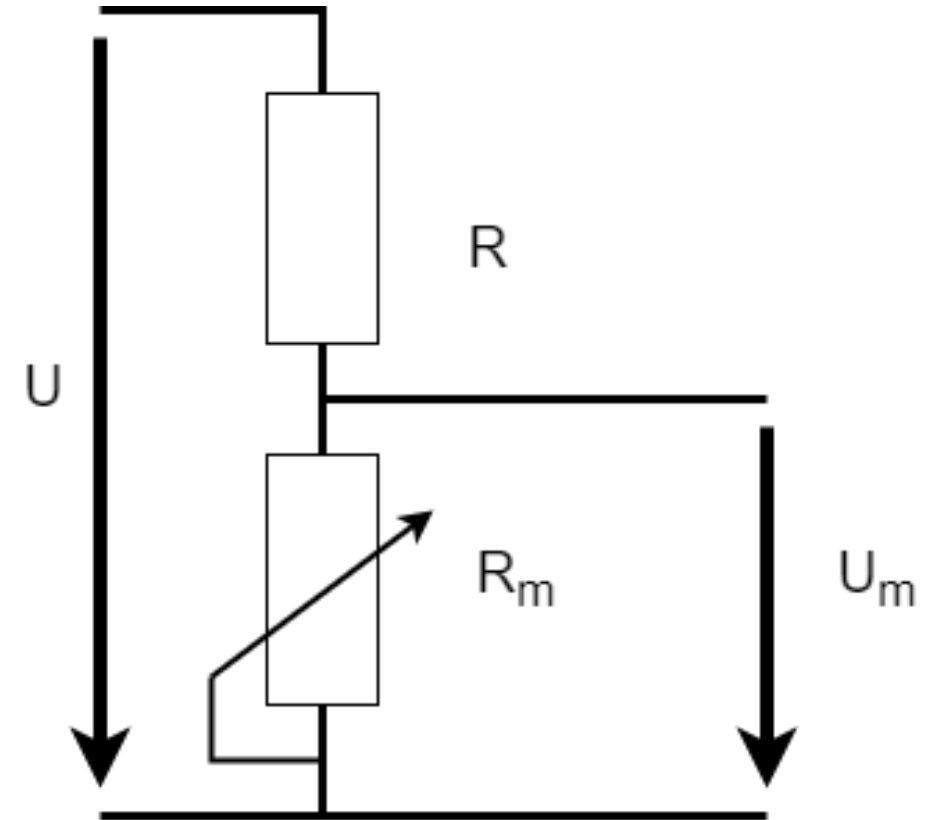
Too small change in resistance, what should we do??

# How would we do this, if the difference was not too small

$$U_m = U \frac{R_m}{R + R_m}$$

- We can't use big **U** and small **R**, because of practical reasons.

( $P = UI^2 \rightarrow$  this will be converted to heat!!!)

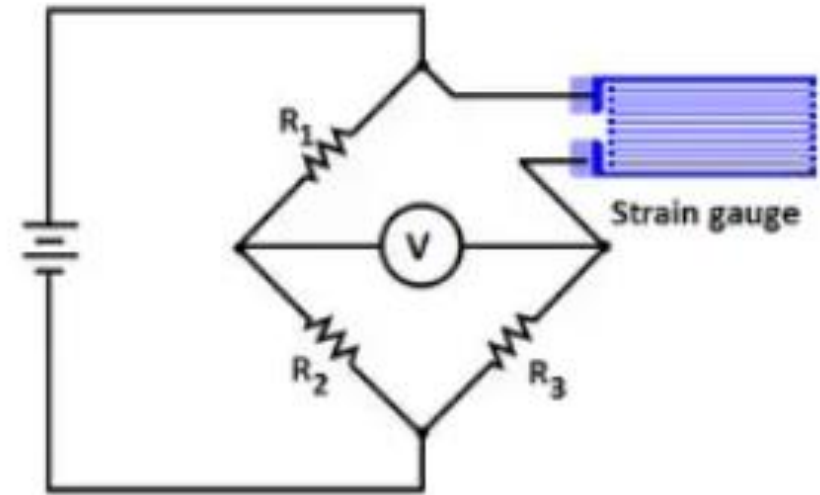


# Measuring precisely small resistance changes

- Wheatstone bridge

$$U_{measured} = U \frac{Rg\varepsilon}{2(2R + Rg\varepsilon)}$$

(if  $R_1 = R_2 = R_3$ )



# Measuring weight - summary

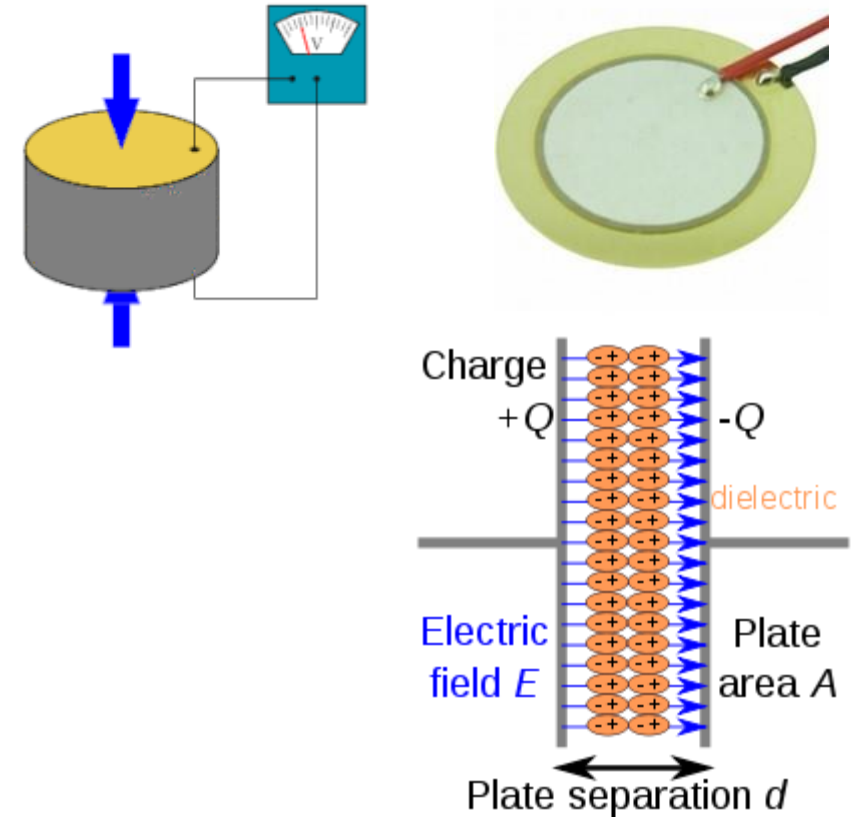
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- Think about:
  - So simple thing to measure
  - So complicated measuring principle (but cheap!!! Only we need to use our brain with the calculations)
  - We had a lot's of simplifications (now!!)
  - We did not processed the signal yet (5th lecture)
  - We did not made our system robust against:
    - Thermal disturbances
    - Electromagnetic disturbances (induction in the wiring)
    - etc ...

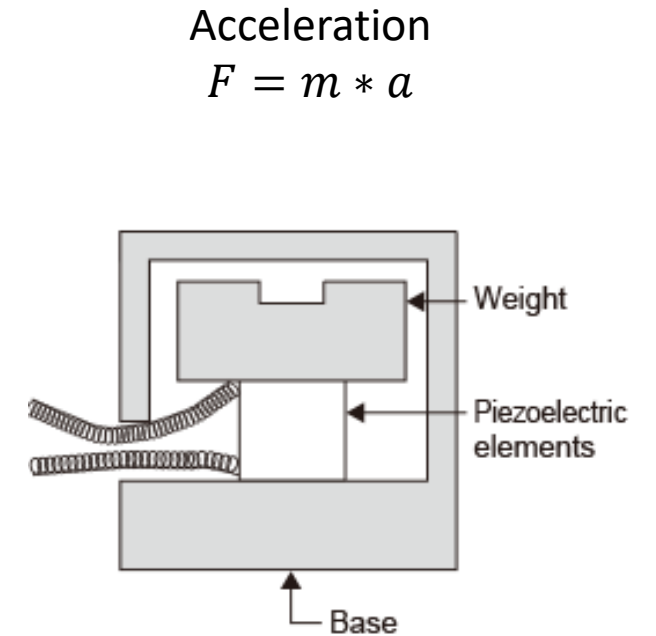
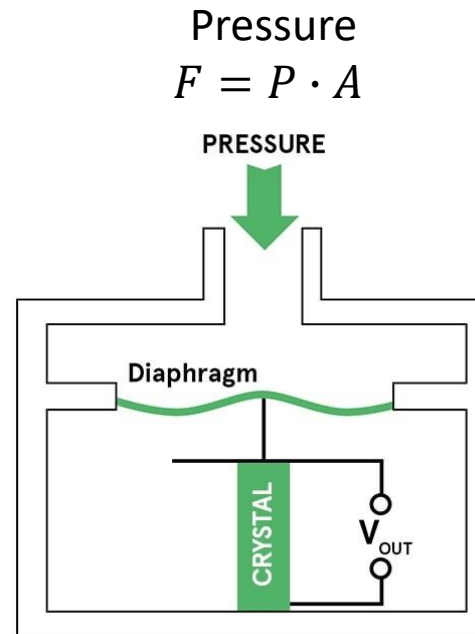
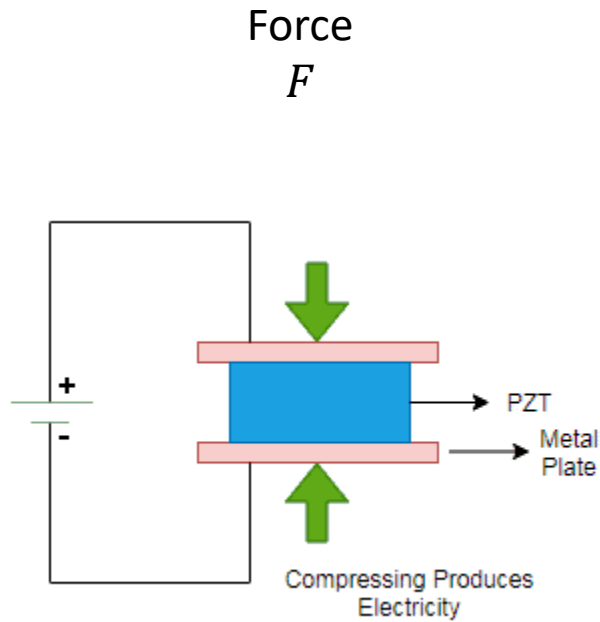


# Measuring linear force/pressure/acceleration

- For (only) dynamical effects we can use Piezzo sensors
- Physical background:
  - In crystalline materials without a symmetry centre, deformation (elastic deformation) leads to the formation of electric dipoles because the positive and negative charge centres separate or the length of the existing dipoles changes. On the opposite faces of the crystal, due to the ordering of the dipoles caused by mechanical stress, electric charges of opposite sign accumulate, creating an electric potential. When the deforming force changes direction, the sign is reversed, and the electric field and voltage change sign.

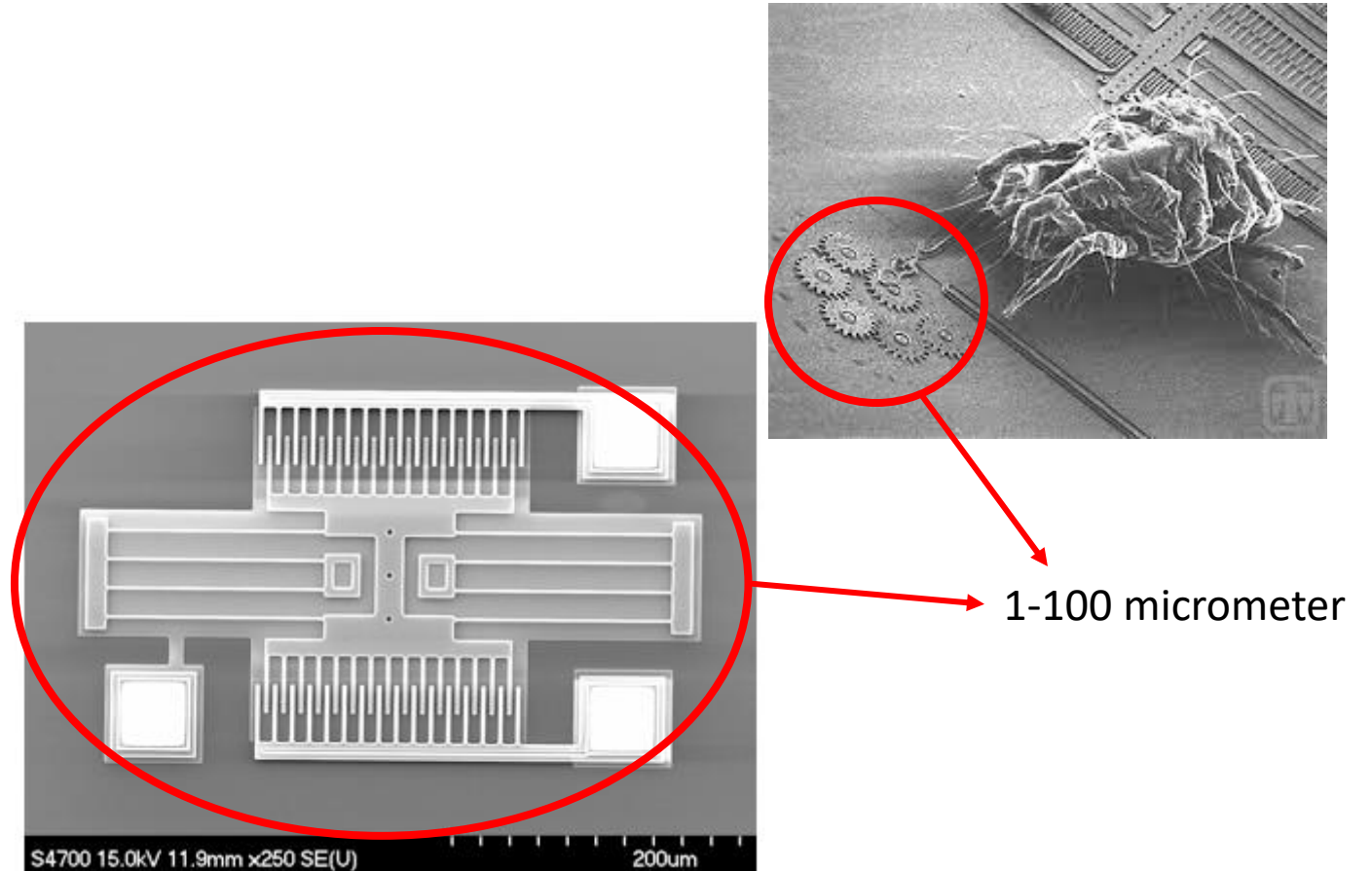


# We use some tricks



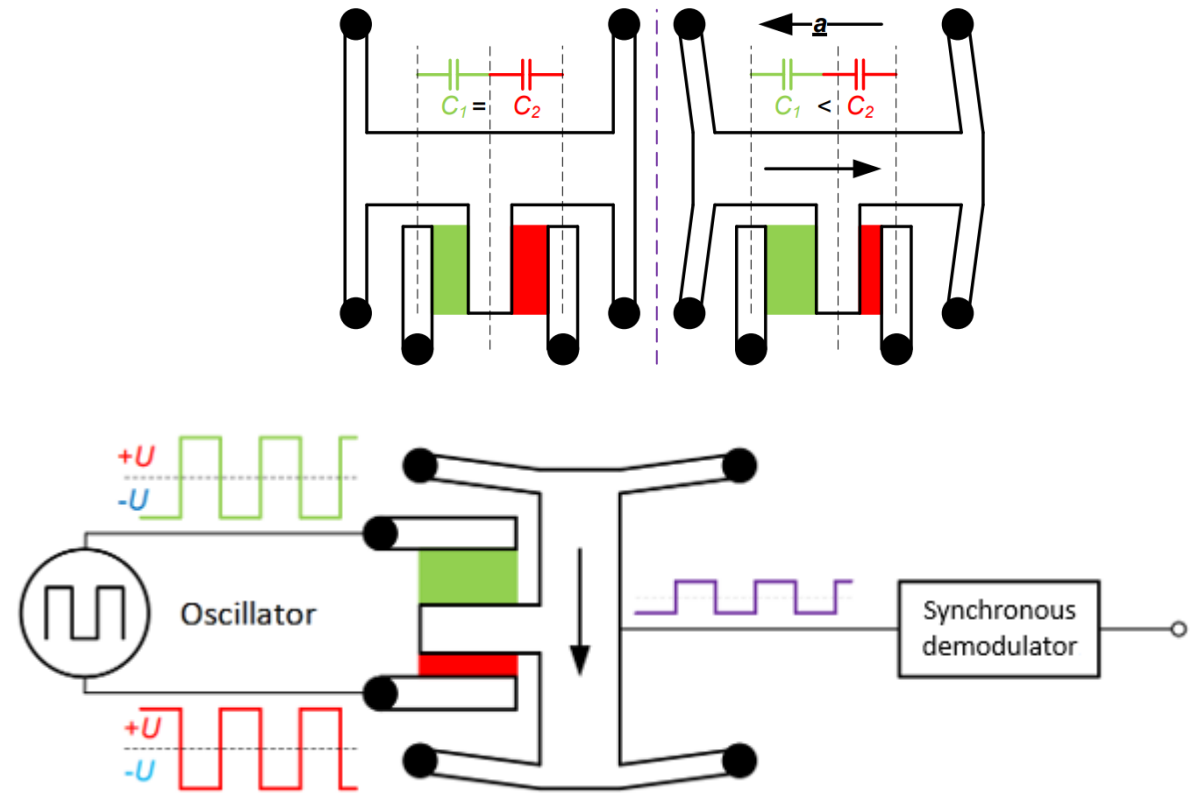
# Measuring acceleration with capacitive sensors

- CMOS MEMS technology
- Able to measure static effects
- Cheap
- Precise and robust
- IMU's accelerometer



# Measuring acceleration with capacitive sensors (cont.)

- Principle of differential capacity
- With a (usually built in) signal generator and demodulator modul we can determine the capacitors value → acceleration



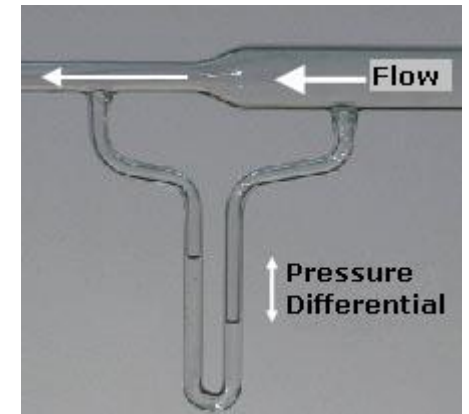
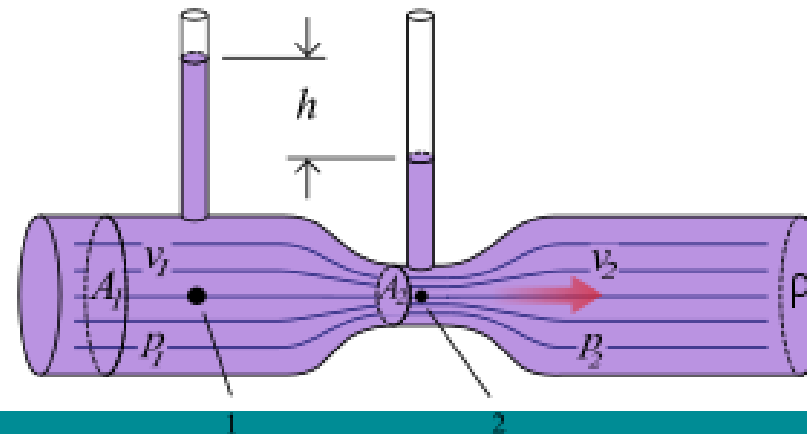
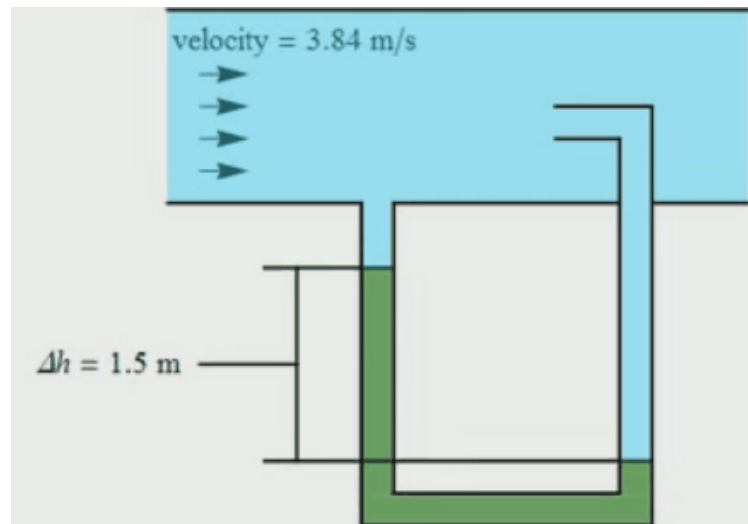
# Measuring waterflow (or gases)

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- We can have several different methods for this
  - Pitot – pipe
  - Venturi – pipe
  - Ultrasound based
  - Doppler effect based

# Pitot pipe and Venturi pipe – Invasive measurements

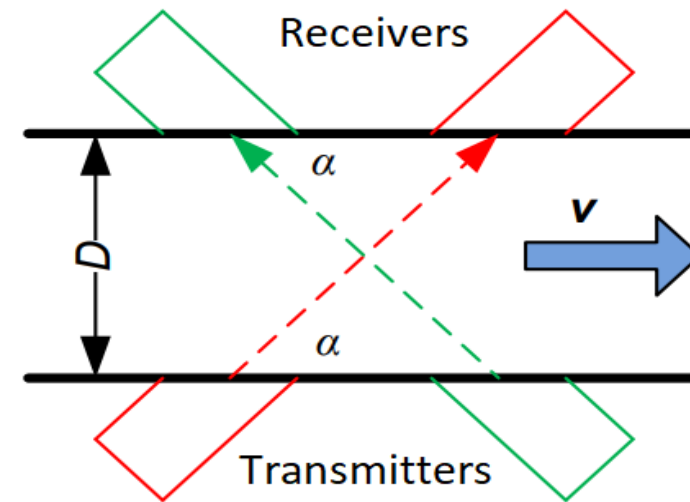
- There will be a difference in the pressure at the tubes edge and the middle
- We measure at the edge of the pipe
- We make a pipe that has different diameters (causing a waterflow difference)



# Non-invasive measurement with ultrasound

- With two ultrasound transmitter – receiver pair
  - One in the same direction
  - One in the opposite direction
- The signals are sent in different (but known) times

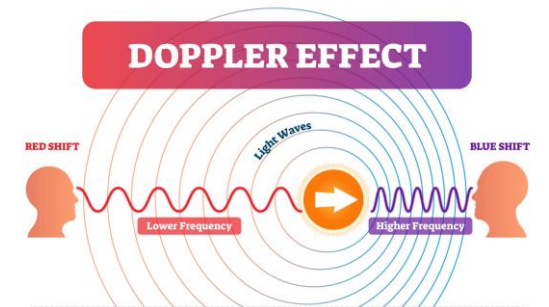
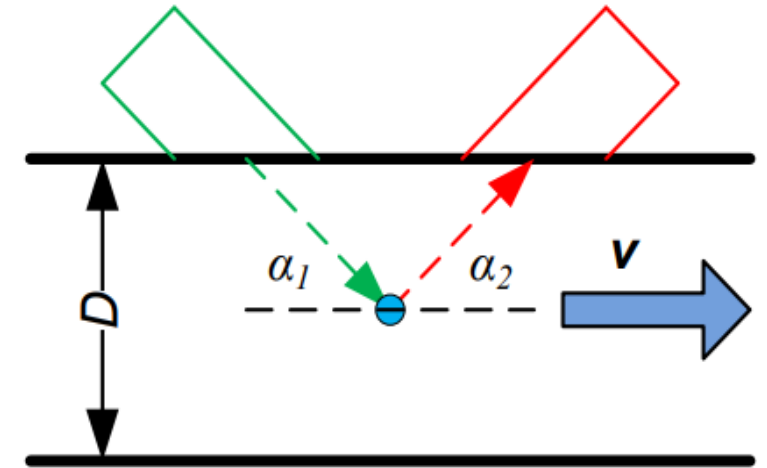
$$t_{sd} = \frac{D}{\sin \alpha \cdot (c + v \cdot \cos \alpha)}$$
$$t_{od} = \frac{D}{\sin \alpha \cdot (c - v \cdot \cos \alpha)}$$
$$\Delta t \approx \frac{2 \cdot Dv \cdot \cos \alpha}{c^2}$$



Precise measurement of time is inevitable (speed of sound in water 1500 m/s)

# Non-invasive measurement with Doppler's effect

- Same method how the velocity of other galaxies are measured
- The frequency of a wave is changing during the relative motion between a wave source and its observer.
- Static receiver and transmitter BUT the medium is not static!



$$f_{receiver} = \frac{c + v_{receiver}}{c + v_{transmitter}} \cdot f_{transmitter}$$



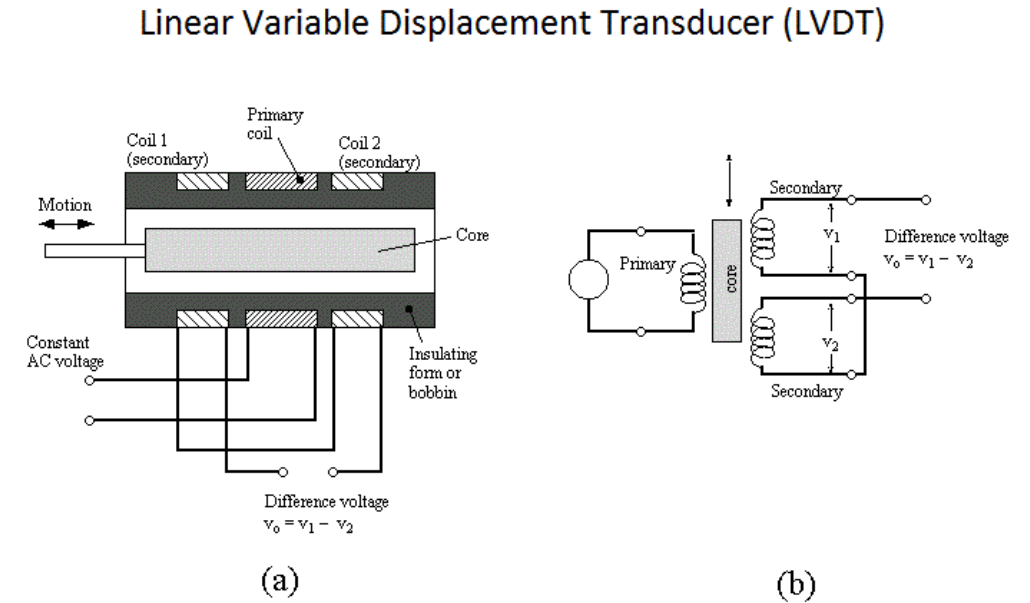
# Measuring linear position and displacement

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- LVDT
- Hall effect
- (double) Integration of the acceleration

# Linear Variable Differential Transformer - LVDTs

- Voltage transformer's principle
- Core is ferromagnetic and moving
- Reliable
- Accurate
- Vibrations, stress testing actuation (feedback)

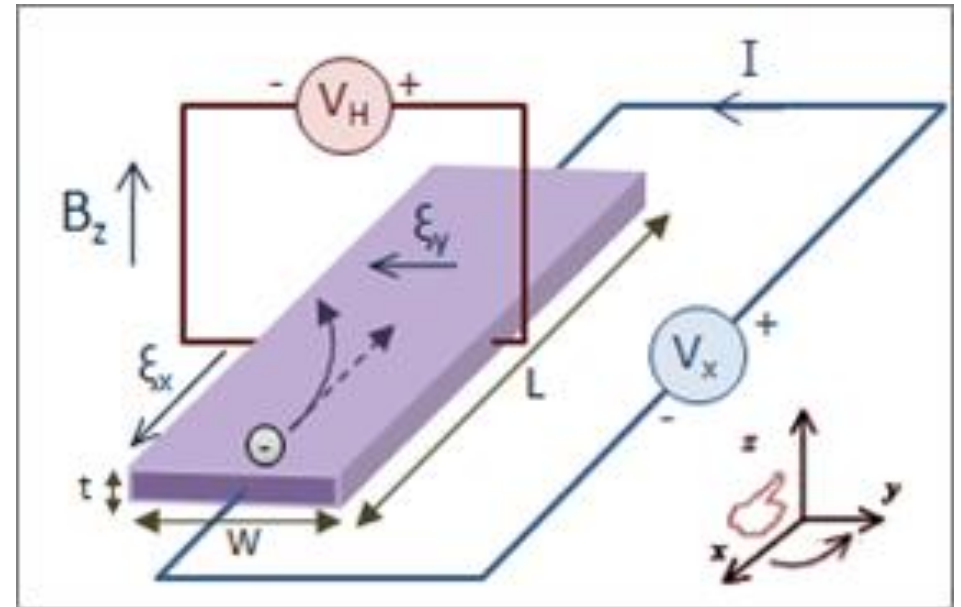


A good presentation of the principle:

[YouTube](#)

# Hall effect transducers

- Hall effect:
  - If a magnetic field is applied perpendicular to the direction of electric current, an electric field is set up, which is perpendicular to both the direction of electric current and the applied magnetic field.
- Measurement of magnetic field or current.  
Proximity.Contactless
- Wheel speed sensors – RPM, switches, proximity sensors



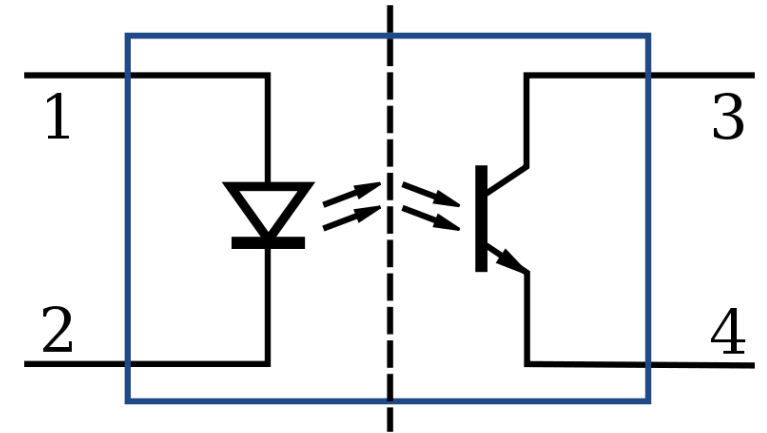
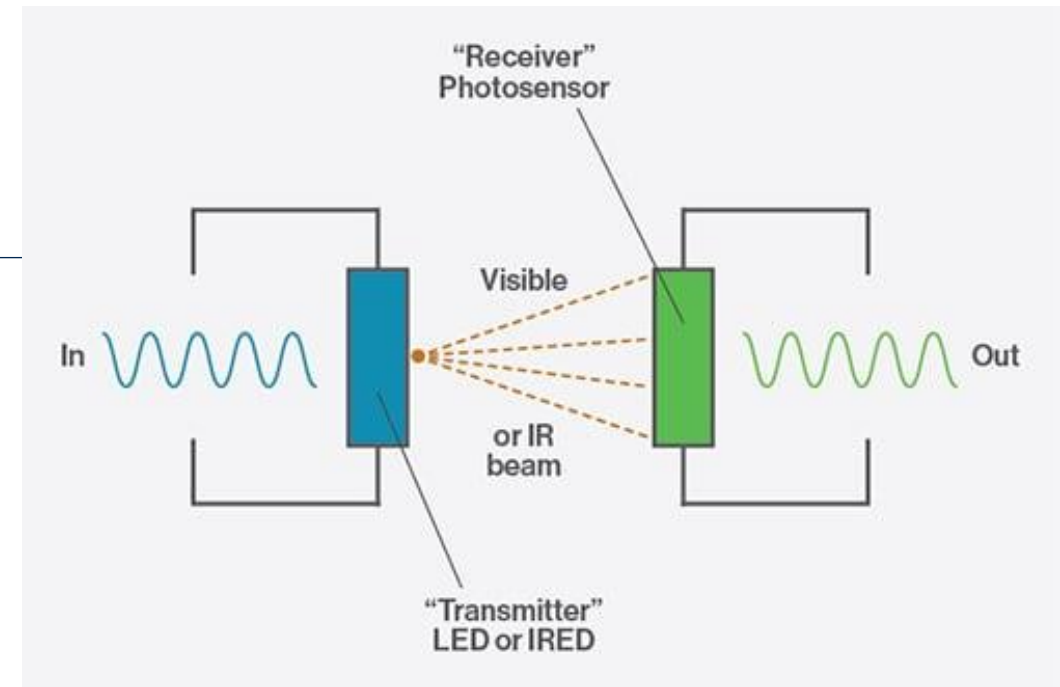
# Measuring rotational movements

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- Optical encoders
- Hall-sensors
- Resolvers

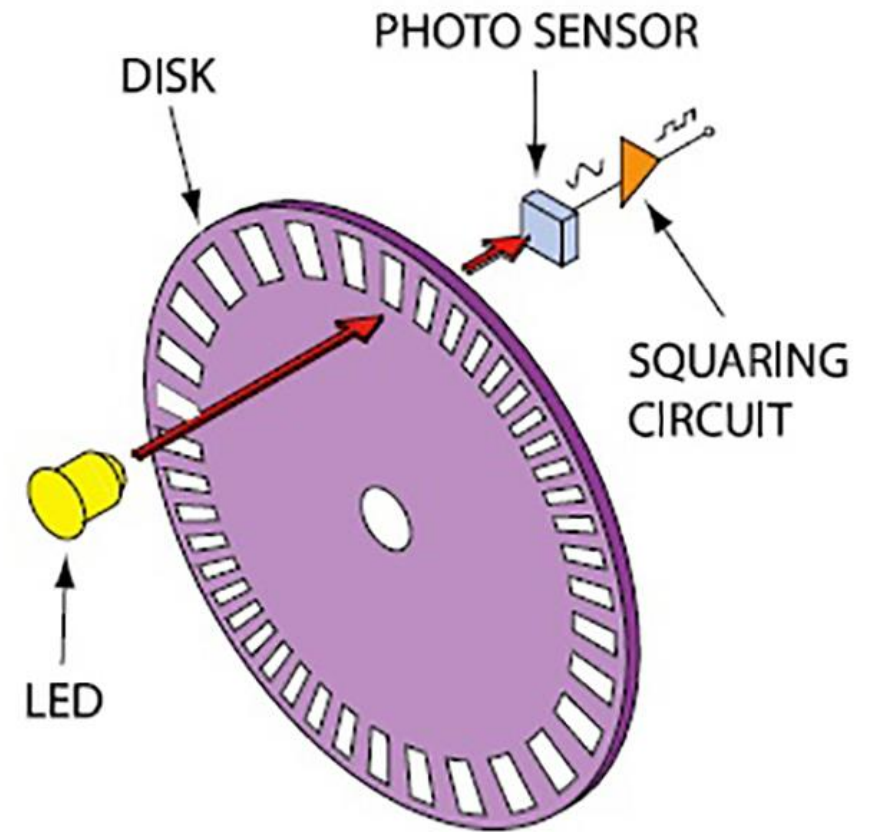
# Optical encoders

- Transmission optocoupler
  - LED + Phototransistor
- Usually used for electrical decoupling of signals
- With a modification we can use this device for measuring revolut movements



# Optical encoders (cont.)

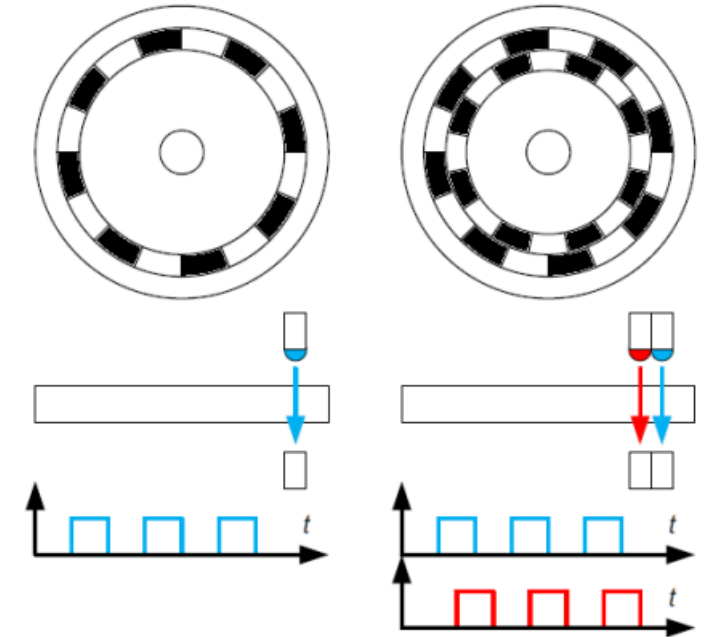
- Putting a disk with holes between the light source and receiver
- The disc is attached to the moving part of the measured device (motor)



Incremental encoder

# Optical encoders (cont.) – Incremental encoders

- 1 circle of holes - movement
- If we need to know the direction
- 2 circle with two receivers (or two receivers in different position)
  - Based on the phase shift we can determine the direction



# Absolute or incremental

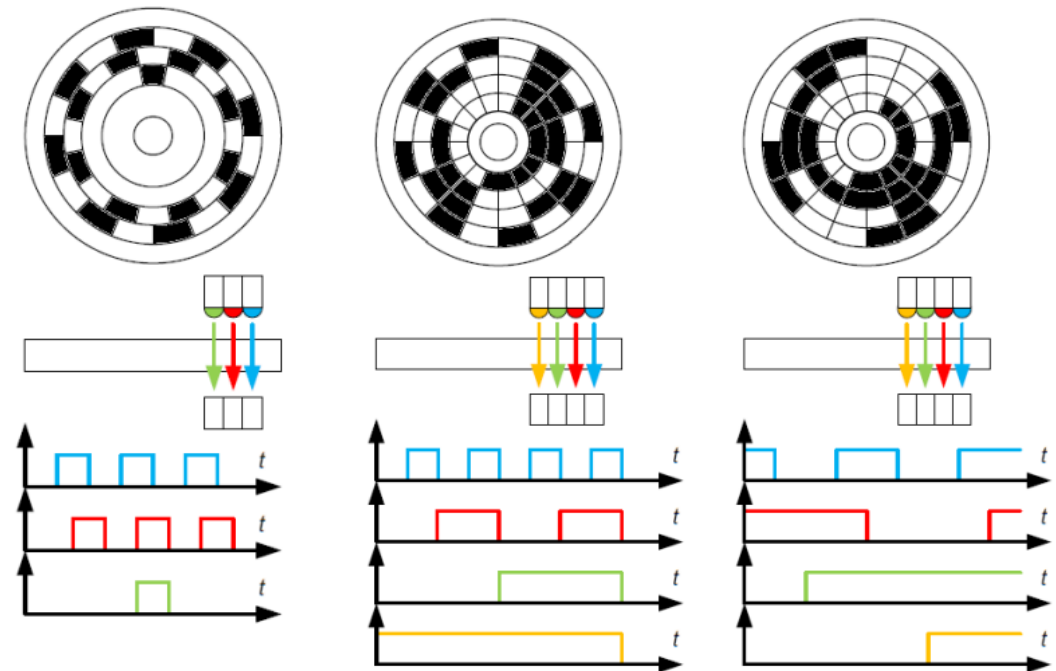
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- Sometimes we need to have the absolute position of the moving part (precise movements, even after a shutdown).
- In older scanners the solution was simple (incremental + switch):
  - Move to one direction on the slide (usually the same direction)
  - UNTIL EndSwitch is pushed
  - You are at the 0 point, You can start to count the steps You made



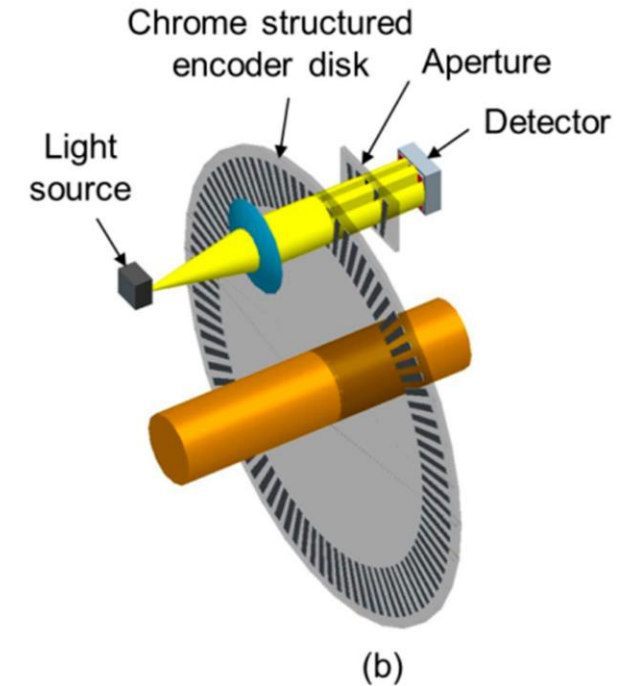
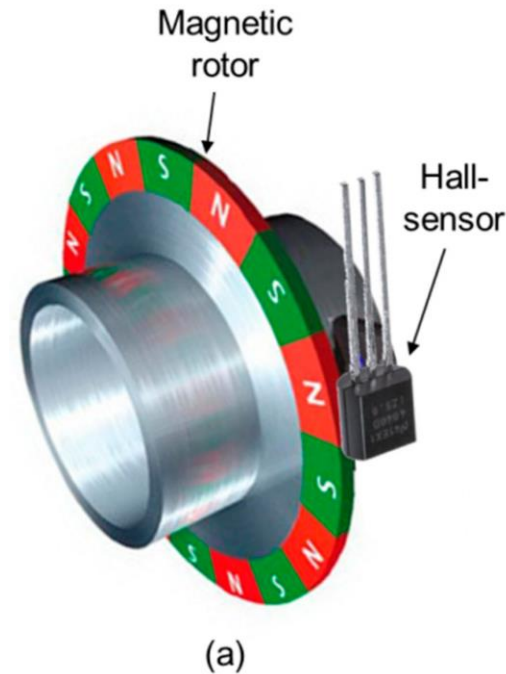
# Optical encoders (cont.) – Absolute encoders

- More expensive
- 3 circle is needed (at least)
- We can use binary or Gray-coded
- Gray-code = at any given time only one bit will change



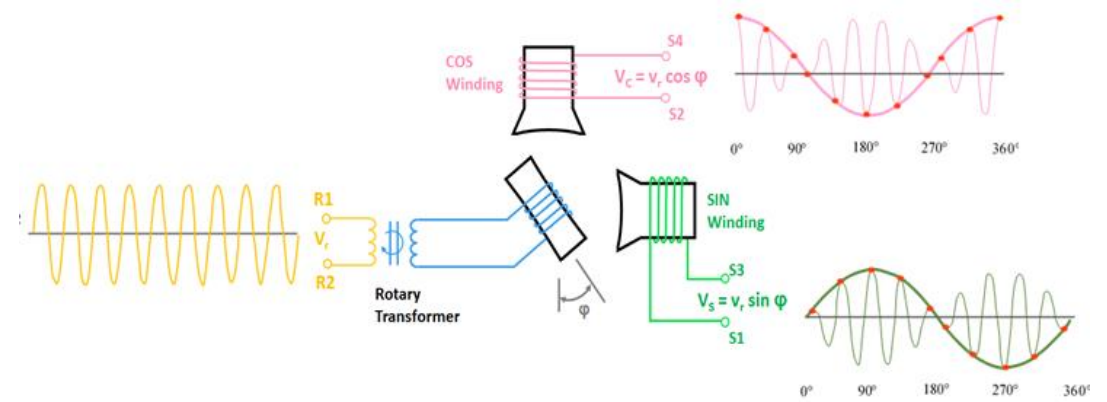
# Hall-sensors

- We can use magnets + Hall sensor instead of optocoupler



# Resolver

- LVDT's pair for rotational movements
- Output: Absolute rotational position
- Originally for military applications were developed (robustness in harsh conditions)
- 2 stationary windings (sin and cos)
- Rotary transformer



From the ratio of the measured voltages and their phase we can calculate the angle of the rotating part.