CLASS-11 CHAPTER-10 STRAIGHT LINES

Excercise 10.4

Q2. Find the values of θ and p, if the equation $x\cos\theta + y\sin\theta = p$ is the normal form of the line $\sqrt{3}x + y + 2 = 0$.

Solution:

From the given line equation normal vector is given by:

$$\mathbf{n} = \begin{pmatrix} -\sqrt{3} \\ 1 \end{pmatrix} \tag{1}$$

$$c = -2 \tag{2}$$

Slope of normal form is given by:

$$\tan \theta = -\frac{1}{m} = \frac{1}{\sqrt{3}}$$

$$\implies \theta = 210^{\circ}$$
(3)

$$\implies \theta = 210^{\circ}$$
 (4)

The perpendicular distance p is given by:

$$p = \frac{|c|}{\|\mathbf{n}\|} = \frac{2}{2} = 1 \tag{5}$$

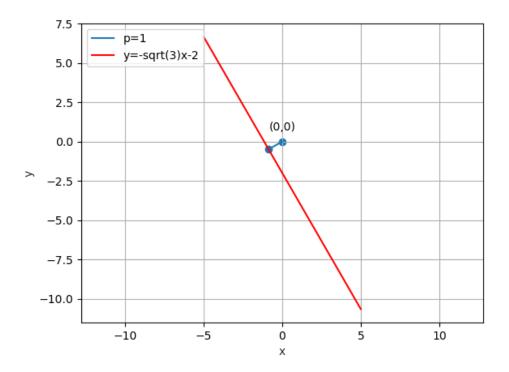


Figure 1: