CHAPTER-7 COORDINATE GEOMETRY

Excercise 7.2

1. Find the coordinates of the point which divides the join (-1,7) and (4,-3) in the ratio 2:3 :

Solution:

The coordinates and ratio are given as

$$\mathbf{P} = \begin{pmatrix} -1\\7 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 4\\-3 \end{pmatrix}, n = \frac{3}{2} \tag{1}$$

$$\mathbf{R} = \frac{\mathbf{Q} + n\mathbf{P}}{1 + n} \tag{2}$$

$$\mathbf{R} = \frac{1}{1 + \frac{3}{2}} \left(\begin{pmatrix} 4 \\ -3 \end{pmatrix} + \frac{3}{2} \begin{pmatrix} -1 \\ 7 \end{pmatrix} \right) \tag{3}$$

$$\mathbf{R} = \frac{1}{1 + \frac{3}{2}} \left(\begin{pmatrix} 4 \\ -3 \end{pmatrix} + \begin{pmatrix} \frac{-3}{2} \\ \frac{21}{2} \end{pmatrix} \right) \tag{4}$$

$$\mathbf{R} = \frac{1}{\frac{5}{2}} \begin{pmatrix} \frac{5}{2} \\ \frac{15}{2} \end{pmatrix} \tag{5}$$

$$\mathbf{R} = \frac{2}{5} \begin{pmatrix} \frac{5}{2} \\ \frac{15}{2} \end{pmatrix} \tag{6}$$

$$\mathbf{R} = \begin{pmatrix} 1 \\ \frac{15}{5} \end{pmatrix} \tag{7}$$

$$\mathbf{R} = \begin{pmatrix} 1\\3 \end{pmatrix} \tag{8}$$

Hence, the coordinates of the point which divides the join is $R\left(1,3\right)$ also shown in Figure:1

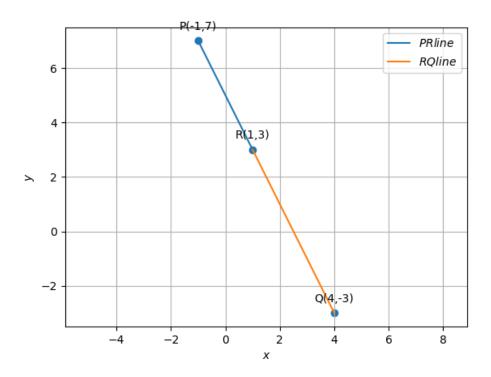


Figure 1: