

CHAPTER-7
COORDINATE GEOMETRY

Exercise 7.2

Q2. Find a relation between x and y if the points (x, y) , $(1, 2)$ and $(7, 0)$ are collinear.

Solution:

The coordinates are given as

$$\mathbf{A} = \begin{pmatrix} x \\ y \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 7 \\ 0 \end{pmatrix} \quad (1)$$

For collinear, $ar(ABC)$ should be equal to zero

$$ar(ABC) = \frac{1}{2} \|(\mathbf{A} - \mathbf{B}) \times (\mathbf{A} - \mathbf{C})\| = 0 \quad (2)$$

$$\mathbf{A} - \mathbf{B} = \begin{pmatrix} x \\ y \end{pmatrix} - \begin{pmatrix} 1 \\ 2 \end{pmatrix} = \begin{pmatrix} x - 1 \\ y - 2 \end{pmatrix} \quad (3)$$

$$\mathbf{A} - \mathbf{C} = \begin{pmatrix} x \\ y \end{pmatrix} - \begin{pmatrix} 7 \\ 0 \end{pmatrix} = \begin{pmatrix} x - 7 \\ y \end{pmatrix} \quad (4)$$

$$= \frac{1}{2} \begin{vmatrix} x - 1 & x - 7 \\ y - 2 & y \end{vmatrix} = 0 \quad (5)$$

$$\implies x + 3y - 7 = 0 \quad (6)$$

Suppose, if $x=-2, y=3$, then area of triangle ABC is equal to zero which is collinear as shown in Figure:1

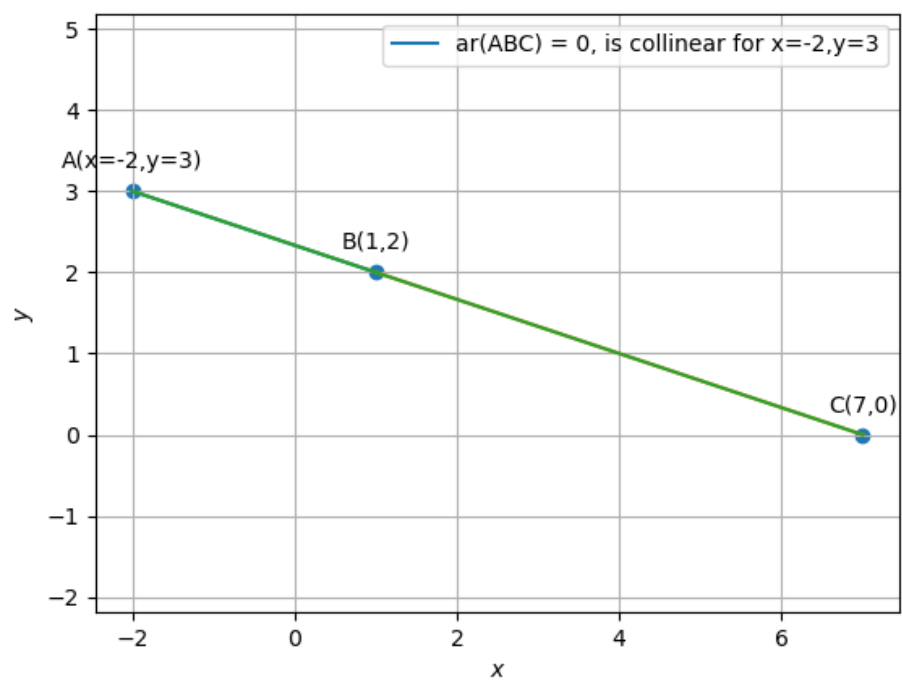


Figure 1: