CHAPTER-7 COORDINATE GEOMETRY

Excercise 7.2

1. Find the coordinates of the point which divides the join (-1,7) and (4,-3) in the ratio 2:3 :

Solution:

The coordinates are given as

$$\mathbf{P} = \begin{pmatrix} -1\\7 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 4\\-3 \end{pmatrix}, n = \frac{3}{2} \tag{1}$$

$$\mathbf{R} = \frac{\mathbf{Q} + n\mathbf{P}}{1 + n} \tag{2}$$

$$\mathbf{R} = \frac{\binom{4}{-3} + \frac{3}{2} \binom{-1}{7}}{1 + \frac{3}{2}} \tag{3}$$

$$\mathbf{R} = \frac{\binom{4}{-3} + \binom{-5}{7}}{1 + \frac{3}{2}} \tag{4}$$

$$\mathbf{R} = \frac{\binom{4}{-3} + \frac{1}{2} \binom{-3}{21}}{1 + \frac{3}{2}} \tag{5}$$

$$\mathbf{R} = \frac{\frac{1}{2} \begin{pmatrix} 5\\15 \end{pmatrix}}{\frac{5}{2}} \tag{6}$$

$$\mathbf{R} = \frac{1}{2} \cdot \frac{2}{5} \begin{pmatrix} 5\\15 \end{pmatrix} \tag{7}$$

$$\mathbf{R} = \frac{1}{5} \begin{pmatrix} 5\\15 \end{pmatrix} \tag{8}$$

$$\mathbf{R} = \begin{pmatrix} 1\\3 \end{pmatrix} \tag{9}$$

Hence, the coordinates of the point which divides the join is $R\left(1,3\right)$ also shown in Figure:1

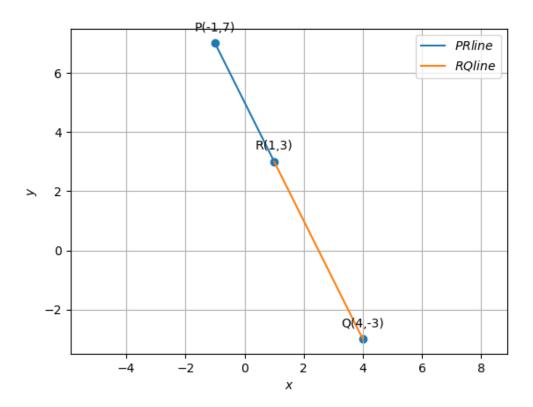


Figure 1: