

SYNTAX ANALYSIS = (ROLE OF SYNTACTIC ANALYZER) :-

- Syntax Analyzer is also called as the parser, the parser obtains the stream of tokens from the lexical analyzer.
- And, verifies the tokens syntactically, if the tokens are syntactically correct then it will generate a parse tree.

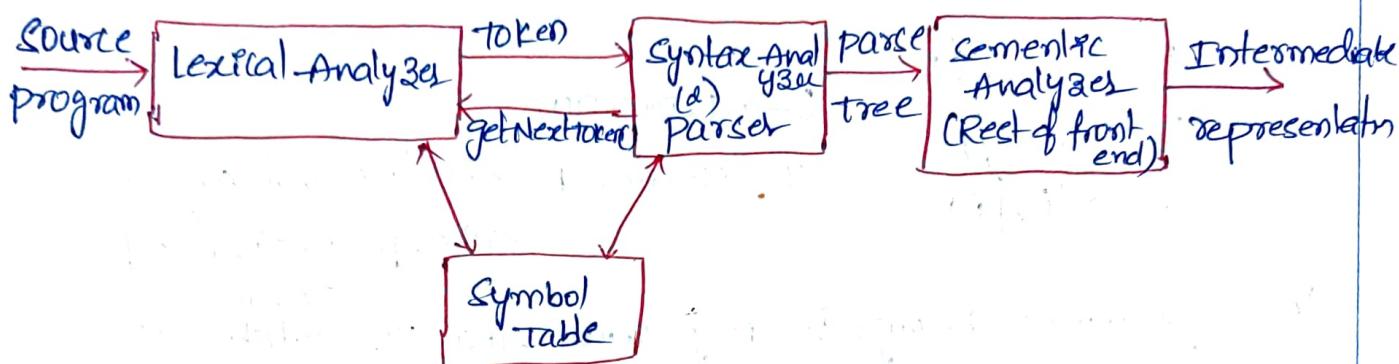
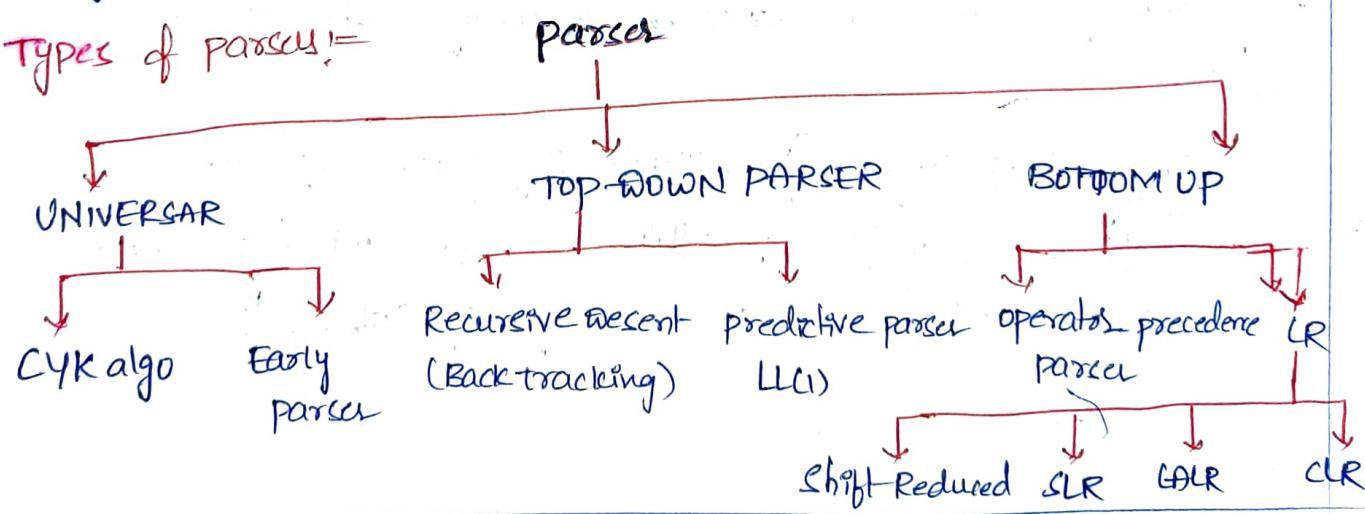


Fig:- position of parser in compiler model.

- The main function of parser is to check the syntactic structure of ip code, if the given ip code is out of syntactic errors then it will generate a parse tree.
- If ip code consists of syntax errors, then the parser reports an error to user, now, the user will correct it. It is responsibility of the user to correct those errors.
- Symbol Table communicate with both Lexical Analyzer & Syntax Analyzer for the token information.

Types of Parsers :-



- In top-down parser construct the parse tree from top(root) to the bottom (leaves)
- Bottom-up parser construct the parse tree from leaves to root (starts from IP symbol and reduced to starting state)

Representative Grammars:

Associativity and precedence are captured in the following grammar

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid id$$

$E \rightarrow Expression$

$T \rightarrow Term$, $F \rightarrow Factors$ that can be either parenthesized expression

These grammars belong to LR grammars that are suitable for bottom-up parsing. This grammar cannot be used for top-down parsing

The following non-left-recursive grammar will be used for top-down parsing

$$E \rightarrow TE^I$$

$$E^I \rightarrow +TE^I \mid \epsilon$$

$$T \rightarrow FT^I$$

$$T^I \rightarrow *FT^I \mid \epsilon$$

$$F \rightarrow (E) \mid id$$

Syntax Error Handling:

Programming errors can occur at many different levels.

Lexical Errors:

→ Include misspelling of identifiers, keywords, & operators

e.g. ~~identific~~ ellipsesize instead of ellipsesize and missing quotes

about text intended as a string. (e.g. "String");

(2)

Syntax Errors := Misplaced semicolon(;), extra or missing braces {},].

Eg := appearance of case statement without an enclosing switch.

Semantic Errors := Eg := $(a + (b *)) \rightarrow$ missing parenthesis.

→ Type mismatch b/w operators and operands.

Eg: ① $2 + a[i] \rightarrow$ type mismatch.

② The return of a value in Java method with result type void.

logical Errors :=

→ errors can be anything from incorrect reasoning on the part of programming.

Eg := In "c" - the assignment operator instead of comparison operator.

if ($C = A$) X if ($C == A$) ✓

Error Handles in parser :=

- should report the presence of errors clearly and accurately.
- should recover from each error quickly enough to detect the subsequent errors.
- should not slow down the processing of remaining program.

Errors Recovery Strategies :=

(i) Panic Mode Recovery :=

Eg := int a, b; }
printf(" ");

→ The parser discards I/P symbols at a time until one of a designated set of synchronizing tokens is found.

→ The synchronizing tokens are delimiters ; ; or }

→ It is simple to implement & does not goto a loop

(ii) phrase level Recovery :=

→ The parser performs local correction on remaining I/P when the error is discovered.

→ The parser replaces the prefix of the remaining I/P by some strings that allows the parser to carry on its execution

Eg: = replace a (,) comma by semicolon (;), delete an extra semicolon, insert a missing semicolon (;)

(i) $\text{print}(" ")$, $\rightarrow \text{printf}(" ")$;

disadvantage = error correction is difficult when actual errors occur before the point of detection

(ii) Error production,

\rightarrow common errors that can be encountered, we can augment the grammar for the language with productions that generate erroneous constructs. \rightarrow

\rightarrow use a new grammar for the parser.

(iv) Global correction:

\rightarrow The aim is to make some changes while converting incorrect i/p string to a valid string
 $\& \text{Grammar } G$

- Given an incorrect i/p x , find a parse tree for a related string w (using the given Grammar) such that no of changes (insertion/deletion) required to transform x to w is minimum
- Too costly to implement

(2) CONTEXT FREE GRAMMAR:

Context Free Grammars consists of 4-tuples

$$CFG = (V, T, P, S)$$

- $V \rightarrow$ Set of variables (or) Non-terminals
- $T \rightarrow$ Set of terminals.
- $P \rightarrow$ Set of Production Rules
- $S \rightarrow$ Start symbol.

(i) Non-terminal:

\rightarrow Denotes set of strings.

- Uppercase letters early in alphabet A, B, C, ...
- $S \rightarrow$ start symbol
- E, T, F (Expression - E, Term - T, Factor - F)

(ii) Terminal:

\rightarrow Terminals are the basic symbols from which strings are formed

- TOKEN-name is also called as terminal
- The following are terminal symbols.
 - (a) lowercase letters in the alphabets such as a, b, c,
 - (b) operator symbols such as +, *, ...
 - (c) punctuations (" ", ")", "(", ")" , ":", "...") & digits 0, 1, ..., 9

(iii) Production:

consists of

- (a) A Non terminal called head or left side of the production.
This production defines some of the symbols denoted by the head
- (b) body or right side \rightarrow consisting of zero or more terminals and Non terminals.
- \Rightarrow uppercase letters late in alphabet X, Y, Z represent Grammar symbols either terminals or Non-terminals.

$\rightarrow \alpha, \beta, \gamma \dots$ represent string of grammar symbols

$\rightarrow A$ set of productions $A \rightarrow \alpha_1, A \rightarrow \alpha_2 \rightarrow A\alpha_1\alpha_2$ also written as
head
Product $A \rightarrow \alpha$
Non-Terminal either terminal or Non-terminal (VNT)*

Eg: Consider the grammar

$$E \rightarrow E+E \quad E \rightarrow E*E \quad E \rightarrow I \quad I \rightarrow a$$

$$CFG = (\{E, I\}, \{+, *, a\}, P, S)$$

\Rightarrow derive

Derivation: Derivation is process of applying a sequence of production rules in order to derive a string.

\rightarrow deriving an i/p string from the start symbol of Grammar in one or more steps by replacing the head of the production by ^{the} body of the production.

There are two types of derivation.

(i) Left most derivation (LMD)

(ii) Right most derivation (RMD)

Left most derivation: In each step

we have to expand left-most Non-terminal by one of its production body.

Eg: $E \rightarrow E+E | E*E | -E | (E) | id$

Derive a string $id + id * id$

LMD: $E \xrightarrow{\text{LMD}} E+E (E \rightarrow E+E)$

$E \xrightarrow{\text{Lm}} id + E (E \rightarrow id)$

$E \xrightarrow{\text{Lm}} id + E*E (E \rightarrow E*E)$

$E \xrightarrow{\text{Lm}} id + id * E (E \rightarrow id)$

$E \xrightarrow{\text{Lm}} id + id * id (E \rightarrow id)$

Right most derivation:

\rightarrow here, we have to expand the Right-most non-terminal by

RMD:

$E \xrightarrow{\text{Rm}} E+E (E \rightarrow E+E)$

$E \xrightarrow{\text{Rm}} E+E*E (E \rightarrow E*E)$

$E \xrightarrow{\text{Rm}} E+E*id (E \rightarrow id)$

$E \xrightarrow{\text{Rm}} E+id*id (E \rightarrow id)$

$E \xrightarrow{\text{Rm}} id + id * id (E \rightarrow id)$

Parse tree

→ A Graphical representation of derivation is called parse tree.

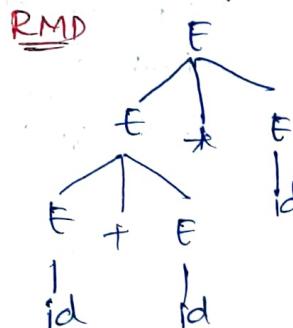
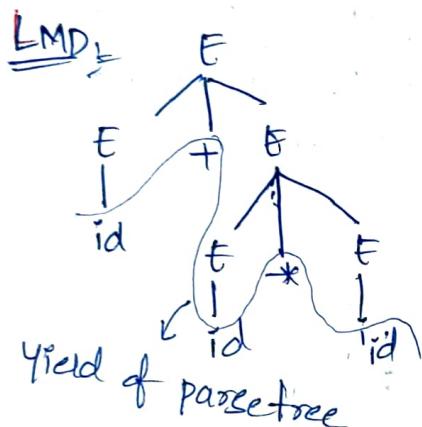
These types of nodes in parse tree

(i) Interior node → are Non terminals

(ii) children node → terminals

→ In parse tree the root node must be start symbol

construct parse tree for i/p string $w = id + id * id$



Ambiguity

($FG \quad G = (V_1, T, P, S)$)

→ If a grammar produces more than one parse-tree, then that grammar is called as ambiguous.

(i) more than one LMD (different)

(ii) more than one RMD (different).

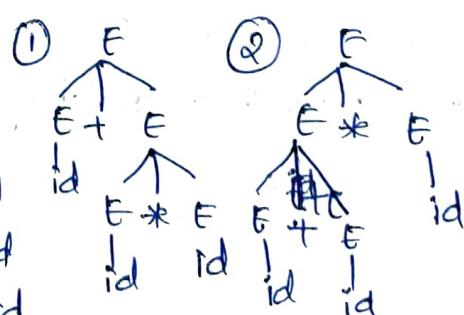
e.g. $E \rightarrow E+E \mid E * E \mid (E) \mid id$ string $w = id + id * id$

LMD1

$$\begin{aligned} E &\Rightarrow E+E \\ &\text{tm} \\ &\Rightarrow id+E \\ &\text{tm} \\ &\Rightarrow id+E*E \\ &\text{tm} \\ &\Rightarrow id+id*E \\ &\text{tm} \\ &\Rightarrow id+id*id. \\ &\text{tm} \end{aligned}$$

RMD1

$$\begin{aligned} E &\Rightarrow E+E \\ &\text{tm} \\ &\Rightarrow E+E*E \\ &\text{tm} \\ &\Rightarrow E+E*id \\ &\text{tm} \\ &\Rightarrow E+id*id \\ &\text{tm} \\ &\Rightarrow id+id*id \end{aligned}$$

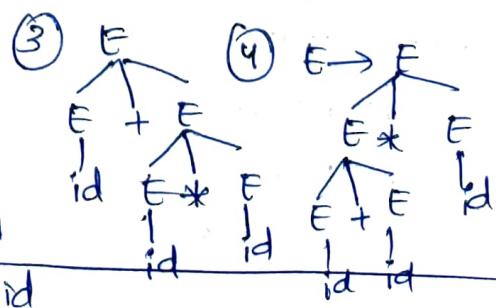


LMD2

$$\begin{aligned} E &\Rightarrow E*E \\ &\Rightarrow E+E*E \\ &\Rightarrow id+E*E \\ &\Rightarrow id+id*E \\ &\Rightarrow id+id*id \end{aligned}$$

RMD2

$$\begin{aligned} E &\Rightarrow E*E \\ &\text{tm} \\ &\Rightarrow E*id \\ &\text{tm} \\ &\Rightarrow E+E*id \\ &\text{tm} \\ &\Rightarrow E+id*id \\ &\text{tm} \\ &\Rightarrow id+id*id \end{aligned}$$



→ For the above string we got 2 LMD & RMD and 2 parse trees

So, the given grammar is ambiguous

→ Top down parser can't handle ambiguous grammar, so we need to convert this grammar into unambiguous grammar.

* While converting ambiguous to unambiguous:

→ The grammars should follow associativity and precedence rules

* , /, +, - → left association (when an ^{operand} has ^{operator} on both sides, the operand should associate with left-side operator)

1, * +, - → precedence order
1 2 3 4

④ WRITING A GRAMMAR:

→ Grammars is used to describe the syntax of programming language.

lexical versus syntactic analysis:

- Separating syntactic structure into smaller and manageable components of lexical and non-lexical parts.
- Lexical rules are simple to understand than grammar.
- We need notations to describe the grammars.
- RE are used to Realtime Examples to make them easy to understand.
- Grammars are used for describing nested structure such as balanced parenthesis, matching begin-end, if-then-else.

Eliminating Ambiguity:

Properties of CFG

1. Ambiguous
2. Left Recursive
3. Left Factoring.

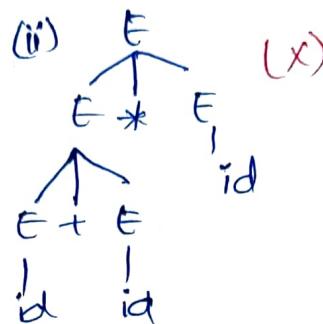
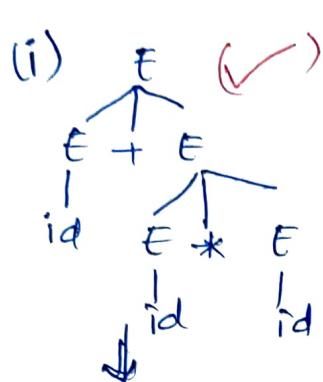
Elimination of ambiguity:-

(Consider CFG) :-

$$\text{Eg}:- E \rightarrow E+E \mid E * E \mid (E) \mid id$$

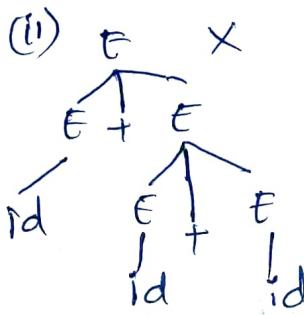
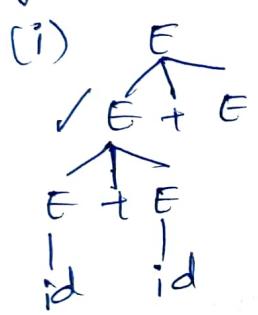
$$w = id + id * id$$

(There are 2 parse trees for string)



→ This is the valid parse tree, because the "*" operator is appeared at bottom of parse, so it is evaluated first.

$$\text{Eg2:- } w = id + id + id$$



→ two factors that are needed to be taken

(1) precedence

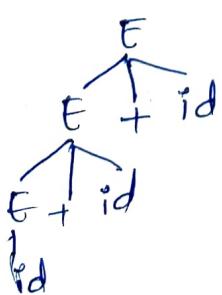
(2) left associativity → to ensure left associativity, we need to convert the grammar into left recursive of RHS

→ left recursive $E \rightarrow E+E$ (the leftmost symbol is equal to the LHS)

* In left recursive, the parse tree can be grown on left side only

$$E \rightarrow E + id \mid id$$

$$id + id + id \Rightarrow (id + id) + id \text{ (left associative)}$$



left associativity can be achieved

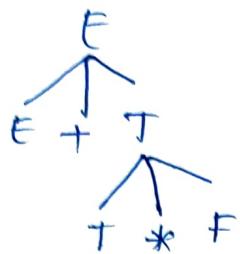
$$(id + id) + id$$

↓
This expression is evaluated first, so that it is valid parse tree.

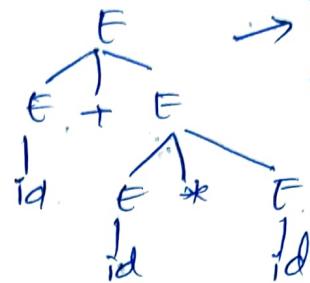
$$E \rightarrow E + T$$

$$T \rightarrow T * F$$

(precedence)

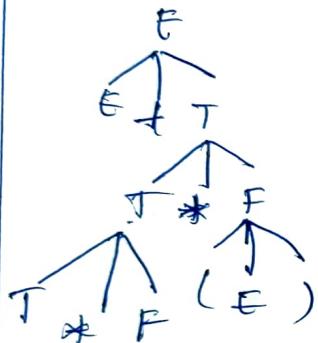
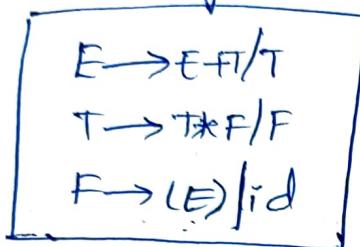


id + (id * id)

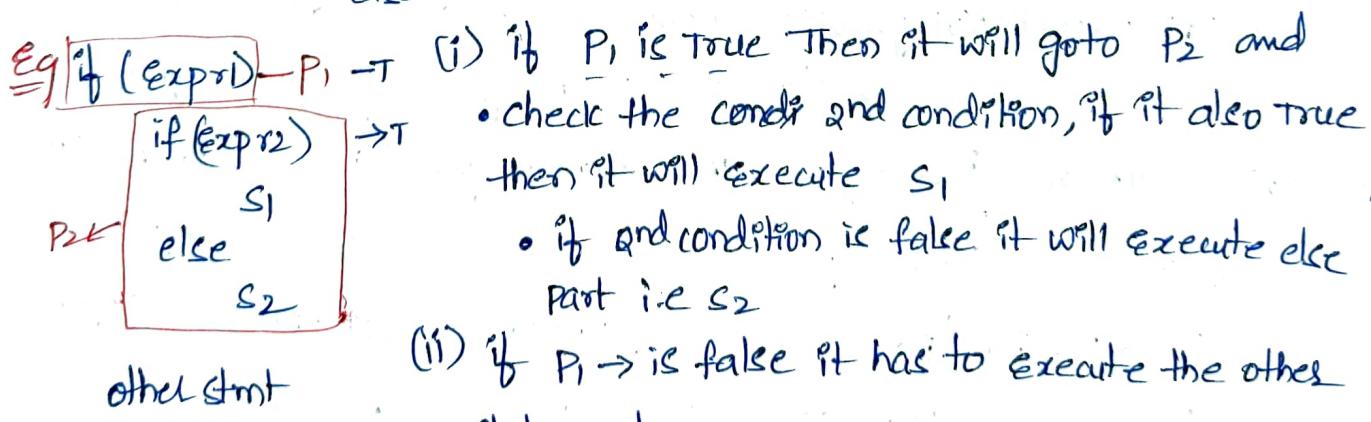


→ highest precedence operation is executing first.

The Final ~~gram~~ unambiguous Grammars



Dangling else: In a program if there are more than one if-stmts then else part is matched with wrong if Stmt, that will lead to wrong results, that is called dangling else.



(iii) But here if P₁ - False then it is executing else part i.e statement 2 it is matching with wrong else.

• Consider the following dangling else grammars.

$\text{stmt} \rightarrow \text{if Expr then stmt}$

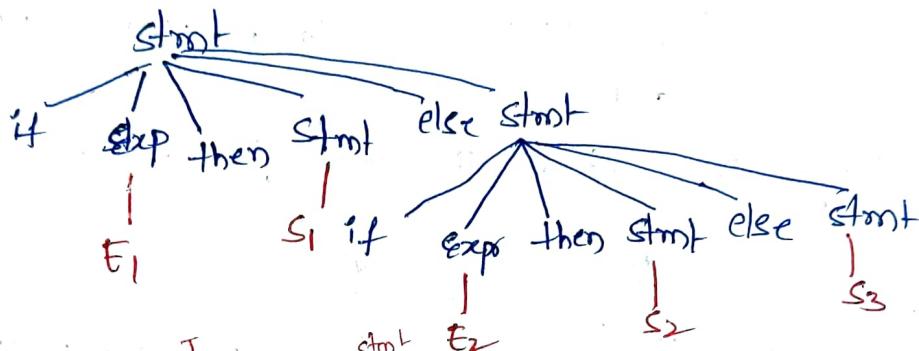
| if Expr then stmt else stmt

| other

• The compound conditional stmt for the above grammar is

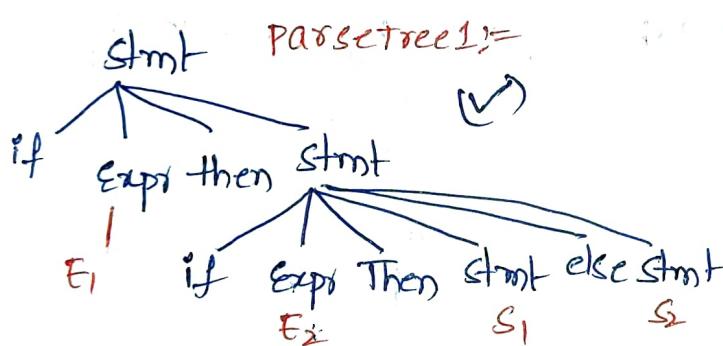
if E_1 , then S_1 [else if E_2 then S_2 else S_3]

• The parse for this stmt

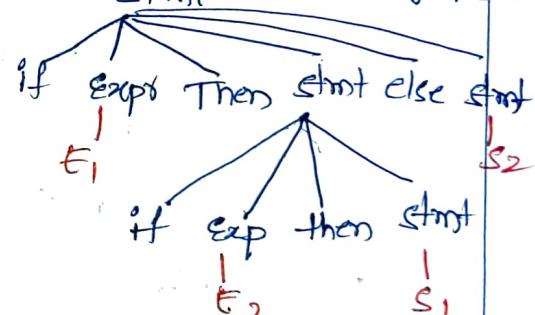


Ex i/p string = if E_1 then [if E_2 then S_1 else S_2]

there exist two parse trees for the given string.



parse tree 2: (X) dangling-else



→ In these two parse trees, in programming language, the 1st parse tree is considered because, match the else statement with closest then. $\boxed{\text{if } E_1 \text{ then } \boxed{\text{if } E_2 \text{ then } S_1 \text{ else } S_2}}$ → matched stmt

→ So, The given Grammars is ambiguous Grammars.

The unambiguous grammar will be.

$\text{stmt} \rightarrow \text{matched stmt} \mid \text{open stmt}$

matched stmt \rightarrow perfect if
open stmt \rightarrow simple if

matched stmt \rightarrow if Expr then matched stmt else matched stmt / other

open stmt \rightarrow if Expr then stmt

| if Expr then matched stmt else open stmt.

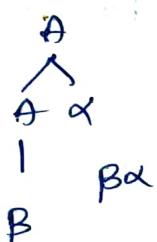
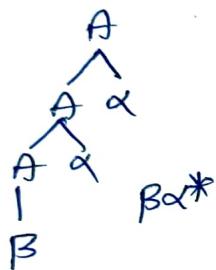
(ii) Elimination of left Recursion:

- A grammar is said to be left recursive if it has a non-terminal A such that there is a derivation $A^+ \Rightarrow A\alpha$ for some string α .
- Top-down parsing methods cannot handle this grammar, so we need to eliminate left recursion.

$A^+ \Rightarrow A\alpha / B$ (left recursive) $\alpha, B \in (VUT)^*$

[if LHS is equal to the leftmost Non-terminal of RHS].

The string derived from the above grammar.



$$\begin{array}{c} A \\ | \\ B \end{array}$$

string(α) = $\beta\alpha^*$

(any production should not contain * symbol)

production $A \rightarrow A\alpha / B$ could be replaced by the following non-left-recursive productions.

$$\begin{aligned} A &\rightarrow BA^1 \\ A^1 &\rightarrow \alpha A^1 / \epsilon \end{aligned}$$

Eg:- $E \rightarrow E + T / T$

$T \rightarrow T * F / F$

$F \rightarrow (E) / id$ (left recursive grammar)

so, we need to eliminate left-recursion from the above grammar

$$(i) \quad \begin{array}{c} E \rightarrow E + T / T \\ | \\ A \quad A \alpha \quad B \end{array}$$

$$\begin{aligned} A &= E \\ \alpha &= +T \\ B &= T \end{aligned}$$

$$\begin{aligned} E &\rightarrow TE^1 \\ E^1 &\rightarrow +TE^1 / \epsilon \end{aligned}$$

(7)

$$(i) T \rightarrow T * F / F$$

$$A \quad A \alpha / B$$

$$T \rightarrow FT$$

$$T^l \rightarrow *FT^l / \epsilon$$

$$\text{eg2: } S \rightarrow \underline{SOSIS} / \underline{01}$$

$$A \quad A \alpha \quad B$$

$$A \rightarrow A \alpha / B$$

$$S \rightarrow \underline{\alpha 1} \quad 01S^l$$

$$S^l \rightarrow OS1SS^l / \epsilon$$

$$(ii) F \rightarrow (E) / id \text{ (Non left recursive)}$$

After eliminating the left recursion
from the grammars

$$E \rightarrow TE^l$$

$$E^l \rightarrow +TE^l / \epsilon$$

$$T \rightarrow FT$$

$$T^l \rightarrow *FT^l / \epsilon$$

$$F \rightarrow (E) / id / \epsilon$$

$$\text{eg3: } S \rightarrow (L) / \epsilon \text{ - No left recursion}$$

$$L \rightarrow L_1 S / S$$

* Elimination of left recursion for multiple production.

$$A \rightarrow A\alpha_1 | A\alpha_2 | \dots | B_1 B_2 \dots$$

$$\boxed{A \rightarrow \beta_1 \alpha^l | \beta_2 \alpha^l}$$

$$\alpha^l \rightarrow \alpha_1 \alpha^l | \alpha_2 \alpha^l | \epsilon \dots$$

$$\text{eg1: } \text{expr} \rightarrow \text{expr} + \text{expr} | \text{expr} * \text{expr} | id$$

$$A \quad A \quad \alpha_1 \quad A \quad \alpha_2 \quad B_1$$

$$\text{expr} \rightarrow id \text{expr}^l$$

$$\text{expr}^l \rightarrow + \text{expr} \text{expr}^l | * \text{expr} \text{expr}^l / \epsilon$$

$$\text{eg2: } S \rightarrow Sx | Ssb | xs | a$$

$$A \quad Ad, A \alpha_2 \quad B_1 \quad B_2$$

$$S \rightarrow xs | as$$

$$S^l \rightarrow xs^l | sb s^l | \epsilon$$

$$\text{eg3: } S \rightarrow Aab$$

$$A \rightarrow Ac | Sd | f$$

$$S \rightarrow Aab \rightarrow \text{No left recursion}$$

$$A \rightarrow Ac | Sd | f$$

(1) Elimination of left factoring

→ A grammar contains production rule in the form

$$A \rightarrow \alpha B_1 | \alpha B_2 | \dots | r_1 | r_2$$

↓

Then that grammar contains left factoring.

→ TD parsers can't handle left factoring if the grammar contains left factoring.

→ we can eliminate the left factoring by replacing with the following production.

$$\begin{array}{l} A \rightarrow \alpha A^1 | f_1 | f_2 \\ A^1 \rightarrow B_1 | B_2 \end{array}$$

$$\text{Eq1: } S \rightarrow iEts | iEts \underset{\alpha}{\cancel{s}} | s \underset{\alpha}{\cancel{B_2}} \underset{f_1}{\cancel{r_1}}$$

(it contains left factoring)

Here, $\alpha = A = S$, $\alpha = iEts$ $B = \epsilon$ $B_2 = es$ $f_1 = s$

$$S \rightarrow iEts s | s$$

$$s \rightarrow \epsilon | es$$

$$\begin{array}{l} \text{Eq3: } B \rightarrow bB | b \\ B \rightarrow bB \\ B \rightarrow B | \epsilon \end{array}$$

$$\begin{array}{l} \text{Eq2: } A \rightarrow \underset{\alpha}{\cancel{a}} \underset{\alpha}{\cancel{B}} | \underset{\alpha}{\cancel{a}} \underset{\alpha}{\cancel{a}} | a \\ \left. \begin{array}{l} B \rightarrow bB | b \\ A \rightarrow aA \\ A^1 \rightarrow AB | A | \epsilon \end{array} \right\} \end{array}$$

$$\text{Eq4: } X \rightarrow \underset{\alpha}{\cancel{x}} + \underset{\alpha}{\cancel{x}} | *x | D$$

$$x \rightarrow xx^1 | D$$

$$x^1 \rightarrow +x | *x$$

$$\begin{array}{l} \text{Eq5: } E \rightarrow T + E / T \\ T \rightarrow \text{int} / \text{int} * T / (E) \end{array}$$

$$\begin{array}{l} T \rightarrow T + E / T \\ \alpha = B_1 = \alpha = B_2 = \epsilon \\ E \rightarrow TE^1 \\ E^1 \rightarrow +E | \epsilon \end{array}$$

$$T \rightarrow \frac{\text{int}}{\alpha} \frac{(\frac{\text{int}}{\alpha} * T)}{B_2} / (E)$$

$$T \rightarrow \text{int} T^1 / (E)$$

$$T^1 \rightarrow \epsilon | *T^1$$

Top-Down Parsing

→ In Top-down parsing, The parse tree is constructed from root node to child node.

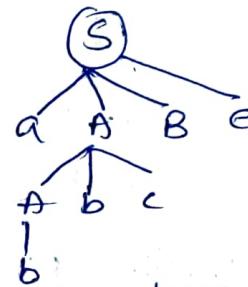
→ Top-down parser uses left-most derivation to derive the input string from the grammar.

→ TDP is starting from start symbol of grammar and reaching the i/p string

Eg:- Grammas is, derive the i/p string $w=abbcde$,

$$\begin{aligned} S &\rightarrow aABe \\ A &\rightarrow Abc/b \\ B &\rightarrow d \end{aligned}$$

LMD:- $S \rightarrow aABe$
 $\quad\quad\quad aAbcBe$
 $\quad\quad\quad abbcBe$
 $\quad\quad\quad abbcde$



→ TDP constructed for the grammar if it is free from

- ambiguity
- left recursion.

→ The problem with TOP parser is if we have more than one alternative for production, which alternative we should use. $\left\{ \begin{array}{l} E \rightarrow E + F / T \rightarrow T * F / F \\ F \rightarrow (E) / id \end{array} \right.$

Eg:- $E \rightarrow TE' \rightarrow$ unambiguous grammar

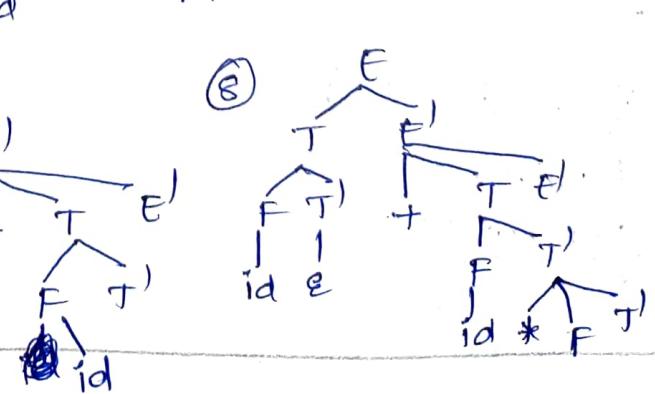
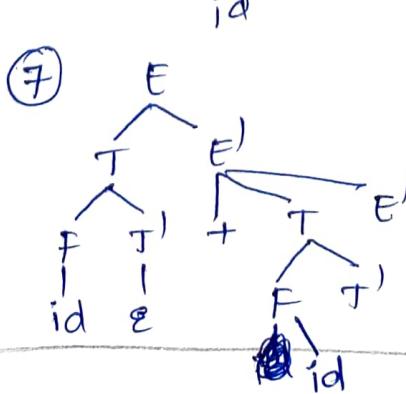
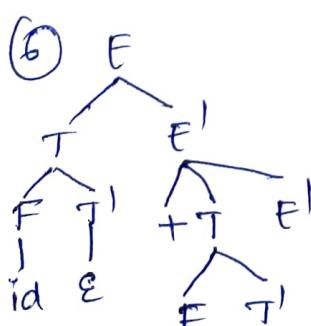
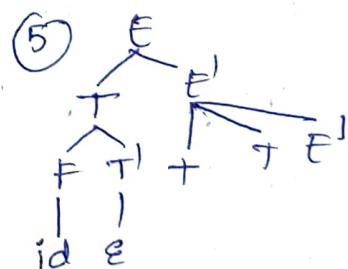
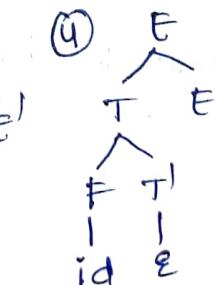
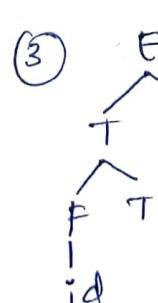
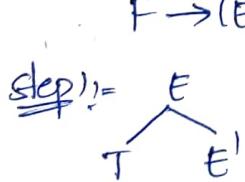
$$E \rightarrow +TE'$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT'/\epsilon$$

$$F \rightarrow (E) / id$$

↳ Derive on i/p string $w=id+id*id$



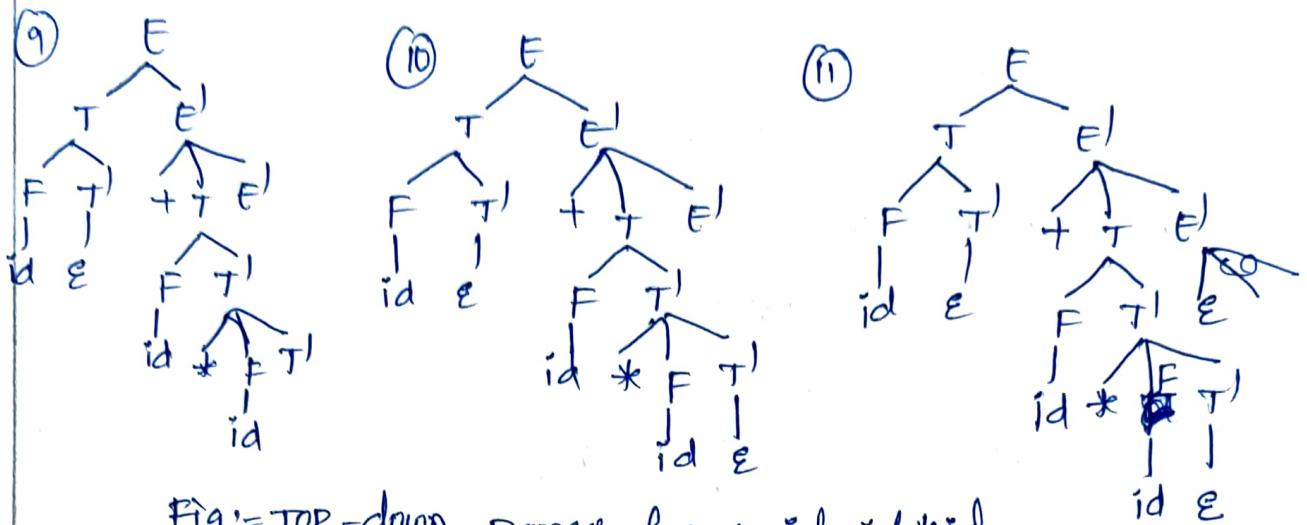


Fig:=TOP-down parses for $w=id+id*id$

i) Recursive-Descent Parsing := (with back tracking)

→ The construction of parse tree starts from root & proceed to child node.

→ Recursion:= A function which is called by itself.

steps for constructing Recursive Descent parser=

(i) If the i/p is a non-terminal, then call corresponding function

(ii) If the i/p is terminal, then compare terminal with i/p symbol
if both are same, then increment input pointer

(iii) If a Non-terminal contains more than one production then
all the production code should be written in the corresponding
function.

$$\text{Eq1: } E \rightarrow iE \quad E \rightarrow +iE \mid \epsilon$$

(In the given grammars we have 2 Nonterminals E, E' , so define
two functions, same as C-long functions)

$E()$

{

```
if (input == 'i')
    input++;
    EPRIME();
}
```

⑨

EPRIME();

```

{
    if (input == '+')
    {
        if (input == '+')
            input++;
        EPRIM();
    }
    else
        return;
}

```

i/p string: i+i

i/p string

Eg2: Grammatical E → TE¹ EL → +TE¹/ε
 T → FT¹ FL → *FT¹/ε F → (E)/ε

```

E()
{
    T();
    EPRIME();
}
EPRIME();
{
    if (input == '+')
    {
        input++;
        T();
        EPRIME();
    }
    else
        return;
}

```

```

T()
{
    F();
    TPRIME();
}
TPRIME();
{
    if (input == '*')
    {
        input++;
        F();
        TPRIME();
    }
    else
        return;
}

```

```

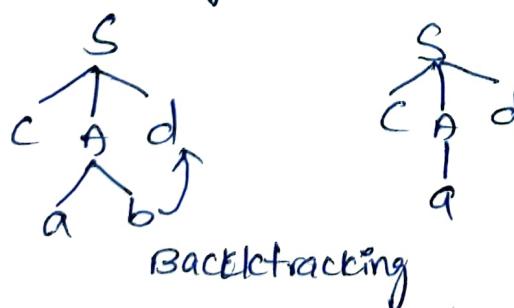
F()
{
    if (input == '(')
    {
        input++;
        E();
        if (input == ')')
            input++;
        else if (input == 'id')
            input++;
    }
}

```

Eg3: S → CAD

A → ab/a

w = i/p string w = cad



If None of the product for ie satisfying the condition then we should check another possibility for "S"

~~input++
EPRIME();~~

{

EPRIME()

{

if (input == '+')

{ input++;
if (input == 'i')

input++;

EPRIME();

else
return;

}

$\frac{P}{D} = \frac{id+id}{id+id}$
~~if $a = b$ then
 $t \rightarrow TE$~~

$E \rightarrow TE | E$

$T \rightarrow FT$

$FT \rightarrow FT | E$

$F \rightarrow (E) | id$

$E()$

$T()$

$EPRIME();$

$EPRIME()$

$EPRIME()$

if (input == '+')
input++

$T()$

$EPRIME();$

{

else
return;

}

$T()$

$F()$

$EPRIME();$

{

if (input == '#')
input++;

$F()$

$EPRIME();$

{

else
return;

}

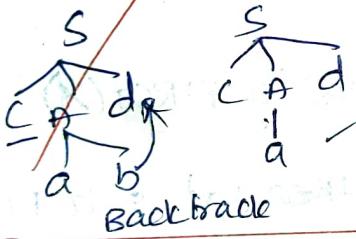
~~F() 10
{
if (input == 'i')
{ input++;
E();
if (input == ')')
input++;
else if (input == 'd')
input++;
}~~

$\frac{P}{D} = \frac{+i\$}{+i\$}$

Eg $S \rightarrow CAD$

$A \rightarrow ab|a$

$w = cad$



(∴ if none of the products for A is satisfying the condition, then we should check another possibility for S)

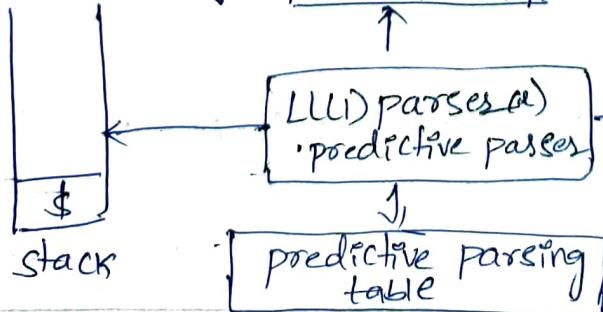
(ii) Predictive Parsing & LL(1) & Non recursive parser :-

LL(1) - means

- It scans the input from left to Right by using

left most derivation.

- $LL(1) \rightarrow 1 - \text{look ahead} - \text{at a time we are reading 1 character at a time}$
Inputting \rightarrow



Steps for constructing LL(1) parser :-

- ① Elimination of left recursion
- ② Elimination of left factoring
- ③ Calculation of FIRST() & FOLLOW()
- ④ Construction of parsing table.

LL(1) parser \rightarrow parsing algorithm

LL(1) parsing table - Data structure which is constructed from the LL(1) grammar

Stack = Data structure used to store the grammar symbols

• Always the bottom of the stack is $\$$

\rightarrow The end of ip buffer is $\$$.

\rightarrow after $\$$, the starting symbol of ip is pushed to the stack.

To construct the parsing table we should compute

two functions. (1) FIRST() (2) FOLLOW()

FIRST(X):

• if X is a terminal then $\text{FIRST}(X) = \{X\}$

• if X is a Non terminal & $X \rightarrow Y_1 Y_2 Y_3 \dots Y_n$ is a production for X .

$$\text{FIRST}(X) = \text{FIRST}(Y_1) \cup$$

If $\text{FIRST}(Y_1)$ contains ϵ add $\text{FIRST}(Y_2)$ to $\text{FIRST}(X)$

If all $\text{FIRST}(Y_1, Y_2, \dots, Y_n)$ contains ϵ then add $\underline{\epsilon}$ to $\text{FIRST}(X)$

FOLLOW(B):

\rightarrow Always the follow() of starting symbol is $\$$.

$$\rightarrow A \rightarrow \alpha B \beta$$

$$\text{Follow}(B) = \text{FIRST}(\beta) \cup$$

If $\text{FIRST}(B)$ contain ϵ or $A \rightarrow \alpha B$ then

add $\text{Follow}(A)$ to $\text{Follow}(B)$

Eg! Given Grammar is

$$E \rightarrow E + T / T \quad \text{left recursion} \quad \left. \begin{array}{l} \text{④ Eliminate left} \\ \text{recursion & left factoring} \end{array} \right\}$$
$$T \rightarrow T * F / F \quad \text{left recursion}$$
$$F \rightarrow (F) / \text{id}$$
$$\text{from these 2 products}$$

$E \rightarrow TE'$ $E' \rightarrow +TE' / \epsilon$ $T \rightarrow FT'$ $T' \rightarrow *FT' / \epsilon$ $F \rightarrow (E) / id$

$\text{FIRST}(E) = \text{FIRST}(T) = \text{FIRST}(F) = \{ \text{, } \text{id} \}$

- $\text{FIRST}(E') = \{ +, \epsilon \}$

- $\text{FIRST}(T) = \text{FIRST}(F) = \{ (, \text{id}) \}$

- $\text{FIRST}(T') = \{ *, \epsilon \}$

$\rightarrow \underline{\text{Follow}(E)} = \{ \text{, } \text{id} \}, \text{Follow}$
 $\downarrow \qquad \qquad \qquad F \rightarrow (E) / id$

$\text{Follow}(E) = \{ \$, \text{FIRST}(T) \} = \{ \$, (, \text{id}) \}$

$\underline{\text{Follow}(E')} = \{ \text{Follow}(E) + \text{Follow}(E') \}$
 $E \rightarrow TE' \qquad \qquad \qquad = \{ \$,) \}$
 $E' \rightarrow +TE' / \epsilon$

$\underline{\text{Follow}(T)} = \{ \text{Follow}(E) \}$

$E \rightarrow TE' \qquad \qquad \qquad \text{Follow}(T) = \text{FIRST}(E') + \text{Follow}(E)$
 $E' \rightarrow +TE' / \epsilon \qquad \qquad \qquad = \{ +, \$,) \}$

$\underline{\text{Follow}(T')} \rightarrow [\text{Follow}(T) + \text{Follow}(T')]$

$T \rightarrow FT' \qquad \qquad \rightarrow \{ +, \$,) \}$
 $T' \rightarrow *FT' / \epsilon$

$\underline{\text{Follow}(F)} = \text{Follow}(T) + \text{FIRST}(T) + \text{Follow}(T)$

$T \rightarrow FT' \qquad \qquad \qquad = \{ *, +, \$,) \}$
 $T' \rightarrow *FT' / \epsilon$

(L1(1))
predictive parsing table :-

	id	+	*	()	\$
E	$E \rightarrow TE^1$			$E \rightarrow TE^1$		
E'		$E^1 \rightarrow +TE^1$			$E^1 \rightarrow e$	$E^1 \rightarrow e$
T	$T \rightarrow FT^1$				$T \rightarrow FT^1$	
T'		$T^1 \rightarrow e$	$T^1 \rightarrow *FT^1$		$T^1 \rightarrow e$	$T^1 \rightarrow e$
F	$F \rightarrow id$				$F \rightarrow (E)$	

$W = id + id$

Stack	Input	Action	
$E \$$	$\underline{id} + id \$$	$E \rightarrow TE^1$	The S/P is parsed
$TE^1 \$$	$\underline{id} + id \$$	$T \rightarrow FT^1$	$Eq2: S \rightarrow (L) / q$ $L \rightarrow L, S / S$
$TE^1 E^1 \$$	$\underline{id} + id \$$	$F \rightarrow id$	$W = (a)$
$\underline{id} T^1 E^1 \$$	$\underline{id} + id \$$		$Eq3: S \rightarrow aAB bA\epsilon$
$T^1 E^1 \$$	$+ id \$$	$T^1 \rightarrow e$	$A \rightarrow aAb \epsilon$
$e E^1 \$$	$+ id \$$		$B \rightarrow bB \epsilon$
$E^1 \$$	$\pm id \$$	$E^1 \rightarrow +TE^1$	$W = "aabbb"$
$*TE^1 \$$	$\cancel{*} id \$$	$T \rightarrow FT^1$	$S \rightarrow iETs ietses q$
$FT^1 E^1 \$$	$\underline{id} \$$	$F \rightarrow id$	$E \rightarrow b$ (Non-LL(1))
$\cancel{i} T^1 E^1 \$$	$\cancel{id} \$$	$T^1 \rightarrow e$	$Eq4: S \rightarrow AaB cbB bq$
$e E^1 \$$	$\$$	$E^1 \rightarrow e$	$A \rightarrow da BC$
$\underline{\$}$	$\$$	accepted	$B \rightarrow g \epsilon$ $C \rightarrow h \epsilon$

Bottom-up parser :-

→ Bottom-up parsers construct parse tree from child (bottom) node to root node (top).

→ Bottom up parsers use RMD, i.e. Reverse order.

→ In bottom-up parser the ^{part of} "reducing" I/P string w to start symbol of grammar

$$\text{eg. } S \rightarrow aABe$$

$$A \rightarrow Abc/b$$

$$B \rightarrow d$$

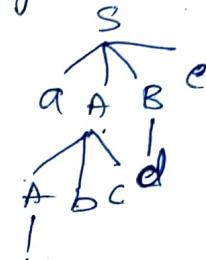
Input string $w = abbcde$

$$a\cancel{A}bcde \quad (A \rightarrow b)$$

$$a\cancel{A}de \quad (A \rightarrow Abc)$$

$$a\cancel{A}Be \quad (B \rightarrow d)$$

$$S \quad (S \rightarrow a\cancel{A}Be)$$



$$S \rightarrow a\cancel{A}Be$$

$$\rightarrow a\cancel{A}de$$

$$\rightarrow a\cancel{A}bcde$$

$$\rightarrow abbcde$$

$$\text{eg. } E \rightarrow ETT/T$$

$$E \rightarrow T*T/F/F$$

$$F \rightarrow (E)/id$$

$$w = id * id$$

$$id * id \quad (F \rightarrow id)$$

$$F * id \quad (T \rightarrow id)$$

$$T * id \quad (T \rightarrow id)$$

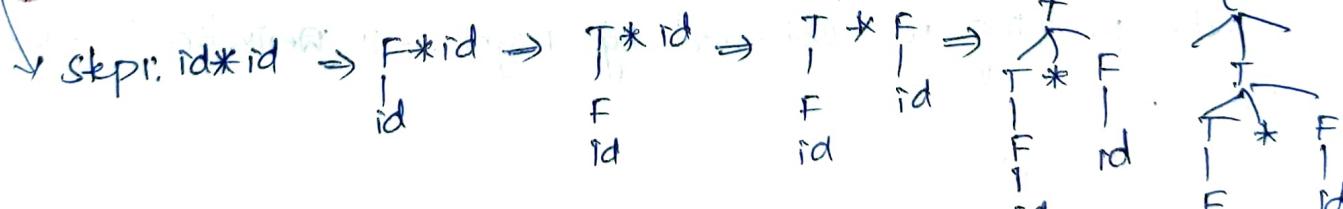
$$\cancel{E * id} \quad T * id \quad (F \rightarrow id)$$

$$T * F \quad (F \rightarrow T * F)$$

$$T \quad (E \rightarrow ST)$$

$$E$$

→ The problem with Bottom-up parser is when to reduce the part to production.



Handle & Handle pruning :-

Handle: Handle is a substring, which matches with right side of production.

→ if Handle matches with the right side of production, then it is replaced with left hand side Non-terminal

Eg1: $S \rightarrow aABC$ $w = abcd$
 $A \rightarrow Abc/b$
 $B \rightarrow d$

Right sentential form	Handle	Reducing production
<u>abbcde</u>	b	$B \rightarrow b$
<u>abcde</u>	Abc	$A \rightarrow Abc$
<u>aAde</u>	d	$B \rightarrow d$
<u>aABC</u>	aABC	$S \rightarrow aABC$
<u>s</u>		

Handles during parse of $id_1 * id_2$

Eg2: $E \rightarrow E+T/T$ $w = id_1 * id_2$
 $T \rightarrow T * F/F$
 $F \rightarrow (E)id$

Right sentential form	Handle	Reducing production
<u>id_1 * id_1</u>	$\oplus id$	$F \rightarrow id$
<u>F * id</u>	F	$F \rightarrow F$
<u>T * id</u>	id	$T \rightarrow F \rightarrow id$
<u>T * F</u>	$T * F$	$T \rightarrow T * F$
<u>T</u>	T	$E \rightarrow T$

→ Handle pruning is obtained by Right most derivation in reverse order.

(f) Shift-Reduce parser:

→ Shift-Reduce parser use two data structures ① Stack ② i/p buffer

① Stack - is used to store the grammar symbol

② Inputbuffer - holds the i/p string to be parsed

Stack	Input string
\$	w\$

Actions of shift-Reduce parser:

1. Shift — shift the next I/p symbol onto the top of the stack.
2. Reduce — If the top of stack is matched with Right side of production, then it is reduced to corresponding non-terminal.
3. Accept — successful completion of parsing
4. Error — discovers a ^{syntax} error and call error recovery methods

Eg :- $E \rightarrow E + T / T$ $w = id * id$
 $T \rightarrow T * F / F$
 $F \rightarrow (E) / id$

Frg :- configuration of shift-Reduce parser on input $id * id$

Stack	Input Buffer	Action
\$	<u>$id * id$</u> \$	shift
\$ <u>id</u>	* id \$	Reduce by $F \rightarrow id$
\$ F	* id \$	Reduce $F \rightarrow F$
\$ T	* id \$	shift
\$ $T *$	id \$	shift
\$ <u>$T * id$</u>	\$	Reduce $F \rightarrow id$
\$ $T * F$	\$	Reduce $T \rightarrow T * F$
\$ T	\$	Reduce $E \rightarrow T$
\$ E	\$	Accepted

conflicts during shift-Reduce parsing

- (1) Shift-Reduce conflict : cannot decide whether to shift or to reduce
- (2) Reduce-reduce conflict :- if the ^{two} productions have same handle (substring),

(4)

Shift-Reduce

Eg 2: $S \rightarrow (L) \cdot a$

$L \rightarrow Ls / S$ Parse the string $(a, (a)a)$ using SR-Parse

Stack	I/P Buffers	pausing Action
\$	$((a, (a)a))\$$	shift
$\$ (a$	$a, (a)a)\$$	shift
$\$ (a$	$, (a)a)\$$	Reduce $S \rightarrow a$
$\$ (S$	$, (a)a)\$$	$L \rightarrow S$ Reduce
$\$ (L$	$, (a)a)\$$	shift
$\$ (L$	$(a)a)\$$	shift
$\$ (L C$	$a, a)\$$	shift
$\$ (L, (a$	$, a)\$$	Reduce $S \rightarrow a$
$\$ (L, (S$	$, a)\$$	shift Reduce $L \rightarrow S$
$\$ (L, (L$	$, a)\$$	shift
$\$ (L, (L, a$	$)\$$	Reduce $S \rightarrow a$
$\$ (L, (L, S$	$)\$$	Reduce $L \rightarrow L, S$
$\$ (L, (L$	$)\$$	shift
$\$ (L, (L$	$)\$$	Reduce $S \rightarrow (L)$
$\$ (L, S$	$)\$$	Reduce $L \rightarrow L, S$
$\$ (L$	$)\$$	shift
$\$ (L)$	$\$$	Reduce $S \rightarrow (L)$
$\$ S$	$\$$	Accept