

# Lasers and Holography

## INTRODUCTION

In the previous chapters, interesting phenomena of interference and diffraction of light including its polarisation have been investigated in detail. It was discussed that the interference has scientific as well as engineering applications. The concept of interference is applied to testing the surface quality of optical components and this led to the development of flatness interferometers. An exciting use of the concept of interference is made in the preparation of nonreflecting or antireflecting coatings that are applied to surfaces of lenses (for example, eye glass lenses) and other optical devices for reducing the reflections and hence in improving the efficiency of the system like telescope. However, you would have learnt that in order to realise the above mentioned phenomena in an efficient way there is a need of using the coherent and monochromatic sources as the phase of incoherent source (light) varies randomly with time and position. This need of monochromatic and coherent sources contributed to the birth of a special type of device that amplifies light and produces a high intense and highly directional beam which mostly has a very pure wavelength. This device is called LASER. Lasers are available with power ranging roughly from  $1 \text{ mW}$  ( $= 10^{-3} \text{ W}$ ) to  $10^6 \text{ PW}$  ( $1 \text{ PW} = 10^{15} \text{ W}$ ) and with frequency ranging from  $100 \text{ GHz}$  ( $1 \text{ GHz} = 10^9 \text{ Hz}$ ) to  $100 \text{ PHz}$ . Now a days the lasers with pulse duration as short as  $\sim 1 \text{ fs}$  ( $\sim 10^{-15} \text{ s}$ ) are available with their pulse energies as high as  $10 \text{ J}$ .

The name LASER is an acronym of Light Amplification by Stimulated Emission of Radiation. The immediate originator to the LASER is the MASER, formerly acronym of Microwave Amplification by Stimulated Emission of Radiation. Since the techniques have been extended to the infrared and optical regions, it has now come to stand for Molecular rather than Microwave amplification. A laser uses some processes that amplify light signals. These processes mainly include stimulated emission and optical feedback provided by mirror. The stimulated emission takes place in amplifying medium contained by the laser. The application of set of mirrors is to feed the light back to the amplifying medium so that the developed beam is grown continuously. The key concept for realisation of the laser operation is the principle of coherence accompanying stimulated emission.



In thermal equilibrium at temperature  $T$ , the absorption and emission probabilities are equal and thus, we can write

$$N_i P_{in} = N_j P_{out}$$

$$N_i P_{in}(v) = N_j [A_{ji} + B_{ji} u(v)]$$

$$\text{or } u(v) = \frac{N_j A_{ji}}{N_i B_{ji} - N_j B_{ji}}$$

$$\text{or } u(v) = \frac{\Lambda_{ji}}{B_{ji} (N_i/N_j) (B_{ji}/B_{ii}) - 1} \quad (\text{vii})$$

But according to Einstein

$$B_{ji} = B_{ii}$$

Then from Eq. (viii) and (ix), we get

$$u(v) = \frac{\Lambda_{ji}}{B_{ii} (N_i/N_j) - 1} \quad (\text{x})$$

According to Boltzmann's law, the distribution of atoms among the energy states  $E_1$  and  $E_2$  at the thermal equilibrium at temperature  $T$  is given by

$$\frac{N_1}{N_2} = \frac{e^{-\epsilon_1/kT}}{e^{-\epsilon_2/kT}} = e^{(\epsilon_2 - \epsilon_1)/kT} \quad (\text{xii})$$

$$\text{or } \frac{N_1}{N_2} = e^{\Delta E/kT} \quad (\text{xiii})$$

$$u(v) = \frac{\Lambda_{ji}}{B_{ii} e^{\Delta E/kT} - 1} \quad (\text{xiv})$$

Planck's radiation formula yields the energy density of radiation  $u(v)$  as

$$u(v) = \frac{8\pi h v^3}{c^5} \frac{1}{e^{\Delta E/kT} - 1} \quad (\text{xv})$$

Comparing Eq. (xiii) and (xv), we get

$$\frac{\Lambda_{ji}}{B_{ii}} = \frac{8\pi h v^3}{c^5}$$

Equation (xv) gives the relation between the probabilities of spontaneous and stimulated emissions. This is also known as the relation between the Einstein's coefficients  $A$  and  $B$ .

### 4.3 CHARACTERISTICS OF LASER LIGHT

As discussed, laser radiation is achieved by the process of stimulated emission and the laser beam is highly intense and directional. This radiation of a very pure frequency has the following main characteristics.

(i) **Coherent:** In simple words, the meaning of coherent is highly ordered. The word coherent comes from another word *Cohere* which has the meaning to stick together. In fact, different parts of the laser beam have a definite relationship with each other. This coherence is described in terms of temporal coherence (coherence in time) and spatial coherence (coherence in space) (Fig. 4.5) which are required to produce high quality interference.

Ordinary light is not coherent because it comes from independent atoms which emit on the time scale of  $10^{-9}$  seconds. A train of incoherent photons is shown in (Fig. 4.6) from which it is clear that these photons are not in order, i.e., they do not have a definite relationship with each other. However, a degree of coherence can be found in sources like the mercury green line, but their coherence does not approach that of a laser.

(ii) **Monochromatic:** The simple meaning of this word is that it is pure in colour or wavelength. The light from a laser typically comes from one atomic transition with a single precise wavelength. So the laser light has a single spectral colour and is almost the purest monochromatic light available. It means the laser light is not exactly monochromatic, but it has a high degree of monochromaticity. The deviation from monochromaticity is due to the Doppler effect of the moving atoms or molecules from which the radiation originate.

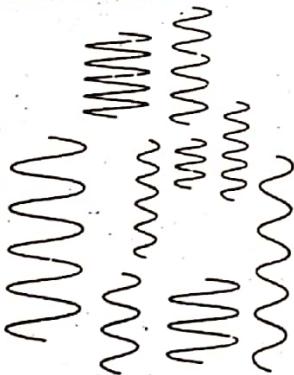
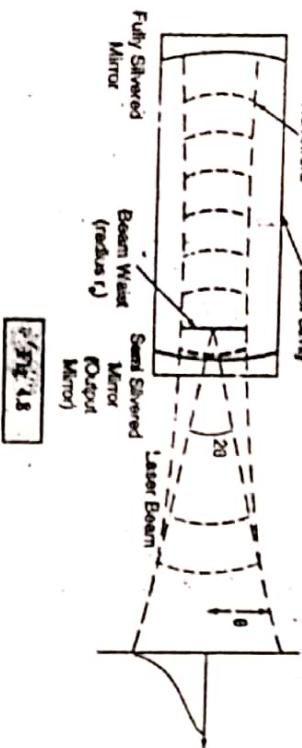


Fig. 4.5

(iii) **Collimated:** Collimated means it does not spread out much. The light from a typical laser emerges in an extremely thin beam with very little divergence, i.e., the beam is highly collimated. The high degree of collimation arises from the fact that the cavity of the laser is very nearly parallel from front and back mirrors as shown in Fig. 4.7. Because of this the light attains a parallel path after reflections from these mirrors. As it is clear from the figure, the back mirror is made almost perfectly reflecting while the front mirror is about 99% reflecting. Thus about 1% beam comes out of it, which we see as the output beam. Under this process, however, the light passes back and forth between the mirrors many times in order to gain intensity by the stimulated emission of more photons at the same wavelength. If the light is off axis, it will be lost from the beam.



The high degree of collimation or the directionality of a laser beam (single mode) is due to the geometrical design of the laser cavity and to the fact that stimulated emission process produces twin photons. A specific cavity design is shown in Fig. 4.8, where the angular spread of a beam is signified by the angle  $\theta$ . In fact the cavity mirrors are shaped with concave surfaces towards the cavity. This way reflecting light is focused back into the cavity, which finally forms a beam waist of radius  $r_0$  at one position in the cavity.



Considering the laser beam as the fundamental  $TEM_{00}$  mode (modes will be discussed in chapter 10), the half angle beam spread can be, written as

$$\theta = \frac{\lambda}{2r_0}$$

From this we obtain the angular spread as

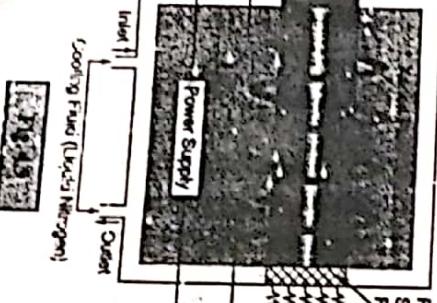
$$2\theta = 0.637\lambda$$

In addition to this, we can calculate the intensity, i.e. the power per unit area of a typical laser which is much greater than other sources of electromagnetic radiation. This is due to the directionality and compactness of the laser beam. In view of this, the intensity or irradiance of a laser beam in terms of its waist radius is given by the following relation

$$I = \frac{P}{A} = \frac{P}{\pi r_0^2}, \text{ where } P \text{ is the power.}$$

## 4.4 MAIN COMPONENTS OF LASERS

In order to understand the working principle of a laser, we should first know about the essential components of the laser. These are given below.

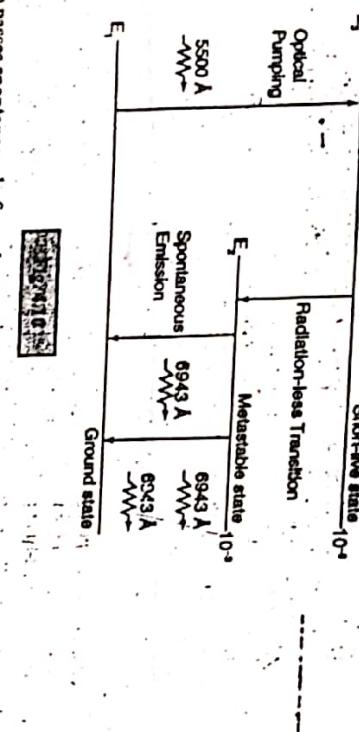


Ruby laser is a solid state laser, which consists three main parts (i) working material (ii) resonant cavity and (iii) excitation source.

**Working Material** Ruby laser is made up crystal of ruby in the form of cylindrical rod, size 2 to 30 cm in length and 0.5 to 2 cm in dia whose both ends are optically flat. One of the fully silvered and other is partially silvered, as they can act as fully and partially reflecting surfaces respectively, as shown in Fig. 4.9. Ruby rod crystal of  $\text{Al}_2\text{O}_3$  in which chromium oxide is as impurity so that some of the  $\text{Al}^{3+}$  ions are replaced by  $\text{Cr}^{3+}$  ions. These 'impurity' chromium ions rise to the laser action.

The space between the two faces A and B is called the resonant cavity. In which the light passes through multiple reflections and through stimulated emission. The ruby rod is connected to a power supply.

**Working Principle of Ruby Laser** In this laser, chromium ions are active centres which are responsible for the laser transition. A simplified energy level diagram of chromium ions in ruby crystal is shown in Fig. 4.11. In the normal state, most of the chromium ions are in the ground state  $E_1$ . When light from the flash tube at wavelength  $550\text{Å}$  is made to fall upon the ruby rod, these incident photons are absorbed by the chromium ions that rise to the excited state  $E_2$ . Then they give a part of their energy to the crystal structure and reach a metastable state, i.e. the  $E_3$  state. These ions in metastable state can remain for a longer duration  $10^{-3}$  sec. Therefore, the number of ions in this state goes on increasing while at the same time number of ions in ground state goes on decreasing due to the optical pumping. Thus, the population inversion is established between metastable state and the ground state.



When an excited ion passes spontaneously from the metastable state to the ground state, it emits a photon of wavelength  $6943\text{ Å}$ . This photon travels parallel to the axis of ruby rod and stimulates the surrounding ions present in the metastable state. Then by stimulated emission other photons are emitted, which are in the phase with the stimulating photons. By successive reflections of these photons at the ends of the rod, every time the stimulated emission is achieved and we obtain an intense, coherent and unidirectional laser beam from the partially silvered face B.

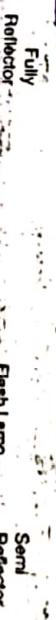
The ruby laser operates at about 1% efficiency. It may produce a laser beam of  $1\text{ mm}$  to  $25\text{ mm}$  in diameter. The beam obtained is in the form of pulses. However, on the advantage side, very strong beam as strong as  $0.50\text{ W}$  in power is produced. Furthermore, the construction of this laser is simple and the operation is very easy. For this reason, this laser is also known as practical laser. Other examples of solid state lasers are Neodymium-YAG (Nd-YAG), Neodymium-Glass (Nd-Glass) and semiconductors lasers.

As we know that the output beam of the ruby laser is not continuous. To overcome this drawback, the gas filled laser was made by A. Javan, W. Bennett and D. Herriott in 1961. It consists of a glass tube having the size about  $1.5\text{ cm}$  in diameter and about  $1\text{ meter}$  in length. The both ends of the tube are sealed by optically flat and parallel mirrors, one of them being partially silvered (90% reflective) and the other one is fully silvered (100% reflective).

### 4.5.2 Nd-YAG Laser: Solid State Laser

This laser is capable of producing very high power emissions, as a result of its lasing medium that operates as a gas level system. The schematic of Nd-YAG laser is shown in Fig. 4.11. The lasing medium in the Nd-YAG laser is colourless, isotropic crystal called Yttrium aluminium garnet ( $\text{YAG-Y}_3\text{Al}_5\text{O}_12$ ). The main dopant in

the lasing medium is Neodimium ( $\text{Nd}^{3+}$ ). When it is used in laser, Neodimium replaces  $1\%$  of Yttrium and the crystal takes a light blue colour. The YAG has a relatively high thermal conductivity, which improves thermal dissipation in thermal cavity. So continuous wave operation up to a few hundred Watts is possible. Average power of up to  $1\text{ kW}$  is available when it is operated in pulse mode.



The energy level diagram for Nd-YAG is shown in Fig. 4.12. These levels arise from three inner shell  $4f$  electrons of the  $\text{Nd}^{3+}$  ion, which are effectively screened by eight outer electrons ( $5\text{S}^2$  and  $5\text{P}^6$ ). For the operation of Nd-YAG lasers a cooling system is required. A Nd-YAG laser produces 30 times as much waste heat as laser output with an efficiency of about 3%. The waste heat must be removed in order to ensure proper laser operation by flooding the optical compartment with water. However optical distortion and image

problem is created due to absorption of significant amount of flash lamp energy by water. This problem can be overcome by flowing water over the outside of the optical cavity and by encasing the lasing rod and flash lamp with transparent cooling jacket.

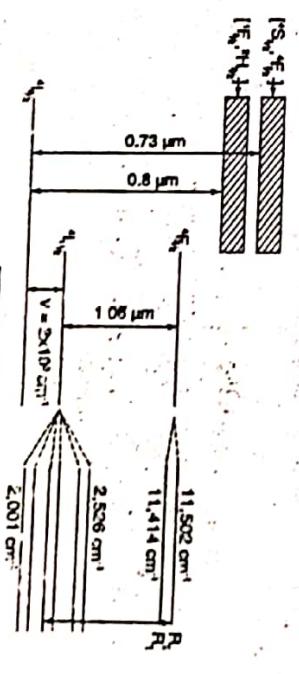


Fig. 4.12

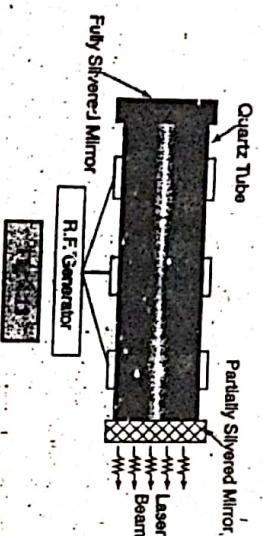
An advantage of Nd-YAG laser is that by using Q-switching, laser beam pulse frequency and shape can be tailored where a shutter moves rapidly in and out of the path of the beam. In this manner beam output is interrupted until a high level of population inversion and energy storage is achieved in the resonator. If the optical cavity is switched from no reflection (low  $Q$ ) to near total reflection (high  $Q$ ), the cycle can be

optimised to build up the maximum population inversion before the pulse is generated. This way, we get a beam pulse with high energy up to 1 J and a short pulse period down to 10ns is obtained.

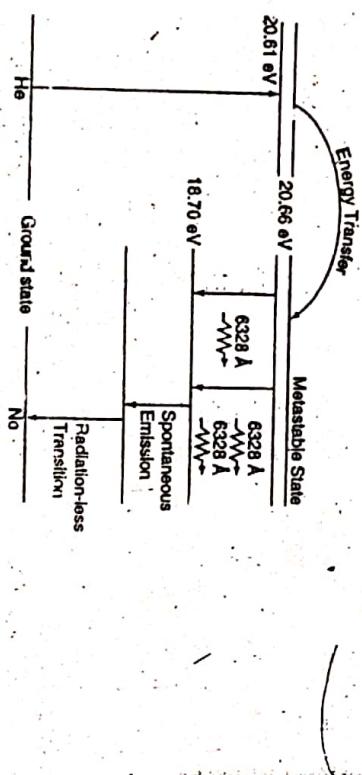
#### Applications

- Nd-YAG is used in material processing such as welding and drilling.
- It is also used in photo disruption of transparent membrane of pathological origin, which can appear in the interior chamber of eye, or for lithotripsy and in endoscopic applications.
- It is used in range finders and target designators used in military context, which use Q-switched lasers.
- In scientific applications the Q-switched lasers with their second harmonic ( $\lambda = 532 \text{ nm}$ ), third harmonic ( $\lambda = 355 \text{ nm}$ ) and fourth harmonic ( $\lambda = 266 \text{ nm}$ ) are used.

#### 4.5.3 Helium-Neon Laser: Gas Laser



In this laser system, a quartz tube is filled with a mixture of helium and neon gases in the ratio 10:1 respectively, at a pressure of about 0.1 mm of mercury (Fig. 4.13). This mixture acts as the active medium. Helium is pumped upto the excited state of 20.61 eV by the electric discharge. The energy level diagram of He-Ne laser is shown in Fig. 4.14.



#### 4.5.4 Carbon Dioxide Gas Laser

It is one of the earliest high power molecular gas laser that uses carbon dioxide gas molecule. The device is capable of continuous output powers above 10 kW. It is also capable of extremely high power operation. It consists of discharge tube of size of about 2.5 cm is diameter and 5.0 cm is length. Both ends of the tube are sealed by optically plane and parallel mirrors, one of them being semi-silvered and is fully silvered. (Fig. 4.15).

#### 4.5.4 Carbon Dioxide Gas Laser

This mixture is fed into the discharge tube through flow loop which is connected at one end of the tube. The dc excitations source is used that produces electric discharge. In starting nitrogen molecules allowed to enter in the discharge tube. They get excited by collision with electrons. Then excited nitrogen molecules flow into the whole volume of resonant cavity and collide with the unexcited CO<sub>2</sub> molecules and transfer their energy to the desired laser level (Fig. 4.16). (Nitrogen (N<sub>2</sub>) and helium (He) are present in the mixture in the ratio 15:70).

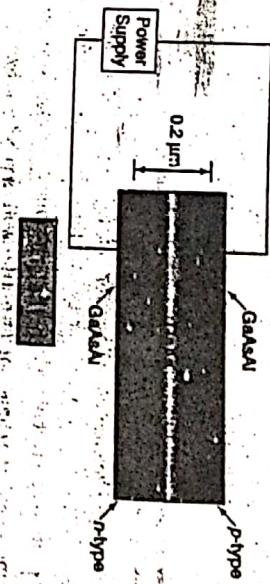
The carbon dioxide gas laser mixture contain 15% CO<sub>2</sub>, 15% N<sub>2</sub> and 70% He at a pressure of few millibars. The dc excitations source is used that produces electric discharge. In starting nitrogen molecules allowed to enter in the discharge tube. They get excited by collision with electrons. Then excited nitrogen molecules flow into the whole volume of resonant cavity and collide with the unexcited CO<sub>2</sub> molecules and transfer their energy to the desired laser level (Fig. 4.16). (Nitrogen (N<sub>2</sub>) and helium (He) are present in the mixture in the ratio 15:70).

producing large populations in upper level and helium helps removing population from lower energy level. Related energy levels of  $N_2$  and  $CO_2$  molecules are shown in Fig. 4.16. The radiated photons travel

Energy transfer



#### 4.5.6 Advantages and Disadvantages of Ruby Laser, He-Ne Laser and Semiconductor Laser



The merits and demerits of solid laser (Ruby), gas laser (He-Ne) and semiconductor laser:

Advantages	He-Ne Laser
1	Easy to construct and operate.
2	Continuous beam.
3	Exceptionally monochromatic beam with high operation duration (10,000 hrs.)
Disadvantage	It has got very low power about 0.5 - 5mW.

#### APPLICATIONS OF LASERS

Lasers have many applications in science, industry and medicine; some of which are listed below:

- (i) Lasers have been used to measure long distances, so they are very useful in surveying and ranging. For this purpose, a fast laser pulse is sent to a corner reflector at the point to be measured and the time of reflection is measured to get the distance.

Pumping  $\Rightarrow$  Pulsed bleaching  
Active medium: doped region

and forth between the end mirrors and get further amplified. It exhibits laser action at several infrared quads but none in the visible. For example, it radiates light at 10.6  $\mu\text{m}$  in far infrared. It is one of the most efficient lasers, capable of operating at more than 30% efficiency. Hence, this laser is suitable for certain applications both in terms of energy efficiency and high power beam; particularly it is used for cutting and cutting.

#### 4.5.7 Semiconductor Laser

Semiconductor laser differs from the solid state and gas laser in many aspects. It has remarkably small size, high efficiency and can be operated at low temperature. When the current is passed through a p-n junction diode, in forward bias, holes move from p-region to n-region and the electrons move from n-region to p-region. These electrons and holes are recombined in the junction region and emit photons due to the release of electrons from the conduction band to the valence band. This results in stimulated radiation emitting a very narrow region near the junction. The action is intensified by increasing the current; and semiconductor laser is made up of an active layer of gallium arsenide (GaAs) of thickness 0.2 microns. This is provided by between n-type GaAsAl and p-type GaAsAl layer as shown in Fig. 4.17. The resonant cavity is formed from opposite faces of the GaAs crystal and the pumping occurs by passing electrical current from an ordinary source (Power Supply). From this system GaAs semiconductor laser beams of wavelength ranging from 7000  $\text{\AA}$  to 30,000  $\text{\AA}$  can be produced.

- (ii) Lasers are electromagnetic waves of very high intensity and can be used to study the laws of interaction of atoms and molecules.
- (iii) Lasers are suitable for communication and they have significant advantages because they are more nearly monochromatic. This allows the pulse shape to be maintained better over long distances. So communication can be sent at higher rates without overlap of the pulses.
- (iv) Laser beams are highly intense and are used for welding, cutting of materials, machining and drilling holes, etc. Generally, carbon dioxide laser are used for such purposes, as it carries large power.
- (v) Lasers are used most successfully in eye surgery, treatment of dental decay and skin diseases.
- (vi) The laser beam is used in recording of intensity as well as in holography.
- (vii) Laser is used in heat treatments for hardening.
- (viii) Lasers are used as barcode scanners in library and in supermarket.
- (ix) Laser is used in printers (Laser printers).
- (x) Lasers are used in photodiode detection.

### **Holography**

So far you have learnt that the laser radiation is highly intense, highly coherent and highly monochromatic light. It is amazing that the field of laser radiation can be used to cool down atoms to very low temperature, for example up to  $10^{-4}$  K. This can be understood based on an atom which is traveling toward a laser beam and absorbs a photon from the laser. In this situation, the atom will be slowed by the fact that the photon has momentum  $p = E/c = h/\lambda$ , where  $E$  is the energy,  $c$  is the speed of light,  $h$  is the Planck's constant and  $\lambda$  is the wavelength associated with the photon. If we assume that a number of sodium atoms are freely moving in a vacuum chamber at 300K (room temperature), i.e. the rms velocity of the sodium atom is about 570 m/s. Then the momentum of the sodium atom can be reduced by the amount of the momentum of the photon, if a laser is tuned just below one of the sodium d-lines ( $5890 \text{ \AA}^*$  and  $5896 \text{ \AA}^*$ , about 2.1 eV) and the sodium atom absorbs a laser photon when traveling toward the laser. It would take a large number of such absorptions to cool the sodium atoms to nearly 0 K. The change in speed from the absorption of one photon can be calculated from,

$$\frac{\Delta p}{p} = \frac{p_{\text{photon}}}{mv} = \frac{\Delta v}{v} \Rightarrow \Delta v = \frac{p_{\text{photon}}}{m}$$

The above expression shows a lot of photons, but according to Chu a laser can induce on the order of  $10^7$  absorptions per second so that an atom could be stopped in a matter of milliseconds.

There is a conceptual problem that an absorption can also speed up an atom if it catches it from behind. So more absorptions from head-on photons are necessary to have. This is accomplished in practice by tuning the laser slightly below the resonance absorption of a stationary sodium atom. More precisely, with the opposing laser beams with perpendicular linear polarisations, atoms can be selectively driven or "optically pumped" into the lower energy levels. This method of cooling sodium atoms was proposed by Theodore Hensch and Arthur Schawlow at Stanford University in 1975 and was achieved by Chu at AT & T Bell Labs in 1985. Here sodium atoms were cooled from a thermal beam at 300K to about 240  $\mu\text{K}$ .

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(x) Lasers are used in photodiode detection.

### **4.8 HOLOGRAPHY**

Holography is one of the remarkable achievements of modern science and technology, possible only because of the lasers. The word "holography" was originated from the Greek and "grapho". The meaning of "holos" is "whole" and of "grapho" is "write". Schrödinger made record of the image] Holography is a three-dimensional (3D) laser photography. It is lensless photograph which an image is captured as an interference pattern. The image thus obtained is called a hologram true 3D record of the object. Holography not only records the amplitude but also the phase of the wave with the help of interferometric techniques! This recorded reference pattern contains more information than a focused image and enables the viewer to view a true 3D image which exhibits parallax. The holography was invented by Gabor in 1947.

### **4.8.1 Principle of Holography**

In holography, there are two basic waves that come together to create the interference pattern, one called **object wave** and another wave is called **reference wave**. When an object wave meets it creates a standing wave pattern of interference. This is then photographed, which we call a

### **4.8.2 Requirements of Holography**

Following are some requirements for the absolute holography.

- (i) Since holography is an interference phenomenon, there should not be a path difference between the object wave and the reference wave more than the coherence length. This is necessary for stable interference fringes.
- (ii) Spatial coherence is important so that the reference wave and the scattered object wave in different regions can interfere properly.
- (iii) Since reconstructed image coordinates depend on wavelength as well as position of the source, it is necessary that the source emits a narrow band of wavelength and it is also of interest of obtaining good resolution in the reconstructed image.
- (iv) In order to obtain aberrations free reconstructed image, it is necessary that the reconstructed image is of the same wavelength and is situated at the same position with respect to the reference source.
- (v) All recording arrangement like film, object, mirrors etc. must be motionless during the process.

### **4.9 HOLOGRAPHY VERSUS CONVENTIONAL PHOTOGRAPHY**

Holography represents a photographic process in a broad sense, but essentially it differs from conventional photography. As the phase of light waves scattered by the object carries the complete information about the object. A conventional photography is a 2D image of a 3D scene, which brings into focus only the scene that falls within the depth of the field of the lens. Due to this, a conventional photograph gives only perception of the depth or the parallax with which we view a real life scene. Since a conventional photograph only records the intensity pattern, 3D character of the object scene is lost. Contrary to this, the

contains depth and parallax, which provides the ability to see around the object to objects placed behind. It gives information about amplitude as well as the phase of an object. So hologram preserves information about the object for latter observation.

In conventional photography, there is one to one relationship between object and image point as the light originating from a particular point of scene is collected by a lens focused on that particular point. However, a holography lens is not used and thus is a complex interference pattern of microscopically spaced fringes.

Hologram receives light from every point of a scene and hence there is no one to one relationship. This is a merit of entire signal wave.

In conventional photography, radiated energy is recorded and phase relationship of wave arriving from different distances and directions is lost. However, in holography, phase relationship is recorded by using the technique of interference of light waves.

## 10 RECORDING AND RECONSTRUCTION ON HOLOGRAPHIC PLATE

Recording of a hologram is a result of superpositions of the object wave and the reference wave, which is mainly a plane wave. This interference pattern is recorded by a photographic plate that contains information about amplitude as well as phase of the object wave. In order to see the image, hologram is illuminated with another wave called the reconstruction wave which is identical to the reference wave in most of the cases. This is called reconstruction of image on the hologram.

### Theory

If the object is a point scatterer and it is made of large number of such points, then the composite wave affected by the object will be the vectorial sum of all object waves scattered from all these points. As mentioned earlier, holography records the object wave, particularly the phase (say  $\phi$ ) associated with it. So we can represent the object wave, which is due to the superposition of waves from point scatterers on the object, as

$$Y_1(x, z) = A_1(x, z) \cos(\phi - \omega t) \quad (1)$$

where  $w$  is the frequency. The object wave represented by Eq. (1) lies in the plane of photographic plate at  $y=0$ . Now we consider a reference wave propagating in the  $xy$  plane and inclined at an angle  $\alpha$  from the  $y$  axis. In view of this, the field associated with the reference wave can be written as

$$Y_2(x, y, z) = A_2 \cos(\vec{k} \cdot \vec{r} - \omega t) \quad (2)$$

$Y_2(x, y, z) = A_2 \cos(kx \sin \alpha + ky \cos \alpha - \omega t)$   
At the photographic plate, i.e., at  $y=0$ , this field becomes

$$Y_2(x, z) = A_2 \cos(kx \sin \alpha - \omega t)$$

Since the propagation constant  $k = 2\pi/\lambda$ ,  $kx \sin \alpha = \frac{\sin \alpha}{\lambda} 2\pi x$   
Here  $\sin \omega t$  is defined as the spatial frequency (say  $s$ ). So the field associated with the reference wave becomes,

$$Y_2(x, z) = A_2 \cos(2\pi kx \sin \alpha - \omega t) \quad (3)$$

A comparison of equation (iii) with equation (1) yields that the phase linearly varies with  $x$ .

Simple method of superposition enables us to calculate the total field at the photographic plate (at  $y=0$ ) as

$$Y = Y_1 + Y_2$$

In view of the response of photographic plate to the intensity we find below the measure of intensity pattern.

$$I(x, z) = \text{Average value of } Y^2(x, z) \quad (iv)$$

or

$$\begin{aligned} I(x, z) &= A_1^2(x, z) \langle \cos^2(\phi - \omega t) \rangle + A_2^2 \langle \cos^2(2\pi kx \sin \alpha - \omega t) \rangle \\ &\quad + 2A_1(x, z) A_2 \langle \cos(\phi - \omega t) \cos(2\pi kx \sin \alpha - \omega t) \rangle \end{aligned} \quad (v)$$

As we know that  $\langle \cos^2(\phi - \omega t) \rangle = V_1$ ,

$$\langle \cos^2(2\pi kx \sin \alpha - \omega t) \rangle = V_2$$

$$\begin{aligned} &\langle 2\cos(\phi - \omega t) \cos(2\pi kx \sin \alpha - \omega t) \rangle \\ &= V_1 \langle \cos(\phi + 2\pi kx \sin \alpha - 2\omega t) + \cos(\phi - 2\pi kx \sin \alpha - 2\omega t) \rangle \end{aligned}$$

[Using  $2\cos(\theta_1 + \theta_2) = \cos(\theta_1 + \theta_2 + \cos(\theta_1 + \theta_2))$ ]

The average value of  $\cos(\phi + 2\pi kx \sin \alpha - 2\omega t)$  can be obtained by using simple integration

$$\frac{1}{T} \int_0^{2\pi/\omega} \cos(\phi + 2\pi kx \sin \alpha - 2\omega t) dt,$$

as the average value of  $\cos \omega t$  over the period  $T = 2\pi/\omega$

$$= \frac{1}{T} \int_0^{2\pi/\omega} \cos \omega t dt.$$

So it comes out to be zero. With this, the intensity  $I(x, z)$  is written as

$$I(x, z) = A_1^2(x, z) V_2 + A_2^2 V_1 + A_1(x, z) A_2 \cos(\phi - 2\pi kx \sin \alpha) \quad (vi)$$

The above equation shows that the intensity  $I$  is the function of phase  $\phi(x, z)$ . It means the phase information of the object wave is recorded in the intensity pattern.

In order to obtain a hologram, we develop the photographic plate containing above intensity pattern. In this context, the ratio of the transmitted field to the incident field is defined as the transmittance of the hologram that depends on  $I(x, z)$ . Using a suitable developing process, the condition under which the transmittance is linearly related to  $I(x, z)$  can be obtained. Under this condition, if  $R_s(x, z)$  denotes the field of the reconstruction wave, at the hologram plane, then the transmitted field can be taken as

$$T_s(x, z) \propto R_s(x, z) I(x, z)$$

Taking  $K_s$  as the proportionality coefficient and putting the value of  $I(x, z)$  from equation (vi), we obtain

$$T(x, z) = K_r R(x, z) \left[ \frac{\Delta_1^2(x, z)}{2} + \frac{\Delta_2^2}{2} + A_1(x, z) A_2 \cos(\phi - 2\pi\xi z) \right] \quad (\text{vii})$$

In the case when the reconstruction wave is identical to the reference wave  $Y_1(x, z)$ , the above equation becomes

$$T(x, z) = K_r A_2 \left[ \frac{\Delta_1^2(x, z)}{2} + \frac{\Delta_2^2}{2} \right] \cos(2\pi\xi x - \omega t) + K_r A_2^2 A_1(x, z) \cos(2\pi\xi x - \omega t) \cos(\phi - 2\pi\xi z)$$

Again using  $2 \cos \theta_i \cos \theta_r = \cos(\theta_i + \theta_r) + \cos(\theta_i - \theta_r)$ , we get the following expression for  $T_r(x, z)$

$$T_r(x, z) = K_r A_2 \left[ \frac{\Delta_1^2(x, z)}{2} + \frac{\Delta_2^2}{2} \right] \cos(2\pi\xi x - \omega t) + \frac{K_r A_2^2 A_1(x, z)}{2} \cos(\phi - \omega t)$$

$$+ \frac{K_r A_2^2 A_1(x, z)}{2} \cos(4\pi\xi z - \phi - \omega t) \quad (\text{viii})$$

The above equation contains three terms, which may be analysed as follows.

- First term being proportional to  $A_2^2$  represents the reconstruction wave whose amplitude is modulated by the term  $\Delta_1^2(x, z)$ , i.e. by the amplitude of object wave. The factor  $\cos(2\pi\xi x - \omega t)$  shows that this part of the total field is traveling in the direction of the reference wave.

- The second term is identical to equation (i) within a constant term. Hence, this represents the original object wave. Having appeared in transmitted field, it gives rise to a virtual image.

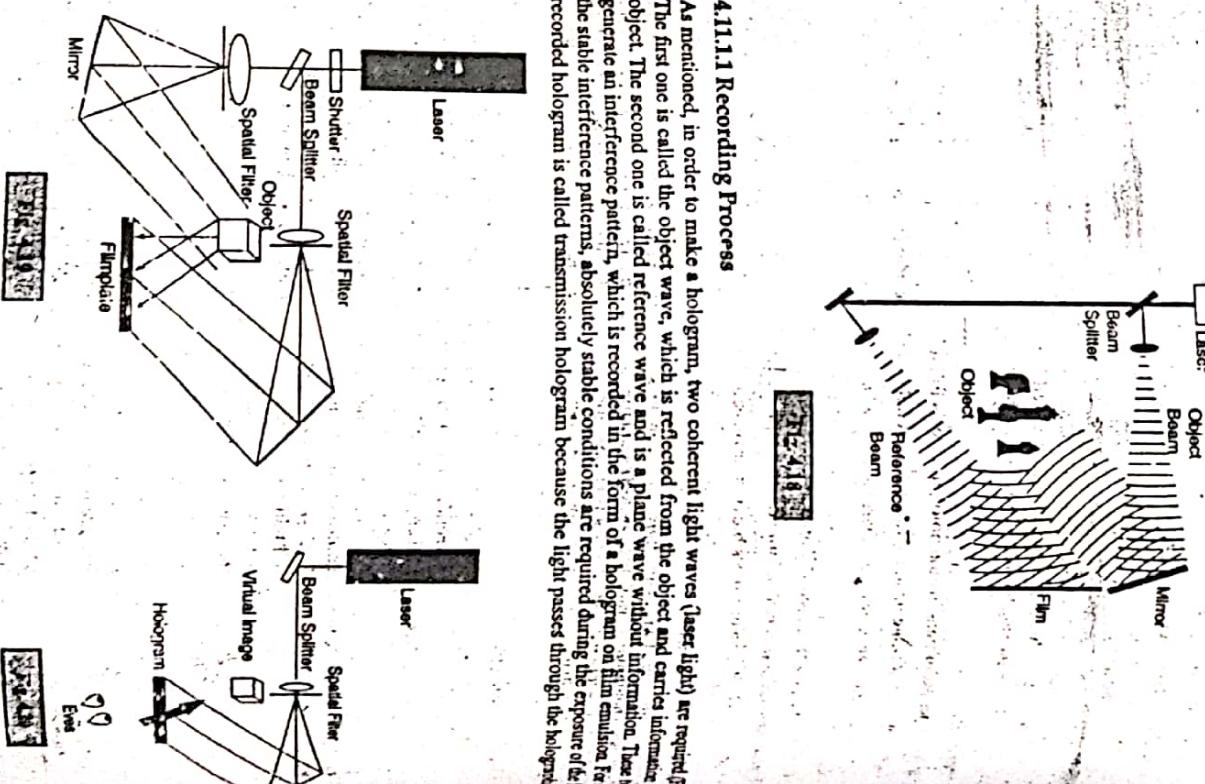
- The third term carries the phase  $\phi(x, z)$  in addition to the term  $4\pi\xi z$ , but with negative sign. It means this wave has a curvature opposite to the object wave, i.e. if the object wave is diverging spherical wave, then the last term (third term) shows a converging spherical wave. Hence, this wave forms a real image of the object contrary to the second term. This image can be photographed with the help of a film.

## 4.11 TYPES OF HOLOGRAMS

In order to construct a hologram, we need two coherent light waves, one is the object wave carrying information about the object and the other is a plane wave that is called reference wave. There are various types of holograms, but the most common ones are the transmission hologram and the reflection holograms.

### 4.11.1 Transmission Hologram

This type of hologram is commonly used. If the object wave and the reference wave emerge from the same side of the holographic film, then the hologram is called transmission hologram (Fig. 4.18). Another characteristic of transmission hologram is the low diffraction efficiency and weak image reconstruction.



#### 4.11.1.1 Recording Process

As mentioned, in order to make a hologram, two coherent light waves (laser light) are required. The first one is called the object wave, which is reflected from the object and carries information of object. The second one is called reference wave and is a plane wave without information. These generate an interference pattern, which is recorded in the form of a hologram on film emulsion. For the stable interference patterns, absolutely stable conditions are required during the exposure of the recorded hologram is called transmission hologram because the light passes through the hologram.

## 4.11.2 Reconstruction Process

If we reconstruct the holographic image by developing the hologram and then placing it in its original position in the reference beam, as during its recording. If we look along the reconstructed object wave, we see an replica of the object and as we shift viewpoints we see object from different perspectives. Thus the object appears to be three-dimensional. During the reconstruction of the transmission hologram, the light does not pass through the image, but it creates a wavefront that makes it appear as though the light had been generated at the position of the object. This image thus formed is called virtual image (Fig. 4.20). Contrary to this, an image having light actually passing through it is called a real image.

### 4.11.3 Properties

Some important properties of transmission hologram are as follows:

- When viewed with white light, the transmission holograms look like a blurry rainbow image.
- These holograms are viewed as sharp images when we use the shining laser light through the hologram.
- Less resolving power is needed in materials.
- Transmission hologram can be formed in a simple setup.
- Greater depth of the scene is possible in transmission holograms.

## 4.12 Reflection Hologram

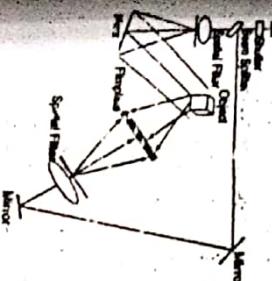
The holograms that are viewed with white light source on the same side as the viewer are known as reflection hologram. In such a hologram, a truly three-dimensional image is seen near its surface. This hologram is the most common type shown in galleries. The light is located on the viewer's side of the hologram at a specific angle and distance. The image thus formed consists of light reflected by the hologram. There are two types of reflection holograms.

### 4.12.1 One Step Hologram

Here, the resolution of film emulsion is high, as the recording of reflection hologram needs 10 to 100 times more power than a transmission hologram. Thus exposure time is long. During the process of recording the hologram, the two waves, namely the reference wave and the object wave illuminate the film plate on opposite sides (Fig. 4.21). In this case, the fringes are formed in layers and are more or less parallel to the surface of the emulsion. If a highly directed beam of white light illuminates a reflection hologram, it selects the appropriate band of wavelengths to reconstruct the image and the remainder of the light passes straight through.

### 4.12.2 Two Step Hologram

This hologram involves two steps. First we make a transmission hologram called H1 (Fig. 4.22). This is called a master or first hologram. We make multiple copies from the master hologram. We make transfer copies of master hologram. Transfer copy means making another hologram using the image on the master as the subject. These transfer holograms are either laser-visible transmission holograms or



4.11.1.3

reflection holograms H2. Suppose we want any object in the final hologram just to appear half in front and half behind the recording plate. In such circumstances, the two step hologram is of great use.

### 4.11.2.3 Properties

Some important properties of reflection hologram are as follows:

- These holograms can be viewed in regular light.
- The finished reflection hologram is monochromatic.

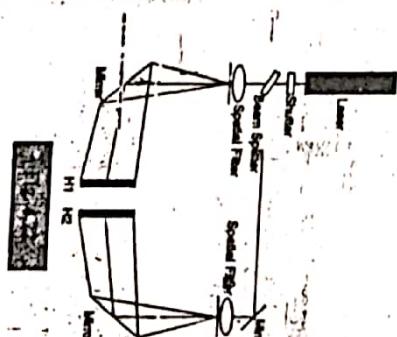
### 4.11.3 White Light Hologram: Rainbow Hologram

Rainbow holograms that can be viewed in white light and produce 3D images are very popular holograms. A double holographic process makes them, in which an ordinary hologram is used as the object and a second hologram is made through it. A horizontal slit limits the vertical perspective of the first image so that there is no vertical parallax. Ordinary room light while maintaining the 3D character of the image as the viewer eye is moved horizontally.

Vertical

perspective of the first image so that there is no vertical parallax.

If viewer eye is moved vertically, no parallax is seen and the image colour sweeps through the rainbow spectrum from blue to red.



### 4.11.3.1 Embossed Hologram

Many variations of hologram can be made between the reflection and transmission types of holograms. Embossed hologram is one of such types of holograms, which is used widely in most security applications. These holograms offer an effective method of protection against any forms of manipulation, as they are too difficult to copy due to their complex structure. All credit cards and passports have embossed hologram. In this hologram, the original hologram is recorded in a photosensitive material called photoresist. These holograms are easily produced at large scale and also at a very low cost.

### 4.11.3.2 Volume Hologram

Volume holograms are produced when the thickness of the recording material is much larger than the light wavelength used for recording. These are transmission holograms and are also known as thick holograms, which are mainly considered as a high-density data storage technology. These are 3D holograms created by recording the interference pattern of two mutually coherent light waves. The angle of difference between the object wave and the reference wave is  $90^\circ$  to  $180^\circ$ . Due to certain unique properties, volume holograms are used widely in various spectroscopic and imaging applications.



Holography represents examples of recombining of scattered radiation. It is a product of interference of light, which is used to measure very small optical path length with precision by using wavelength of light and interference. Now holography is being used in industry, communication and other engineering problems also. You would have seen hologram on tickets, original covers of software programs, credit cards etc. This is used to prevent falsification. Another important application is through bar code readers used in shops, warehouses, libraries and so on. In aircraft industry, holography technology is used through head up displays (HUD). Which help the pilot to see instrument panel on to the windscreen.

Some other important applications of holography are given below.

#### 4.12.1 Time Average Holographic Interferometry

This interferometry is very useful for determining or studying the modes of vibration of complex structures. Hologram is prepared using a long exposure time than the periods of vibrations being studied. This hologram freezes many images, mapping the motion of vibrating surface. Interference fringes pattern provides information about the relative vibrational amplitudes as a function of position on the surface.

#### 4.12.2 Microscopy

A hologram contains many separate observations of microscopic particles. Image provided by hologram may be viewed by focusing on any depth of illuminating field. Microscopic hologram is made by illuminating the specimen by laser light, a part of which is split off outside the microscope and is routed to the photographic plate to rejoin the subject beam processed by the microscope. It can be shown that if  $\lambda_r > \lambda_s$ , where  $\lambda_r$  is the wavelength of reconstructing light and  $\lambda_s$  is the wavelength used in holography, then the magnification is

$$M = (\frac{\nu}{u}) / (\frac{\nu}{\lambda_s})$$

Here  $u$  is the object distance from the film and  $\nu$  is the corresponding image distance from the hologram. However, these distances are equal, i.e.,  $u = \nu$ , if the reference and reconstructed wavefronts are both plane wave.

#### 4.12.3 Ultrasonic Hologram

As the words "ultrasonic holograms" suggest, the waves producing a hologram may not necessarily be electromagnetic in nature. Also, the holographic principles do not depend on the transverse nature of the radiation. Holograms generated with the help of ultrasonic waves are very useful because of the ability of such waves to penetrate the objects that are opaque to visible light. Holograms formed by ultrasonic waves are very useful to get 3D images inside the opaque bodies.

#### 4.12.4 Hologcameras

Hologram can be developed and viewed with the help of hologcameras, which do not use photographic film. Thermoplastic recording material is used in hologcameras and image development is done by electrical and thermal means. The image development does not need wet chemical processing. Also, it can be completed in a few seconds without repositioning the recording.

#### 4.12.5 Holographic Data Storage

Data can be stored by holographic technique. It is very interesting that the data can be reduced to dimensions of the order of wavelength of light. Therefore, volume holograms can be useful to record vast quantities of information. Photosensitive crystal like potassium bromide with colour centres or lithium niobate are used in place of thick layered photocellulose. Small rotation of crystal takes place of turning pages.

## SUMMARY

The main topics discussed in this chapter are summarized below.

- (1) Laser was introduced as a special type of device that amplifies light and produces a very directional beam which mostly has a very pure frequency.
- (2) It was made clear the population inversion is the basic requirement for the operation of lasers.
- (3) For achieving the laser radiation, the concept of stimulated emission was discussed in detail with the inclusion of Einstein's coefficients.
- (4) The main components of laser were discussed and based on the gain medium lasers were classified as solid state laser, gas laser or semiconductor laser.
- (5) Ruby laser, Nd-YAG laser, He-Ne laser, CO<sub>2</sub> laser and semiconductor laser were discussed and the energy diagrams provided.
- (6) It was mentioned that the lasers have diverse applications in different fields of technology. These applications were talked about in brief.
- (7) A new concept of laser cooling was discussed in detail. It was shown how a highly coherent light of laser can cool the sodium atoms to 10<sup>-6</sup>K.
- (8) Another exciting field of holography was introduced and it was mentioned that with lasers the holograms can be developed that give 3D picture of the objects.
- (9) Principle and the requirements of the holography were discussed.

(10) The advance/additional features of holography from those of conventional photography were talked about.

- (11) Detailed description of recording and reconstruction of image on hologram were discussed in detail along with their recording and reconstruction processes and the properties.
- (12) Two types of holograms, namely transmission holograms and reflection holograms were discussed.
- (13) White light hologram was introduced, which is also known as rainbow hologram. embossed and volume holograms were talked about.
- (14) Various applications of holography were discussed including time average holography, interferometry, microscopy, ultrasonic holograms, hologcameras and the holographic data storage.

## SOLVED EXAMPLES

**Ques. 1** A three-level laser emits a light of wavelength of 5500 Å.

What will be the ratio of population of upper level ( $E_u$ ) to the lower energy level ( $E_l$ ) if the pumping mechanism is shut off (Assume  $T = 500$  K).

At what temperature for the conditions of (a) would the ratio of populations be 1 : 1?

For an ordinary source, the coherence time  $\tau_c = 10^{-10}$  sec. Obtain the degree of hetero-monochromativity for  $\lambda_0 = 5400 \text{ \AA}$ .

$$\Delta V = \frac{1}{10} = 10 \text{ mV}$$

$$\text{For } \lambda_0 = 5400 \text{ Å}, v_0 = \frac{c}{\lambda_0} = \frac{3.0 \times 10^8}{5400 \times 10^{-10}} = \frac{1}{18} \times 10^{17}$$

$$\frac{\Delta V}{V} = \frac{18 \times 10^{-10}}{10^{16}} = 18 \times 10^{-16} = 0.000018.$$

OBJECTIVE TYPE QUESTIONS

- LASER is a short form of

  - Light Amplification Stimulated Emission Radiation
  - Light Absorption by Stimulated Emission of Radiation
  - Light Absorption by Spontaneous Emission of Radiation

What is the life-time of electron in metastable state?

~~Very~~  $10^{-3}$  sec.      (b)  $10^{-1}$  sec.  
 (c)  $10^{-4}$  sec.      (d)  $10^{-7}$  sec.

In the population inversion

  - the number of electrons in higher energy state is more than
  - the number of electrons in lower energy state is more than
  - the number of electrons in higher and lower energy state is
  - none of them.

The relation between Einstein's coefficient A and B is

~~(a)~~  $\frac{g_{\text{high}}}{g_{\text{low}}} \nu^2$       (b)  $\frac{g_{\text{high}} \nu^2}{c^2}$   
 (c)  $\left( \frac{2gh\nu}{c} \right)^2$       (d)  $\frac{g_{\text{high}}}{\lambda}$

15 "Laser beam is made of

  - electrons
  - very light inelastic particles
  - highly cohesive
  - none of the

### PRACTICE PROBLEMS

- Q.1** What do you mean by laser and its working principle, important requirements and applications?

**Q.2** (a) Explain the term 'absorption', 'spontaneous' and 'stimulated' emission of radiation. Obtain relation between transition probabilities of spontaneous and stimulated emission.

(b) What are Einstein's coefficient? Derive Einstein relation.

**Q.3** Explain the construction and working principle of Ruby laser.

**Q.4** What is the principle of laser?

**Q.5** Discuss salient characteristics of laser beam

**Q.6** Describe various applications of laser?

**Q.7** Explain the characteristics of laser beam. What are the necessary conditions for Lasing action?

**Q.8** Explain the concept of directionality and monochromaticity as applied to lasers.

**Q.9** Discuss Einstein's coefficients. Derive relation between them.

**Q.10** Explain the terms: spontaneous and stimulated emission, population inversion, optical pumping.

**Q.11** What is meant by population inversion and how is it achieved in practice?