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# MCQ's on Taylor's n Maclaurin Thm, Indeterminate Forms -- Vijay Hirap

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## Multiple choice questions

### Type I: Maclaurin's Theorem & Expansion Of Functions:

1. Expansion Of  $f(x)$  in ascending powers of  $x$  by Maclaurin's Theorem is

(A)  $f(x) + xf'(x) + \frac{x^2}{2!} f''(x) + \dots$  (B)  $1 + x + \frac{x^2}{2!} + \dots$

(C)  $f(0) + xf'(0) + \frac{x^2}{2!} f''(0) + \dots$  (A)  $f(x) - xf'(x) + \frac{x^2}{2!} f''(x) - \frac{x^3}{3!} f'''(x) + \dots$

2. Expansion Of  $\sin x$  in ascending powers of  $x$  is

(A)  $x + \frac{x^3}{3!} + \frac{x^5}{5!} + \dots$  (B)  $x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$

(C)  $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$  (D)  $1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$

3. Expansion of  $\cos x$  in ascending powers of  $x$  is.....

(A)  $1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \frac{x^6}{6!} + \dots$  (B)  $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$

(C)  $x + \frac{x^2}{2!} + \frac{x^4}{4!} + \frac{x^6}{6!} + \dots$  (D)  $1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots$

4. Expansion of  $\tan x$  in ascending powers of  $x$  is.....

(A)  $1 + x + \frac{1}{3}x^3 + \frac{2}{15}x^5 + \dots$  (B)  $x - \frac{1}{3}x^3 + \frac{2}{15}x^5 - \dots$

(C)  $x + \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^6}{6!} + \dots$  (D)  $x + \frac{1}{3}x^3 + \frac{2}{15}x^5 + \dots$

5. Expansion of  $e^x$  in ascending of  $x$  is.

(A)  $1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$  (B)  $1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \dots$

(C)  $1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots$  (D)  $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$

6. Expansion of  $e^{-x}$  in ascending powers of  $x$  is.....

(A)  $1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$  (B)  $1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \dots$

(C)  $1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots$  (D)  $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$

7. Expansion of  $\sinh x$  in ascending powers of  $x$  is

(A)  $1+x+\frac{x^2}{2!}+\frac{x^3}{3!}+\dots$  (B)  $x-\frac{x^3}{3!}+\frac{x^5}{5!}-\frac{x^7}{7!}+\dots$

(C)  $1+\frac{x^2}{2!}+\frac{x^4}{4!}+\frac{x^6}{6!}+\dots$  (D)  $x+\frac{x^3}{3!}+\frac{x^5}{5!}+\frac{x^7}{7!}+\dots$

8. Expansion of  $\cosh x$  in ascending powers of  $x$  is

(A)  $1+x+\frac{x^2}{2!}+\frac{x^3}{3!}+\dots$  (B)  $x-\frac{x^3}{3!}+\frac{x^5}{5!}-\frac{x^7}{7!}+\dots$

(C)  $1+\frac{x^2}{2!}+\frac{x^4}{4!}+\frac{x^6}{6!}+\dots$  (D)  $x+\frac{x^3}{3!}+\frac{x^5}{5!}+\frac{x^7}{7!}+\dots$

9. Expansion of  $\tanh x$  in ascending powers of  $x$  is

(A)  $1+x+\frac{1}{3}x^3+\frac{2}{15}x^5+\dots$  (B)  $x-\frac{1}{3}x^3+\frac{2}{15}x^5-\dots$

(C)  $x-\frac{x^3}{3!}+\frac{x^5}{5!}-\frac{x^7}{7!}+\dots$  (D)  $x+\frac{1}{3}x^3+\frac{2}{15}x^5+\dots$

10. Expansion of  $\log(1+x)$  in ascending powers of  $x$  is

(A)  $x-\frac{x^2}{2}+\frac{x^3}{3}-\frac{x^4}{4}+\dots$  (B)  $-x-\frac{x^2}{2}-\frac{x^3}{3}-\frac{x^4}{4}+\dots$

(C)  $1+\frac{x^2}{2!}+\frac{x^4}{4!}+\frac{x^6}{6!}+\dots$  (D)  $x+\frac{x^3}{3!}+\frac{x^5}{5!}+\frac{x^7}{7!}+\dots$

11. Expansion of  $\log(1-x)$  in ascending powers of  $x$  is

(A)  $-x-\frac{x^2}{2}-\frac{x^3}{3}-\frac{x^4}{4}-\dots$  (B)  $-x-\frac{x^2}{2}-\frac{x^3}{3}-\frac{x^4}{4}+\dots$

(C)  $1+\frac{x^2}{2!}+\frac{x^4}{4!}+\frac{x^6}{6!}+\dots$  (D)  $x+\frac{x^3}{3!}+\frac{x^5}{5!}+\frac{x^7}{7!}+\dots$

12. Expansion of  $\frac{1}{(1-x)}$  in ascending powers of  $x$  is

(A)  $-1-x-x^2-x^3-\dots$  (B)  $1-x+x^2-x^3+\dots$

(C)  $1+\frac{x^2}{2!}+\frac{x^4}{4!}+\frac{x^6}{6!}+\dots$  (D)  $1+x+x^2+x^3+\dots$

13. Expansion of  $\frac{1}{(1+x)}$  divided by  $(1+x)$  in ascending powers of  $x$  is

- (A)  $-1 - x - x^2 - x^3 - \dots$     (B)  $1 - x + x^2 - x^3 + \dots$   
 (C)  $1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \frac{x^6}{6!} + \dots$     (D)  $1 + x + x^2 + x^3 + \dots$

14. Expansion of  $(1+x)^n$  in ascending powers of x is

- (A)  $1 - nx + \frac{n(n-1)}{2!}x^2 - \frac{n(n-1)(n-2)}{3!}x^3 + \dots$     (B)  $1 - nx + \frac{n(n+1)(n+2)}{3!}x^3 + \dots$   
 (C)  $1 + nx + \frac{n(n+1)}{2!}x^2 + \frac{n(n+1)(n+2)}{3!}x^3 + \dots$     (D)  $1 + nx + \frac{n(n-1)}{2!}x^2 + \frac{n(n-1)(n-2)}{3!}x^3 + \dots$

15. The limit of series  $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$  as x approaches to  $\pi/2$  is ...

- (A) 0    (B)  $\pi/2$     (C) 1    (D) -1

16. First two terms in expansion of  $\log(1+e^x)$  by Maclaurins theorem is

- (A)  $\log 2 + \frac{1}{2}x + \dots$     (B)  $\log 2 - \frac{1}{2}x + \dots$   
 (C)  $x - \frac{x^2}{2} + \dots$     (D)  $x + \frac{x^2}{2} + \dots$

17. First two terms in expansion of  $\sec x$  by Maclaurins theorem is

- (A)  $1 - \frac{x^2}{2!} + \dots$     (B)  $x - \frac{x^3}{3!} + \dots$   
 (C)  $1 + \frac{x^2}{2!} + \dots$     (D)  $x + \frac{x^3}{3!} + \dots$

18. First two terms in expansion of  $e^x \sec x$  by Maclaurins theorem is

- (A)  $x + x^2 + \dots$     (B)  $x - x^2 + \dots$   
 (C)  $1 + x + \dots$     (D)  $1 - x + \dots$

19. First two terms in expansion of  $\tan^{-1}(1+x)$  by Maclaurins theorem is

- (A)  $\frac{\pi}{4} + \frac{x}{2} - \dots$     (B)  $\frac{\pi}{4} - \frac{x}{2} - \dots$   
 (C)  $x - \frac{x^3}{3!} + \dots$     (D)  $x + \frac{x^3}{3!} + \dots$

20. Expansion of  $\sin(\frac{x}{2}) + \cos(\frac{x}{2})$  in ascending powers of x is

$$(A) \ 1 - \frac{x}{2} + \frac{x^2}{8} - \frac{x^3}{48} + \frac{x^4}{384} + \dots \quad (B) \ 1 + \frac{x}{2} - \frac{x^2}{8} + \frac{x^3}{48} - \frac{x^4}{384} + \dots$$

$$(C) \ 1 + \frac{x}{2} - \frac{x^2}{8} + \frac{x^3}{24} - \frac{x^4}{120} + \dots \quad (D) \ \frac{x^2}{8} - \frac{x^3}{48} + \frac{x^4}{384} + \dots$$

21. Expansion of  $\log(1-x^4) - \log(1-x)$  in ascending powers of  $x$  is

$$(A) \ -x - \frac{x^2}{2} - \frac{x^3}{3} - \frac{3}{4}x^4 + \dots \quad (B) \ x + \frac{x^2}{2} + \frac{x^3}{3} - \frac{3}{4}x^4 + \dots$$

$$(C) \ x + \frac{x^2}{2!} + \frac{x^3}{3!} - \frac{3}{4!}x^4 + \dots \quad (D) \ -x - \frac{x^2}{2!} - \frac{x^3}{3!} - \frac{3}{4!}x^4 + \dots$$

22 Expansion of  $\log(1+x)^{1/x}$  in ascending powers of  $x$  is

$$(A) \ 1 - \frac{x}{2} + \frac{x^2}{3} - \frac{x^3}{4} + \dots \quad (B) \ -1 - \frac{x}{2} - \frac{x^2}{3} - \frac{x^3}{4} - \dots$$

$$(C) \ 1 - \frac{x}{2!} + \frac{x^2}{3!} - \frac{x^3}{4!} + \dots \quad (D) \ -1 - \frac{x}{2!} - \frac{x^2}{3!} - \frac{x^3}{4!} - \dots$$

23 Expansion of  $\log(1+x)^x$  in ascending powers of  $x$  is

$$(A) \ x^2 + \frac{x^3}{2} + \frac{x^4}{3} + \frac{x^5}{4} + \dots \quad (B) \ x^2 - \frac{x^3}{2!} + \frac{x^4}{3!} - \frac{x^5}{4} + \dots$$

$$(C) \ 1 + x + x \frac{x^2}{2} - \frac{x^3}{3} + \frac{x^4}{4} - \frac{x^5}{5} + \dots \quad (D) \ x^2 - \frac{x^3}{2} + \frac{x^4}{3} - \frac{x^5}{4} + \dots$$

24 Expansion of  $\cos^2 x$  in ascending powers of  $x$  is

$$(A) \ \frac{1}{2} \left\{ 1 + \left( 1 - \frac{2^2 x^2}{2!} + \frac{2^4 x^4}{4!} - \dots \right) \right\} \quad (B) \ \frac{1}{2} \left\{ 1 - \left( 1 - \frac{2^2 x^2}{2!} + \frac{2^4 x^4}{4!} - \dots \right) \right\}$$

$$(C) \ \frac{1}{2} \left\{ 1 + \left( 2x - \frac{2^3 x^3}{3!} + \frac{2^5 x^5}{5!} - \dots \right) \right\} \quad (D) \ \frac{1}{2} \left\{ 2x - \left( 1 - \frac{2^3 x^3}{3!} + \frac{2^5 x^5}{5!} - \dots \right) \right\}$$

25. Expansion of  $\sin x \cos x$  in ascending powers of  $x$  is

$$(A) \ \frac{1}{2} \left( 1 - \frac{2^2 x^2}{2!} + \frac{2^4 x^4}{4!} - \dots \right) \quad (B) \ \frac{1}{2} \left( 1 - \frac{2^2 x^2}{2!} + \frac{2^4 x^4}{4!} - \dots \right)$$

$$(C) \ \frac{1}{2} \left( 2x - \frac{2^3 x^3}{3!} + \frac{2^5 x^5}{5!} - \dots \right) \quad (D) \ \frac{1}{2} \left( x - \frac{2^3 x^3}{3!} + \frac{2^5 x^5}{5!} - \dots \right)$$

26 Expansion of  $\sin 2x \cos 3x$  in ascending powers of  $x$  is

- (A)  $\frac{1}{2} \left[ \left( 5x - \frac{5^3 x^3}{5!} + \frac{5^5 x^5}{5!} - \dots \right) - \left( x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots \right) \right]$
- (B)  $\frac{1}{2} \left[ \left( 5x - \frac{5^3 x^3}{3!} + \frac{5^5 x^5}{5!} - \dots \right) + \left( x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots \right) \right]$
- (C)  $\frac{1}{2} \left[ \left( 1 - \frac{5^2 x^2}{2!} + \frac{5^4 x^4}{4!} - \dots \right) - \left( 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \dots \right) \right]$
- (D)  $\frac{1}{2} \left[ \left( 1 - \frac{5^2 x^2}{2!} + \frac{5^4 x^4}{4!} - \dots \right) + \left( 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \dots \right) \right]$

27. Expansion of  $\tan^{-1}x$  in ascending powers of  $x$  is

- (A)  $x + \frac{x^3}{3!} + \frac{x^5}{5!} + \dots$  (B)  $x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots$
- (C)  $x - \frac{x^3}{3} + \frac{x^5}{5} - \dots$  (D)  $x + \frac{x^3}{3} + \frac{x^5}{5} + \dots$

28. Simplified expression of  $1 + \left( x^2 - \frac{x^3}{2} + \frac{x^4}{3} - \frac{x^5}{4} + \dots \right) + \frac{1}{2} \left( x^2 - \frac{x^3}{2} + \frac{x^4}{3} - \frac{x^5}{4} + \dots \right)^2 + \dots$  on neglecting  $x^5$  and higher powers of  $x$  is

- (A)  $1 + x^2 + \frac{x^3}{2} + \frac{5x^4}{6} + \dots$  (B)  $1 + x^2 - \frac{x^3}{2} - \frac{x^4}{6} - \dots$
- (C)  $x - \frac{x^3}{3} + \frac{x^5}{5} - \dots$  (D)  $1 + x^2 - \frac{x^3}{2} + \frac{5x^4}{6} - \dots$

29. By using substitution  $x = \tan \theta$ , simplified form of  $\sin^{-1} \left( \frac{2x}{1+x^2} \right)$  is

- (A)  $\tan^{-1} x$  (B)  $2 \cot^{-1} x$
- (C)  $2 \tan^{-1} x$  (D) *none of these*

30. By using substitution  $x = \tan \theta$ , simplified form of  $\cos^{-1} \left( \frac{x+x^{-1}}{x+x^{-1}} \right)$  is

- (A)  $\frac{\pi}{2} + 2 \tan^{-1} x$  (B)  $\pi - 2 \tan^{-1} x$
- (C)  $2 \tan^{-1} x$  (D) *none of these*

31. If  $x = \log(1+y)$ , then expansion of  $y$  in ascending powers of  $x$  is

$$\begin{aligned}
 & \text{(A)} \quad x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots \quad \text{(B)} \quad x - \frac{x^2}{2!} + \frac{x^3}{3!} - \dots \\
 & \text{(C)} \quad x + \frac{x^2}{2} - \frac{x^3}{3} + \dots \quad \text{(D)} \quad -x - \frac{x^2}{2!} - \frac{x^3}{3!} - \dots
 \end{aligned}$$

TYPE-II: Taylor's Theorem and Expansion of Functions:

32. The Taylor's series expansion of  $f(x+h)$  in ascending powers of  $h$  is

$$\begin{aligned}
 & \text{(A)} \quad f(x) + hf'(x) + \frac{h^2}{2!} f''(x) + \dots \quad \text{(B)} \quad -f(x) - hf'(x) - \frac{h^2}{2!} f''(x) - \dots \\
 & \text{(C)} \quad f(0) + hf'(0) + \frac{h^2}{2!} f''(0) + \dots \quad \text{(D)} \quad f(x) - hf'(x) + \frac{h^2}{2!} f''(x) - \frac{h^3}{3!} f'''(x) + \dots
 \end{aligned}$$

33. The Taylor's series expansion of  $f(x+h)$  in ascending powers of  $x$  is

$$\begin{aligned}
 & \text{(A)} \quad f(h) - xf'(h) + \frac{h^2}{2!} f''(h) - \frac{x^3}{3!} f'''(h) + \dots \quad \text{(B)} \quad f(x) + hf'(x) + \frac{h^2}{2!} f''(x) + \dots \\
 & \text{(C)} \quad f(0) + xf'(0) + \frac{x^2}{2!} f''(0) + \dots \quad \text{(D)} \quad f(h) + xf'(h) + \frac{x^2}{2!} f''(h) + \dots
 \end{aligned}$$

34. The Taylor's series expansion of  $f(a+h)$  in ascending powers of  $h$  is

$$\begin{aligned}
 & \text{(A)} \quad f(a) + hf'(a) + \frac{h^2}{2!} f''(a) + \dots \quad \text{(B)} \quad f(h) + af'(h) + \frac{a^2}{2!} f''(h) + \dots \\
 & \text{(C)} \quad f(0) + hf'(0) + \frac{h^2}{2!} f''(0) + \dots \quad \text{(D)} \quad f(a) - hf'(a) + \frac{h^2}{2!} f''(a) - \frac{h^3}{3!} f'''(a) + \dots
 \end{aligned}$$

35. Expansion of  $f(x)$  in ascending powers of  $(x-a)$  by Taylor's theorem is

$$\begin{aligned}
 & \text{(A)} \quad f(x) + af'(x) + \frac{a^2}{2!} f''(x) + \dots \\
 & \text{(B)} \quad f(a) + (x-a)f'(a) + \frac{(x-a)^2}{2!} f''(a) + \dots \\
 & \text{(C)} \quad f(0) - (x-a)f'(0) + \frac{(x-a)^2}{2!} f''(0) - \frac{(x-a)^3}{3!} f'''(0) + \dots \\
 & \text{(D)} \quad f(a) - (x-a)f'(a) + \frac{(x-a)^2}{2!} f''(a) - \frac{(x-a)^3}{3!} f'''(a) + \dots
 \end{aligned}$$

36. First two terms in expansion of  $\log \sec x$  by Taylor's Theorem in ascending powers of  $(x-\pi/4)$  is

- (A)  $\frac{1}{2} \log 2 - \left(x - \frac{\pi}{4}\right) + \dots$       (B)  $\frac{1}{2} \log 2 + \left(x - \frac{\pi}{4}\right) \frac{1}{2} \dots$   
 (C)  $\frac{1}{2} \log 2 + \left(x - \frac{\pi}{4}\right) \dots$       (D)  $\frac{1}{2} \log 2 - \left(x - \frac{\pi}{4}\right) \frac{1}{2} \dots$

37. First two terms in expansion of  $\sqrt{x+h}$  by Taylor's Theorem in ascending powers of  $h$  is

- (A)  $\sqrt{x} + h \frac{1}{\sqrt{2}} - x + \dots$       (B)  $\sqrt{x} - \frac{h}{2} \frac{1}{\sqrt{x}} + \dots$   
 (C)  $\frac{1}{\sqrt{x}} + \frac{h}{2} \frac{1}{\sqrt{x}} + \dots$       (D)  $\sqrt{x} + \frac{h}{2} \frac{1}{\sqrt{x}} + \dots$

38. First two terms in expansion of  $\log \cos \left(x + \frac{\pi}{4}\right)$  by Taylor's Theorem in ascending powers of  $x$  is

- (A)  $\log \frac{1}{\sqrt{2}} - x + \dots$       (B)  $\log \frac{1}{\sqrt{2}} + x + \dots$   
 (C)  $\log \frac{\sqrt{3}}{2} - x + \dots$       (D)  $\log \frac{\sqrt{3}}{2} + x + \dots$

39. First two terms in expansion of  $(x+2)^5 + 3(x+2)^4$  by Taylor's Theorem in ascending powers of  $x$  is

- (A)  $48 + 98x + \dots$       (B)  $80 + 176x + \dots$   
 (C)  $80 + 98x + \dots$       (D)  $48 + 176x + \dots$

40. First two terms in expansion of  $(x-1)^5 + 2(x-1)^4$  by Taylor's Theorem in ascending powers of  $x$  is

- (A)  $3 - 13x + \dots$       (B)  $1 + 13x + \dots$   
 (C)  $1 - 3x + \dots$       (D)  $3 - 3x + \dots$

41. First two terms in expansion of  $\sinh(x+a)$  by Taylor's Theorem in ascending powers of  $x$  is

- (A)  $\sinh a + x \cosh a + \dots$       (B)  $\sinh a - x \cosh a + \dots$   
 (C)  $\cosh a + x \sinh a + \dots$       (D) *none of these*.....



42. First two terms in expansion of  $f(x+2) + 3(x+2)^3 + (x+2)^4$  by Taylor's Theorem in ascending powers of  $x$  is

- (A)  $42 + 168x + \dots$  (B)  $42 + 66x + \dots$   
 (C)  $42 + 69x + \dots$  (D)  $40 + 69x + \dots$

43. First two terms in expansion of  $e^x$  by Taylor's Theorem in ascending powers of  $(x-2)$  is

- (A)  $e^{-2} - e^2(x-2) + \dots$  (B)  $e^{-2} + e^{-2}(x-2) + \dots$   
 (C)  $e^2 - e^2(x-2) + \dots$  (D)  $e^2 + e^2(x-2) + \dots$

44. First two terms in expansion of  $\tan^{-1} x$  by Taylor's Theorem in ascending powers of  $(x-1)$  is

- (A)  $\frac{\pi}{4} - \frac{1}{2}(x-1) + \dots$  (B)  $\frac{\pi}{4} + \frac{1}{2}(x-1) + \dots$   
 (C)  $1 + \frac{1}{2}(x-1) + \dots$  (D)  $1 - \frac{1}{2}(x-1) + \dots$

45. First two terms in expansion of  $\sin x$  by Taylor's Theorem in ascending powers of  $\left(x - \frac{\pi}{2}\right)$  is

- (A)  $\left(x - \frac{\pi}{2}\right) - \frac{1}{3!}\left(x - \frac{\pi}{2}\right)^3 + \dots$  (B)  $1 + \frac{1}{2!}\left(x - \frac{\pi}{2}\right)^2 + \dots$   
 (C)  $\left(x - \frac{\pi}{2}\right) + \frac{1}{3!}\left(x - \frac{\pi}{2}\right)^3 + \dots$  (D)  $1 - \frac{1}{2!}\left(x - \frac{\pi}{2}\right)^2 + \dots$

46. First two terms in expansion of  $\log \cos x$  by Taylor's Theorem in ascending powers of  $\left(x - \frac{\pi}{4}\right)$  is

- (A)  $\log \frac{1}{2} - \left(x - \frac{\pi}{4}\right) + \dots$  (B)  $\log \frac{1}{\sqrt{2}} + \left(x - \frac{\pi}{4}\right) + \dots$   
 (C)  $\log \frac{1}{\sqrt{2}} - \left(x - \frac{\pi}{4}\right) + \dots$  (D)  $\log \frac{1}{2} + \left(x - \frac{\pi}{4}\right) + \dots$

47. First two terms in expansion of  $\sin^{-1} x$  by Taylor's Theorem in ascending powers of  $\left(x - \frac{1}{2}\right)$  is

- (A)  $\frac{\pi}{6} + \left(x - \frac{1}{2}\right) \frac{2}{\sqrt{3}} + \dots$       (B)  $\frac{\pi}{6} - \left(x - \frac{1}{2}\right) \frac{2}{\sqrt{3}} + \dots$   
 (C)  $\frac{\pi}{6} + \left(x - \frac{1}{2}\right) \frac{1}{\sqrt{2}} + \dots$       (D)  $\frac{\pi}{6} - \left(x - \frac{1}{2}\right) \frac{1}{\sqrt{2}} + \dots$

48. First two terms in expansion of  $x^{1/3}$  by Taylor's Theorem in ascending powers of  $(x-8)$  is

- (A)  $2 - (x-8) \frac{1}{12} + \dots$       (B)  $2 + (x-8) \frac{1}{12} + \dots$   
 (C)  $2 + (x-8) \frac{1}{24} + \dots$       (D)  $2 - (x-8) \frac{1}{24} + \dots$

49. First two terms in expansion of  $\sqrt{x+2}$  by Taylor's Theorem in ascending powers of  $(x-2)$  is

- (A)  $2 + (x-2) \frac{1}{4} + \dots$       (B)  $2 - (x-2) \frac{1}{4} + \dots$   
 (C)  $2 + (x-2) \frac{1}{8} + \dots$       (D)  $2 - (x-2) \frac{1}{8} + \dots$

50. In the Taylor's series expansion of  $e^x + \sin x$  about the point  $x=\pi$  the coefficient of  $(x - \pi)^2$  is

- (A)  $e^\pi$       (B)  $e^\pi + 1$   
 (C)  $e^\pi - 1$       (D)  $\frac{1}{2}e^\pi$

51. Which of the following functions will have only odd powers of  $x$  in its Taylor's series expansion about the point  $x=0$  ?

- (A)  $\sin(x^2)$       (B)  $\sin(x^3)$   
 (C)  $\cos(x^2)$       (D)  $\cos(x^3)$

## INDETERMIONATE FORMS

TYPE-I :Indeterminate Forms  $\left( \frac{0}{0}, \frac{\infty}{\infty}, 0 \times \infty, \infty - \infty \right)$

52 If  $f(x)$  and  $g(x)$  be functions such that  $f(a)=0$  and  $g(a) = 0$  then  $\lim_{x \rightarrow a} \frac{f(x)}{g(x)}$  is

is equal to .....

- (A)  $\lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$  (B)  $\lim_{x \rightarrow a} \frac{g'(x)}{f'(x)}$  (C)  $\frac{f(a)}{g(a)}$  (D) none of these

53 If  $f(x)$  and  $g(x)$  be functions such that  $f(a)=0, g(a)=0$  and  $f'(a) = 0$  then  $\lim_{x \rightarrow a} \frac{f(x)}{g(x)}$  is equal to .....

- (A)  $\frac{f'(a)}{g'(a)}$  (B)  $\lim_{x \rightarrow a} \frac{g'(x)}{f'(x)}$  (C)  $\lim_{x \rightarrow a} \frac{f''(a)}{g''(x)}$  (D) none of these

54 If  $f(x)$  and  $g(x)$  be functions such that  $f(a)=\infty$  and  $g(a)=\infty$  then  $\lim_{x \rightarrow a} \frac{f(x)}{g(x)}$  is equal to.....

- (A)  $\lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$  (B)  $\lim_{x \rightarrow a} \frac{g'(x)}{f'(x)}$  (C)  $\frac{f(a)}{g(a)}$  (D) none of these

(55)  $\lim_{x \rightarrow \pi/2} \frac{1-\sin x}{\cos x}$  is equal to ....

- (A) 1 (B) 0 (C)  $\frac{1}{2}$  (D) -1

(56)  $\lim_{x \rightarrow 0} \frac{\sin x}{x}$  is equal to

- (A) 2 (B) 0 (C) -1 (D) 1

(57)  $\lim_{x \rightarrow 0} \frac{\tan x}{x}$  is equal to

- (A) 2 (B) -1 (C)  $\frac{\pi}{2}$  (D)  $\frac{3}{2}$

(58)  $\lim_{x \rightarrow 0} \frac{\sin^{-1}x}{x}$  is equal to

- (A) 1    (B) -1    (C)  $\frac{1}{2}$     (D)  $\frac{\pi}{2}$

(59)  $\lim_{x \rightarrow 0} (1+x)^{1/x}$  is equal to

- (A) 1    (B)  $e^2$     (C)  $\frac{1}{e}$     (D) e

(60)  $\lim_{x \rightarrow 0} (1 + \frac{1}{x})^x$  is equal to

- (A) 1    (B) e    (C)  $\frac{1}{e}$     (D)  $e^2$

(61)  $\lim_{x \rightarrow 0} \frac{e^x - 1}{x}$  is equal to

- (A) 2    (B)  $\frac{1}{2}$     (C) 1    (D) none of these

(62)  $\lim_{x \rightarrow 0} \frac{a^x - 1}{x}$  is equal to

- (A) a    (B)  $-\log a$     (C)  $\log a$     (D) 1

(63)  $\lim_{\theta \rightarrow 0} \frac{\sin(\frac{\theta}{2})}{\theta}$  is equal to

- (A) 1    (B) 2    (C)  $\frac{1}{2}$     (D) not defined

(64)  $\lim_{x \rightarrow 0} \frac{\sin^2 x}{x}$  is equal to

- (A) -1    (B) 1    (C) 0    (D) not defined

(65)  $\lim_{x \rightarrow 0} \frac{1 - \cos x}{x}$  is equal to

- (A) 0    (B) 1    (C) -1    (D) 2

(66)  $\lim_{x \rightarrow 3} \frac{2x^2 - 7x + 3}{5x^2 - 12x - 9}$  is equal to

- (A)  $-\frac{1}{3}$     (B)  $\frac{2}{5}$     (C)  $\frac{5}{18}$     (D) 0

(67)  $\lim_{x \rightarrow 0} \frac{a^x - b^x}{x}$  is equal to

(A) 0      (B) 1      (C)  $\log \frac{b}{a}$       **(D)  $\log \frac{a}{b}$**

(68)  $\lim_{x \rightarrow 0} \frac{\sin^2 x}{x \cos x}$  is equal to

**(A) 0**      (B) 1      (C) -1      (D) 2

(69)  $\lim_{x \rightarrow 0} \frac{e^{ax} - e^{-ax}}{\log(1+bx)}$  is equal to

(A)  $\frac{a}{2b}$       (B) 0      (C)  $\frac{b}{2a}$       **(D)  $\frac{2a}{b}$**

(70)  $\lim_{x \rightarrow 0} \frac{(1+x^n)-1}{x}$  is equal to

**(A) n**      (B) 1      (C) e      (D) 0

(71)  $\lim_{x \rightarrow 0} \frac{2^x - 1}{\sqrt{(1+x)} - 1}$  is equal to

(A)  $\log 2$       (B)  $\frac{1}{2} \log 2$       (C) 0      **(D)  $2 \log 2$**

(72) if  $\lim_{x \rightarrow 0} \frac{\sqrt{(1+x)} - \sqrt{(1-x)}}{x}$  is equal to

(A) 0      (B) -1      **(C) 1**      (D) 2

(73) if  $\lim_{x \rightarrow 0} \frac{\sin 2x + p \sin x}{x^3}$  is finite then value of a is equal to

**(A) -2**      (B) 2      (C) 1      (D) -1

(74) if  $\lim_{x \rightarrow 0} \frac{a \sinh x - 5 \sin x}{x^3}$  is finite then value of a is equal to

(A) -5      **(B) 5**      (C) 0      (D) 10

(75) if  $\lim_{x \rightarrow 0} \frac{a \sin 2x + \tan x}{x^3}$  is finite then value of a is equal to

(A) -2    (B) 2    **(C) -1/2**    (D) 1/2

(76) if  $\lim_{x \rightarrow 0} \frac{2\cos x - 2 + bx^2}{x^4}$  is finite then value of b is equal to

(A) 2    (B) 0    **(C) 1**    (D) -1

(77) if  $\lim_{x \rightarrow \pi/4} \frac{1 - \tan x}{1 - \sqrt{2} \sin x}$  is equal to

**(A) 2**    (B) 0    (C) 1    (D) -2

(78) if  $\lim_{x \rightarrow \infty} \frac{\log x}{x^n}$  is equal to

(A) 2    (B) -2    (C) 1    **(D) 0**

(79) if  $\lim_{x \rightarrow \infty} \frac{\log(1 + e^{3x})}{x}$  is equal to

(A) 9    **(B) 3**    (C) 1/3    (D) 0

(80) if  $\lim_{x \rightarrow 0} x \log x$  is equal to

(A) 2    (B) -1    (C) 1    **(D) 0**

(81) if  $\lim_{x \rightarrow \infty} x \sin \frac{1}{x}$  is equal to

(A) 2    (B) 0    **(C) 1**    (D) -1

(82)  $\lim_{x \rightarrow 1} (1 - x) \tan \frac{\pi x}{2}$  is equal to

**(A)  $\frac{2}{\pi}$**     (B)  $0 \frac{\pi}{2}$     (C)  $\pi$     (D) 0

(83)  $\lim_{x \rightarrow \pi/2} (1 - \sin x) \tan x$  is equal to

(A) 1    (B) -1    (C)  $\pi$     **(D) 0**

(84)  $\lim_{x \rightarrow \pi/2} (\sec x - \tan x)$  is equal to

(A) 1 (B) -1 (C)  $\pi$  **(D) 0**

(85)  $\lim_{x \rightarrow \pi/2} \left( x \tan x - \frac{\pi}{2} \sec x \right)$  is equal to

(A) 1 **(B) -1** (C)  $\pi$  (D) 0

(86)  $\lim_{x \rightarrow \infty} \left( x - x^2 \log \left( 1 + \frac{1}{x} \right) \right)$  is equal to

(A) 1 (B)  $-\frac{1}{2}$  **(C)  $\frac{1}{2}$**  (D) 0

(87)  $\lim_{x \rightarrow 0} \left( \frac{1}{x} - \frac{1}{x^2} \log(1+x) \right)$  is equal to

(A) 1 (B)  $-\frac{1}{2}$  **(C)  $\frac{1}{2}$**  (D) 0

(88)  $\lim_{x \rightarrow 0} \left( \frac{1}{x} - \frac{1}{\sin x} \right)$  is equal to

(A) 1 (B)  $-\frac{1}{2}$  (C)  $\frac{1}{2}$  **(D) 0**

(89)  $\lim_{x \rightarrow 0} \left( \frac{1}{x} - \frac{1}{e^x - 1} \right)$  is equal to

(A) 1 (B)  $-\frac{1}{2}$  **(C)  $\frac{1}{2}$**  (D) 0

(90)  $\lim_{x \rightarrow \pi/2} \left( \tan x - \frac{2x \sec x}{\pi} \right)$  is equal to

**(A)  $\frac{2}{\pi}$**  (B)  $-\frac{2}{\pi}$  (C)  $\frac{\pi}{2}$  (D) 0

(91)  $\lim_{x \rightarrow 1} \left( \frac{x}{\log x} - \frac{1}{\log x} \right)$  is equal to

(A) -1 **(B) 1** (C)  $\frac{1}{2}$  (D) 0

## TYPE -2

INDETERMINATE FORMS (  $0^0$ ,  $\infty^0$ ,  $1^\infty$ ):

(92)  $\lim_{x \rightarrow \infty} \left(\frac{1}{x}\right)^{1/x}$  is equal to

- (A)  $e$  (B)  $-\frac{1}{2}$  (C)  $\frac{1}{2}$  (D) 1

(93)  $\lim_{x \rightarrow \pi/0} (\sin x)^{\tan x}$  is equal to

- (A) 1 (B)  $e$  (C)  $-1$  (D)  $\frac{1}{e}$

(94)  $\lim_{x \rightarrow \pi/2} (\cos x)^{\cos x}$  is equal to

- (A)  $-1$  (B)  $e$  (C) 1 (D)  $\frac{1}{e}$

(95)  $\lim_{x \rightarrow 0} (x)^x$  is equal to

- (A)  $e$  (B) 1 (C)  $-1$  (D) none of these

(96)  $\lim_{x \rightarrow \infty} (x)^{1/x}$  is equal to

- (A)  $e$  (B)  $-1$  (C) 1 (D) none of these

(97)  $\lim_{x \rightarrow \pi/2} (\sec x)^{\cot x}$  is equal to

- (A)  $e$  (B) 1 (C)  $\frac{1}{e}$  (D) none of these

(98)  $\lim_{x \rightarrow \infty} \left(1 + \frac{a}{x}\right)^x$  is equal to

- (A)  $e^{-a}$  (B)  $e^a$  (C) 1 (D) none of these

(99)  $\lim_{x \rightarrow 1} (x)^{\frac{1}{x-1}}$  is equal to

- (A)  $e$  (B) 1 (C)  $-1$  (D) none of these



(100)  $\lim_{x \rightarrow 0} (\cos x)^{1/x}$  is equal to

(A)  $e$  (B)  $1$  (C)  $-1$  (D) none of these

(101)  $\lim_{x \rightarrow 0} (\cos x)^{\cot x}$  is equal to

(A)  $1$  (B)  $e$  (C)  $-1$  (D) none of these

(102)  $\lim_{x \rightarrow 1} (1 - x^2)^{\frac{1}{\log(1-x)}}$  is equal to

(A)  $e$  (B)  $\frac{1}{e}$  (C)  $1$  (D)  $e^2$

(103)  $\lim_{x \rightarrow 0} \left( \frac{a+x}{a-x} \right)^{1/x}$  is equal to

(A)  $e^{2/a}$  (B)  $e^{1/2a}$  (C)  $1$  (D)  $e^{a/2}$

(104)  $\lim_{x \rightarrow 0} (1 + \sin x)^{\cot x}$  is equal to

(A)  $e^{1/2}$  (B)  $e^2$  (C)  $1$  (D)  $e$

(105)  $\lim_{x \rightarrow \pi/2} (\operatorname{cosec} x)^{\tan x}$  is equal to

(A)  $e^{-1}$  (B)  $e^2$  (C)  $1$  (D)  $e$

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