

Rules for means.

If  $X$  is a random variable and  $a$  and  $b$  are fixed numbers, then  $\mu_{a+bX} = a + b\mu_X$

If  $X$  and  $Y$  are random variables, then  $\mu_{X+Y} = \mu_X + \mu_Y$

Rules for variances and standard deviations:

If  $X$  is a random variable and  $a$  and  $b$  are fixed numbers, then  $\sigma_{a+bX}^2 = b^2\sigma_X^2$

If  $X$  and  $Y$  are independent random variables, then  $\sigma_{X+Y}^2 = \sigma_X^2 + \sigma_Y^2$  and  $\sigma_{X-Y}^2 = \sigma_X^2 + \sigma_Y^2$

If  $X$  and  $Y$  have correlation  $\rho$ , then  $\sigma_{X+Y}^2 = \sigma_X^2 + \sigma_Y^2 + 2\rho\sigma_X\sigma_Y$  and  $\sigma_{X-Y}^2 = \sigma_X^2 + \sigma_Y^2 - 2\rho\sigma_X\sigma_Y$

Definition of conditional probability:  $P(B/A) = \frac{P(A \text{ and } B)}{P(A)}$

Normal approximation to the binomial distribution:

If  $X$  is a count having the  $B(n, p)$  distribution, then when  $n$  is large,

$X$  is approximately  $N(np, \sqrt{np(1-p)})$

The sample proportion  $\hat{p} = \frac{X}{n}$  is approximately  $N\left(p, \sqrt{\frac{p(1-p)}{n}}\right)$

We will use these approximations when  $np \geq 10$  and  $n(1-p) \geq 10$ .