* Space complexity or Auxilary Space :-

1) Auxilary space :- It is the extra space or temporary space taken by an algorithm.

∴ Space complexity = input space + Auxilary space.

Suppose :-
Take an ip of array ~~size~~ size N & do something with it.
So the sap: Space complexity will be the input you're taking from the size N + extra space the algo is using
This is known as Space complexity.

- So, in the binary search the space complexity was constant. So, that means auxilary space was constant it was not taking any extra space.
- Taking 3 variable i.e Start, End & Mid.
- If the array is of size 100 or more than that. Every single time it's only going to take 3 that variable i.e start, end & mid.
Hence, constant

Q

```
for( i = 1 ; i ≤ N ; ' ){
    for( j = 1 ; j ≤ k ; j++) {
        // some operations that
           takes time at t
    }
    i = i+k
}
```

Here,

1) inner loop is running k times & for every time it's running it's taking t amount of time.

∴ $O(kt)$ time.

2) If inner loop is running once, once, so it's taking t amount of time. So, here it's actully running k times. Hence kt.

3) Ans :- $O(kt *$ times outer loop is running)

conditions :- here i will starts from 1, & the loop will break when i is ≤ N & i is incrementing with k

4) So let's say, $i_{last} = 1, 1+k, 1+2k, 1+3k \ldots 1+xk$
So, if the x^{th} value is 'xk' that means is & satisfy the condions. Hence x should be ≤ N

'1+xk is the value & x is the no. of times its running

$\therefore 1 + xk \leq N$

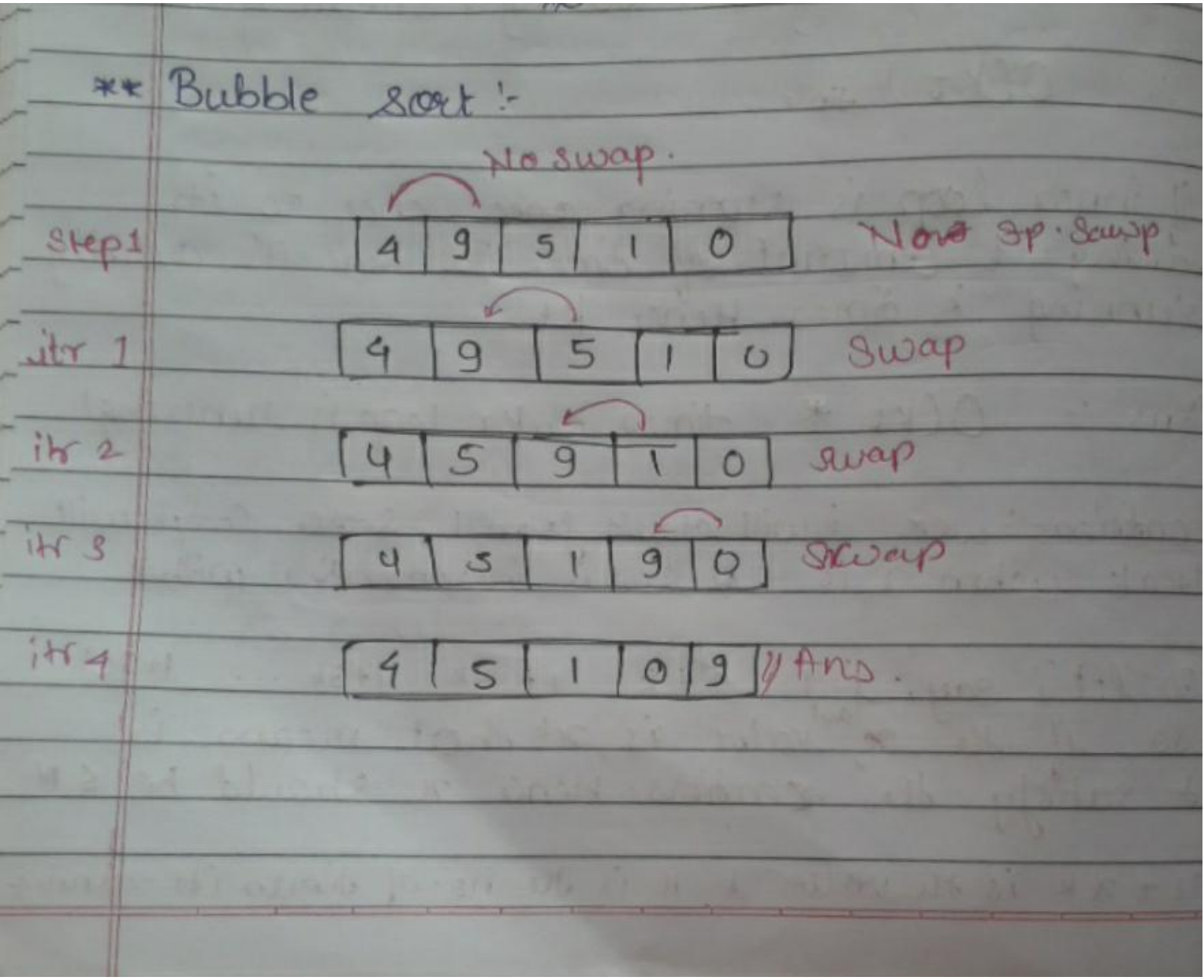
$xk \leq N-1$

$\therefore x = \frac{N-k}{k}$ — x = no of times the outer loop is running

Complexity : $O\left(kt * \frac{(N-1)}{k}\right)$ — const are removed

$\therefore = O(N * t)$

** Bubble sort :-


No swap.
step1
4 9 5 1 0
No sp. swap
itr 1
4 9 5 1 0
swap
itr 2
4 5 9 1 0
swap
itr 3
4 5 1 9 0
swap
itr 4
4 5 1 0 9
// Ans.

* Worst & Average case time complexity :-
O(n*n)
Worst case occurs when array is reverse sorted.

* Best case time complexity :-
O(n)
Best case occurs when array is already sorted

* Auxilary space
O(1)

* Boundary cases :-
Bubble sort takes minimum time (order of n) when elements are already sorted.

* Sorting in place :- Yes

* Stable :- Yes

** Selection Sort :

Worst complexity : n^2

Average complexity : n^2

Best complexity : n^2

Space complexity : 1

Method : Selection

Stable : No

Note: The good thing about selection sort is it never makes more than O(n) swaps & can be useful when memory write is a costly operation.

Eg:- (max) 4 , 5 , 1 , 2 , 3 — swap 5 & 3

4 , 3 , 1 , 2 , 5 — swap 4 & 2

2 , 3 , 1 , 4 , 5 — swap 3 & 1

2 , 1 , 3 , 4 , 5 — swap 2 & 1

1 , 2 , 3 , 4 , 5 ✓

** Insertion sort :-

Time complexity :- O(n * 2)

Auxiliary Space :- O(1)

Boundary Cases :- Insertion sort takes a maximum time to sort if element are sorted in reverse order. And it takes minimum time (Order of n) when elements are already sorted.

Sorting in Place :- Yes.

Eg :- 5 , 3 , 4 , 1 , 2

(Swap)

3 , 5 , 4 , 1 , 2

(sort & swap)

3 , 4 , 5 , 1 , 2

(sort)

1 , 3 , 4 , 5 , 2

(sort)

1 , 2 , 3 , 4 , 5 #.