# 291K Deep Learning for Machine Translation Recurrent Neural Network Sequence to sequence learning

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## Outline

- Language Modeling
- Recurrent Neural Network
- Long-short term memory network (LSTM)
- Gated Recurrent Unit (GRU)
- Attention
- Encoder-decoder framework
- LSTM Seq2seq

# Language Modeling

Given a sentence y, estimate the probability

$$-P(y) = \prod_{t} P(y_{t+1} | y_1...y_t)$$

$$-P(y_{t+1} | y_1...y_t) = f_{\theta}(y_1, ..., y_t)$$

$$\text{mat} \quad 0.15$$

$$\text{rug} \quad 0.13$$

$$\text{The cat sits on a} \quad \text{chair} \quad 0.08$$

$$\text{Y}_1 \quad \text{Y}_2 \quad \text{Y}_3 \quad \text{Y}_4 \quad \text{Y}_5 \quad \text{Y}_6 \quad \text{hat} \quad 0.05$$

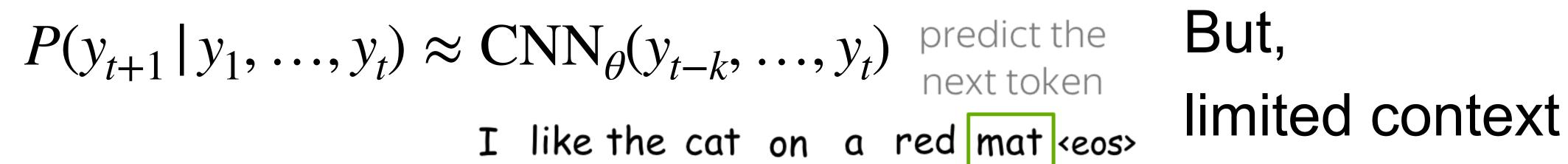
$$\text{dog} \quad 0.01$$

## **Predict Next Token Probability**

There are many methods to predict the next token:

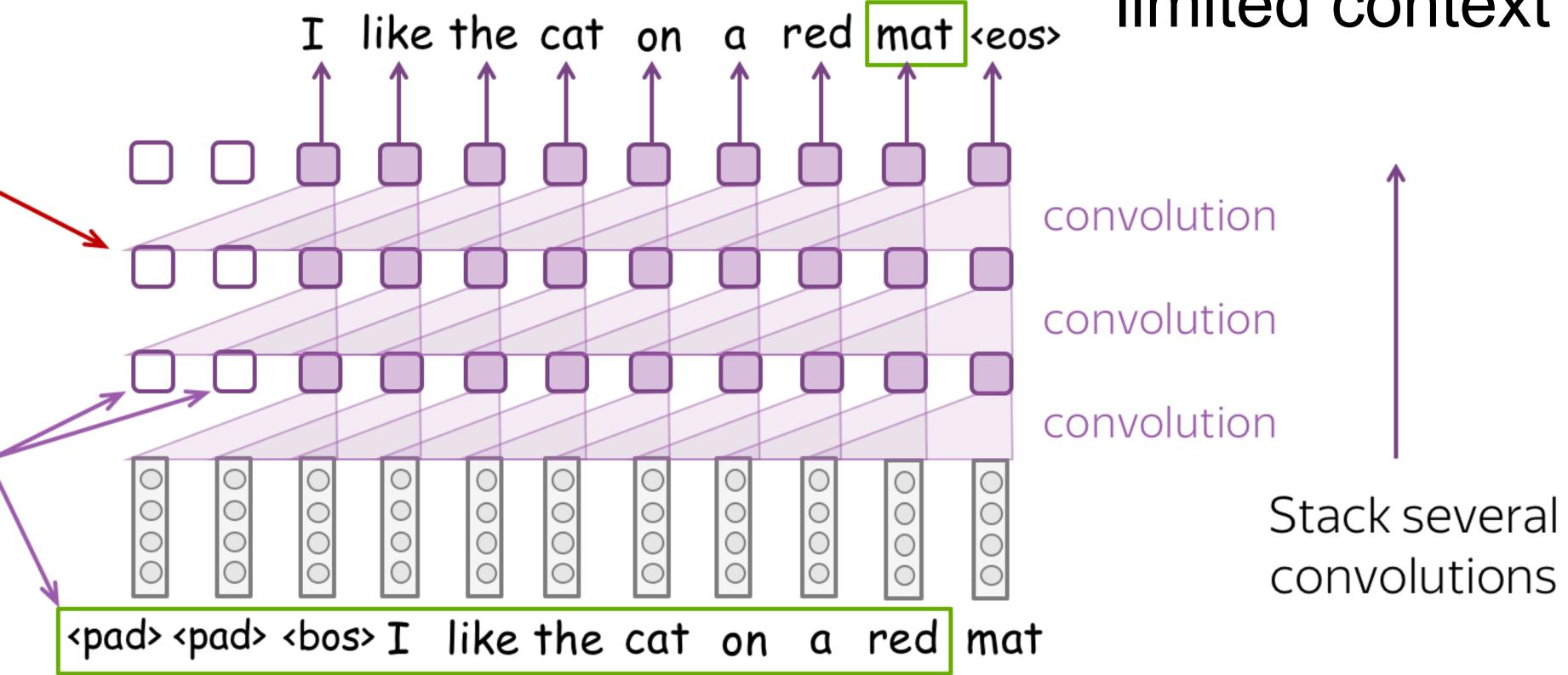
- N-gram: assuming  $p(x_t \mid x_1,..., x_{t-1}) = p(x_t \mid x_{t-k},..., x_{t-1}),$  and estimate it directly
- Context MLP: use DNN to estimate  $p(x_t | x_{t-k}, ..., x_{t-1})$
- CNN-LM (previous lecture)
- RNN-LM, LSTM, GRU
- GPT

# CNN Language Model (recap)



No pooling between convolutions: do not want to lose positional information

Padding to shift tokens: we need to prevent information flow from future tokens



condition on the previous tokens

## Limitation of CNN-LM

- CNN-LM only has a fixed-length receptive field
  - probability of next token only dependent on a fixed-size context
- But sentences are of variable length
- How to handle sentences with variable length?
- Idea:
  - adding memory to network
  - adaptive updating memory

## Recurrent Memory

- Introduce memory representation
- RNN-LM: use RNN to estimate

$$p(x_t | x_1, ..., x_{t-1}) = \operatorname{softmax}(W \cdot h_t)$$

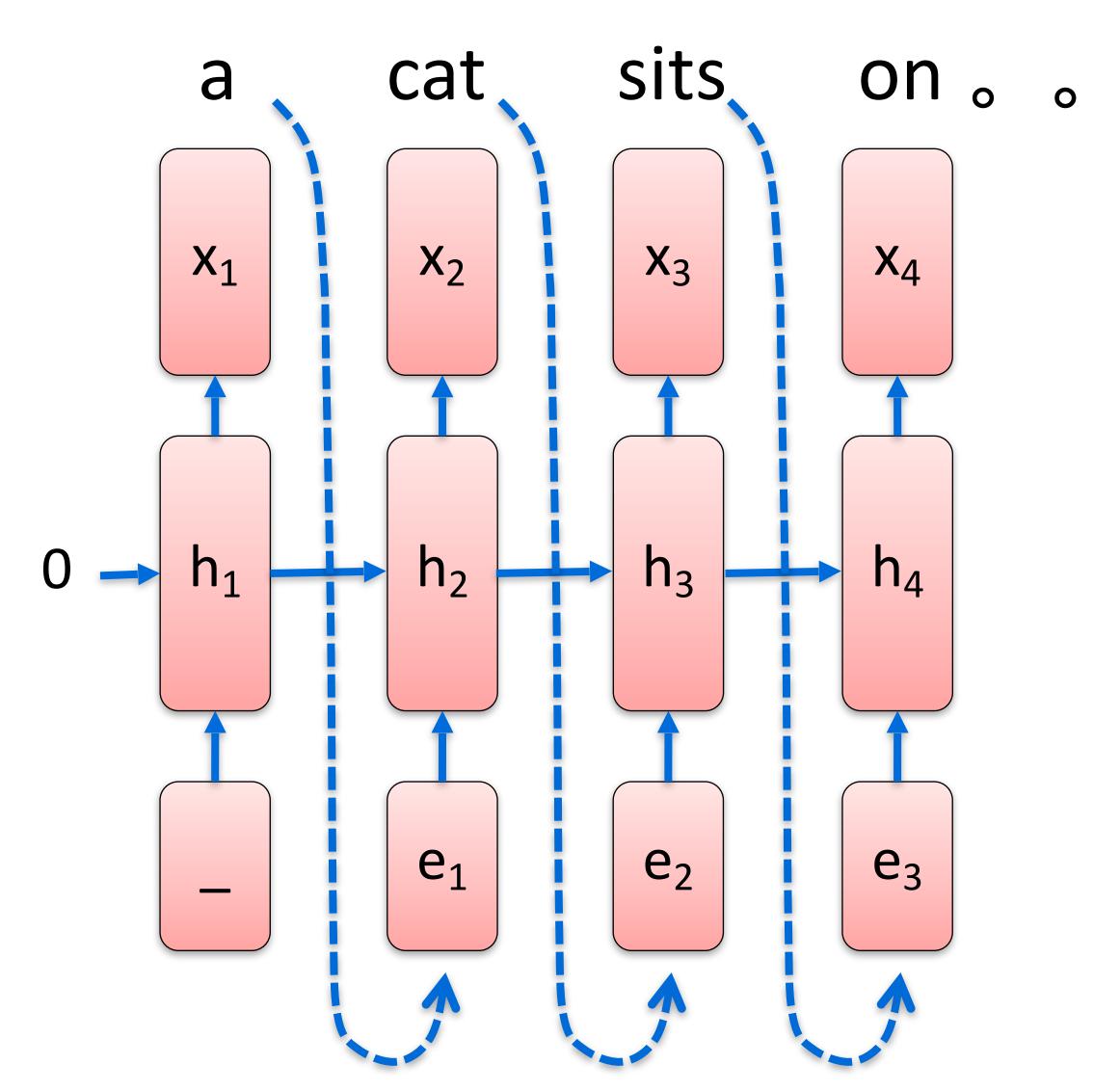
$$h_t = RNN(h_{t-1}, Emb(x_{t-1}))$$

- RNN cell can be
  - Simple feedforward neural network
  - Long-short term memory
  - Gated recurrent units

## Recurrent Neural Network

$$p(x_t | x_1, ..., x_{t-1}) = \operatorname{softmax}(U \cdot h_t)$$

$$h_t = \sigma \left( W \cdot \begin{bmatrix} h_{t-1} \\ x_t \end{bmatrix} + b \right)$$



# Training RNN-LM

#### Risk:

- Loss: cross-entropy for every next-token given prefix context
- $-CE(x_t+1, f(x_1, ..., x_t))$
- SGD
  - Calculate gradient: Back-propagation through time (BPTT)
  - $-\nabla E_t$

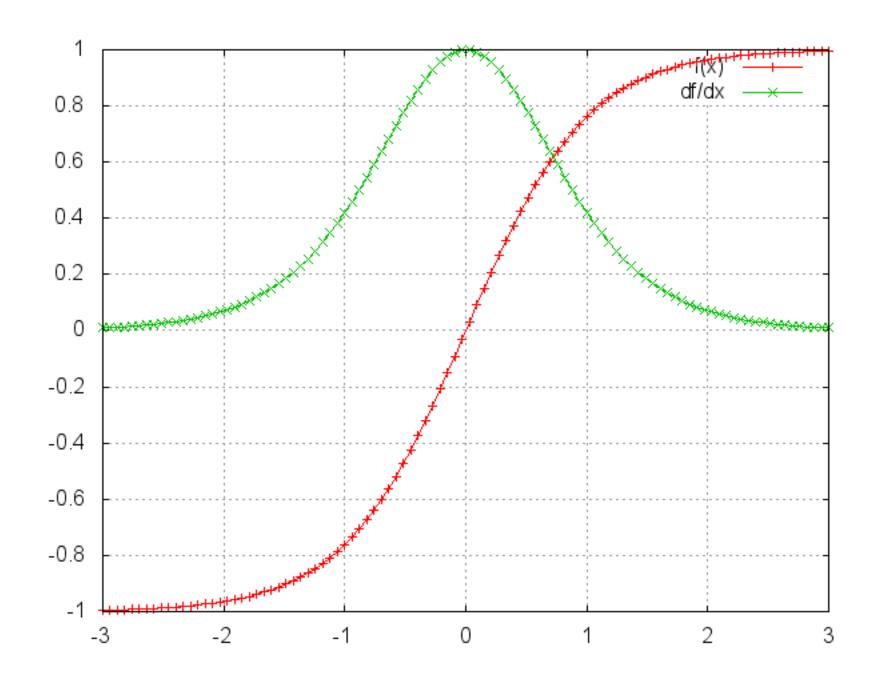
## Exercise: Gradient for RNN

# Back-propagation for RNN (python)

```
def bptt(self, x, y):
        T = len(y)
       # Perform forward propagation
        o, s = self.forward_propagation(x)
        # We accumulate the gradients in these variables
 6
        dLdU = np.zeros(self.U.shape)
        dLdV = np.zeros(self.V.shape)
8
        dLdW = np.zeros(self.W.shape)
9
        delta_o = o
10
        delta_o[np.arange(len(y)), y] -= 1.
11
        # For each output backwards...
12
        for t in np.arange(T)[::-1]:
13
            dLdV += np.outer(delta_o[t], s[t].T)
14
            # Initial delta calculation: dL/dz
15
            delta_t = self.V.T.dot(delta_o[t]) * (1 - (s[t] ** 2))
16
            # Backpropagation through time (for at most self.bptt_truncate steps)
17
            for bptt_step in np.arange(max(0, t-self.bptt_truncate), t+1)[::-1]:
18
                # Add to gradients at each previous step
19
                dLdW += np.outer(delta_t, s[bptt_step-1])
20
                dLdU[:,x[bptt_step]] += delta_t
                # Update delta for next step dL/dz at t-1
                delta_t = self.W.T.dot(delta_t) * (1 - s[bptt_step-1] ** 2)
22
23
        return [dLdU, dLdV, dLdW]
```

# Computational Issue: Gradient Vanishing

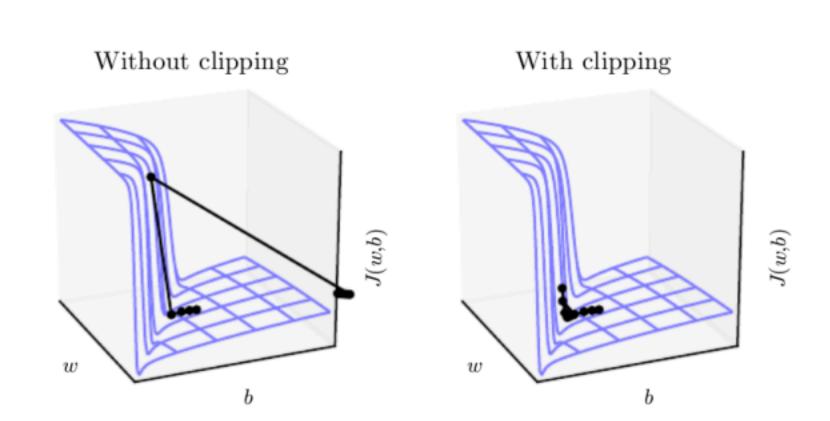
tanh has derivative close to zero at both ends



# Gradient Exploding

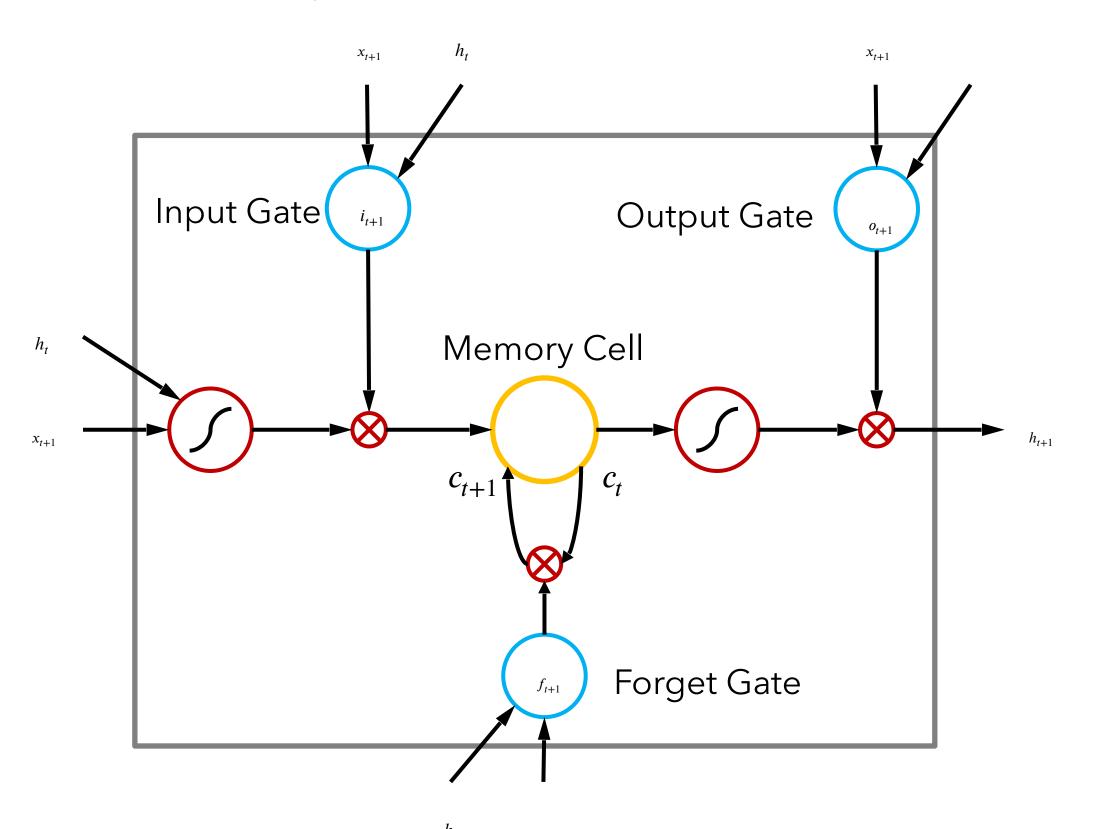
- Use gradient clipping
- Two options: clip by absolute value or rescale norm

• if 
$$|g| > \eta$$
,  $\hat{g} \leftarrow \eta$   
• if  $|g| > \eta$ ,  $\hat{g} \leftarrow \frac{\eta}{|g|} g$ 



# Long-Short Term Memory (LSTM)

- Replace cell with more advanced one
- Adaptively memorize short and long term information



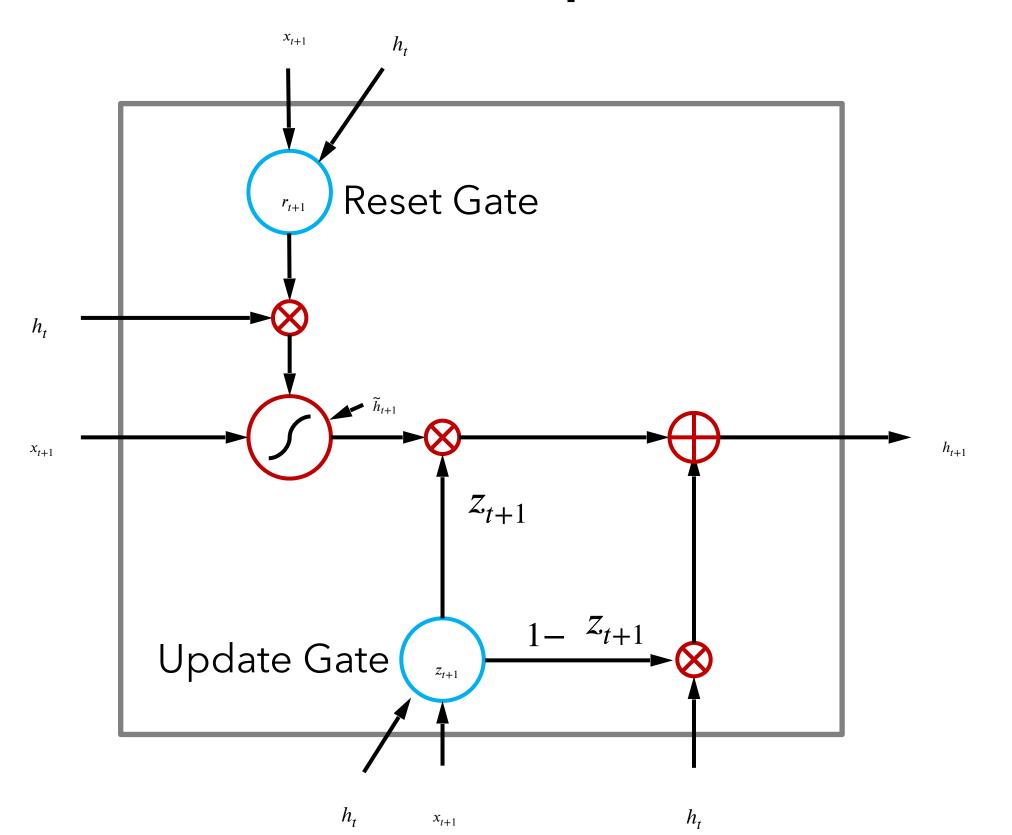
$$\begin{split} i_{t+1} &= \sigma(M_{ix}x_{t+1} + M_{ih}h_t + b_i) \\ f_{t+1} &= \sigma(M_{fx}x_{t+1} + M_{fh}h_t + b_f) \\ o_{t+1} &= \sigma(M_{ox}x_{t+1} + M_{oh}h_t + b_o) \\ a_{t+1} &= \tanh(M_{cx}x_{t+1} + M_{ch}h_t + b_a) \end{split}$$

$$c_{t+1} = f_{t+1} \otimes c_t + i_{t+1} \otimes a_{t+1}$$

$$h_{t+1} = o_{t+1} \otimes \tanh(c_{t+1})$$

# Gated Recurrent Unit (GRU)

- Adaptively memorize short and long term information
- like LSTM, but fewer parameters



Input:  $x_t$ Memory:  $h_t$ 

$$r_{t+1} = \sigma(M_{rx}x_{t+1} + M_{rh}h_t + b_r)$$
  

$$z_{t+1} = \sigma(M_{zx}x_{t+1} + M_{zh}h_t + b_z)$$

$$\tilde{h}_{t+1} = \tanh(M_{hx}x_{t+1} + M_{hh}(r_{t+1} \otimes h_t) + b_h)$$

$$h_{t+1} = z_{t+1} \otimes \tilde{h}_{t+1} + (1 - z_{t+1}) \otimes h_t$$

Cho et al. Learning Phrase Representations using RNN Encoder–Decoder for Statistical Machine Translation. 2014 15

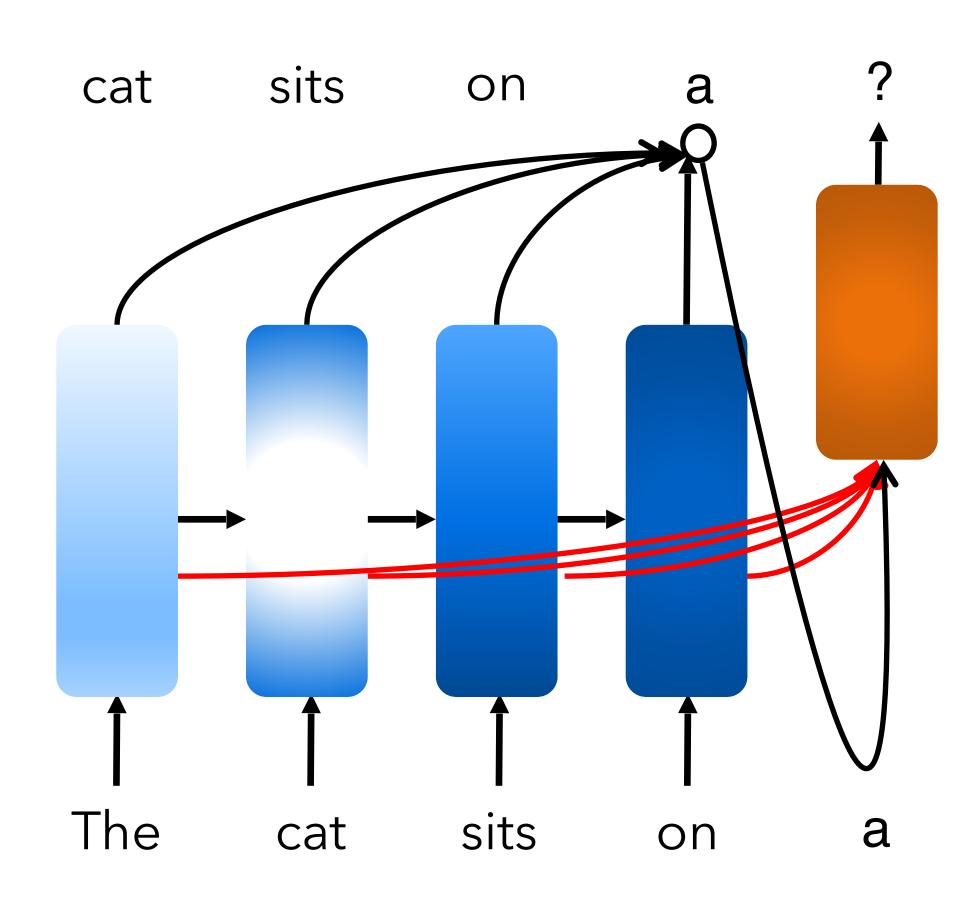
# Expressive power of RNN-LM

Perplexity: 
$$PPL = P(x_1, ..., x_N)^{-\frac{1}{N}} = \exp(-\frac{1}{N} \sum_{n=1}^{N} \log P(x_n | x_1 ... x_{n-1}))$$

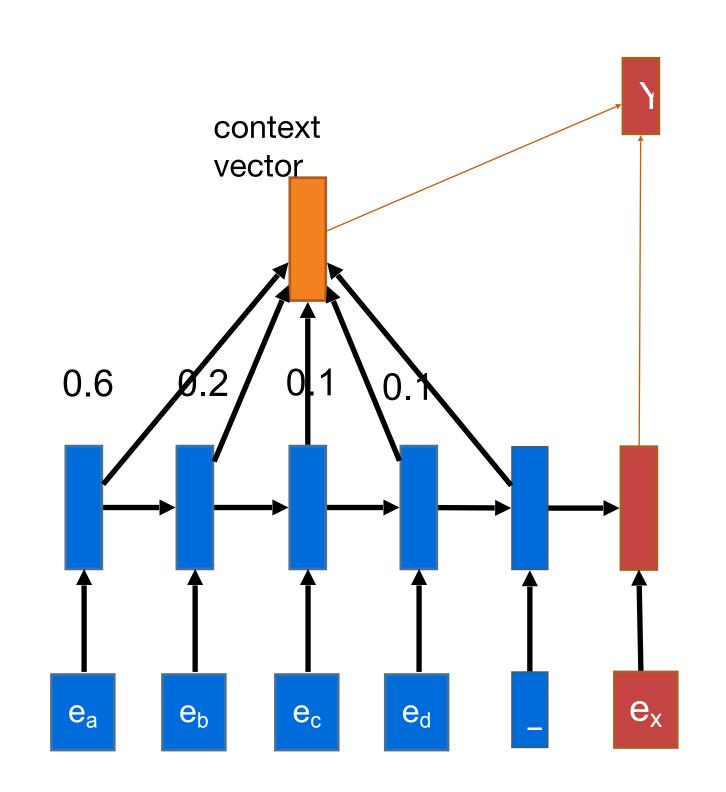
Model	TEST PERPLEXITY	Number of Params [billions]
SIGMOID-RNN-2048 (JI ET AL., 2015A)	68.3	4.1
INTERPOLATED KN 5-GRAM, 1.1B N-GRAMS (CHELBA ET AL., 2013)	67.6	1.76
SPARSE NON-NEGATIVE MATRIX LM (SHAZEER ET AL., 2015)	52.9	33
RNN-1024 + MAXENT 9-GRAM FEATURES (CHELBA ET AL., 2013)	51.3	20
LSTM-512-512	54.1	0.82
LSTM-1024-512	48.2	0.82
LSTM-2048-512	43.7	0.83
LSTM-8192-2048 (No Dropout)	37.9	3.3
LSTM-8192-2048 (50% DROPOUT)	32.2	3.3
2-Layer LSTM-8192-1024 (BIG LSTM)	30.6	1.8
BIG LSTM+CNN INPUTS	30.0	1.04
BIG LSTM+CNN INPUTS + CNN SOFTMAX	39.8	0.29
BIG LSTM+CNN INPUTS + CNN SOFTMAX + 128-DIM CORRECTION	35.8	0.39
BIG LSTM+CNN INPUTS + CHAR LSTM PREDICTIONS	47.9	0.23

Jozefowicz et al. Exploring the limits of language modelling, 2016

#### Attention



#### Generation by Attention



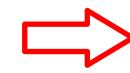
A context vector c will be predicted before, which represents the related source context for current predicted word.

$$\alpha_{nj} = \text{Softmax}(D(s_n, h_{1...n-1})) = \frac{\exp(D(s_n, h_j))}{\sum_k \exp(D(s_n, h_k))}$$

$$c_n = \sum_{j} \alpha_{nj} h_j$$

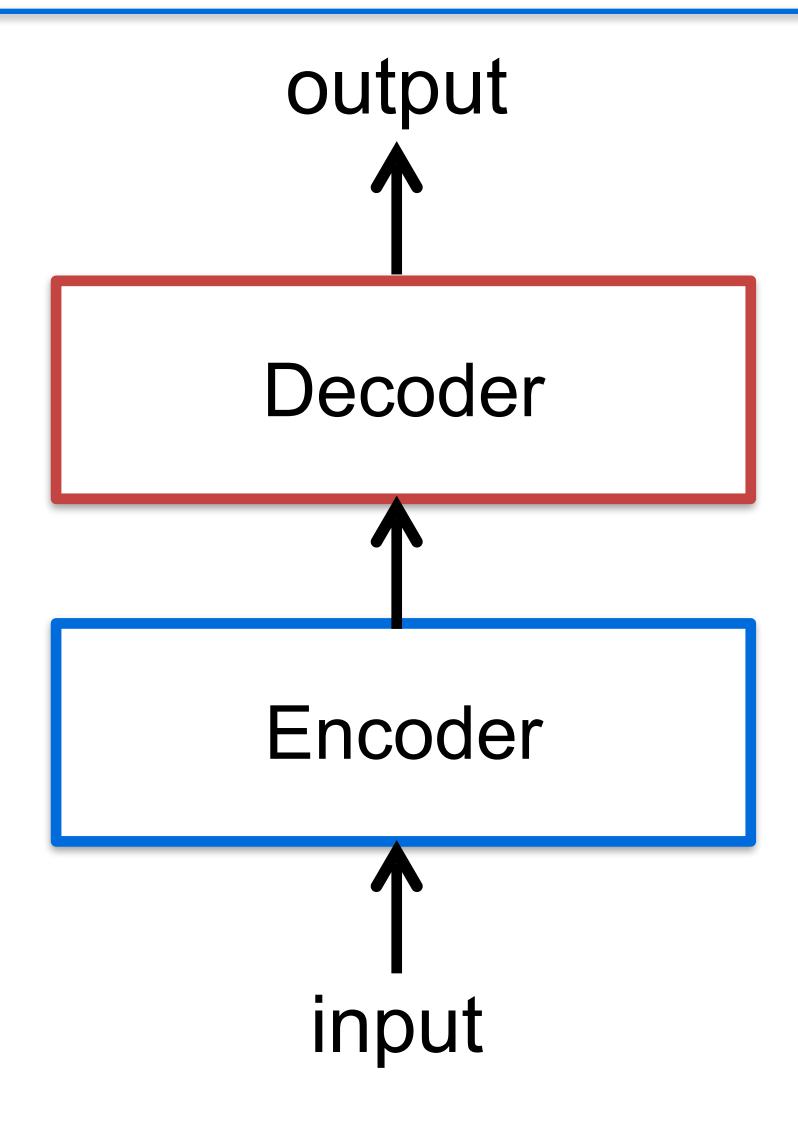
The probability of word y\_i is computed as:

$$p(y_i) \propto \exp(Wh_i)$$





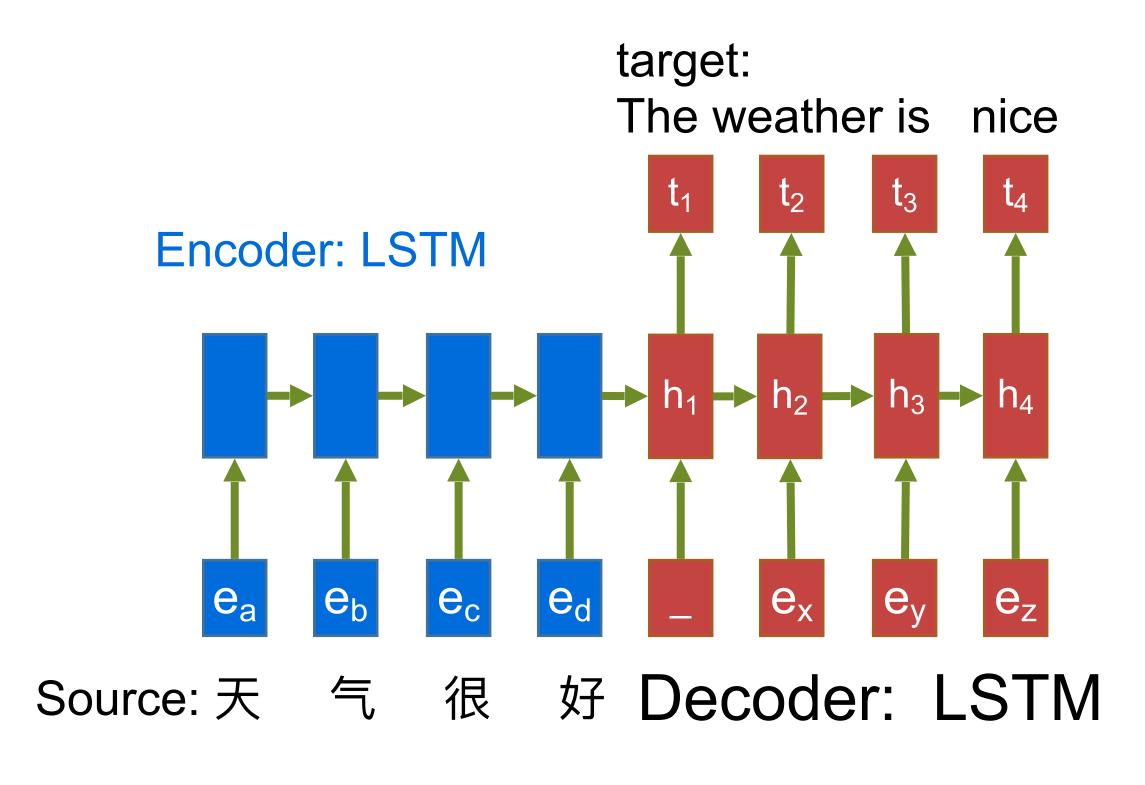
## Encoder-decoder framework



A generic formulation
ImageCaption
Text-to-Image Generation
ASR (speech-to-text)
MT (text-to-text)

# Sequence To Sequence (Seq2seq)

 Machine translation as directly learning a function mapping from source sequence to target sequence



$$P(Y|X) = \prod P(y_t|y_{< t}, x)$$

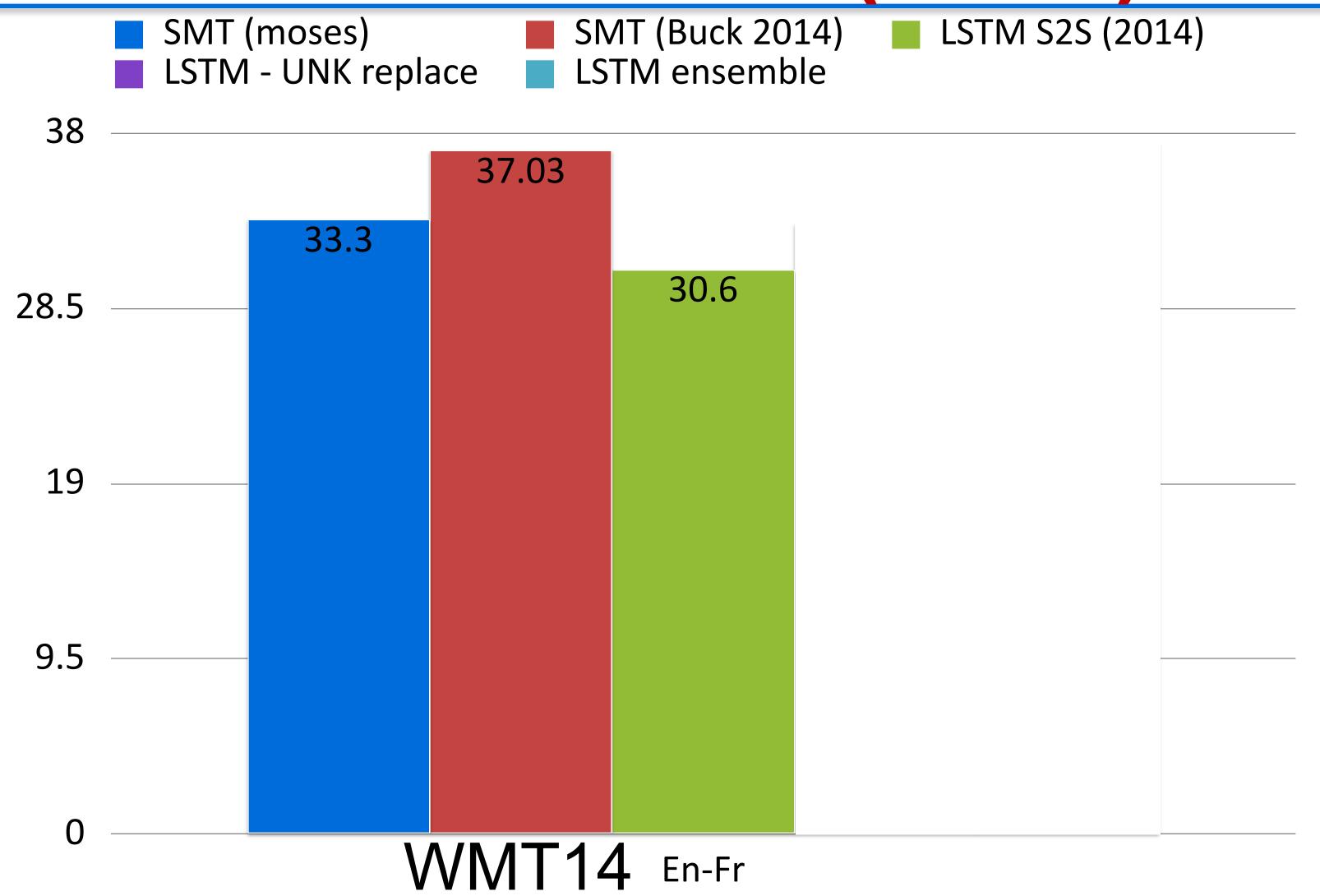
Training loss: Cross-Entropy

$$l = -\sum_{n} \sum_{t} \log f_{\theta}(x_n, y_{n,1}, ..., y_{n,t-1})$$

Teacher-forcing during training.

(pretend to know groundtruth for prefix)

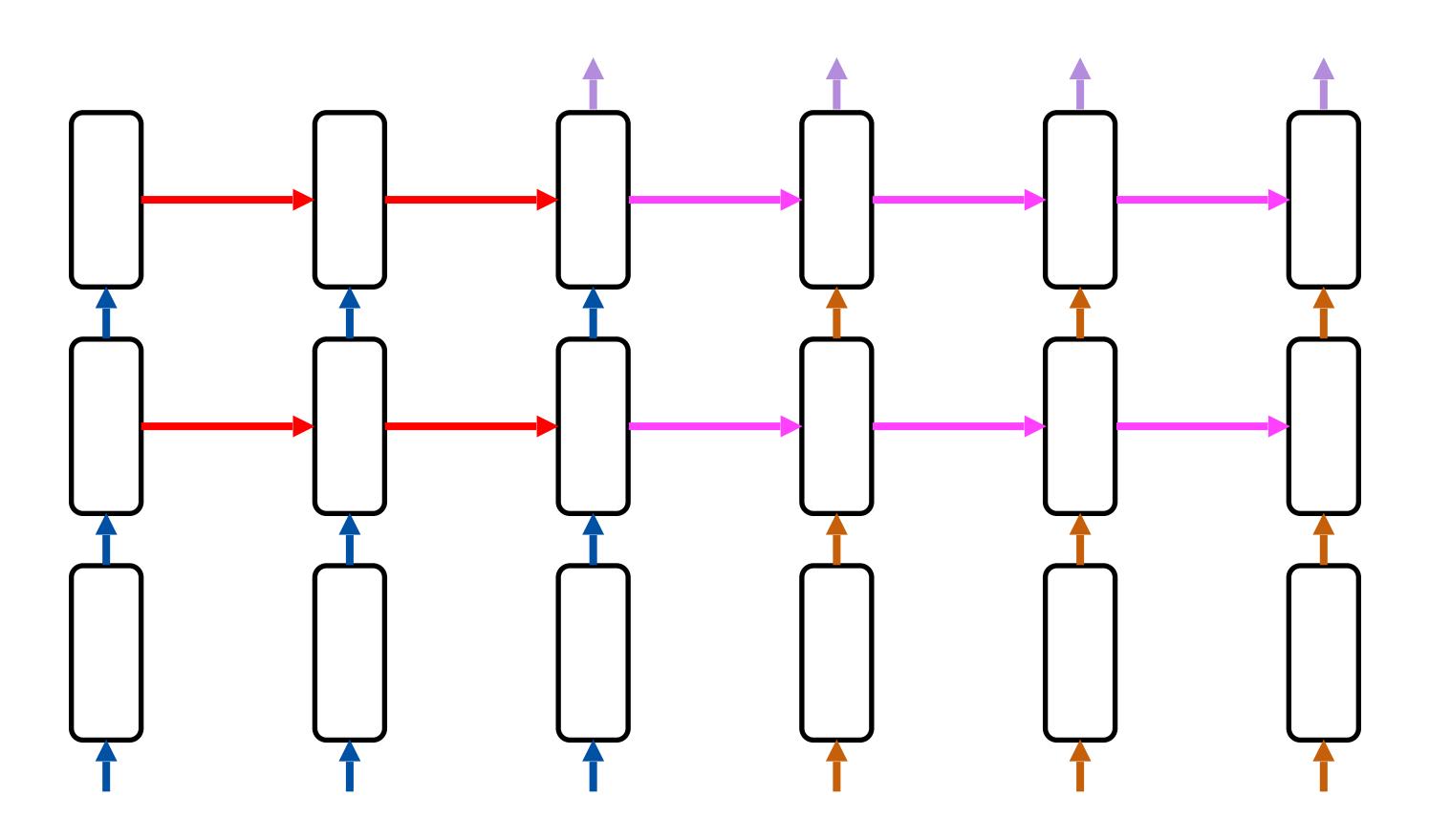
# Performance (2014)



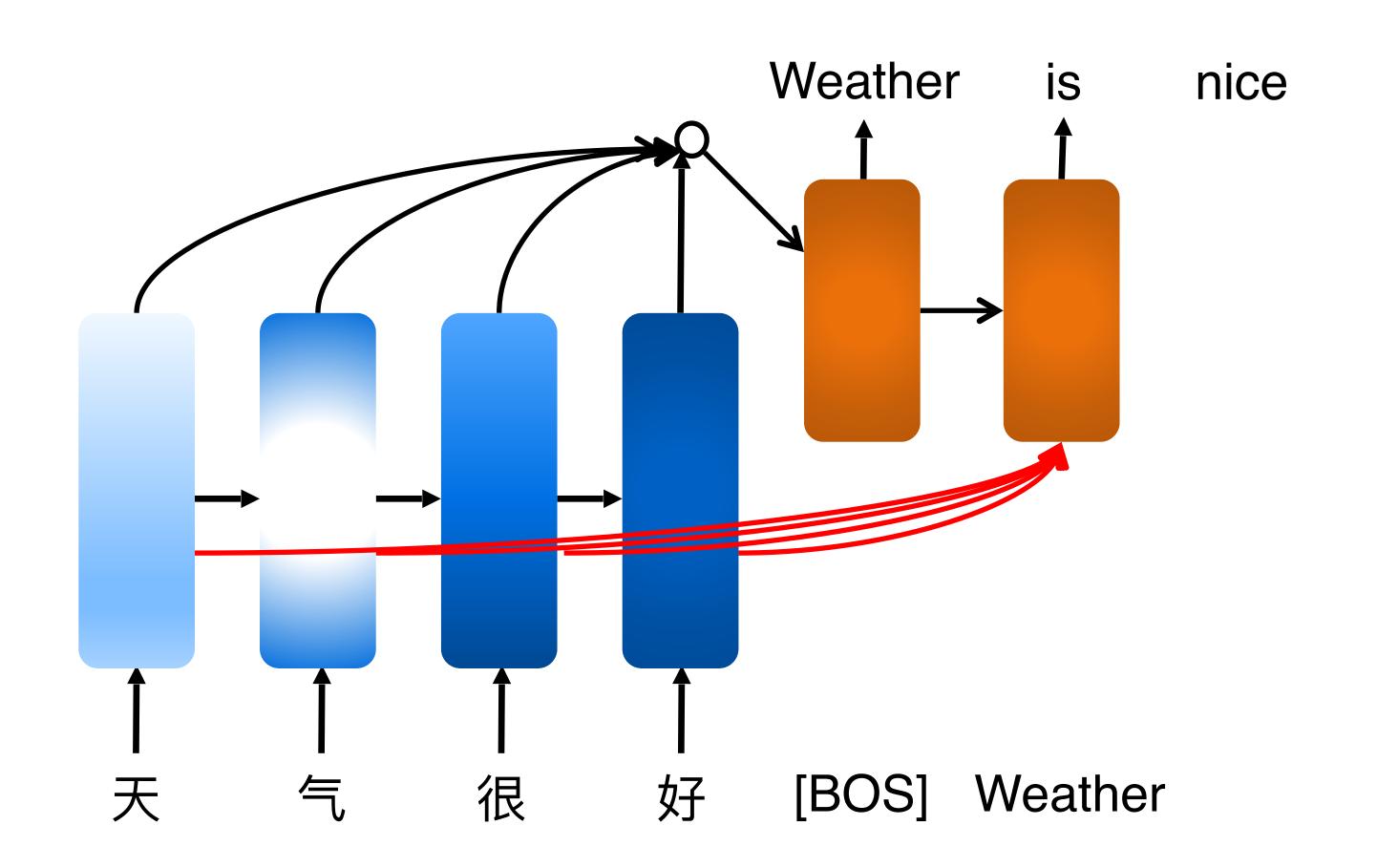
Sutskever et al. Sequence to Sequence Learning with Neural Networks. 2014 Durrani et al. Edinburgh's Phrase-based Machine Translation Systems for WMT-14. 2014

# Stacked LSTM for seq-2-seq

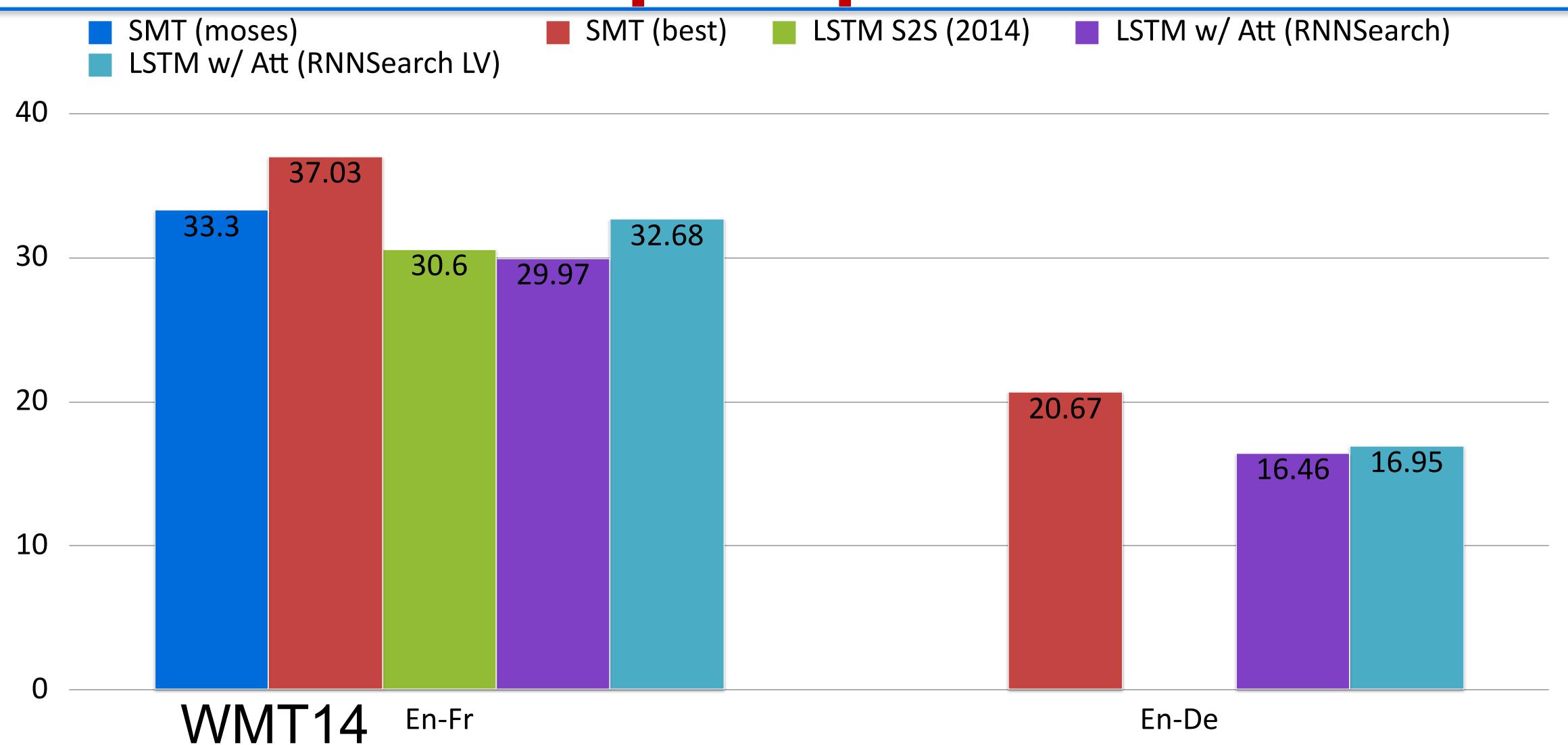
More layers of LSTM



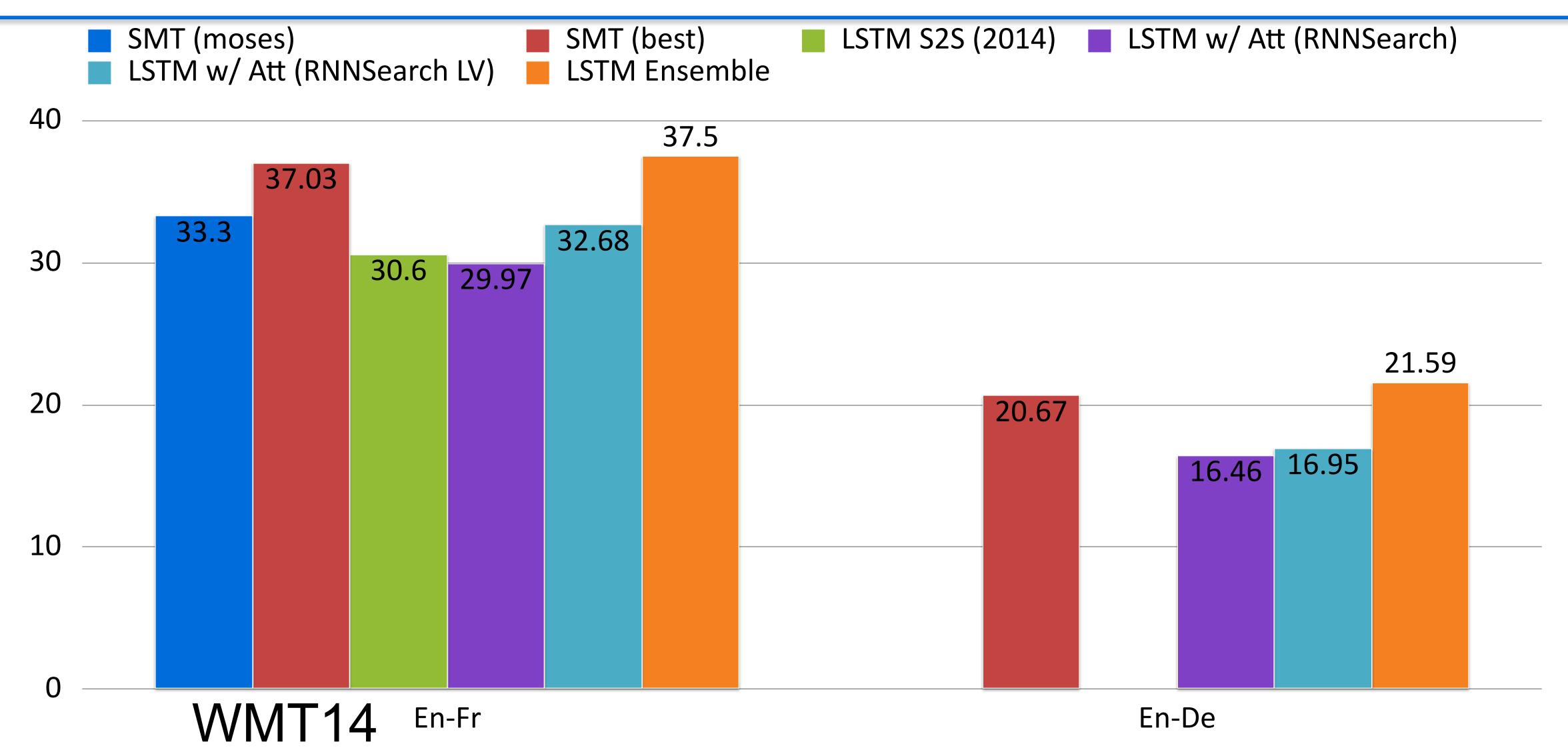
## LSTM Seq2seq with Attention



# LSTM Seq2Seq w/ Attention



## Performance with Model Ensemble



# Reading

- Gers et al. Learning to Forget: Continual Prediction with LSTM. 2000
- Sutskever et al. Sequence to Sequence Learning with Neural Networks. 2014
- Bahdanau et al., Neural Machine Translation by Jointly Learning to Align and Translate. 2015
- Luong et al. Effective Approaches to Attention-based Neural Machine Translation. 2015