




# 课后作业 (Assignments)

## 一、阅读 (Reading)

1. 阅读教材.
2. 课外阅读:

 逻辑的引擎 (电子图书, 仅供学习, 不可非法传播).pdf

 propositional logic (2) -dnf (by gordon j. pace).pdf

 主析取范式的求法及其应用.pdf

## 二、问题解答 (Problems)

1. 请分析总结定理 1.3 的证明思路, 并完成未证明部分.
2. 教材 P29 题 8.
3. 教材 P29 题 9 (1, 3, 5) .
4. 教材 P29 题 10 (3, 4) .
5. 教材 P29 题 11 (3, 4) .
6. 教材 P29 题 12 (2, 3, 4) .
7. Use other equivalences to prove the equivalence

$$A \rightarrow B \equiv A \wedge \neg B \rightarrow \text{False}.$$

$$A \wedge \neg B \rightarrow \text{False} \equiv \neg (A \wedge \neg B) \vee \text{False} \equiv \neg (A \wedge \neg B) \equiv \neg A \vee \neg \neg B \equiv \neg A \vee B \equiv A \rightarrow B.$$

8. Show that  $\rightarrow$  is not associative.

That is, show that  $(A \rightarrow B) \rightarrow C$  is not equivalent to  $A \rightarrow (B \rightarrow C)$ .

$$A=B=0 ?$$

9. For each of the following functions, write down the full DNF and full CNF representations.

a.  $f(P, Q) = \text{True}$  if and only if  $P$  is True.

b.  $f(P, Q, R) = \text{True}$  if and only if either  $Q$  is True or  $R$  is False.

a. Full DNF:  $(P \wedge Q) \vee (P \wedge \neg Q)$ . Full CNF:  $(P \vee \neg Q) \wedge (P \vee Q)$ .

b. Full CNF:  $(P \vee Q \vee \neg R) \wedge (\neg P \vee Q \vee \neg R)$ ,  $m_1 \wedge m_5$ .

Full DNF:  $m_0 \vee m_2 \vee m_3 \vee m_4 \vee m_6 \vee m_7$

### 三、项目实践 (Programming) (Optional)

1. 输入命题公式, 求解命题公式主范式. 请应用你的程序求解 — (4, 5) 题.