

$$U_{\max} = 3 \text{ J}$$

$$U = mgh$$

$$K = \frac{1}{2}mv^2$$

measurements & constants:

$$\text{mass } m = 0.08 \text{ kg}$$

$$\text{gravity } g = 9.81 \text{ m/s}^2$$

$$\text{launch } \theta = 80^\circ$$

assuming $\frac{1}{2}$ goes into rotation,

$$U_{\text{translation}} = 1.5 \text{ J}$$

$$U_0 + K_0 = U + K$$

$$1.5 + 0 = 0 + \frac{1}{2}mv^2 = \frac{1}{2} \cdot 0.08 \cdot v^2$$

$$v = \sqrt{\frac{1.5 \cdot 2}{0.08}} = \sqrt{\frac{300}{8}} = 6.12 \text{ m/s}$$

solving for max Δy :

$$v_y = v \cdot \sin \theta = 6.03 \text{ m/s}$$

$$v_f^2 = v_0^2 + 2ad \text{ where } v_0 = 0 \text{ \& } a = g$$

$$y_{\max} = \frac{v_y^2}{2g} = \boxed{1.85 \text{ m}}$$

solving for Δx max:

$$v_f = v_0 + at \text{ where } v_0 = 0 \text{ \& } a = g$$

$$t = \frac{v_y}{g} = 0.61 \text{ sec}$$

$$x_{\max} = v_x \cdot t = v \cdot \cos(\theta) \cdot t = \boxed{0.65 \text{ m}}$$

overall, there is a fair amount of energy that is lost to heat, as well as rotation, which is important to the theatrical performance.

I'd guess that my final hopper will jump about $\boxed{1.0 \text{ m}}$ upwards and $\boxed{0.5 \text{ m}}$ sideways.

recalculating w/

my prototype, which stores 2 J energy:

$$v = \sqrt{\frac{2}{0.08}} = 5 \text{ m/s}$$

$$v_y = v \cdot \sin \theta = 4.92 \text{ m/s}$$

$$y_{\max} = \frac{v_y^2}{2g} = \boxed{1.23 \text{ m}}$$

$$t = \frac{v_y}{g} = 0.50 \text{ sec}$$

$$x_{\max} = v \cdot \cos \theta \cdot t = \boxed{0.43 \text{ m}}$$

this estimate makes sense,

comparing to my

slow video where

my hopper travelled

about 1 foot sideways, 2 feet upwards

$(0.3, 0.6)$ as compared to

$(0.43, 1.23)$. This shows

that I have overestimated

by a bit, but not

too much.