

PHY566 Group Project 2b

Predator Prey Model

Team 2

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Introduction

Here we are asked to simulate a shark/fish ecosystem via
predator prey model

Formally, predator prey models are those that obey the
Lotka-Volterra equations:

Here, x represents prey, y represents predators

Note that the prey loss term and predator growth term

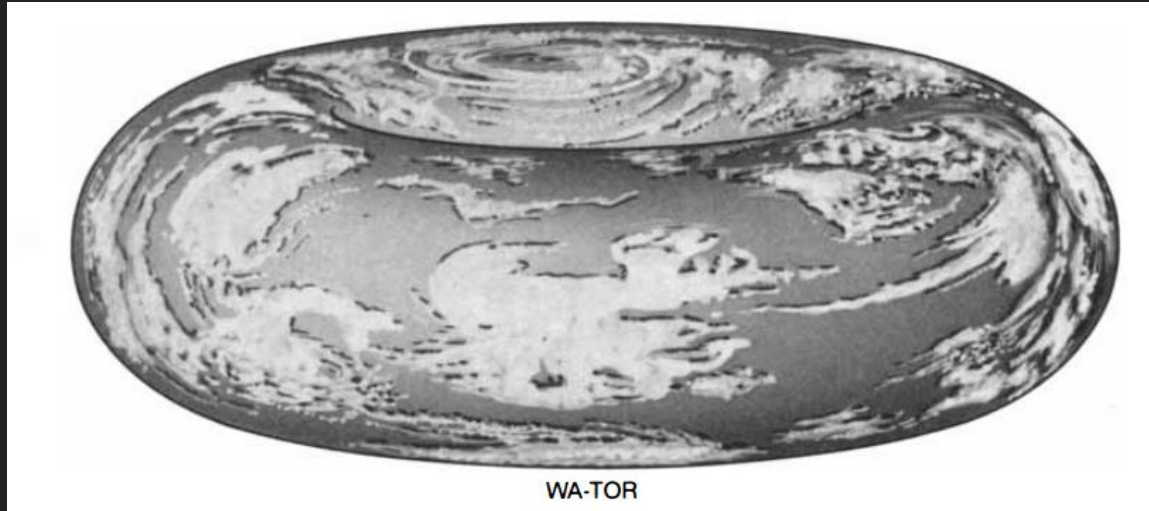
both depend on number of prey and predators.

$$\begin{aligned}\frac{dx}{dt} &= x(\alpha - \beta y) \\ \frac{dy}{dt} &= -y(\gamma - \delta x)\end{aligned}$$

Introduction

- These equations have **periodic solutions** (as expected) with population peaks shifted 90 degrees out of phase. (Note: extinction can of course occur.)
- To implement this model, a toroidal, 2 dimensional world was constructed.

A.K. Dewdney, Sharks and fish wage an ecological war on the toroidal planet Wa-Tor, 1984.



Introduction

The following rules governed the dynamics of the program:

Fish:

Move randomly to available adjacent spaces one at a time.

If fish reach breeding age, a new fish is born and age is reset.

Sharks:

If a fish is next to a shark, shark moves there and eats it. Otherwise, sharks move randomly to unoccupied locations.

If breeding age, sharks reproduce. If a shark has not eaten in a certain number of steps however, that shark starves and dies.

Algorithm

Five parameters: `nfish(3000)`, `nsharks(300)`, `fbreed(4)`, `sbreed(10)` and `sstarve(4)`. From Wa-Tor.

Three matrices: `fish[i,j]` (its value tells the age of fish. 0 means no fish), `shark[i,j]` and `starve[i,j]`. i in $\text{range}(L)$, j in $\text{range}(W)$

Algorithm

In each time step, perform one `move()` function.

Fish move first: `tmp=copy(fish)`, `tmp` will be looped so that every fish moves only once. However, only `fish[i,j]` will be modified.

`checkandgetrandomdirection_fish(i,j)` returns a position `[inew,jnew]` that fish can move in. Avoid sharks and fish. 2D random walk.

If fish age > `fbreed`, a new fish is born at `[i,j]` and renew both fish's ages.

Algorithm

Sharks move next: `tmp=copy(shark)`

`checkandgetrandomdirection_stof(i,j)` returns a position `[inew,jnew]` that has a fish. No fish will return `[-1,-1]` and if so, `starve[i,j]` will be checked. If `starve[i,j] < shark starve age`, do the same thing as the fish--`checkandgetrandomdirection_shark(i,j)`. Otherwise the shark will be deleted.

If there is a fish, eat it and renew `starve[inew,jnew]`. Also check breeding age.

`move()` function ends.

'for loop' can see the change of `fish[i,j]` and `shark[i,j]`.

Results

Initial parameters:

Grid size = 100x80

fish = 3000

sharks = 300

fishbreed = 4

sharkbreed = 10

sharkstarve = 4

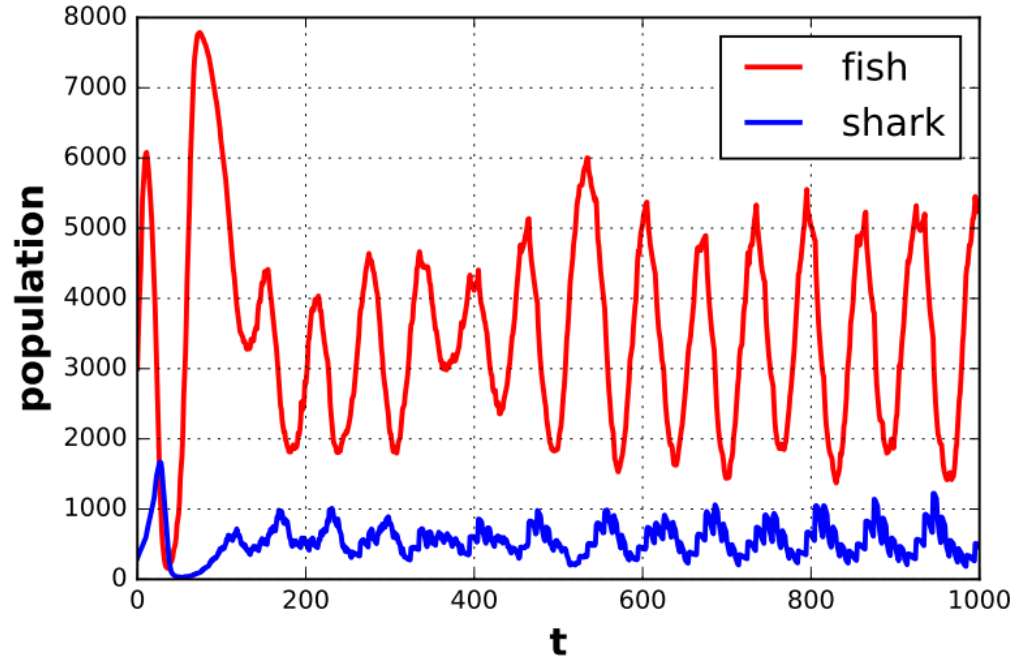
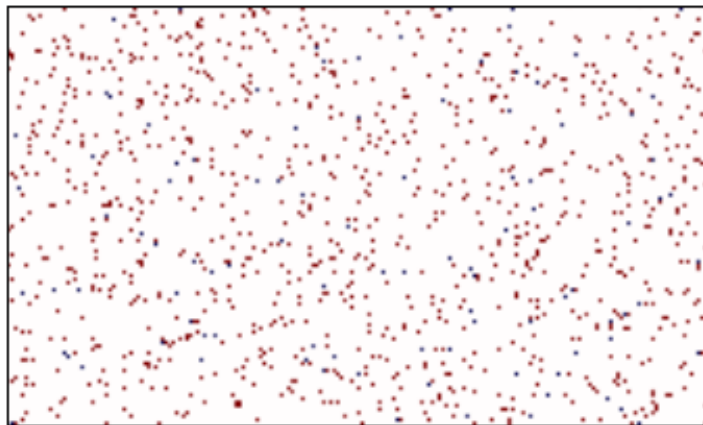


Figure 1: Fish and Shark population as a function of time.

Results

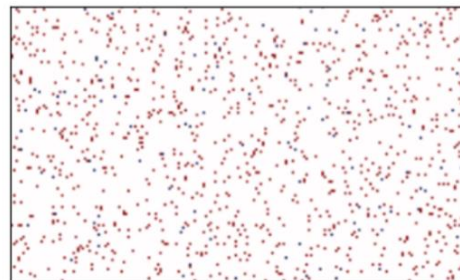
Snapshots at various t



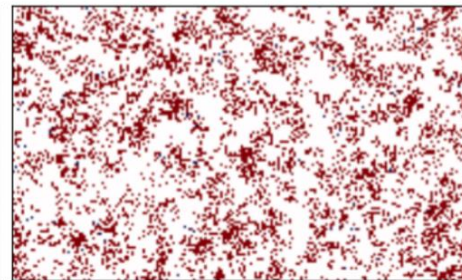
Fish



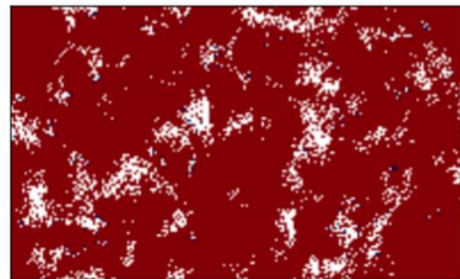
Shark



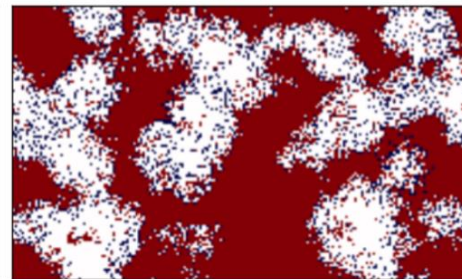
(a) $t=0$



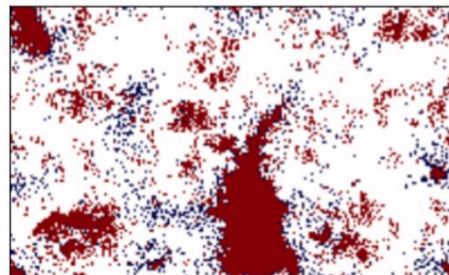
(b) $t=5$



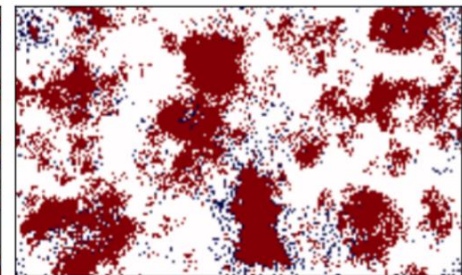
(c) $t=10$



(d) $t=20$



(e) $t=40$



(f) $t=50$

Figure 2: Configurations of the 2D ecosystem. Red: fish. Blue: Shark.

Thanks!

Source code:

github.com/vyu16/PHY556-DUKE

Questions?