Loading and Preparing Data

Purpose: Load predictions from different meta-learners and prepare the data for analysis.

```
In []: import pandas as pd
    import matplotlib.pyplot as plt
    import seaborn as sns
    from sklearn.metrics import mean_squared_error

# Load the CSV files
slearner_data = pd.read_csv('../results/s_predictions.csv')
tlearner_data = pd.read_csv('../results/t_predictions.csv')
xlearner_data = pd.read_csv('../results/x_predictions.csv')
rlearner_data = pd.read_csv('../results/r_predictions.csv')

# Add a Learner identifier column
slearner_data['Learner'] = 'S-Learner'
tlearner_data['Learner'] = 'T-Learner'
rlearner_data['Learner'] = 'R-Learner'
xlearner_data['Learner'] = 'X-Learner'
# Combine all data into one DataFrame
combined_data = pd.concat([slearner_data, tlearner_data, rlearner_data], ignore_index=True)
```

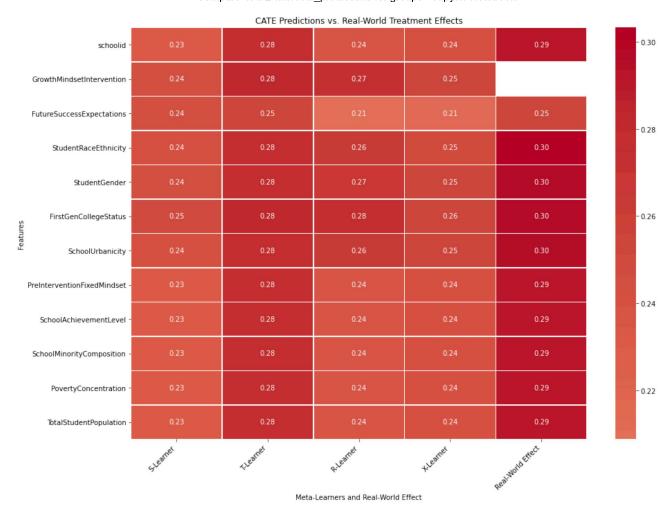
Calculating CATE for Each Feature

Purpose: Calculate the average CATE for each feature using the predictions from each meta-learner.

```
In [2]: # List of features to calculate CATE for
         features = [
              'schoolid', 'GrowthMindsetIntervention', 'FutureSuccessExpectations',
'StudentRaceEthnicity', 'StudentGender', 'FirstGenCollegeStatus', 'SchoolUrbanicity',
              'PreInterventionFixedMindset', 'SchoolAchievementLevel', 'SchoolMinorityComposition',
              'PovertyConcentration', 'TotalStudentPopulation'
         # Initialize a dictionary to hold CATE results
         cate_results = {}
         # Function to calculate CATE for a given feature
         def calculate_cate(feature):
             grouped_data = combined_data.groupby(['Learner', feature]).agg({'CATE': 'mean'}).reset_index()
             grouped_data.columns = ['Learner', feature, 'CATE']
             return grouped_data
         # Calculate CATE for each feature and store the results
         for feature in features:
             cate_results[feature] = calculate_cate(feature)
                                        S-Learner T-Learner R-Learner X-Learner \
```

```
schoolid
                        0.230647 0.278851 0.238911 0.240691
GrowthMindsetIntervention
                       0.244798 0.279892 0.270576 0.253454
FutureSuccessExpectations
                       0.243297 0.252234 0.208768 0.212314
                       0.240382 0.278262 0.2606 0.248819
StudentRaceEthnicity
StudentGender
                       0.243489 0.279347 0.267875 0.251988
0.240176 0.278914 0.263373 0.251655
PreInterventionFixedMindset 0.230647 0.278851 0.238911 0.240691
SchoolAchievementLevel 0.230647 0.278851 0.238911 0.240691
SchoolMinorityComposition 0.230647 0.278851 0.238911 0.240691
PovertyConcentration 0.230647 0.278851 0.238911 0.240691
TotalStudentPopulation
                       0.230647 0.278851 0.238911 0.240691
                       Real-World Effect
cchoolid
                               0 20207/
```

scnoolia	0.292974
GrowthMindsetIntervention	NaN
FutureSuccessExpectations	0.252985
StudentRaceEthnicity	0.303306
StudentGender	0.298372
FirstGenCollegeStatus	0.297111
SchoolUrbanicity	0.295658
PreInterventionFixedMindset	0.292974
SchoolAchievementLevel	0.292974
SchoolMinorityComposition	0.292974
PovertyConcentration	0.292974
TotalStudentPopulation	0.292974



Calculating Real-World Treatment Effects

Purpose: Compute the actual difference in student achievement scores between treated and control groups for each feature, representing the real-world effect.

```
In []: # Calculate Real-World Treatment Effects
    real_world_effects = {}

for feature in features:
    # Group by the feature and treatment
    grouped_data = combined_data.groupby([feature, 'GrowthMindsetIntervention'])['StudentAchievementScore'].mean()

# Calculate the real-world treatment effect as the difference between treated and control
    real_world_effect = grouped_data[1] - grouped_data[0]

# Store the result
    real_world_effects[feature] = real_world_effect
```

Creating and Displaying the Comparison Matrix

Purpose: Compare the predicted CATE values from each meta-learner with the real-world treatment effects

```
In [ ]: # Create a new DataFrame to compare the predicted CATE with real-world treatment effects
        comparison_matrix_with_real = pd.DataFrame(index=features, columns=['S-Learner', 'T-Learner', 'R-Learner', 'X-Lear
        # Fill the matrix with the predicted CATE values and real-world treatment effects
        for feature in features:
            for learner in ['S-Learner', 'T-Learner', 'R-Learner']:
                learner_data = cate_results[feature]
                mean_cate = learner_data[learner_data['Learner'] == learner]['CATE'].mean()
                comparison_matrix_with_real.loc[feature, learner] = mean_cate
            # Fill in the real-world effect for the feature
            comparison_matrix_with_real.loc[feature, 'Real-World Effect'] = real_world_effects[feature].mean()
        # Display the updated comparison matrix
        print(comparison_matrix_with_real)
        # Visualize the Comparison
        plt.figure(figsize=(14, 10))
        # Heatmap showing both CATE predictions and real-world effects
        sns.heatmap(comparison_matrix_with_real.astype(float), annot=True, cmap="coolwarm", center=0, cbar=True, fmt=".2f"
        plt.title('CATE Predictions vs. Real-World Treatment Effects')
        plt.xlabel('Meta-Learners and Real-World Effect')
        plt.ylabel('Features')
        plt.xticks(rotation=45, ha='right')
        plt.yticks(rotation=0)
        plt.tight_layout()
        plt.show()
```

Handling NaN Values and Recalculating Real-World Effects

Purpose: Resolve NaN values in the real-world effects by manually recalculating the mean scores for treated and control groups.

```
In [3]: # Step 1: Check for missing values in the relevant columns
        missing_values = combined_data[['GrowthMindsetIntervention', 'StudentAchievementScore']].isnull().sum()
        print("Missing values:\n", missing_values)
        Missing values:
         GrowthMindsetIntervention
                                      0
        StudentAchievementScore
        dtype: int64
In [4]: # Step 2: Inspect data for GrowthMindsetIntervention to see if treated or control group has insufficient data
        print("\nData distribution for GrowthMindsetIntervention:")
        print(combined_data['GrowthMindsetIntervention'].value_counts())
        Data distribution for GrowthMindsetIntervention:
        0
             28028
             13536
        Name: GrowthMindsetIntervention, dtype: int64
In [6]: # Step 3: Investigate the distribution of StudentAchievementScore for treated and control groups
        treated_scores = combined_data[combined_data['GrowthMindsetIntervention'] == 1]['StudentAchievementScore']
        control_scores = combined_data[combined_data['GrowthMindsetIntervention'] == 0]['StudentAchievementScore']
```

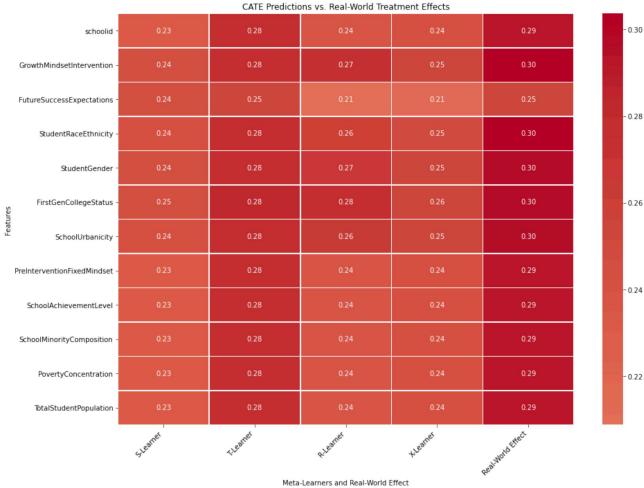
```
In [7]: print("\nTreated group scores (first few rows):")
        print(treated_scores.head())
        print("\nControl group scores (first few rows):")
        print(control_scores.head())
        Treated group scores (first few rows):
            0.081602
           -0.385869
        1
        2
            0.398184
          -0.175037
        3
            0.884583
        Name: StudentAchievementScore, dtype: float64
        Control group scores (first few rows):
        3384 -1.434893
        3385
               0.999290
        3386
              0.197742
        3387
              -0.059160
        3388
              -0.041489
        Name: StudentAchievementScore, dtype: float64
In [8]: # Manually calculate the mean scores for treated and control groups
        mean_treated_score = treated_scores.mean()
        mean_control_score = control_scores.mean()
        # Calculate the real-world effect
        real world effect growth mindset = mean treated score - mean control score
        print("\nManually Recalculated Real-World Effect for GrowthMindsetIntervention:", real_world_effect_growth_mindset
        Manually Recalculated Real-World Effect for GrowthMindsetIntervention: 0.3036748422490185
In [9]: # Update the comparison matrix with the manually recalculated real-world effect
        comparison_matrix_with_real.loc['GrowthMindsetIntervention', 'Real-World Effect'] = real_world_effect_growth_minds
        # Display the updated comparison matrix
        print("\nUpdated comparison matrix with recalculated Real-World Effect:")
        print(comparison_matrix_with_real)
        Updated comparison matrix with recalculated Real-World Effect:
                                 S-Learner T-Learner R-Learner X-Learner
        schoolid
                                   0.230647 0.278851 0.238911 0.240691
       StudentRaceEthnicity 0.240382 0.278262 0.2606 0.248819
        StudentGender
                                 0.243489 0.279347 0.267875 0.251988
       FirstGenCollegeStatus 0.246866 0.280338 0.277363 0.255865 SchoolUrbanicity 0.240176 0.278914 0.263373 0.251655
        PreInterventionFixedMindset 0.230647 0.278851 0.238911 0.240691
        SchoolAchievementLevel 0.230647 0.278851 0.238911 0.240691
        SchoolMinorityComposition 0.230647 0.278851 0.238911 0.240691
        TotalStudentPopulation
                                  0.230647 0.278851 0.238911 0.240691
                                  Real-World Effect
        schoolid
                                          0.292974
        GrowthMindsetIntervention
                                          0.303675
        FutureSuccessExpectations
                                          0.252985
        StudentRaceEthnicity
                                          0.303306
        StudentGender
                                          0.298372
        FirstGenCollegeStatus
                                          0.297111
        SchoolUrbanicity
                                          0.295658
        PreInterventionFixedMindset
                                         0.292974
        SchoolAchievementLevel
                                          0.292974
        SchoolMinorityComposition
                                         0.292974
                                          0.292974
        PovertyConcentration
        TotalStudentPopulation
                                          0.292974
```

```
In [10]: # Visualize the Comparison
    plt.figure(figsize=(14, 10))

# Heatmap showing both CATE predictions and real-world effects
    sns.heatmap(comparison_matrix_with_real.astype(float), annot=True, cmap="coolwarm", center=0, cbar=True, fmt=".2f"

plt.title('CATE Predictions vs. Real-World Treatment Effects')
    plt.xlabel('Meta-Learners and Real-World Effect')
    plt.ylabel('Features')
    plt.xticks(rotation=45, ha='right')
    plt.yticks(rotation=45, ha='right')
    plt.tight_layout()

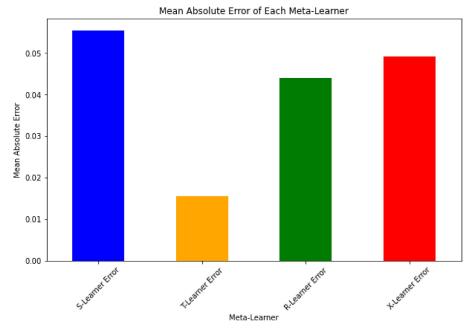
plt.show()
```



Comparative Analysis of Meta-Learners

Purpose: Evaluate the accuracy of each meta-learner by comparing their predicted CATE values with the real-world effects, and identify the best-performing learner for each feature.

```
In [19]: import numpy as np
         # Ensure all errors are numeric and handle NaN values by filling them with a large number (infinity)
         comparison_matrix_with_real['S-Learner Error'] = pd.to_numeric(comparison_matrix_with_real['S-Learner Error'], err
         comparison_matrix_with_real['T-Learner Error'] = pd.to_numeric(comparison_matrix_with_real['T-Learner Error'], err
         comparison_matrix_with_real['R-Learner Error'] = pd.to_numeric(comparison_matrix_with_real['R-Learner Error'], err
         comparison_matrix_with_real['X-Learner Error'] = pd.to_numeric(comparison_matrix_with_real['X-Learner Error'], err
         # Identify the best learner for each feature by finding the minimum error
         comparison_matrix_with_real['Best Learner'] = comparison_matrix_with_real[['S-Learner Error', 'T-Learner Error',
         #print("\nBest Learner for each feature:")
         #print(comparison_matrix_with_real[['S-Learner', 'T-Learner', 'R-Learner', 'X-Learner', 'Real-World Effect', 'Best
         # Visualize the mean absolute errors using a bar plot
         plt.figure(figsize=(10, 6))
         mean_errors = comparison_matrix_with_real[['S-Learner Error', 'T-Learner Error', 'R-Learner Error', 'X-Learner Err
mean_errors.plot(kind='bar', color=['blue', 'orange', 'green', 'red'])
         plt.title('Mean Absolute Error of Each Meta-Learner')
         plt.ylabel('Mean Absolute Error')
         plt.xlabel('Meta-Learner')
         plt.xticks(rotation=45)
         plt.show()
         # Display the updated comparison matrix with error calculations
         #print("\nUpdated comparison matrix with error calculations:")
         print(comparison_matrix_with_real)
```



```
S-Learner T-Learner R-Learner X-Learner \
                           0.230647 0.278851 0.238911 0.240691
schoolid
GrowthMindsetIntervention
                          0.244798 0.279892 0.270576 0.253454
FutureSuccessExpectations
                          0.243297 0.252234 0.208768 0.212314
StudentRaceEthnicity
                          0.240382 0.278262 0.2606 0.248819
                          0.243489 0.279347 0.267875 0.251988
StudentGender
PreInterventionFixedMindset 0.230647 0.278851 0.238911 0.240691
SchoolAchievementLevel 0.230647 0.278851 0.238911 0.240691
                          0.230647 0.278851 0.238911 0.240691
SchoolMinorityComposition
                          0.230647 0.278851 0.238911 0.240691
PovertyConcentration
TotalStudentPopulation
                         0.230647 0.278851 0.238911 0.240691
                          Real-World Effect S-Learner Error
schoolid
                                  0.292974
                                                  0.062327
GrowthMindsetIntervention
                                  0.303675
                                                  0.058877
FutureSuccessExpectations
                                  0.252985
                                                  0.009688
                                                  0.062923
StudentRaceEthnicity
                                  0.303306
StudentGender
                                  0.298372
                                                  0.054884
FirstGenCollegeStatus
                                 0.297111
                                                  0.050245
SchoolUrbanicity
                                 0.295658
                                                  0.055483
PreInterventionFixedMindset
                                 0.292974
                                                  0.062327
SchoolAchievementLevel
                                 0.292974
                                                  0.062327
SchoolMinorityComposition
                                  0.292974
                                                  0.062327
PovertyConcentration
                                  0.292974
                                                  0.062327
                                  0.292974
                                                  0.062327
TotalStudentPopulation
                           T-Learner Error R-Learner Error \
schoolid
                                 0.014123
GrowthMindsetIntervention
                                 0.023783
                                                 0.033099
FutureSuccessExpectations
                                 0.000751
                                                 0.044217
StudentRaceEthnicity
                                 0.025044
                                                 0.042706
                                 0.019025
                                                 0.030497
StudentGender
FirstGenCollegeStatus
                                 0.016773
                                                 0.019748
SchoolUrbanicity
                                 0.016744
                                                 0.032285
PreInterventionFixedMindset
                                 0.014123
                                                0.054063
SchoolAchievementLevel
                                 0.014123
                                                0.054063
SchoolMinorityComposition
                                 0.014123
                                                 0.054063
PovertyConcentration
                                 0.014123
                                                 0.054063
TotalStudentPopulation
                                 0.014123
                                                 0.054063
                          X-Learner Error
                                             Best Learner
schoolid
                                 0.052283 T-Learner Error
GrowthMindsetIntervention
                                 0.050221 T-Learner Error
FutureSuccessExpectations
                                 0.040671 T-Learner Error
StudentRaceEthnicity
                                 0.054487 T-Learner Error
                                 0.046384 T-Learner Error
StudentGender
FirstGenCollegeStatus
                                 0.041246 T-Learner Error
                                 0.044004 T-Learner Error
SchoolUrbanicity
PreInterventionFixedMindset
                               0.052283 T-Learner Error
SchoolAchievementLevel
                                 0.052283 T-Learner Error
SchoolAchievementLevel
SchoolMinorityComposition
                                 0.052283 T-Learner Error
                                 0.052283 T-Learner Error
PovertyConcentration
                                 0.052283 T-Learner Error
```

Summary of the Results:

 ${\tt TotalStudentPopulation}$

Best Learner Identification: The Best Learner column in the final matrix shows which meta-learner most accurately predicted the real-world effects for each feature based on the smallest absolute error, T-Learner Performance: The T-Learner consistently appears as the best performer across multiple features, indicating it may be the most accurate model in this scenario.