

# Quantifying metapopulation portfolio effects with the **ecofolio** package

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This vignette accompanies the **ecofolio** R package and the manuscript *Ecological prophets: Quantifying metapopulation portfolio effects*, which is in preparation for the journal *Methods in Ecology and Evolution*. Here, we briefly illustrate the use and interpretation of the functions in the **ecofolio** package with a sample dataset.

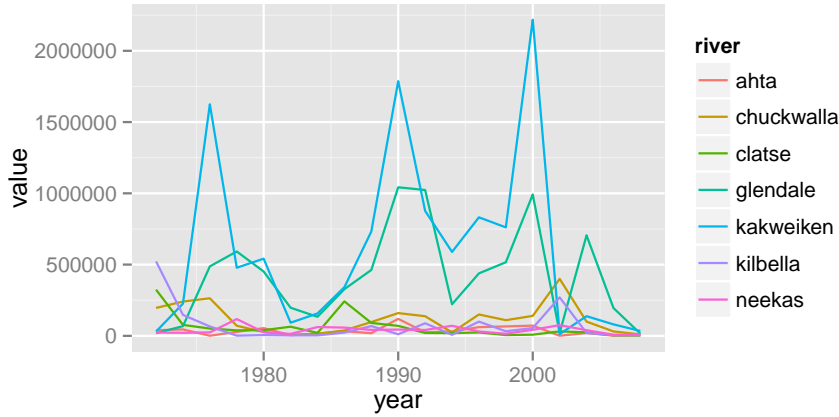
First, let's load the package and load the sample dataset. These data represent pink salmon recruits in the Broughton Archipelago for even years. Each column represents abundance for a different river through time. You can find these data in the supplementary materials of Krkošek et al. (2011) and they were originally collected by Fisheries and Oceans Canada.

```
> library(ecofolio)
> data(pinkbr)
> head(pinkbr)
```

	year	ahta	chuckwalla	clatse	glendale	kakweiken	kilbella	neekas
1	1972	39611	195937	324023	18815	29708	522499	23565
2	1974	45248	240733	76827	67873	226242	147115	21341
3	1976	812	263522	51206	487456	1624853	65881	24181
4	1978	27983	70752	38581	591956	477870	1415	117885
5	1980	54148	26999	39704	451232	541478	5400	25524
6	1982	4604	8156	64224	197308	92077	3058	13447

Let's plot the time series:

```
> library(reshape)
> library(ggplot2)
> x_long <- melt(pinkbr, id.vars = "year", variable_name = "river")
> ggplot(x_long, aes(year, value, colour = river)) + geom_line()
```



We can estimate Taylor's power law for this population:

```
> fit_taylor(pinkbr[, -1])
```

```
$c
[1] 0.2805908
```

```
$z
[1] 1.977981
```

These values reflect the equation:

$$\sigma^2 = c\mu^z \quad (1)$$

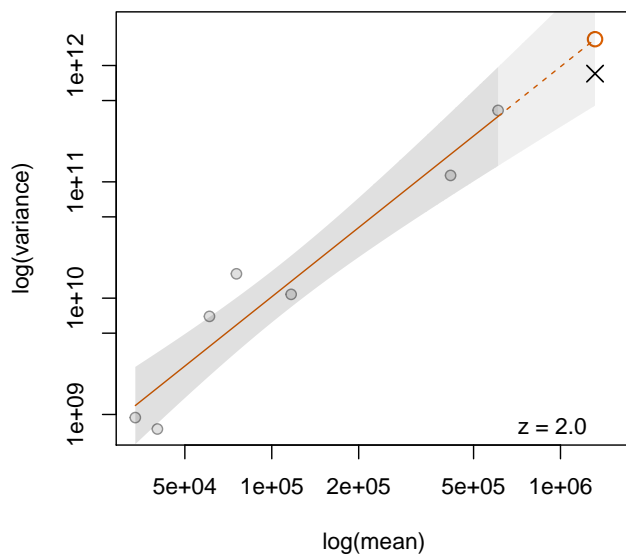
where  $\sigma^2$  is the temporal variance and  $\mu$  is the temporal mean. The parameter  $c$  does not affect the portfolio effect. The parameter  $z$  is often referred to as Taylor's power law exponent. Specifically, `fit_taylor` and the function `pe_mv` fit the mean-variance relationship on a log-log scale:

$$\log(\sigma_i^2) = c + z \cdot \log(\mu_i) + \epsilon_i \quad (2)$$

where  $i$  represents an individual subpopulation, and  $\epsilon_i$  represents independent and identically distributed residual error with mean zero and an estimated variance.

The package also contains a function `plot_mv` to visualize the various mean-variance model fits to empirical data. Let's look at the linear model we just fit:

```
> plot_mv(pinkbr[, -1], show = "linear", ci = TRUE)
```



In this plot, we see the  $\log(\text{mean})$  and  $\log(\text{variance})$  values for each river as grey dots. The orange line shows the mean-variance fit. The  $\times$  shows the observed metapopulation  $\log(\text{mean})$  and  $\log(\text{variance})$  values. The orange-open circle shows the expected  $\log(\text{variance})$  value at the observed  $\log(\text{mean})$  value for the metapopulation. The ratio of the y-value of the open-orange circle and the  $\times$  represents the mean-variance portfolio effect. It's the ratio of the expected to the observed variability at the metapopulation size.

So,  $z$  is around 2. Let's look at the default mean-variance portfolio effect, which uses the linear model we just fit:

```
> pe_mv(pinkbr[, -1], ci = TRUE)
```

```
$pe
[1] 1.412039
```

```
$ci
[1] 0.7269781 2.7426593
```

This tells us that the metapopulation is 1.4 times more stable than if it acted as a homogeneous population. These (frequentist) confidence intervals indicate that

under repeated conditions, we would expect 95% of these intervals to contain the true value of the mean-variance portfolio effect given that our model is correct.

We can compare this to the average-CV portfolio effect. In this case, we find that the average-CV portfolio effect is similar for this population. We would expect this given that Taylor's power law z-value is close to 2.

```
> pe_avg_cv(pinkbr[, -1], ci = TRUE, boot_reps = 500)
```

```
$pe
```

```
[1] 1.516637
```

```
$ci
```

```
[1] 1.062932 2.168973
```

The `pe_avg_cv` function uses (bias-adjusted) bootstrap confidence intervals (BCa in the `boot` package). These confidence intervals are obtained by re-sampling the subpopulations with replacement and re-calculating the portfolio effect. If there aren't many subpopulations, these confidence intervals may not be an accurate reflection of the uncertainty in the average-CV portfolio effect.

Returning to the mean-variance portfolio effect, we can explore whether different kinds of mean-variance extrapolations would yield different results. Let's fit some different mean-variance extrapolations:

```
> pe_mv(pinkbr[, -1], type = "linear_robust")
```

```
[1] 1.405554
```

```
> pe_mv(pinkbr[, -1], type = "quadratic")
```

```
[1] 1.412039
```

```
> pe_mv(pinkbr[, -1], type = "linear_quad_avg")
```

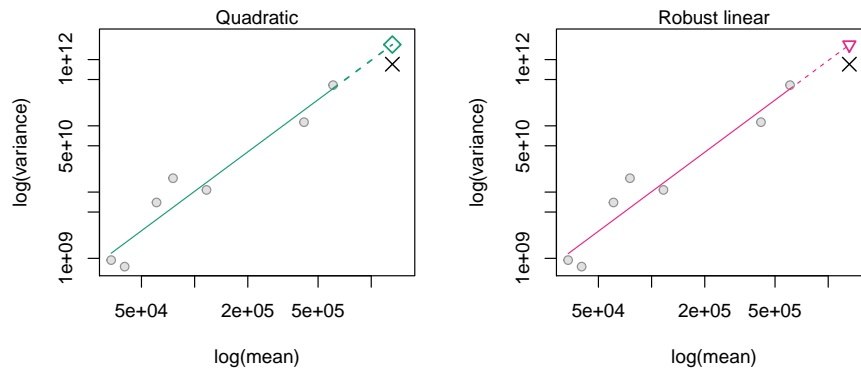
```
[1] 1.412039
```

The `quadratic` and `linear_quad_avg` options give us the same value as the `linear` version because the quadratic model curvature has been bounded to only curve up. In this case, they simplify to the linear model. We could look at these using the `plot_mv` function:

```

> par(mfrow = c(1, 2))
> plot_mv(pinkbr[, -1], show = "quadratic", add_z = FALSE)
> mtext("Quadratic")
> plot_mv(pinkbr[, -1], show = "robust", add_z = FALSE)
> mtext("Robust linear")

```



We can also try detrending the time series with linear or loess models to see how that affects the mean-variance portfolio effect. Estimates of variability such as the variance and CV can be biased upward if the time series are non-stationary.

```

> pe_mv(pinkbr[, -1], type = "linear")
[1] 1.412039
> pe_mv(pinkbr[, -1], type = "linear_detrended")
[1] 1.421514
> pe_mv(pinkbr[, -1], type = "loess_detrended")
[1] 1.43015

```

We've suppressed the confidence intervals here for brevity, but we can see that for this population, the estimates are similar whether or not we detrend the data.

## References

Krkošek, M., Connors, B.M., Morton, A., Lewis, M.A., Dill, L.M. & Hilborn, R. (2011). Effects of parasites from salmon farms on productivity of wild salmon. *Proceedings of the National Academy of Sciences of the United States of America*, 108, 14700–14704.